

$$z = f(x, y) = x^2 + y^2$$

$$\begin{aligned} a.) \quad \nabla f(x, y) &= \left(\frac{\partial f}{\partial x}(x, y), \frac{\partial f}{\partial y}(x, y) \right) \\ &= (2x, 2y) \end{aligned}$$

$$b.) \quad N_0 : x^2 + y^2 = 0$$

$$N_1 : x^2 + y^2 = 1$$

$$N_2 : x^2 + y^2 = 2$$

$$N_4 : x^2 + y^2 = 4 \text{ (bevat de punten } (2, 0) \text{ en } (0, 2))$$

$$N_8 : x^2 + y^2 = 8 \text{ (bevat het punt } (2, 2))$$

$$\nabla f(2, 0) = (2 \cdot 2, 2 \cdot 0) = (4, 0)$$

$$\nabla f(0, 2) = (2 \cdot 0, 2 \cdot 2) = (0, 4)$$

$$\nabla f(2, 2) = (2 \cdot 2, 2 \cdot 2) = (4, 4)$$

