demo

October 15, 2025

```
[1]: # Example sketch
     import sys
     # Allow notebooks to import project modules
     from pathlib import Path
     def resolve project root():
         candidates = []
         try:
             candidates.append(Path.cwd().resolve())
         except FileNotFoundError:
             candidates.append(None)
         if "__file__" in globals():
             candidates.append(Path(__file__).resolve().parent)
         candidates.append(Path("/home/bram/work/PE-LiNN/pelinn-qem"))
         for base in candidates:
             if base is None:
                 continue
             if (base / "pelinn").exists():
                 return base
             parent = base.parent
             if (parent / "pelinn").exists():
                 return parent
         return candidates[-1]
     project_root = _resolve_project_root()
     if project_root is not None and str(project_root) not in sys.path:
         sys.path.insert(0, str(project_root))
     import torch, numpy as np, random
     from torch.utils.data import Dataset, DataLoader
     from pelinn.data.qiskit_dataset import synthesize_samples
     from pelinn.model import PELiNNQEM, physics_loss
     from qiskit import QuantumCircuit
     from qiskit.quantum_info import SparsePauliOp
     from pelinn.data.qiskit_dataset import synthesize_samples
     def toy_circuits(n=4, m=20):
```

```
cs, os = [], []
   for _ in range(m):
       qc = QuantumCircuit(n)
       for q in range(n): qc.h(q)
       for q in range(0, n-1, 2): qc.cx(q, q+1)
       qc.measure_all(False) # no classical regs; Estimator uses state
       cs.append(qc)
       os.append(SparsePauliOp.from_list([("Z"+"I"*(n-1), 1.0)]))
   return cs, os
circs, obs = toy circuits(n=4, m=40)
noise_grid = [
 {"p1_depol": 0.001, "p2_depol": 0.01, "p_amp": 0.001, "readout_p01": 0.02, [

¬"readout_p10": 0.02},
 {"p1_depol": 0.003, "p2_depol": 0.02, "p_amp": 0.002, "readout_p01": 0.03, [

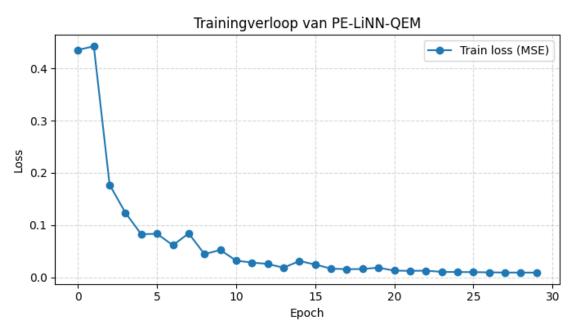
¬"readout_p10": 0.03},
samples = synthesize_samples(circs, obs, noise_grid, shots_noisy=4096)
```

```
[2]: import inspect
     if "torch" not in globals():
         import torch
     if "nn" not in globals():
         import torch.nn as nn
     if "F" not in globals():
         import torch.nn.functional as F
     if "PELiNNQEM" not in globals():
         from pelinn.model import PELiNNQEM
     required_state = ("X_full", "y_star", "y_noisy", "batches", "N")
     if not all(name in globals() for name in required_state):
         torch.manual_seed(0)
         N, D = 256, 12
         X = torch.randn(N, D)
         w = torch.randn(D)
         y_star = torch.tanh(0.5 * (X @ w))
         scales = torch.randint(1, 4, (N,)).float()
         noise = 0.25 * scales * torch.tanh(torch.randn(N))
         y_noisy = torch.clamp(y_star + noise, -1, 1)
         shots = 4096.0
         var_est = (1 - y_noisy**2) / shots
         X full = torch.cat(
             [X, y_noisy[:, None], (scales / 3.0)[:, None], var_est[:, None], torch.
