

Q.1

1.1

$$R_1 = \rho_{l_1}(\text{lives})$$

$$R_2 = \rho_{l_2}(\text{lives} \bowtie \text{manages})$$

$$R_3 = R_1 \bowtie (R_1.\text{manager-name} = R_2.\text{person-name}$$

$$\wedge R_1.\text{street} = R_2.\text{street}$$

$$\wedge R_1.\text{city} = R_2.\text{city})(R_2)$$

$$\boxed{\text{Result} = \pi_{\text{person-name}}(R_3)}$$

1.2.

$$R_1 = \sigma_{\text{company-name} = \text{"CITY BANK"}}(\text{works})$$

$$\boxed{\text{Result} = \pi_{\text{person-name}, \text{city}}(\text{lives} \bowtie R_1)}$$

1.3.

$$R_1 = \sigma_{(\text{company-name} = \text{"CITY BANK"} \wedge \text{Salary} > 528000)}(\text{works})$$

$$\boxed{\begin{aligned} \text{Result} = \\ \pi_{\text{person-name}, \text{street}, \text{city}}(\text{lives} \bowtie R_1) \end{aligned}}$$

Q.1

1.4.

Result =

$$\pi_{\text{person-name}} (\text{lives} \bowtie \text{works} \bowtie \text{located-in})$$

1.5:

→ Assuming all person works in a company.

$$\pi_{\text{person-name}} (\sigma_{\text{company-name} \neq \text{"CITY BANK"}} (\text{works}))$$

→ If some person does not work:

$$R_1 = \pi_{\text{person-name}} (\sigma_{\text{company-name} = \text{"CITY BANK"}} (\text{works}))$$

$$\text{Result} = \pi_{\text{person-name}} (\text{lives}) - R_1$$

Q.2

2.1)

```
SELECT company-name  
FROM works GROUP BY company-name  
HAVING SUM(salary) ≤  
ALL (SELECT SUM(salary)  
FROM works  
GROUP BY company-name);
```

2.2)

```
SELECT C1. company-name FROM located-in C1  
WHERE NOT EXISTS  
(SELECT city FROM located-in  
WHERE company-name = 'CITY BANK')  
EXCEPT  
(SELECT CITY FROM located-in C2  
WHERE C1. company-name = C2. company-  
name));
```


Q2

2.3) Assuming all person work:

```
SELECT person-name FROM works  
WHERE company-name <> 'CITY BANK';
```

However,

if not all person work for a company
then query would be

```
SELECT person-name FROM lives LEFT OUTER JOIN  
works ON lives.person-name = works.person-name  
WHERE works.company-name <> 'CITY BANK';
```

2.4)

```
SELECT person-name FROM works  
WHERE salary > (SELECT MAX(salary)  
FROM works WHERE  
company-name = 'CITY BANK');
```

Q.2

2.5)

SELECT person-name FROM works w1

WHERE salary > (SELECT Avg(salary)

FROM works w2

WHERE w1.company-name

= w2.company-name);

Q.3

3.1 Relation R:

$$P \rightarrow Q$$

$$R \rightarrow Q$$

$$S \rightarrow P \cup R$$

$$PR \rightarrow S$$

Step 1 ÷ Breaking RHS

- (i) $P \rightarrow Q$ (ii) $R \rightarrow Q$ (iii) $S \rightarrow P$ (iv) $S \rightarrow R$
 (v) $S \rightarrow R$ (vi) $PR \rightarrow S$

Step 2 ÷ check essential dependency

$$(i) \quad P \rightarrow Q, (P)^+ = \{P, Q\}$$

$$\therefore (P)_Q^+ = \{P\}$$

 \therefore essential

$$(ii) \quad R \rightarrow Q; (R)^+ = \{R, Q\}$$

$$\therefore (R)_Q^+ = \{R\}, \rightarrow \text{different then can}$$

 \therefore essential

$$(iii) \quad S \rightarrow P; (S)^+ = \{P, Q, R, S\}$$

$$(S)_P^+ = \{Q, R, S\} \rightarrow \text{different}$$

 \therefore essential

Q.3

3.1 (continued)

$$(iv) S \rightarrow Q : (S)^+ = \{P, Q, R, S\}$$

$$(S)_Q^+ = \{P, Q, R, S\} \rightarrow \text{Redundant.}$$

$$\therefore \text{Redundant.}$$

$$(v) S \rightarrow R : (S)^+ = \{P, Q, R, S\}$$

$$(S)_R^+ = \{P, Q, S\} \rightarrow \text{different}$$

$$\therefore \text{Essential}$$

$$(vi) PR \rightarrow S : (PR)^+ = \{P, Q, R, S\}$$

$$\therefore (PR)_S^+ = \{P, Q, R\} \rightarrow \text{different}$$

$$\therefore \text{Essential.}$$

So we get following.

