

Lecture #8

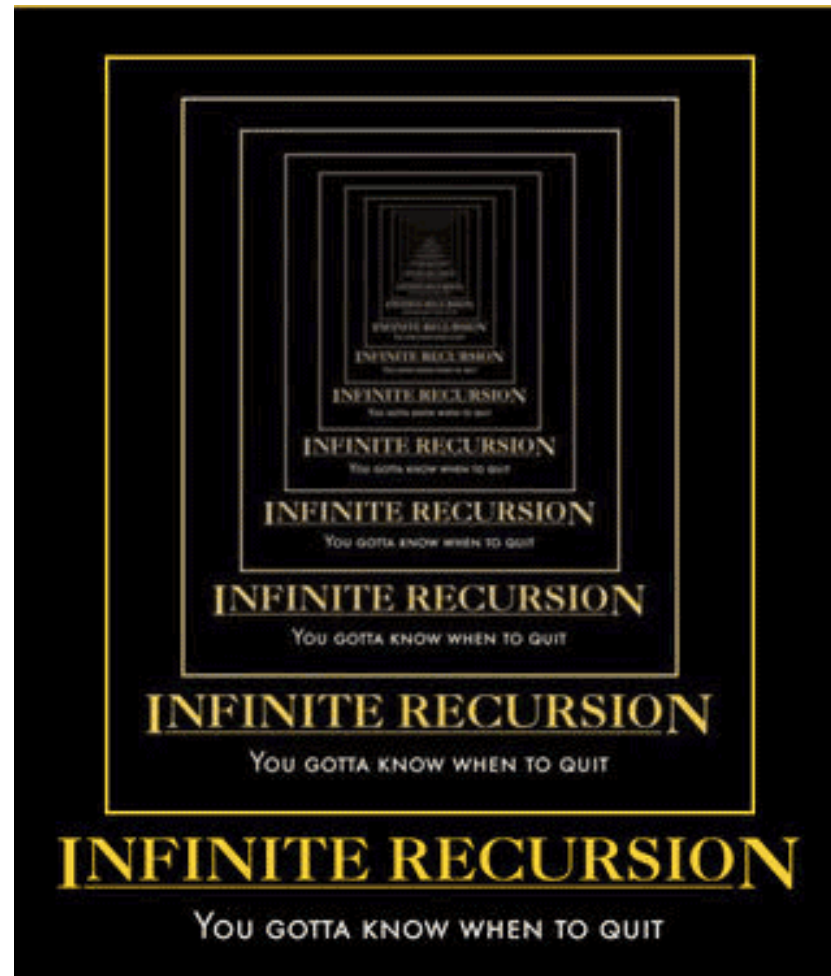
- Recursion
- How to *design* an Object Oriented program (on your own study)
- Project 3 Design Tips



This is a ship-shipping ship,
shipping shipping ships.



Recursion



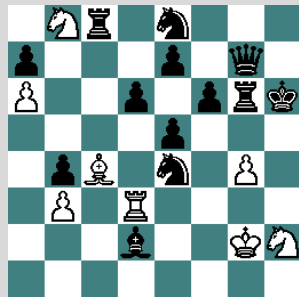
Recursion

Why should you care?

Recursion is one of the most difficult...
but powerful computer science topics.

Use it for things like...

AI for Games



Solving SuDoKu

9			6				3
1		5		9	3	2	6
	4			5			9
8						4	7
		4	8	7			
7		2	6		1		8
2							
5				3	2		9
	8	7		1	6	3	5

Cracking Codes



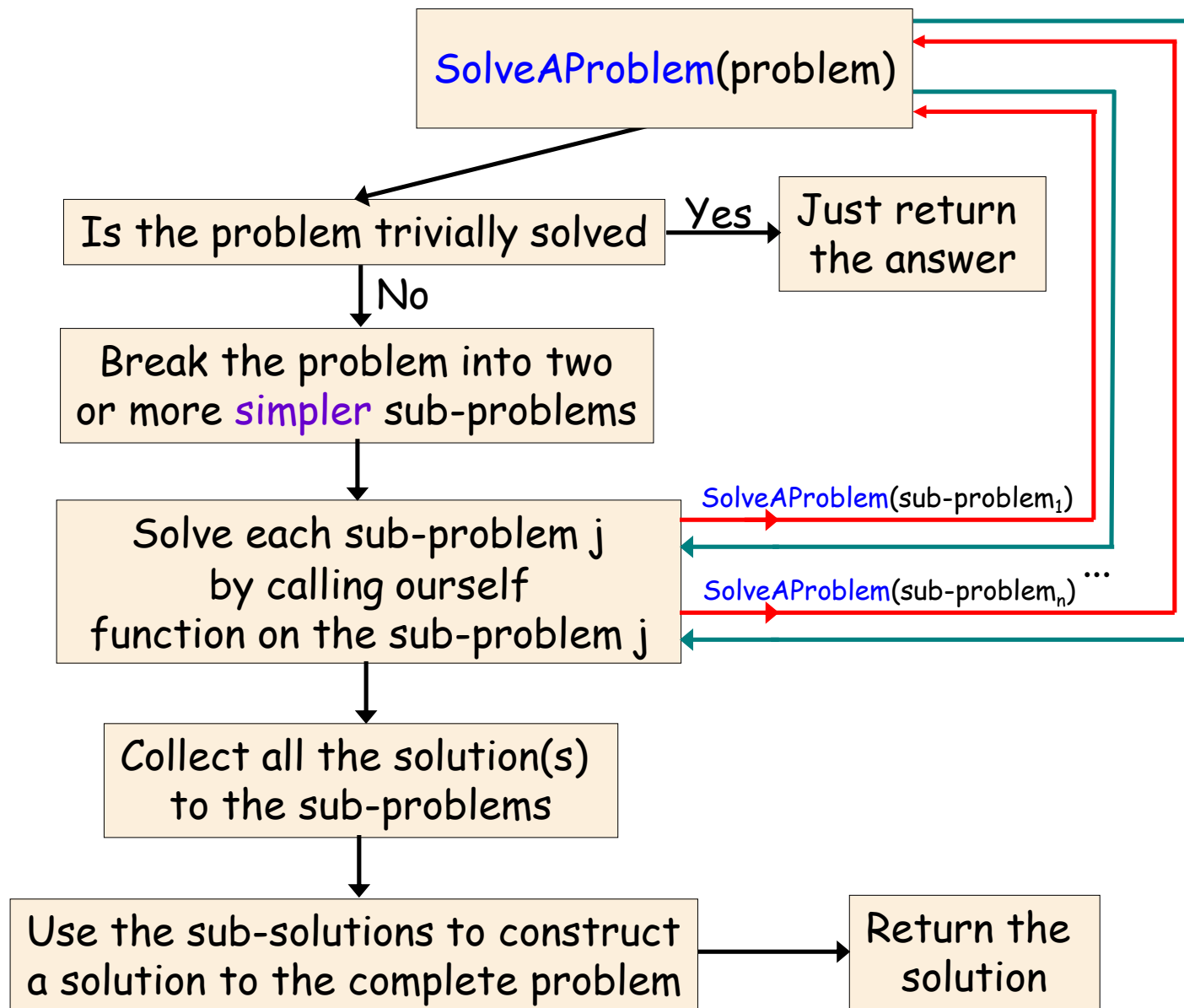
And they *love* to ask you to write recursive functions during job interviews.

So pay attention!

Why
should
I care?



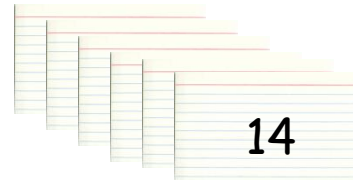
Idea Behind Recursion



"The Lazy Person's Sort"

Let's design a new **sorting algorithm**,
called the **"lazy person's sort"**...

The input to this sort
are a bunch of index
cards with #s.



Lazy Person's Sort:

Split the cards into two roughly-equal piles

Hand one pile to nerdy student A and ask them to sort it

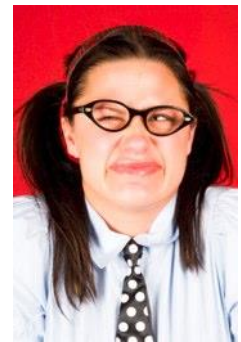
Hand the other pile to nerdy student B and ask them to sort it

Take the two sorted piles and merge them into a single sorted pile



6	17	22
---	----	----

3	14	95
---	----	----



"The Lazy Person's Sort"



6	17	22
---	----	----

3	14	95
---	----	----



Lazy Person's Sort:

Split the cards into two roughly-equal piles

Hand one pile to nerdy student A and ask them to sort it

Hand the other pile to nerdy student B and ask them to sort it

Take the two sorted piles and merge them into a single sorted pile



"The Lazy Person's Sort"



Very clever, students.