      \hookrightarrowones(N, 1)],
             dim=1,
         )
```

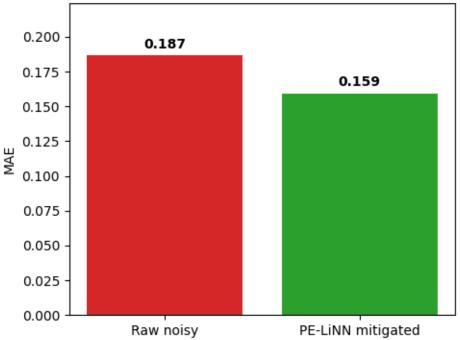
```
def batches(bs=128):
        idx = torch.randperm(N)
        for i in range(0, N, bs):
            j = idx[i:i + bs]
            yield X_full[j], y_star[j]
# Normalize inputs
Xmu = X_full.mean(0, keepdim=True)
Xstd = X_full.std(0, keepdim=True).clamp_min(1e-6)
Xn = (X_full - Xmu) / Xstd
model_kwargs = {"hid_dim": 96, "steps": 6, "dt": 0.25}
try:
    init_sig = inspect.signature(PELiNNQEM.__init__)
except (TypeError, ValueError):
    init_sig = None
if init_sig and "use_tanh_head" in init_sig.parameters:
    model_kwargs["use_tanh_head"] = False
model = PELiNNQEM(Xn.shape[1], **model_kwargs)
opt = torch.optim.AdamW(model.parameters(), lr=1e-3, weight_decay=5e-3)
sched = torch.optim.lr_scheduler.CosineAnnealingLR(opt, T_max=30)
loss out = []
for epoch in range(30):
    tot = 0.0
    for xb, yb in batches():
       xb = (xb - Xmu) / Xstd
        yhat = model(xb)
        loss = F.mse_loss(yhat, yb)
        opt.zero_grad()
        loss.backward()
        nn.utils.clip_grad_norm_(model.parameters(), 1.0)
        opt.step()
        tot += loss.item() * len(xb)
    sched.step()
    print(f"epoch {epoch:02d} loss={tot / N:.4f}")
    loss_out.append(tot / N)
# Switch head to tanh for bounded expectations where supported
if hasattr(model, "use_tanh_head"):
    model.use_tanh_head = True
with torch.no_grad():
    yh = model((X_full - Xmu) / Xstd)
    raw_mae = (y_noisy - y_star).abs().mean().item()
    mae = (yh - y_star).abs().mean().item()
```

```
print("Raw noisy MAE:", round(raw_mae, 4))
         print("PE-LiNN MAE:", round(mae, 4))
    epoch 00 loss=0.4357
    epoch 01 loss=0.4427
    epoch 02 loss=0.1772
    epoch 03 loss=0.1236
    epoch 04 loss=0.0825
    epoch 05 loss=0.0834
    epoch 06 loss=0.0613
    epoch 07 loss=0.0841
    epoch 08 loss=0.0443
    epoch 09 loss=0.0524
    epoch 10 loss=0.0318
    epoch 11 loss=0.0282
    epoch 12 loss=0.0255
    epoch 13 loss=0.0183
    epoch 14 loss=0.0311
    epoch 15 loss=0.0244
    epoch 16 loss=0.0166
    epoch 17 loss=0.0154
    epoch 18 loss=0.0159
    epoch 19 loss=0.0184
    epoch 20 loss=0.0128
    epoch 21 loss=0.0123
    epoch 22 loss=0.0127
    epoch 23 loss=0.0103
    epoch 24 loss=0.0101
    epoch 25 loss=0.0099
    epoch 26 loss=0.0094
    epoch 27 loss=0.0090
    epoch 28 loss=0.0090
    epoch 29 loss=0.0089
    Raw noisy MAE: 0.1866
    PE-LiNN MAE: 0.1594
[3]: import matplotlib.pyplot as plt
     # --- Plot settings ---
     epochs = list(range(30))
     losses = loss_out
     raw_mae = raw_mae
     mitigated_mae = mae
     # --- Plot 1: training loss ---
     plt.figure(figsize=(7,4))
```

```
plt.plot(epochs, losses, marker='o', label='Train loss (MSE)')
plt.xlabel("Epoch")
plt.ylabel("Loss")
plt.title("Trainingverloop van PE-LiNN-QEM")
plt.grid(True, linestyle='--', alpha=0.5)
plt.legend()
plt.tight_layout()
plt.show()
# --- Plot 2: MAE-vergelijking ---
plt.figure(figsize=(5,4))
bars = ['Raw noisy', 'PE-LiNN mitigated']
values = [raw_mae, mitigated_mae]
colors = ['tab:red', 'tab:green']
plt.bar(bars, values, color=colors)
plt.ylabel("MAE")
plt.title("Vergelijking van gemiddelde absolute fout (MAE)")
for i, v in enumerate(values):
    plt.text(i, v + 0.005, f"{v:.3f}", ha='center', fontweight='bold')
plt.ylim(0, max(values)*1.2)
plt.tight_layout()
plt.show()
```







```
[4]: # scripts/train_pelinn.py
     import sys
     # Allow notebooks to import project modules
     from pathlib import Path
     def _resolve_project_root():
         candidates = []
         try:
             candidates.append(Path.cwd().resolve())
         except FileNotFoundError:
             candidates.append(None)
         if "__file__" in globals():