$$P \rightarrow Q$$

$$R \rightarrow Q$$

$$S \rightarrow P \quad \text{>} \quad S \rightarrow PR$$

$$S \rightarrow R$$

$$PR \rightarrow S$$

STEP.3 \div Break LHS to single attribute

$$PR \rightarrow S ; (PR)^+ = \{P, Q, R, S\}$$

$$(P)^+ = \{P, Q\}, (R)^+ = \{R, Q\}$$

Q.3

Since $(P)^+$ & $(R)^+$ is different;

final canonical cover is same as step 2

∴ final =

- $P \rightarrow Q$
- $R \rightarrow Q$
- $S \rightarrow PR$
- $PR \rightarrow S$

3.2

$R = (P, Q, R, S, T)$

$P \rightarrow Q$

$PQ \rightarrow R$

$S \rightarrow PQT$

STEP (1)

$P \rightarrow Q$

$PQ \rightarrow R$

$S \rightarrow P$

$S \rightarrow Q$

$S \rightarrow T$

Q.2)

Q.2) continued

Step (2)

$$P \rightarrow Q ; (P)^+ = \{P, Q, R\} ; (P)^+_Q = \{P\}$$

$$PQ \rightarrow R ; (PQ)^+ = \{P, Q, R\} ; (PQ)^+_R = \{P, Q\}$$

$$S \rightarrow P ; (S)^+ = \{P, Q, R, S, T\} ; (S)^+_P = \{S, Q, T\}$$

$$S \rightarrow Q ; (S)^+ = \{P, Q, R, S, T\} ; (S)^+_Q = \{P, Q, R, S, T\}$$

└──────────────────┘
Redundant

$$S \rightarrow T ; (S)^+ = \{P, Q, R, S, T\} ; (S)^+_T = \{P, Q, R, S\}$$

So we get ,

$$(i) P \rightarrow Q \quad (ii) PQ \rightarrow R, \quad (iii) S \rightarrow P \quad (iv) S \rightarrow T.$$

Step (3) for $PQ \rightarrow R$

$$(PQ)^+ = \{P, Q, R\} \quad \left. \begin{array}{l} (P)^+ = \{P, Q, R\} \\ (Q)^+ = \{Q\} \end{array} \right\} \text{Redundant}$$

$$(P)^+ = \{P, Q, R\}$$

$$(Q)^+ = \{Q\}$$

Q.3

P.2) continued

So, we get

(i) $P \rightarrow Q$ (ii) $P \rightarrow R$ (iii) $S \rightarrow P$ (iv) $S \rightarrow T$ \therefore Final canonical cover $= P \rightarrow QR$ $S \rightarrow PT$

P.3) Given $R = Q \rightarrow P$
 $PS \rightarrow QR$
 $R \rightarrow PQS.$

Step (i)(i) $Q \rightarrow P$ (ii) $PS \rightarrow Q$ (iii) $PS \rightarrow R$ (iv) $R \rightarrow P$ (v) $R \rightarrow Q$ (vi) $R \rightarrow S$

Q.3

3.3 - ContinuedStep (ii)

$$(i) Q \rightarrow P ; (Q)^+ = \{P, Q, R\} ; (Q)^+_P = \{Q\}$$

$$(ii) PS \rightarrow Q ; (PS)^+ = \{P, S, Q, R\} ; (PS)^+_Q = \{P, S, Q, R\}$$

Redundant, so remove

$$(iii) PS \rightarrow R ; (PS)^+ = \{P, S, Q, R\} ; (PS)^+_R = \{P, S, \}$$

$$(iv) R \rightarrow P ; (R)^+ = \{P, Q, R, S\} ; (R)^+_P = \{P, Q, R, S\}$$

Redundant, so remove

$$(v) R \rightarrow Q ; (R)^+ = \{P, Q, R, S\} ; (R)^+_Q = \{R, S\}$$

$$(vi) R \rightarrow S ; (R)^+ = \{P, Q, R, S\} ; (R)^+_S = \{P, Q, R\}$$

So after removing

$$(i) Q \rightarrow P \quad (ii) PS \rightarrow R \quad (iii) R \rightarrow Q \quad (vi) R \rightarrow S$$