But your approach has one **flaw**, can you see it?



Lazy Person's Sort:

Split the cards into two roughly-equal piles

Hand one pile to nerdy student A and say "do the Lazy Person's Sort"

Hand the other pile to **hot** student B and say "do the Lazy Person's Sort"

Take the two sorted piles and merge them into a single sorted pile



"The Lazy Person's Sort"



Correct!

Amazing, huh? By having an algorithm use itself over and over, you can solve big problems!



Lazy Person's Sort:

If you're handed just one card, then just give it right back.

Split the cards into two roughly-equal piles

Hand one pile to studly student A and say "do the Lazy Person's Sort"

Hand the other pile to hot student B and say "do the Lazy Person's Sort"

Take the two sorted piles and merge them into a single sorted pile




```
void MergeSort(an array)
{
    if (array's size == 1)
        return;                // array has just 1 item, all done!

    MergeSort( first half of array );    // process the 1st half of the array
    MergeSort( second half of array);    // process the 2nd half of the array

    Merge(the two array halves);        // merge the two sorted halves
    // now the complete array is sorted
}
```

The Lazy Person's Sort (also known as **Merge Sort**) is a perfect example of a recursive algorithm!

Every time our MergeSort function is called, it breaks up its input into two smaller parts and calls **itself** to solve each sub-part.

When you write a recursive function...

Your job is to figure out how the function can use itself (on a subset of the problem) to get the complete problem solved.

When you add the code to make a function call itself, you need to have faith that that call will work properly (on the subset of data).

It takes some time to learn to think in this way, but once you "get it," you'll be a programming Ninja!



The Two Rules of Recursion

RULE ONE:

Every recursive function must have a "stopping condition!"

The Stopping Condition (aka Base Case):

Your recursive function must be able to solve the simplest, most basic problem *without using recursion*.

Remember: A recursive function *calls itself*.

Therefore, every recursive function must have some mechanism to allow it to stop calling itself.

The Stopping Condition



```
void eatCandy(int layer)
{
    if (layer == 0)
    {
        cout << "Eat center!";
        return;
    }

    cout<<"Lick layer "<<<layer;

    eatCandy(layer-1);
}
```

```
main()
{
    eatCandy(3);
}
```

Here's a simple recursive function that shows how to eat a **tootsie-roll pop**.

Can you identify the **stopping condition** in this function?

What if we **didn't have** this **stopping condition**/base case?

Right! Our function would never stop running.
(We'd just keep licking forever)

The Two Rules of Recursion

RULE TWO:

Every recursive function must have a "simplifying step".

Simplifying Step:

Every time a recursive function **calls itself**, it **must** pass in a **smaller sub-problem** that ensures the algorithm will eventually reach its **stopping condition**.

Remember: A recursive function must eventually reach its **stopping condition** or it'll run forever.

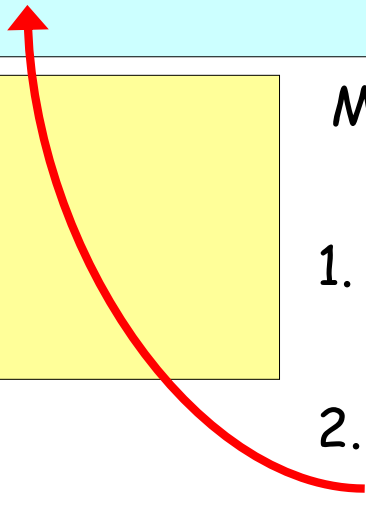
Simplifying Code

```
void eatCandy(int layer)
{
    if (layer == 0)
    {
        cout << "Eat center!";
        return;
    }

    cout<<"Lick layer "<<layer;

    eatCandy(layer-1);
}
```

```
main()
{
    eatCandy(3);
}
```



Can you identify the **simplifying code** in our eatCandy function?

What if we **didn't have simplifying code**?

Our function would never get closer to our stopping condition and never stop running.

Most recursive functions simplify their inputs in one of two ways:

1. Each recursive call **divides its input problem in half** (like MergeSort)
2. Each recursive call operates on an input that's **one smaller** than the last

(Rule 2.5 of Recursion)

Recursive functions should never use
global, *static* or *member* variables.

They should only use *local variables* and
parameters!



(So be forewarned... If your recursive functions use
globals/statics/members on a test/HW, you'll get a ZERO!)

Tracing Through our Function

```
void eatCandy(int layer)
{
    if (layer == 0)
    {
        cout << "Eat center!";
        return;
    }
    cout<<"Lick layer "<<layer;
    eatCandy(layer-1);
}
```

```
void eatCandy(int layer)
{
    if (layer == 0)
    {
        cout << "Eat center!";
        return;
    }
    cout<<"Lick layer "<<layer;
    eatCandy(layer-1);
}
```

```
void eatCandy(int layer)
{
    if (layer == 0)
    {
        cout << "Eat center!";
        return;
    }
    cout<<"Lick layer "<<layer;
    eatCandy(layer-1);
}
```

It's very difficult to trace through a function that calls itself...

So, let's use a little trick and pretend like this call is actually calling a different function (one that just happens to have the same name ☺).



```
main()
{
    int layers = 2;
    eatCandy(layers);
}
```


Writing (Your Own) Recursive Functions: 6 Steps

What if we want to **write our own** recursive function?

Here's a proven **six-step method** to help you!

Step #1:

Write the function header

Step #2:

Define your magic function

Step #3:

Add your base case code

Step #4:

Solve the problem w/the magic function

Step #5:

Remove the magic

Step #6:

Validate your function

Let's use these steps
to write a recursive
function to calculate
factorials.

Recall, the definition of
fact(N) is:

1	for $N = 0$
$N * \text{fact}(N-1)$	for $N > 0$

Example #1: Factorial



Step #1: Write the function header

Figure out what **argument(s)** your function will take and what it needs to **return** (if anything).

First, a factorial function takes in an integer as a parameter, e.g., factorial(**6**).

Second, the factorial computes (and should return) an integer result. Let's add a return type of int.

And here's how we'd call our factorial function to solve a problem of **size n**...

So far, so good. Let's go on to step #2.

```
int fact(int n)
{

}
```

```
int main()
{
    int n = 6, result;

    result = fact( n );

}
```

Step #2: Define your magic function

Pretend that you are given a **magic function** that can compute a factorial. It's already been written for you and is guaranteed to work!

It takes the **same parameters** as your factorial function and **returns the same type** of result/value.

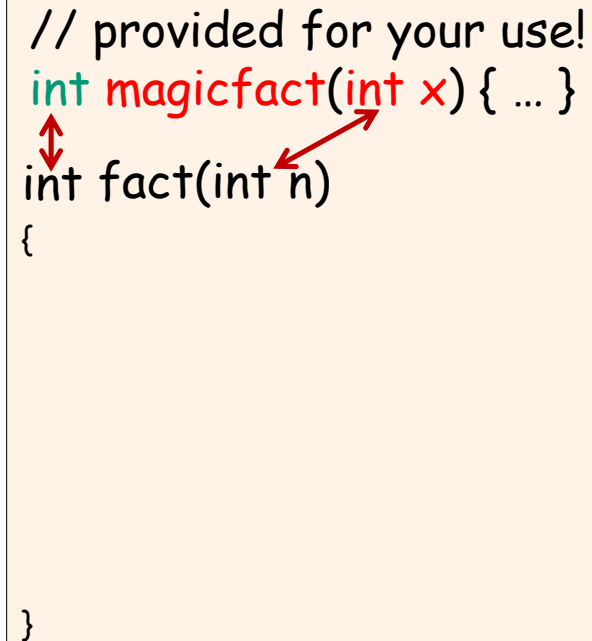
There's only one catch! You are **forbidden** from passing in a value of **n** to this magic function.

So you can't use it to compute **n!**

But you can use it to solve smaller problems, like **(n-1)!** or **(n/2)!**, etc.

Show how you could use this **magic function** to compute **(n-1)!**.

```
// provided for your use!  
int magicfact(int x) { ... }  
↑  
int fact(int n)  
{  
  
}  
}
```



```
int main()  
{  
    int n = 6, result;  
    // use magicfact to solve subproblems  
    result = magicfact( n-1 );  
}
```

Step #3: Add your base case Code

Determine your *base case(s)* and write the code to handle them *without recursion!*

Our goal in this step is to *identify* the *simplest possible input(s)* to our function...

And then have our function *process* those *input(s)* *without calling itself* (i.e., just like a normal function would).

Ok, so what is the *simplest factorial* we might be asked to compute?

Well, the user could pass *0* into our function.

0!, by definition, is equal to *1*.

Let's add a check for this and handle it *without using any recursion*.