             candidates.append(Path(__file__).resolve().parent)
         candidates.append(Path("/home/bram/work/PE-LiNN/pelinn-qem"))
         for base in candidates:
             if base is None:
                 continue
             if (base / "pelinn").exists():
                 return base
             parent = base.parent
             if (parent / "pelinn").exists():
                 return parent
```

```
return candidates[-1]
project_root = _resolve_project_root()
if project root is not None and str(project root) not in sys.path:
    sys.path.insert(0, str(project_root))
import torch, numpy as np, random
from torch.utils.data import Dataset, DataLoader
from pelinn.data.qiskit_dataset import synthesize_samples
from pelinn.model import PELiNNQEM, physics_loss
if ("circuits" not in globals()) or ("observables" not in globals()):
   from qiskit import QuantumCircuit
   from qiskit.quantum_info import SparsePauliOp
   def _default_circuit_family(n=4, m=24):
        cs, obs = [], []
        for _ in range(m):
            qc = QuantumCircuit(n)
            for q in range(n): qc.h(q)
            for q in range(0, n - 1, 2): qc.cx(q, q + 1)
            qc.measure_all(False) # keep state for estimators
            cs.append(qc)
            obs.append(SparsePauliOp.from_list([("Z" + "I" * (n - 1), 1.0)]))
        return cs, obs
    circuits, observables = _default_circuit_family()
if "noise_grid" not in globals():
   noise_grid = [
        {"p1_depol": 0.001, "p2_depol": 0.01, "p_amp": 0.001, "readout_p01": 0.
 ⇔02, "readout_p10": 0.02},
        {"p1 depol": 0.003, "p2 depol": 0.02, "p amp": 0.002, "readout p01": 0.
 →03, "readout_p10": 0.03},
   1
class QemDataset(Dataset):
   def __init__(self, samples):
       self.X = np.stack([s.x for s in samples]).astype(np.float32)
       self.y = np.array([s.y_ideal for s in samples], dtype=np.float32)
        self.cid = np.array([id(s.meta["qc"]) for s in samples], dtype=np.
 ⇒int64) # circuit id for grouping
   def __len__(self): return len(self.X)
   def __getitem__(self, i): return self.X[i], self.y[i], self.cid[i]
def make_groups(cids):
    # group indices sharing the same circuit id
   groups = {}
```

```
for i, c in enumerate(cids): groups.setdefault(int(c), []).append(i)
    return list(groups.values())
def train(model, loader, opt, device="cpu"):
    model.train()
    for X, y, cid in loader:
        X, y = X.to(device), y.to(device)
        pred = model(X)
        groups = make groups(cid.tolist())
        loss = physics_loss(pred, y, groups, alpha_inv=0.1)
        opt.zero grad(); loss.backward(); opt.step()
# usage sketch
def synthesize_training_samples(circuits, observables, noise_grid):
    return synthesize_samples(circuits, observables, noise_grid)
required_symbols = ("circuits", "observables", "noise_grid")
_missing = [name for name in required_symbols if name not in globals()]
if _missing:
    samples = []
    print(f"Missing variables required to synthesize training data: {', '.
 →join(_missing)}")
else:
    samples = synthesize_training_samples(circuits, observables, noise_grid)
# ds = QemDataset(samples); dl = DataLoader(ds, batch_size=128, shuffle=True)
\label{eq:model} \textit{\# model = PELiNNQEM(in\_dim=ds.X.shape[1]).to("cuda" if torch.cuda.}
⇔is_available() else "cpu")
# opt = torch.optim.AdamW(model.parameters(), lr=3e-4, weight_decay=1e-2)
# for epoch in range(100): train(model, dl, opt)
model = PELiNNQEM(in_dim=ds.X.shape[1]).to("cuda" if torch.cuda.is_available()
```

```
[5]: ds = QemDataset(samples); dl = DataLoader(ds, batch_size=128, shuffle=True)
model = PELiNNQEM(in_dim=ds.X.shape[1]).to("cuda" if torch.cuda.is_available()
else "cpu")

opt = torch.optim.AdamW(model.parameters(), lr=3e-4, weight_decay=1e-2)
for epoch in range(100): train(model, dl, opt)
```

- [6]: epoch
- [6]: 99