Q.33.3 → continuedStep (III)

Remove LHS Redundancy

$$PS \rightarrow R$$

$$(PS)^+ = \{P, Q, R, S\}$$

$$(P)^+ = \{P\}$$

$$(S)^+ = \{S\}$$

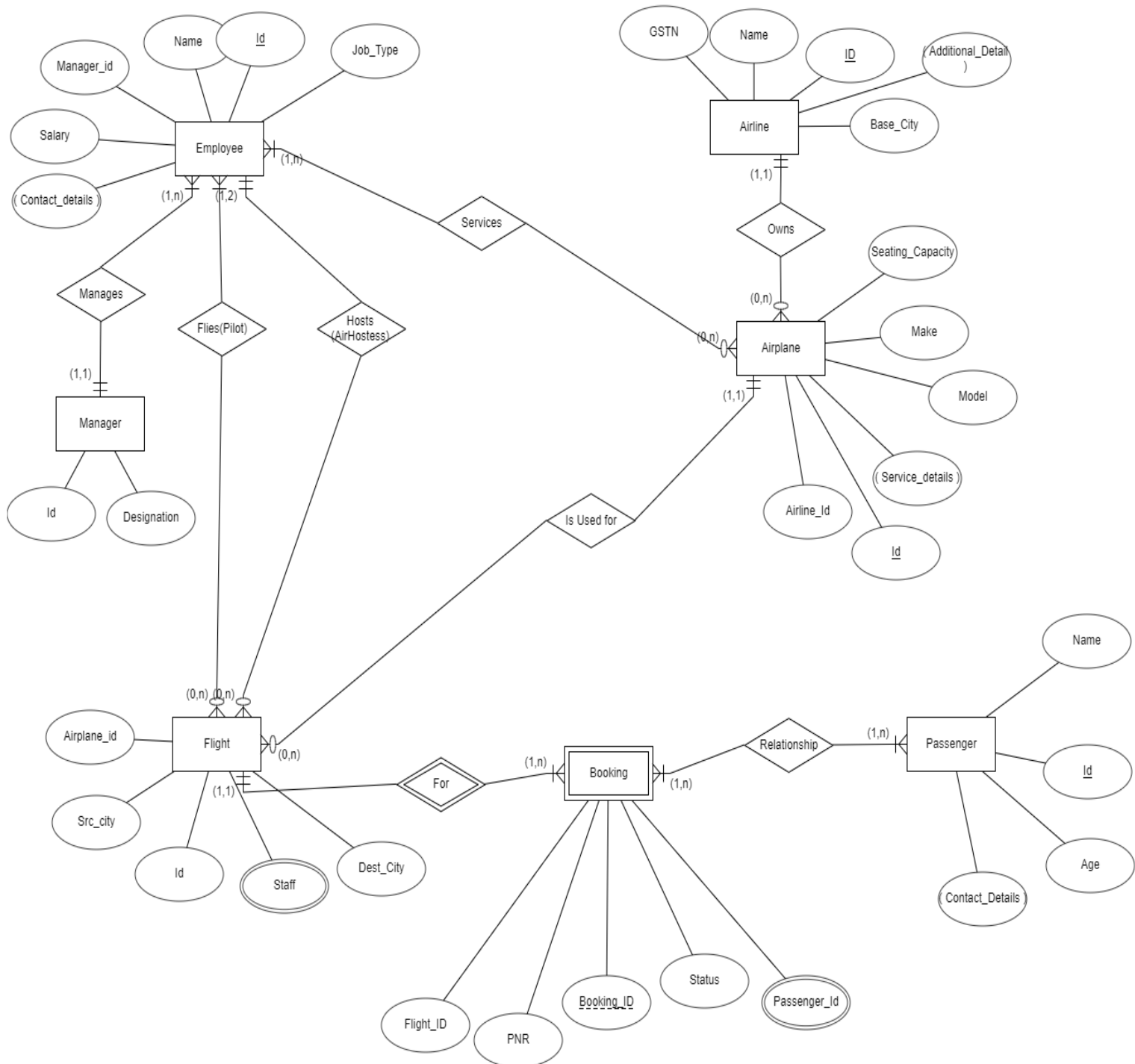
∴ No redundancy so cannot be removed.

