

# BIOFLUID MECHANICS

## ON COMPUTATIONAL FLUID DYNAMICS

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Ugent

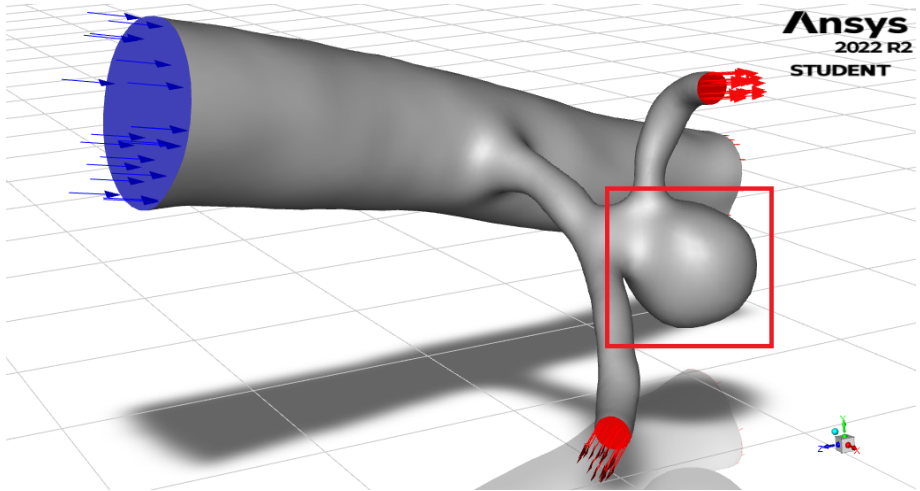
# Table of Contents

- 1 Meshing
- 2 Running an initial simulation
- 3 Mesh sensitivity analysis

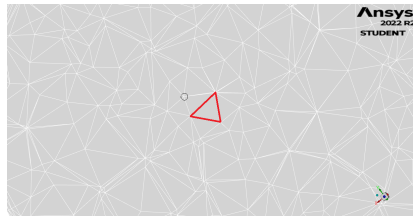
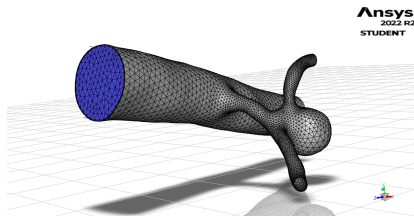
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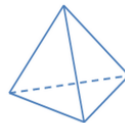
# The Aneurysm



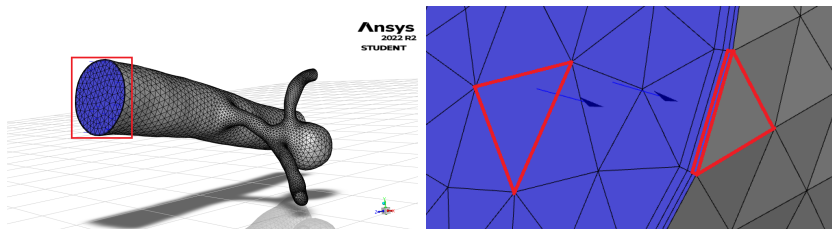
# Mesh element types



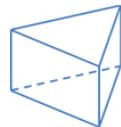
→ in bulk tetrahedral (4 faces)



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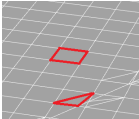

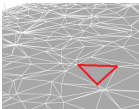



- in bulk tetrahedral (4 faces)
- at boundaries prism



Triangular Prism

# Mesh comparison

file	Element Type	$N$	Bulk View
Mesh1.cas	hexahedral, prism	496718	
Mesh2.cas	tetrahedral, prism	80846	
Mesh3.cas	tetrahedral, prism	319342	
Mesh4.cas	tetrahedral, prism	486960	

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# Blood modelling

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- At small scales (around the size of a RBC) and relative slow velocities, blood can no longer be assumed homogeneous and it's apparent viscosity becomes very important.
- ⇒ This model is physiological.