In this example, this is the only base condition, but some problems may require 2 or 3 different checks.

```
// provided for your use!  
int magicfact(int x) { ... }  
  
int fact(int n)  
{  
    if (n == 0)  
        return 1; // base case  
  
    // Always consider all possible  
    // base cases and add checks  
    // for them before proceeding!  
}
```

```
int main()  
{  
    int n = 6, result;  
    // use magicfact to solve subproblems  
    result = magicfact( n-1 );  
}
```

Step #4: Solve the problem using the magic function

Now try to figure out how to use the **magic function** in your new function to help you solve the problem.

Unfortunately, you can't use the **magic function** to do all the work for you...
(it can't solve problems of size **n**)

So let's try to break our problem into **two** (or more) simpler sub-problems and use our magic function to solve those.

Well, by definition, $N! = N * (N-1)!$
So it's already split into two parts for us, & each part is simpler than the original problem.

Let's figure out a way to solve each of these sub-problems.

Cool! Now we can combine the results of our sub-problems to get the overall result!

```
// provided for your use!  
int magicfact(int x) { ... }  
  
int fact(int n)  
{  
    if (n == 0)  
        return 1; // base case  
  
    int part1 = n;  
    int part2 = magicfact( n-1 );  
  
    return part1 * part2;  
}
```

```
int main()  
{  
    int n = 6, result;  
  
    // use magicfact to solve subproblems  
    result = magicfact( n-1 );  
  
}
```

Step #5: Remove the n

OK, so let's see what this **magic function** really looks like!

Wait a second! Our **magicfact** function basically just calls **fact**!

That means that **fact** is really just calling itself!

The **magicfact** function hid this from us, but that's what's really happening!

OK, well in that case, let's replace our call(s) to the magic function with calls directly to our own function.

Will that work? **Yup!**

Woohoo! We've just created our first **recursive function** from scratch!



```
int magicfact(int x)
{
    return fact(x);
}
```

```
// provided for your use!
int magicfact(int x) { ... }

int fact(int n)
{
    if (n == 0)
        return 1; // base case

    int part1 = n;
    int part2 = magicfact( n-1 );
    return part1 * part2;
}
```

```
int main()
{
    int n = 6, result;
    // use magicfact to solve subproblems
    result = magicfact( n-1 );
}
```


Step #6: Validating our Function

You SHOULD do this step **EVERY** time you write a recursive function!

Start by testing your function with the **simplest possible input**.

Next test your function with **incrementally more complex inputs**.
(You can usually stop once you've validated at least one recursive call)

```
int fact(int n)
{
    if (n == 0)
        return 1;

    return n * fact(n-1);
}
```

Excellent! We've tested all of the base case(s) as well as validated a single level of recursion...

We can be pretty certain our function works now...

```
int fact(int n)
{
    if (n == 0)
        return 1;

    return n * fact(n-1);
}
```

```
int main()
{
    cout << fact( 0 );
    cout << fact( 1 );
}
```

Factorial Trace-through

```
int fact(int n)    n 0
{
    if (n == 0)
        return (1);

    return(n * fact(n-1));
}
```

```
int fact(int n)    n 1
{
    if (n == 0)
        return (1);

    return(n * fact(n-1));
}
```

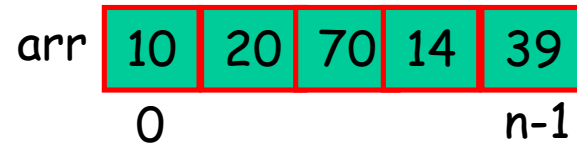
```
int fact(int n)    n 2
{
    if (n == 0)
        return (1);

    return(n * fact(n-1));
}
```

```
int main()
{
    int result;
    result = fact(2);
    cout << result;
}
```

Example #2: Recursion on an Array

For our next example, let's learn how to use recursion to get the sum of all the items in an array.



Step #1: Write the

Figure out what **argument(s)** your function will take and what it needs to **return** (if anything).

To sum up all of the items in an array, we need a **pointer to the array** and its **size**.

Our function will return the total sum of items in the array, so we can make the return type an **int**.

And here's how we'd call our array-summer function to solve a problem of **size n**...

So far, so good.

Let's go on to step #2.

You could also have written:
int *arr
It's the same thing!

```
int sumArr(int arr[ ], int n)
{

```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16}, s;
    s = sumArr( arr , n);           // whole array

```

Step #2: Define your magic function

Pretend that you are given a **magic function** that sums up the values in an array and returns the result...

There's only one catch! You are **forbidden** from passing in an array with **n elements** to this function.

So you can't use it to sum up an entire array (**one with all n items**)...

```
// provided for your use!
int magicsumArr(int arr[], int x) { ... }
↕
int sumArr(int arr[], int n)
{
}
↗
```

But you can use it to sum up smaller arrays (e.g., with **n-1** elements)!

Show how to use the **magic function** to sum the **first n-1** items of the array.

Now show how to use the **magic function** to sum the **last n-1** items of the array.

Now show how to use the **magic function** to sum the **first half** of the array.

Finally show how to use the **magic function** to sum the **last half** of the array.

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16 }, s;

    s = magicsumArr( arr, n-1 ); // first n-1
    s = magicsumArr( arr+1, n-1 ); // last n-1
    s = magicsumArr( arr, n/2 ); // sums 1st half
    s = magicsumArr( arr+n/2, n-n/2 ); // 2nd half
}
```

Step #3: Add your base case Code

Determine your **base case(s)** and write the code to handle them *without recursion!*

Ok, so what is the smallest array that might be passed into our function?

Well, someone could pass in a **totally empty array** of size **n = 0**. What should we do in that case?

Well, what's the sum of an empty array? Obviously it's **zero**. Let's add the code to deal with this case.

Do we have any other base cases? For example, what if the user passes in an array with **just one element**?

Let's see what that would look like...

Good. Let's keep both of those.

```
// provided for your use!
int magicsumArr(int arr[], int x) { ... }

int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
}
```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16 }, s;

    s = magicsumArr( arr, n-1 ); // first n-1
    s = magicsumArr( arr+1, n-1 ); // last n-1
    s = magicsumArr( arr, n/2 ); // sums 1st half
    s = magicsumArr( arr+n/2, n-n/2 ); // 2nd
}
```

Step #4: Solve the problem using the magic function

Now try to figure out how to use the **magic function** in your new function to help you solve the problem.

Unfortunately, you can't use the **magic function** to do all the work for you...
(it can't solve problems of size **n**)

So let's try to break our problem into **two** (or more) simpler sub-problems and use our magic function to solve those.

```
// provided for your use!
int magicsumArr(int arr[], int x) { ... }

int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int s = magicsumArr(arr, n);
    return s;
}
```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16 }, s;

    s = magicsumArr(arr, n-1); // first n-1
    s = magicsumArr(arr+1, n-1); // last n-1
    s = magicsumArr(arr, n/2); // sums 1st half
    s = magicsumArr(arr+n/2, n-n/2); // 2nd
}
```


Step #4: Solve the problem using the magic function

Now try to figure out how to use the **magic function** in your new function to help you solve the problem.

Unfortunately, you can't use the **magic function** to do all the work for you... (it can't solve problems of size **n**)

So let's try to break our problem into **two** (or more) simpler sub-problems and use our magic function to solve those.

Strategy #1: Front to back

Your function uses the magic function to process the **first n-1** elements of the array, ignoring the **last element**.

Once it gets the result from the magic function, it combines it with the **last element** in the array.

It then returns the full result.

```
// provided for your use!
int magicsumArr(int arr[], int x) { ... }

int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int front = magicsumArr(arr, n-1);
    int total = front + arr[n-1];
    return total;
}
```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16 }, s;

    s = magicsumArr(arr, n-1); // first n-1
    s = magicsumArr(arr+1, n-1); // last n-1
    s = magicsumArr(arr, n/2); // sums 1st half
    s = magicsumArr(arr+n/2, n-n/2); // 2nd
}
```

Step #4: Solve the problem using the magic function

Now try to figure out how to use the **magic function** in your new function to help you solve the problem.

Unfortunately, you can't use the **magic function** to do all the work for you... (it can't solve problems of size **n**)

So let's try to break our problem into **two** (or more) simpler sub-problems and use our magic function to solve those.

Strategy #2: Back to front

Your function uses the magic function to process the **last n-1** elements of the array, ignoring the **first element**.

Once it gets the result from the magic function, it combines it with the **first element** in the array.

It then returns the full result.

```
// provided for your use!
int magicsumArr(int arr[], int x) { ... }

int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int rear = magicsumArr( arr+1, n-1 );
    int total = a[0] + rear;
    return total;
}
```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16}, s;

    s = magicsumArr( arr, n-1 ); // first n-1
    s = magicsumArr( arr+1, n-1 ); // last n-1
    s = magicsumArr( arr, n/2 ); // sums 1st half
    s = magicsumArr( arr+n/2, n - n/2 ); // 2nd
}
```

Step #4: Solve the problem using the magic function

Now try to figure out how to use the **magic function** in your new function to help you solve the problem.