∴ Final Canonical cover =

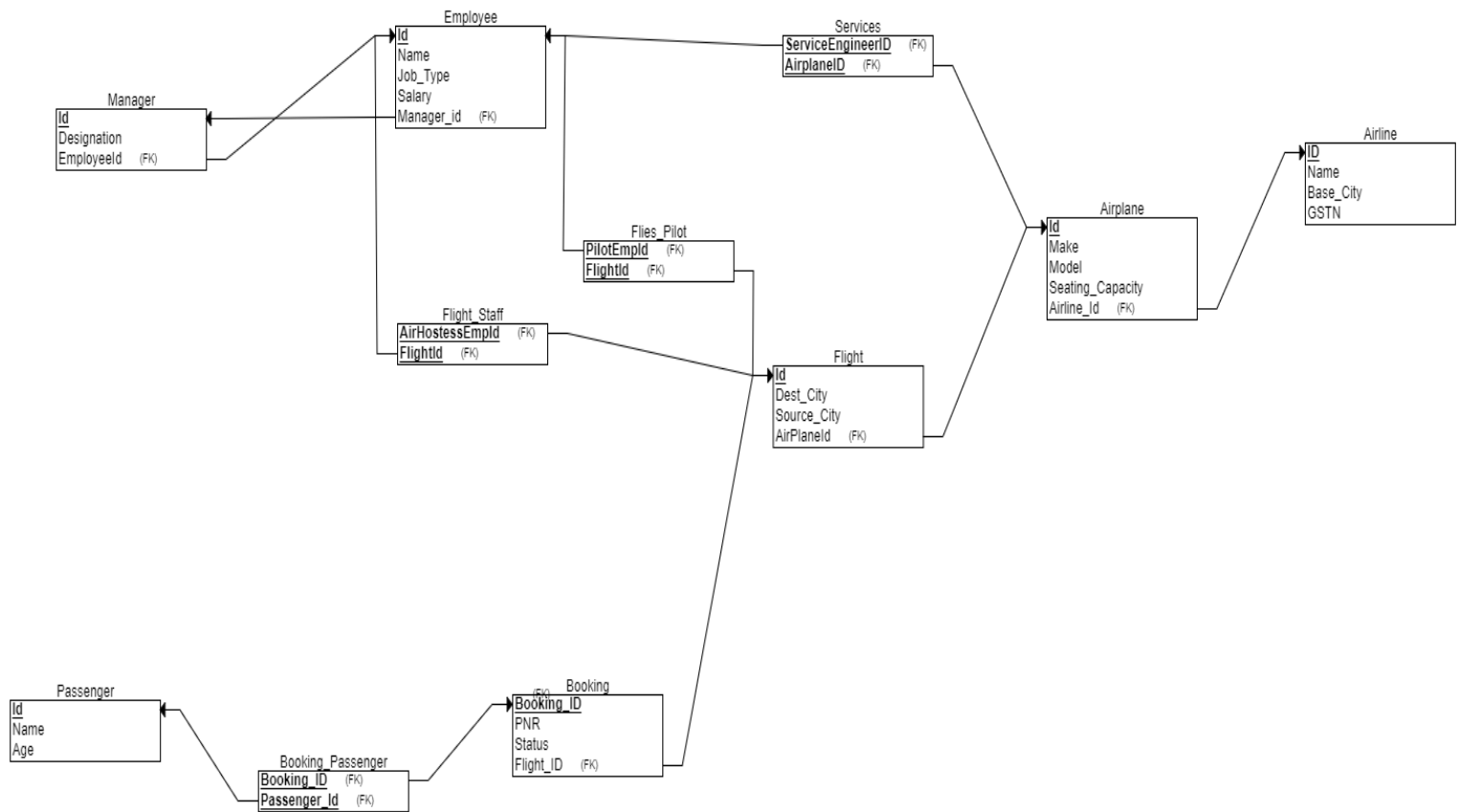
$$\begin{array}{l} Q \rightarrow P \\ PS \rightarrow R \\ R \rightarrow SQ \end{array}$$

Q4

ER Diagram for the Airline: I have used a tool to draw this diagram to ensure clarity.



Relational Model for the diagram:



THE END