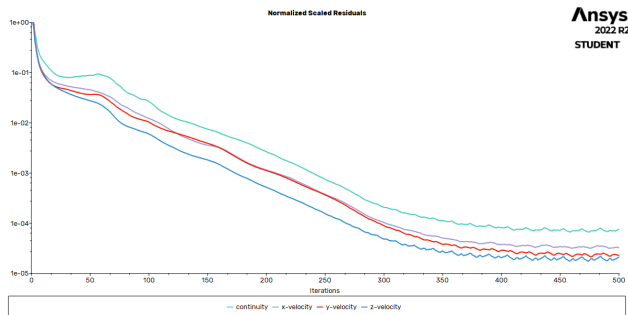
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→ Mesh2 has the lowest number of elements  $\Rightarrow$  Mesh2 is the coarsest mesh

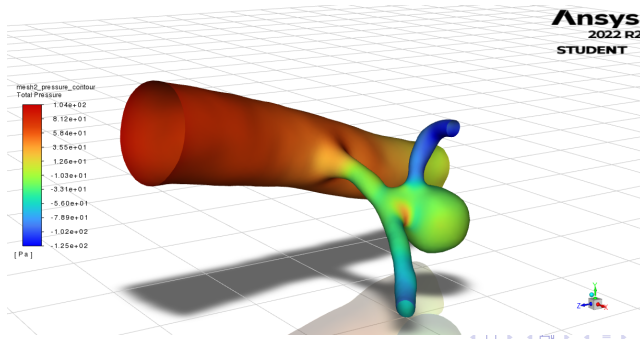
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- Conservation of mass?

Mass Flow Rate	[kg/s]
inlet.1.1	0.078264423
outlet-1.1.1	-0.0039132212
outlet-2.1.1	-0.0039132212
outlet-3.1.1	-0.070437981
Net	-1.3877788e-17

→ Net mass flow rate  $\approx 0$   
 $\Rightarrow$  mass is conserved!

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Consider a quantity  $A$  calculated via computational fluid dynamics with a mesh size  $N$ . Let's say that  $A_1$  is calculated with a mesh size  $N_1$  and  $A_2$  is calculated with a mesh size  $N_2$ , with  $N_2 > N_1$ . Then the mesh sensitivity, here denoted as  $\epsilon$ , between  $A_1$  and  $A_2$  is defined as

$$\epsilon = \frac{|A_2 - A_1|}{N_2 - N_1} = \frac{|\Delta A|}{\Delta N}.$$

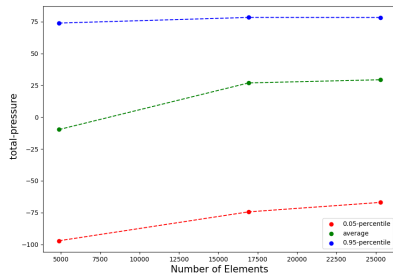
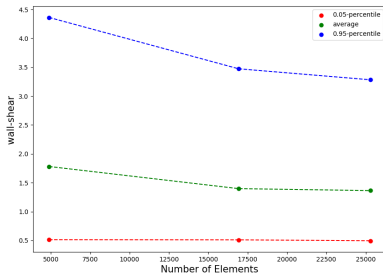
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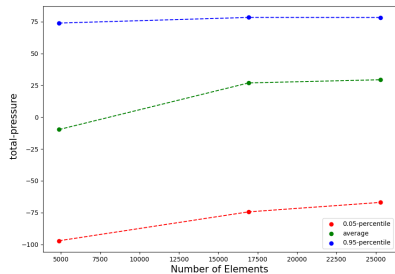
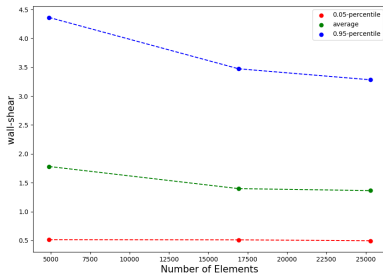
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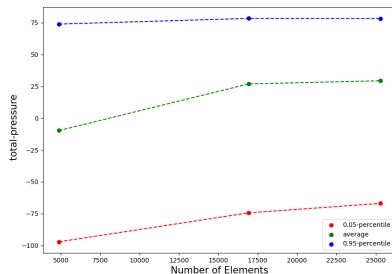
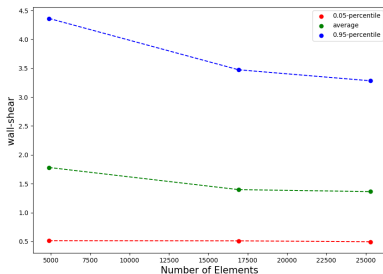
$$\epsilon = \frac{|A_2 - A_1|}{N_2 - N_1} = \frac{|\Delta A|}{\Delta N}.$$