Unfortunately, you can't use the **magic function** to do all the work for you...
(it can't solve problems of size **n**)

So let's try to break our problem into **two** (or more) simpler sub-problems and use our magic function to solve those.

Strategy #3: Divide and conquer

Your function uses the magic function to process the **first half** of the array.

Your function uses the magic function to process the **last half** of the array.

Once it gets both results, it combines them and returns the full result.

```
// provided for your use!
int magicsumArr(int arr[], int x) { ... }

int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];

    int first = magicsumArr( arr, n/2 );
    int last = magicsumArr( arr+n/2,
                           n - n/2 );
    return first + last;
}
```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16 }, s;

    s = magicsumArr( arr, n-1 ); // first n-1
    s = magicsumArr( arr+1, n-1 ); // last n-1
    s = magicsumArr( arr, n/2 ); // sums 1st half
    s = magicsumArr( arr+n/2, n - n/2 ); // 2nd
}
```

```
int magicsumArr(int arr[], int x)
{
    return sumArr(arr, x);
}
```

ve the magic

OK, so let's see what this **magic function** really looks like!

Wait a second! Our **magicsumArr** function just calls **sumArr**!

This means that **sumArr** is really just calling itself!

The **magic** function hid this from us, but that's what's really happening!

OK, well in that case, let's replace our calls to the magic function with calls directly to our own function.

Will that work? **Yup!**

Woohoo! We've just created our second **recursive function**!

// provided for your use!

```
int magicsumArr(int arr[], int x) { ... }

int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];

    int first = magicsumArr(arr, n/2);
    int scnd = magicsumArr(arr+n/2, n-n/2);
    return first + scnd;
}
```

```
int main()
{
    const int n = 5;
    int arr[n] = { 10, 100, 42, 72, 16 }, s;

    s = magicsumArr(arr, n-1); // first n-1
    s = magicsumArr(arr+1, n-1); // last n-1
    s = magicsumArr(arr, n/2); // sums 1st half
    s = magicsumArr(arr+n/2, n-n/2); // 2nd
}
```

Step #6: Validating our Function

As before, make sure to test your function with at least one input that exercises the base case...

and one input that causes a recursive call.

```
int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int first = sumArr( arr, n/2 );
    int scnd = sumArr( arr+n/2, n-n/2);
    return first + scnd;
}
```

```
int main()
{
    int arr[2] = { 10, 20 };

    cout << sumArr( arr, 0 );

    cout << sumArr( arr, 2 );
}
```

Array-summer Trace-through

```
int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int first = sumArr( arr, n/2 );
    int scnd = sumArr( arr+n/2, n-n/2);
    return first + scnd;
}
```

```
int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int first = sumArr( arr, n/2 );
    int scnd = sumArr( arr+n/2, n-n/2);
    return first + scnd;
}
```

```
int sumArr(int arr[], int n)
{
    if (n == 0) return 0;
    if (n == 1) return arr[0];
    int first = sumArr( arr, n/2 );
    int scnd = sumArr( arr+n/2, n-n/2);
    return first + scnd;
}
```

```
int main()
{
    const int n = 3;
    int nums[n] = { 10, 20, 42 };

    cout << sumArr( nums , n );
}
```

Your Turn: Recursion Challenge

Write a **recursive** function called **printArr** that prints out an array of integers in reverse from **bottom** to **top**.

Step #1:

Write the function header

Step #2:

Define your magic function

Step #3:

Add your base case code

Step #4:

Solve the problem w/the magic function

Step #5:

Remove the magic

Step #6:

Validate your function

Recursion Challenge

Step #1: Write the function header

Step #2: Define your magic function

Step #3: Add your base case code

Step #4: Solve the problem using
your magic function

Step #5: Remove the magic

Step #6: Validate your function

Write a **recursive**
function called **printArr**
that prints out an array
from **bottom** to **top**.

```
int main()
{
    const int size = 5;
    int arr[size] = {7, 9, 6, 2, 4};

}
```

Recursion

names		
[0]	Leslie	2000
[1]	Phyllis	2020
[2]	Nan	2040

```
38 void reversePrint(string arr[ ], int size)
{
    if (size == 0) // an empty array
        return;
    else
    {
        reversePrint(arr + 1, size - 1 );
        cout << arr[0] << "\n";
    }
}
```

```

{
    if (size == 0) // an empty array
        return;
    else
    {
        reversePrint(arr + 1, size - 1 );
        cout << arr[0] << "\n";
    }
}
```

```

{
    if (size == 0) // an empty array
        return;
    else
    {
        reversePrint(arr + 1, size - 1 );
        cout << arr[0] << "\n";
    }
}
```

```
main()
{
    string names[3];
    ...
    reversePrint(names,3);
}
```

Recursion

```
39 void reversePrint(string arr[ ], int size)
{
    if (size == 0) // an empty array
        return;
    else
    {
        reversePrint(arr + 1, size - 1);
        cout << arr[0] << "\n";
    }
}
```

arr 2040
size 1

names

[0]	Leslie	2000
[1]	Phyllis	2020
[2]	Nan	2040

```
    if (size == 0) // an empty array
        return;
    else
    {
        reversePrint(arr + 1, size - 1);
        cout << arr[0] << "\n";
    }
}
```

arr 2020
size 2

```
    if (size == 0) // an empty array
        return;
    else
    {
        reversePrint(arr + 1, size - 1);
        cout << arr[0] << "\n";
    }
}
```

arr 2000
size 3

```
main()
{
    string names[3];
    ...
    reversePrint(names,3);
}
```

Recursion

```
void reversePrint(string arr[ ], int size)
```

```
{  
    if (size == 0) // an empty array
```

arr [0] is
" Nan "

```
    reversePrint(arr + 1, size - 1);  
    cout << arr[0] << "\n";  
}
```

arr 2040
size 1

names		
[0]	Leslie	2000
[1]	Phyllis	2020
[2]	Nan	2040

```
if (size == 0) // an empty array
```

arr [0] is
" Phyllis "

```
    reversePrint(arr + 1, size - 1);  
    cout << arr[0] << "\n";  
}
```

arr 2020
size 2

```
if (size == 0) // an empty array
```

arr [0] is
" Leslie "

```
    reversePrint(arr + 1, size - 1);  
    cout << arr[0] << "\n";  
}
```

arr 2000
size 3

```
main()
```

```
{  
    string names[3];  
    ...  
    reversePrint(names, 3);  
}
```

Example #3: Recursion on a Linked List

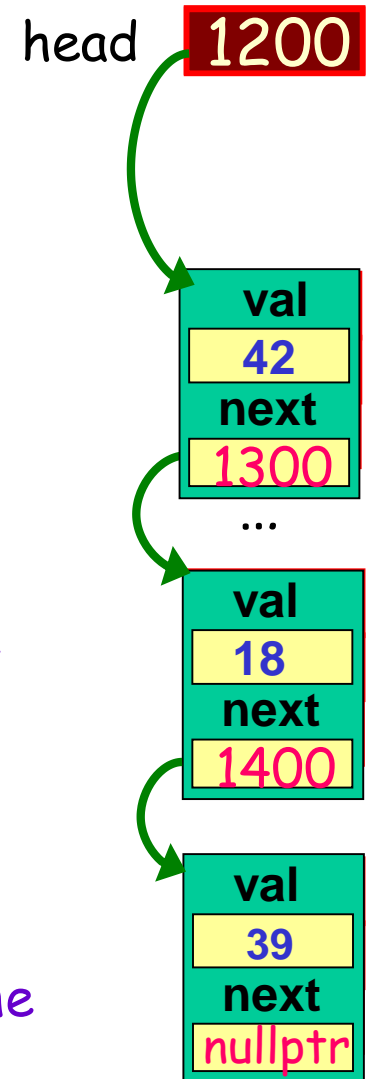
When we process a **linked list** using recursion, it's very much like processing an **array using strategy #2**!

```
struct Node
{
    int val;
    Node *next;
};
```

There are two differences:

1. Instead of passing in a **pointer to an array element**, you pass in a **pointer to a node**
2. You **don't** need to pass in a **size value** for your list (this is determined via the **next** pointers)

Let's see an example. We'll write a function that **finds the biggest number** in a **NON-EMPTY** linked list.



Step #1: Write the function header

Figure out what **argument(s)** your function will take and what it needs to **return** (if anything).

To find the biggest item in a linked list, what kind of parameter should we pass to our function?

Right! All we need to pass in is a **pointer to a node** of the linked list.

Our function will return the biggest value in the list, so we can make the return type an **int**.

So far, so good. Let's go on to step #2.

