

# FOL S-Expression Syntax

## S-Expressions for untyped FOL

Expression Type	Fitch Syntax	S-Expression Syntax
Propositional Statements	$P$	P
Not	$\neg P$	(not P)
And	$P \wedge Q$	(and P Q)
Or	$P \vee Q$	(or P Q)
Material Conditional	$P \rightarrow Q$	(implies P Q)
Bi-conditional	$P \leftrightarrow Q$	(iff P Q)
XOR	$P \oplus Q$	(xor P Q)
Variable/constant	$x, a$	x, a
Predicate	$P(a)$	(P a)
Function	$s(a)$	(s a)
Universal Quantifier	$\forall x P(x)$	(forAll x (P x))
Existential Quantifier	$\exists x P(x)$	(exists x (P x))

## S-Expressions for sorted/typed FOL

If you're writing software for sorted FOL, you can extend the S-expression syntax as follows in order to allow the user to define sorts/types, define constants under those sorts/types, define functions returning specific sorts/types and accepting arguments of fixed sorts/types, and finally express statements quantified over specific sorts/types.

Expression Type	Expression Structure	Example
Type/Sort Declarations	(declare-sort <i>new-sort supersort</i> )	(declare-sort Dog Animal)
Constant Declarations	(sort <i>object-name</i> )	(Object a)
Function Declarations	(return-type <i>function name argument-types ...</i> )	(Number <i>s</i> Number)
Universal Quantifier	(forAll ( <i>sort</i> x) <i>quantified-statement</i> )	(forAll (Object x) (P x))
Existential Quantifier	(exists ( <i>sort</i> x) <i>quantified-statement</i> )	(exists (Object x) (P x))