$\epsilon$  indicates how much accuracy the model gains if the mesh size would be increase by  $\Delta N$  elements. If  $\epsilon$  is very small and the computational time relatively large then it would not be favorable to increase the mesh size.





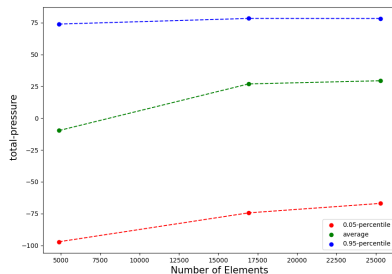
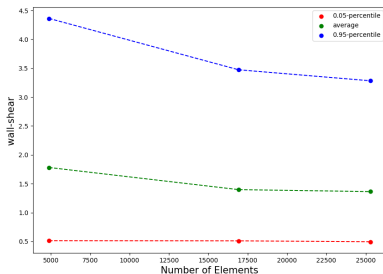
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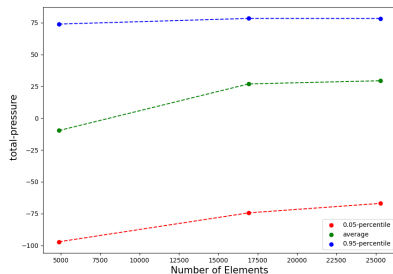
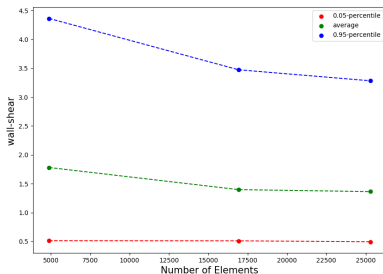
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- From Medium to Fine: relative low improvement



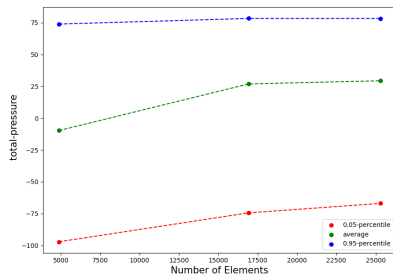
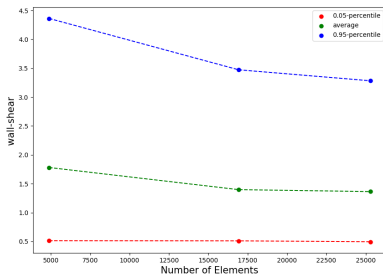
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- Estimate computation time (all **converged!**):

Coarse:  $T < 3$  min

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Fine:  $5 \text{ min} < T$



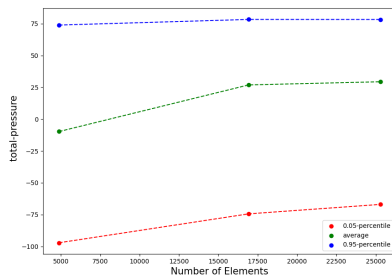
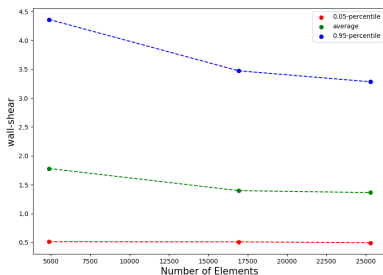
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- ⇒ Medium mesh will suffice

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- Why usage of percentiles and not minimum or maximum?
  - preventing outliers to influence conclusion
- More advanced techniques for mesh sensitivity analysis?
  - Numerical Mathematics Divergence Theory: knowing the structure of the CFD model at its properties

**Me: If I'm patient, eventually ANSYS will solve. I'll just do something in the meantime**

**Inner Me: Loosen the convergence criteria and coarsen the mesh. It'll solve faster**