```
struct Node
{
    int val;
    Node *next;
};

int biggest( Node *cur )
{
}
}
```

Step #2: Define your magic function

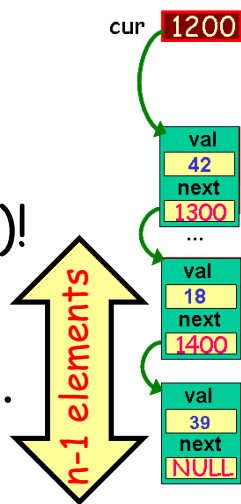
Pretend that you are given a **magic function** that finds the biggest value in a linked list and returns it...

There's only one catch! You are **forbidden** from passing in a full linked list with **all n elements** to this function.

So you can't use it to find the biggest item in the entire list (**one with all n items**)...

But you can use it to find the biggest item in a partial list (e.g., with **n-1 elements**)!

Let's see how to do this.



```

struct Node
{
    int val;
    Node *next;
};

// provided for your use!
int magicbiggest(Node *n) { ... }

↕
int biggest( Node *cur )
{
    }
  
```

```

int main()
{
    Node *cur = createLinkedList();
    int biggest = magicbiggest(cur->next);
}
  
```

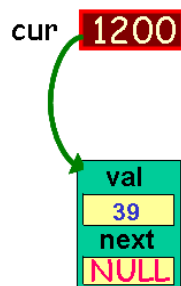
Step #3: Add your base case Code

Determine your **base case(s)** and write the code to handle them *without recursion!*

For this problem, we're assuming that the user must pass in a linked list with **at least one element**.

So, what's the **simplest case** that our function must handle?

Well, if a linked list **has only one node**...



Then by *definition* that node *must* hold the biggest (only!) value in the list, right?

Are there any other base cases?

```

struct Node
{
    int val;
    Node *next;
};

// provided for your use!
int magicbiggest(Node *n) { ... }

int biggest( Node *cur )
{
    if (cur->next == nullptr) // the only node
        return cur->val; // so return its value
}
  
```

```

int main()
{
    Node *cur = createLinkedList();
    int biggest = magicbiggest(cur->next);
}
  
```


Step #4: Solve the problem using the magic function

Now try to figure out how to use the **magic function** in your new function to help you solve the problem.

Unfortunately, you can't use the **magic function** to process **all n nodes** of the list.

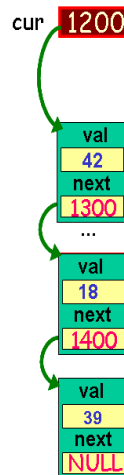
So let's break our problem into **two** (or more) simpler sub-problems and use our magic function to solve those.

Strategy for Linked Lists:

Use the magic function to process the **last n-1** elements of the list, ignoring the **first element**.

Once you get a result from the magic function for the **last n-1** nodes, combine it with the **first element** in the list.

Then return the full result.



```

struct Node
{
    int val;
    Node *next;
};

// provided for your use!
int magicbiggest(Node *n) { ... }

int biggest( Node *cur )
{
    if (cur->next == nullptr) // the only node
        return cur->val; // so return its value

    int rest = magicbiggest(cur->next);
    // pick biggest of 1st node and last n-1 nodes
    return max( rest , cur->val );
}
  
```

```

int main()
{
    Node *cur = createLinkedList();
    int biggest = magicbiggest(cur->next);
}
  
```

Step #5: Remove the

OK, so let's see what this **magic function** really looks like!

Wait a second! Our **magicbiggest** function just calls **biggest**!

That means our **biggest** function is really just calling itself!

The **magic** function hid this from us, but that's what's really happening!

OK, well in that case, let's replace our calls to the magic function with calls directly to our own function.

Will that work? **Yup!**

Woohoo! We've just created our third **recursive function**!

```
int magicbiggest(Node *n)
{
    return biggest(n);
}
```

```
Node *next;
};

// provided for your use!
int magicbiggest(Node *n) { ... }

int biggest( Node *cur )
{
    if (cur->next == nullptr) // the only node
        return cur->val; // so return its value

    int rest = magicbiggest(cur->next);
    // pick biggest of 1st node and last n-1 nodes
    return max( rest , cur->val );
}
```

```
int main()
{
    Node *cur = createLinkedList();
    int biggest = magicbiggest(cur->next);
}
```

Step #6: Validating our Function

Don't forget to test your function!

Since the problem states that the list is never empty...

The two simplest test cases would be a
one-node list and a **two-node list**!

```
int biggest( Node *cur )
{
    if (cur->next == nullptr) // the only node
        return cur->val; // so return its value

    int rest = biggest( cur->next );
    return max ( rest, cur->val );
}
```

```
int main()
{
    Node *head1 = mkLstWith1Item();

    cout << biggest( head1 );

    Node *head2 = mkLstWith2Items();

    cout << biggest( head2 );
}
```

```

int biggest(Node *cur)
{
    if (cur->next == nullptr)
        return(cur->val);

    int rest = biggest( cur->next );
    return max( rest, cur->val );
}

```

```

int biggest(Node *cur)
{
    if (cur->next == nullptr)
        return(cur->val);

    int rest = biggest( cur->next );
    return max( rest, cur->val );
}

```

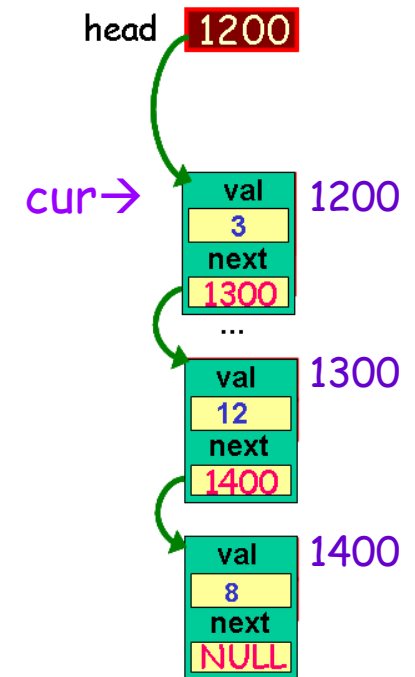
```

int biggest(Node *cur)
{
    if (cur->next == nullptr)
        return(cur->val);

    int rest = biggest( cur->next );
    return max( rest, cur->val );
}

```

Biggest-in-List Trace-through



```

main()
{
    Node *head;

    ... // create linked list
    cout << biggest(head);
}

```

Writing Recursive Functions: **A Critical Tip!**

Your recursive function should generally **only access** the **current node/array cell** passed into it!

Your recursive function should **rarely/never** access the value(s) in the **node(s)/cell(s) below** it!

// good examples!

```
int recursiveGood(Node *p)
{
    ...
    if (p->value == someValue)
        do something;

    if (p == nullptr || p->next == nullptr)
        do something;

    int v = p->value +
        recursiveGood(p->next);

    if (p->value > recursiveGood(p->next))
        do something;
}
```

// bad examples!!!

```
int recursiveBad(Node *p)
{
    ...
    if (p->next->value == someValue)
        do something;

    if (p->next->next == nullptr)
        do something;

    int v = p->value + p->next->value +
        recursiveBad(p->next->next);

    if (p->value > p->next->value)
        do something;
}
```

Writing Recursive Functions: **A Critical Tip!**

Your recursive function should generally **only access** the **current node/array cell** passed into it!

// good examples!

```
int recursiveGood(int a[], int count)
{
```

```
    ...
    if (count == 0 || count == 1)
        do something;
```

```
    if (a[0] == someValue)
        do something;
```

```
    int v = a[0] +
        recursiveGood(a+1, count-1);
```

```
    if (a[0] > recursiveGood(a+1, count-1))
        do something;
```

```
}
```

Your recursive function should **rarely/never** access the value(s) in the **node(s)/cell(s) below** it!

// bad examples!!!

```
int recursiveBad(int a[], int count)
{
```

```
    ...
    if (count == 2)
        do something;
```

```
    if (a[1] == someValue)
        do something;
```

```
    int v = a[0] + a[1] +
        recursiveBad(a+2, count-2);
```

```
    if (a[0] > a[1])
        recursiveBad(a+2, count-2);
```

```
}
```

Recursion Challenge #2

Write a **recursive** function called **count** that counts the number of times a number appears in an array.

```
main()
{
    const int size = 5;
    int arr[size] = {7, 9, 6, 7, 7};

    cout << countNums(arr, size, 7);
    // should print 3
}
```

Recursion Challenge #2

Step #1: Write the function header

Step #2: Define your magic function

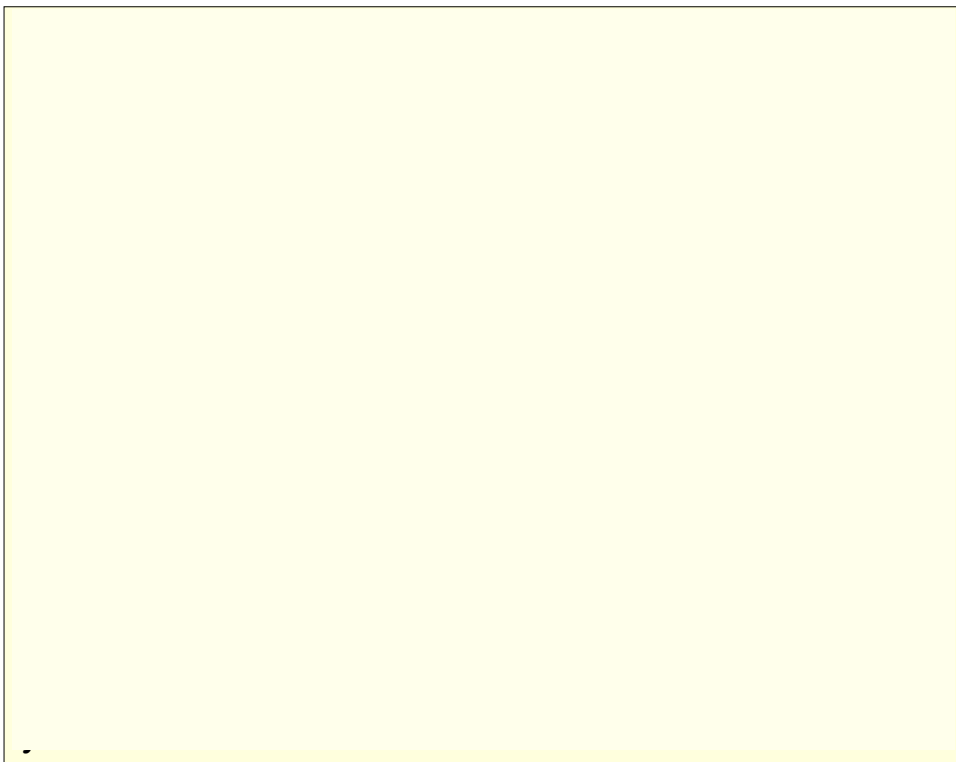
Step #3: Add your base case code

Step #4: Solve the problem using
your magic function

Step #5: Remove the magic!

Step #6: Validate your function

Write a **recursive**
function called
count that counts
the number of
times a number
appears in an array.

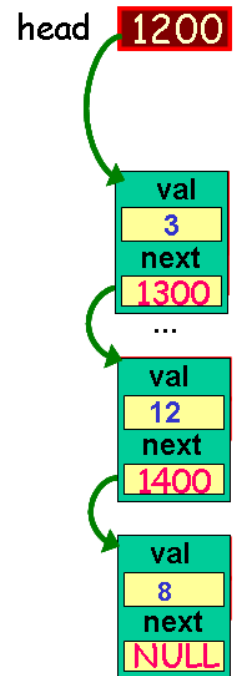


Recursion Challenge #3

Write a function that finds and returns the earliest position of a number in a linked list. If the number is not in the list or the list is empty, your function should return -1 to indicate this.

```
main()
{
    Node *cur = <make a linked list>;

    cout << findPos(cur,3); // prints 0
    cout << findPos(cur,8); // prints 2
    cout << findPos(cur,19); // prints -1
}
```



- Step #1: Write the function header
- Step #2: Define your magic function
- Step #3: Add your base case code
- Step #4: Solve the problem using your magic function
- Step #5: Remove the magic!
- Step #6: Validate your function

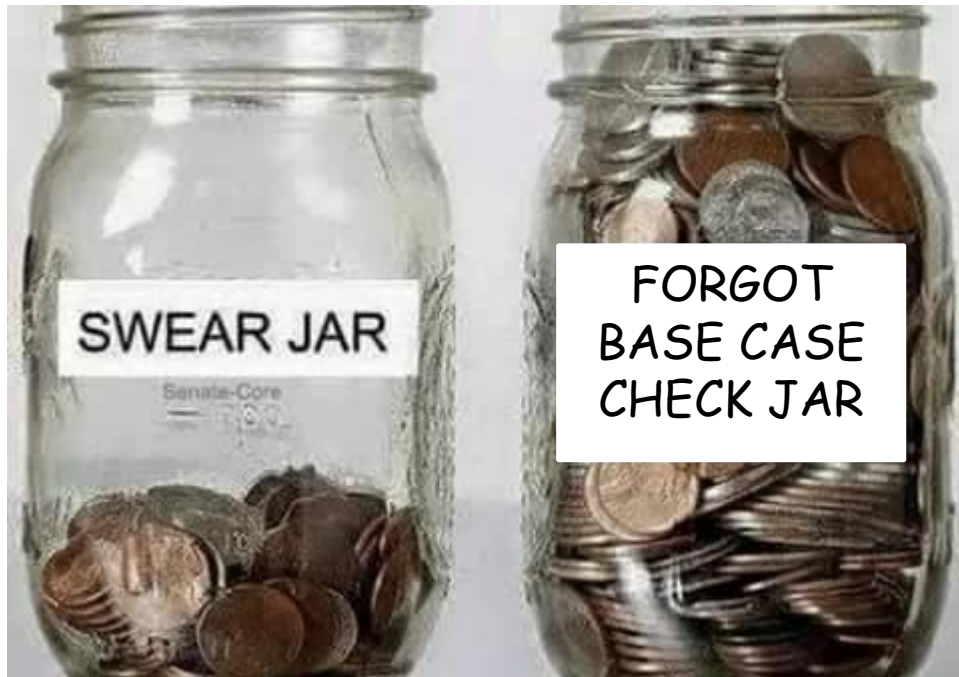
Recursion Challenge #3

Write a function that finds and returns the earliest position of a number in a linked list. If the number is not in the list or the list is empty, your function should return -1 to indicate this.

Let's see some REAL examples!

Ok, enough with the **toy recursion examples**!

Let's see some situations where **recursion really shines**!



Recursion: Binary Search

Goal: Search a *sorted* array of data for a particular item.

Idea: Use recursion and a divide-and-conquer approach!

Pseudocode:

```
bool Search(sortedArray, findMe)
{
    if (array.size == 0) // empty array
        return false;

    middle_word = sortedArray.size / 2;
    if (findMe == sortedArray[middle_word])
        return true;

    if (findMe < sortedArray[middle_word])
        return Search( first ½ of sortedArray );
    else // findWord > middle word
        return Search( second ½ of sortedArray );
}
```

Notice how Binary Search code recurses on **either** the **first half** **or** the **second half** of the array... **But never both**. This is for **efficiency**.

Binary Search: C++ Code

Here's a real [binary search](#) implementation in C++. Let's see how it works!

```
int BS(string A[], int top, int bot, string f)
{
    if (numItemsBetween(top, bot) == 0)
        return (-1);    // Value not found
    else
    {
        int Mid = (top + bot) / 2;
        if (f == A[Mid])
            return Mid; // found - return where!
        else if (f < A[Mid])
            return BS(A, top, Mid - 1, f);
        else if (f > A[Mid])
            return BS(A, Mid + 1, bot, f);
    }
}
```

Recursive Binary Search

As our binary search progresses, **top** will move **down** and **bot** will move **up**.

If the # of items between them is zero, it means our value was not in the array.

```
int BS(string A[], int top, int bot, string f)
{
    if (numItemsBetween(top, bot) == 0)
        return (-1);    // Value not found
    else
    {
        int Mid = (top + bot) / 2;
        if (f == A[Mid])
            return Mid; // found - return where!
        else if (f < A[Mid])
            return BS(A, top, Mid - 1, f);
        else if (f > A[Mid])
            return BS(A, Mid + 1, bot, f);
    }
}
```

top ➡ 0	Albert
1	Brandy
2	Carol
3	David
4	Eugene
Mid ➡ 5	Frank
6	Gordon
7	Grendel
8	Hank
9	Wayne
bot ➡ 10	Yentle

```
= {"Albert", ...};

, "David") != -1)
    it!";
```

Recursion: Binary Search

```
int BS(string A[], int top, int bot, string f)
{
    if (numItemsBetween(top, bot) == 0)
        return (-1);    // Value not found
    else
    {
        int Mid = (top + bot) / 2;
        if (f == A[Mid])
            return Mid; // found - return where!
        else if (f < A[Mid])
            return BS(A, top, Mid - 1, f);
        else if (f > A[Mid])
            return BS(A, Mid + 1, bot, f);
    }
}
```

```
    return BS(A, top, Mid - 1, f);
else if (f > A[Mid])
    return BS(A, Mid + 1, bot, f);
}
```

top ➡ 0	Albert
1	Brandy
Mid ➡ 2	Carol
3	David
4	Eugene
Mid ➡ 5	Frank
6	Gordon
7	Grendel
8	Hank
9	Wayne
bot ➡ 10	Yentle

```
= {"Albert", ...};
, "David") != -1)
it!";
```

Recursion: Binary Search

```
int BS(string A[], int top, int bot, string f)
{
    if (numItemsBetween(top, bot) == 0)
        return (-1);    // Value not found
    else
    {
        int Mid = (top + bot) / 2;
        if (f == A[Mid])
            return Mid; // found - return where!
        else if (f < A[Mid])
            return BS(A, top, Mid - 1, f);
        else if (f > A[Mid])
            return BS(A, Mid + 1, bot, f);
    }
}
```

top → 0

1

Mid → 2

3

bot → 4

5

6

7

8

9

10

Albert

Brandy

Carol

David

Eugene

Frank

Gordon

Grendel

Hank

Wayne

Yentle

→ return

;

{"Albert", ...};

"David") != -1)

it!";

61 Recursion: Binary Search

```
int BS(string A[], int top, int bot, string f)
{
    if (numItemsBetween(top, bot) == 0)
        return (-1);    // Value not found
    else
    {
        int Mid = (top + bot) / 2;
        if (f == A[Mid])
            return Mid; // found - return where!
        else if (f < A[Mid])
            return BS(A, top, Mid - 1, f);
        else if (f > A[Mid])
            return BS(A, Mid + 1, bot, f);
    }
}
```

top ➡ 0	Albert
1	Brandy
Mid ➡ 2	Carol
3	David
bot ➡ 4	Eugene
5	Frank
6	Gordon
7	Grendel
8	Hank
9	Wayne
10	Yentle

{"Albert",...};

"David") != -1)
it!";

Recursion: Binary Search

top ➡ 0	Albert
1	Brandy
2	Carol
3	David
4	Eugene
Mid ➡ 5	Frank
6	Gordon
7	Grendel
8	Hank
9	Wayne
bot ➡ 10	Yentle

```
int BS(string A[], int top, int bot, string f)
{
    if (numItemsBetween(top, bot) == 0)
        return (-1);    // Value not found
    else
    {
        int Mid = (top + bot) / 2;
        if (f == A[Mid])
            return Mid; // found - return where!
        else if (f < A[Mid])
            return BS(A, top, Mid - 1, f);
        else if (f > A[Mid])
            return BS(A, Mid + 1, bot, f);
    }
}
```

```
= {"Albert", ...};
, "David") != -1)
    it!";
```

Recursion Helper Functions



So we just saw a recursive version of **Binary Search**:

```
int BS(string A[], int top, int bot, string f)
{
  ...
}
```

Notice how many **crazy parameters** it takes?
What is **top**? What's **bot**? That's going to be really **confusing** for the user!

Wouldn't it be nicer if we just provided our user with a simple function (with a few, obvious params) and then hid the complexity?

```
int SimpleBinarySearch(string A[], int size, string findMe)
{
  return BS(A , 0 , size-1 , findMe);
}
```

This simple function can then call the complex recursive function to do the dirty work, without confusing the user.

Solving a Maze

We can also use **recursion** to find a **solution to a maze**.

In fact, the recursive solution works in the same basic way as the **stack-based solution** we saw earlier.

The algorithm uses recursion to keep **moving down paths** until it hits a **dead end**.

Once it hits a dead end, the function returns until it finds another path to try.

This approach is called "**backtracking**" or "**depth first search**."

Solving a Maze

```
void solve(int sx, int sy)
{
    m[sy][sx] = '#'; // drop crumb
    if (sx == dx && sy == dy)
        solveable = true; // done!
    if (m[sy-1][sx] == ' ')
        solve(sx, sy-1);
    if (m[sy+1][sx] == ' ')
        solve(sx, sy+1);
    if (m[sy][sx-1] == ' ')
        solve(sx-1, sy);
    if (m[sy][sx+1] == ' ')
        solve(sx+1, sy);
}
```

```
    solve(sx, sy+1);
    if (m[sy][sx-1] == ' ')
        solve(sx-1, sy);
    if (m[sy][sx+1] == ' ')
        solve(sx+1, sy);
}
```

```
bool solvable; // globals
int dx, dy;
char m[11][11] = {
    "*****",
    "*               *",
    "* * * ** *",
    "*** * * *",
    "* * ** * *",
    "*       *** *",
    "* *      * *",
    "* ***** *",
    "*          * *",
    "*****"
};

// Start is at (1,1) and Finish is at (10,10)
// The maze is represented by a grid of characters where '*' is a wall and ' ' is a path.
// The start is at (1,1) and the finish is at (10,10).

main()
{
    solvable = false;
    dx = dy = 10;

    solve(1,1);
    if (solvable == true)
        cout << "possible!";
}
```

```
void solve(int sx, int sy)
{
    m[sy][sx] = '#'; // drop crumb
    if (sx == dx && sy == dy)
        solveable = true; // done!
    if (m[sy-1][sx] == ' ')
        solve(sx, sy-1);
    if (m[sy+1][sx] == ' ')
        solve(sx, sy+1);
    if (m[sy][sx-1] == ' ')
        solve(sx-1, sy);
    if (m[sy][sx+1] == ' ')
        solve(sx+1, sy);
}
```

And on it goes...

```
    solve(sx, sy+1);
    if (m[sy][sx-1] == ' ')
        solve(sx-1, sy);
    if (m[sy][sx+1] == ' ')
        solve(sx+1, sy);
}
```

```
    solve(sx+1, sy);
}
```

```
    solve(sx+1, sy);
}
```

```
bool solvable; // globals
int dx, dy;
char m[11][11] = {
    "*****",
    "*               *",
    "* * * * *",
    "*** * * *",
    "* * ** * *",
    "*       *** *",
    "* *   * *",
    "* *****",
    "*       * *",
    "*****"
};

// Finish
};

main()
{
    solvable = false;
    dx = dy = 10;

    solve(1,1);
    if (solvable == true)
        cout << "possible!";
};
```

```

void solve(int sx, int sy)
{
    m[sy][sx] = '#'; // drop crumb
    if (sx == dx && sy == dy)
        solveable = true; // done!
    if (m[sy-1][sx] == ' ')
        solve(sx, sy-1);
    if (m[sy+1][sx] == ' ')
        solve(sx, sy+1);
    if (m[sy][sx-1] == ' ')
        solve(sx-1, sy);
    if (m[sy][sx+1] == ' ')
        solve(sx+1, sy);
}

```

And on it goes...

```

        solve(sx, sy+1);
    if (m[sy][sx-1] == ' ')
        solve(sx-1, sy);
    if (m[sy][sx+1] == ' ')
        solve(sx+1, sy);
}

```

```

    solve(sx+1, sy);
}

```

```

    solve(sx+1, sy);
}

```

```

bool solveable; // globals
int dx, dy;
char m[11][11] = {
    "*****",
    "*#####*",
    "*#*#*#*#",
    "***#*#*#*",
    "*#*#*#*#",
    "*#####*",
    "*###*#####*",
    "*###*#####*",
    "*#####*",
    "*****"
};

```

art →

Finish

```

main()
{
    solveable = false;
    dx = dy = 10;

    → solve(1, 1);
    if (solveable == true)
        cout << "possible!";
}

```

Writing a TicTacToe Player

```
bool gameIsOver()
{
    if (X has three in a row) // X wins
        return true;
    if (O has three in a row) // O wins
        return true;
    if (all squares are filled) // tie game
        return true;

    return false;
}
```

Have you ever wondered
how to build an
intelligent **chess player**?

Let's learn how - but for
simplicity, we'll look at
TicTacToe!

x	o	x
	o	o
	x	

```
GameBoard b;
while (!gameIsOver())
{
    move = getBestMoveForX(); // Get X move from AI
    applyMove('X', move);

    move = GetHumanMove(); // Get O move from human
    applyMove('O', move);
}
```

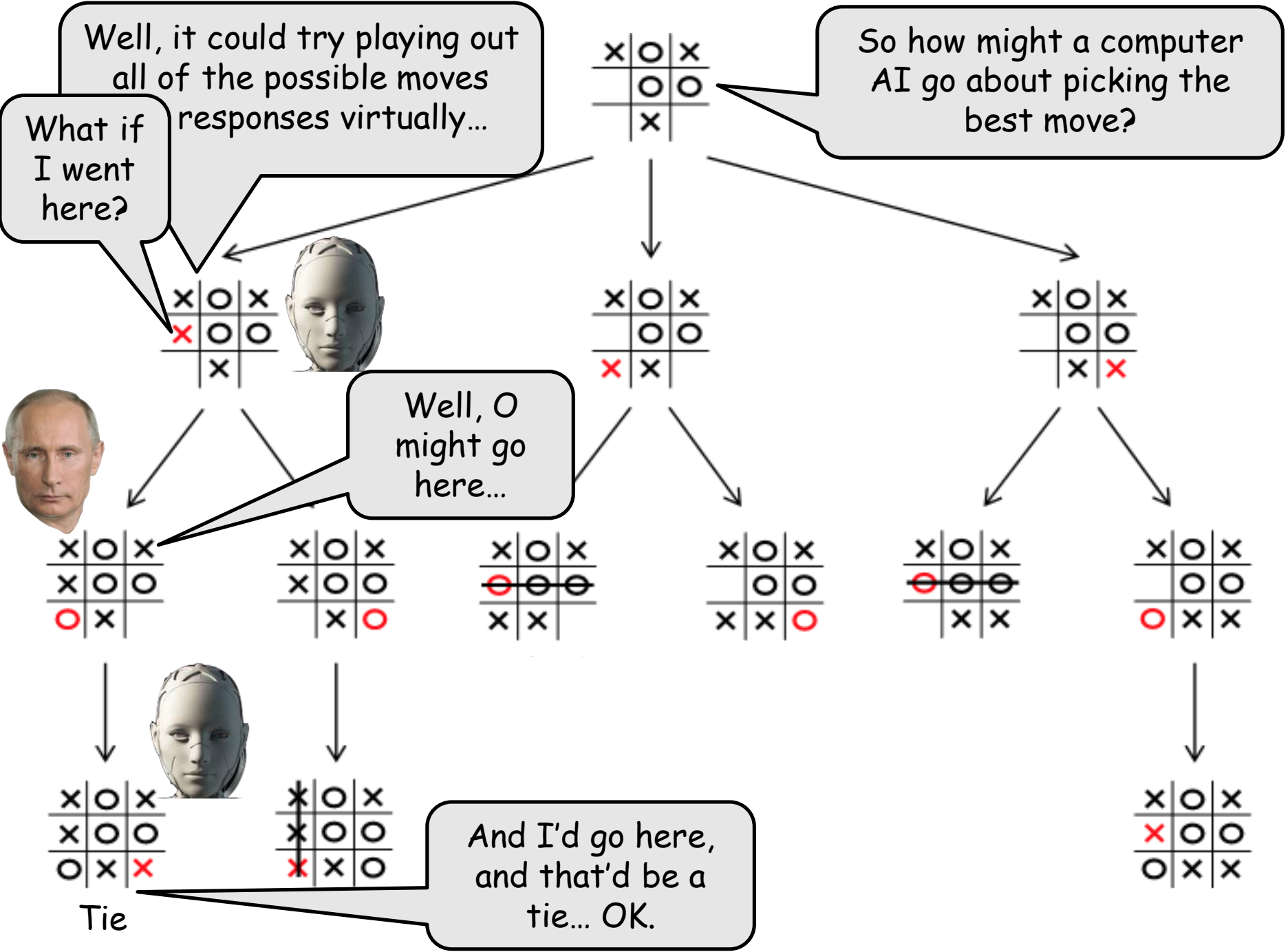

Writing a Tic Tac Toe Player

X	O	X
	O	O
	X	

First, let's see what our game looks like at a high level.

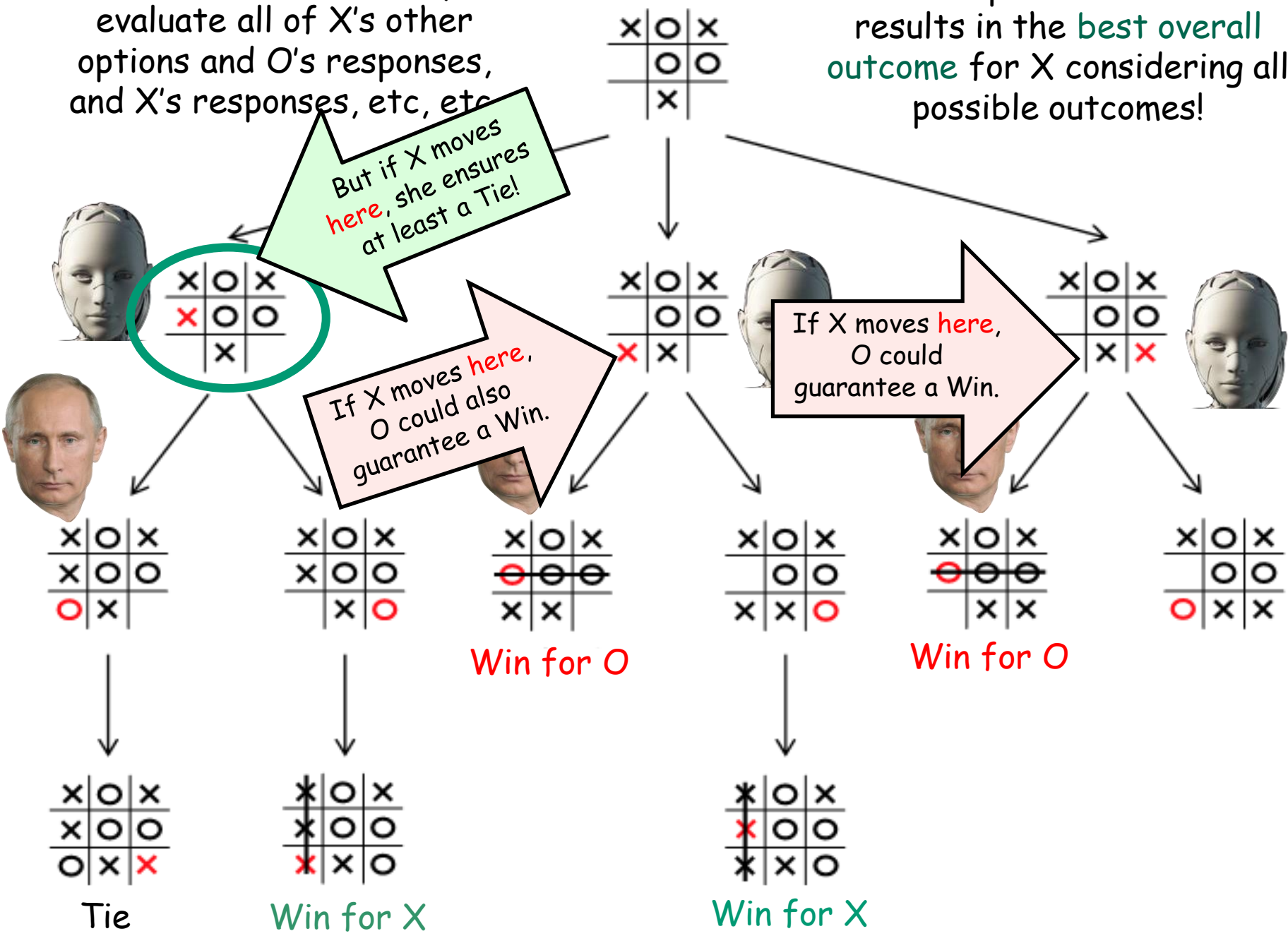
OK, now let's consider how the `getBestMoveForX()` function might work!

```
GameBoard b;  
while (!gameIsOver())  
{  
    move = getBestMoveForX(); // Get X move from AI  
    applyMove('X', move);  
  
    move = GetHumanMove(); // Get O move from human  
    applyMove('O', move);  
}
```



And we could similarly evaluate all of X's other options and O's responses, and X's responses, etc, etc

And then pick the move that results in the **best overall outcome** for X considering all possible outcomes!



So how can we teach a computer to perform this deep evaluation?

Using **recursion**, of course!

x	o	x
	o	o
x		



getBestMoveForX():

1. Try each X move
 - a. If that ends the game, return result
 - b. Otherwise, see how O would respond
2. Return the best move we found for X

getBestMoveForO():

1. Try each O move
 - a. If that ends the game, return result
 - b. Otherwise, see how X would respond
2. Return the best move we found for O

SIMULATED

The function for X calls the function for O...

And the function for O calls the function for X...

getBestMoveForX():

1. Try each X move
 - a. If that ends the game, return result
 - b. Otherwise, see how O would respond
2. Return the best move we found for X

getBestMoveForO():

1. Try each O move
 - a. If that ends the game, return result
 - b. Otherwise, see how X would respond
2. Return the best move we found for O

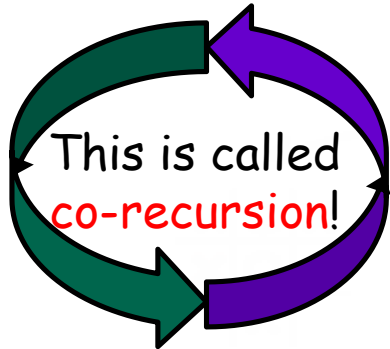
SIMULATED

And the function for X calls the function for O...



Until we hit the bottom...

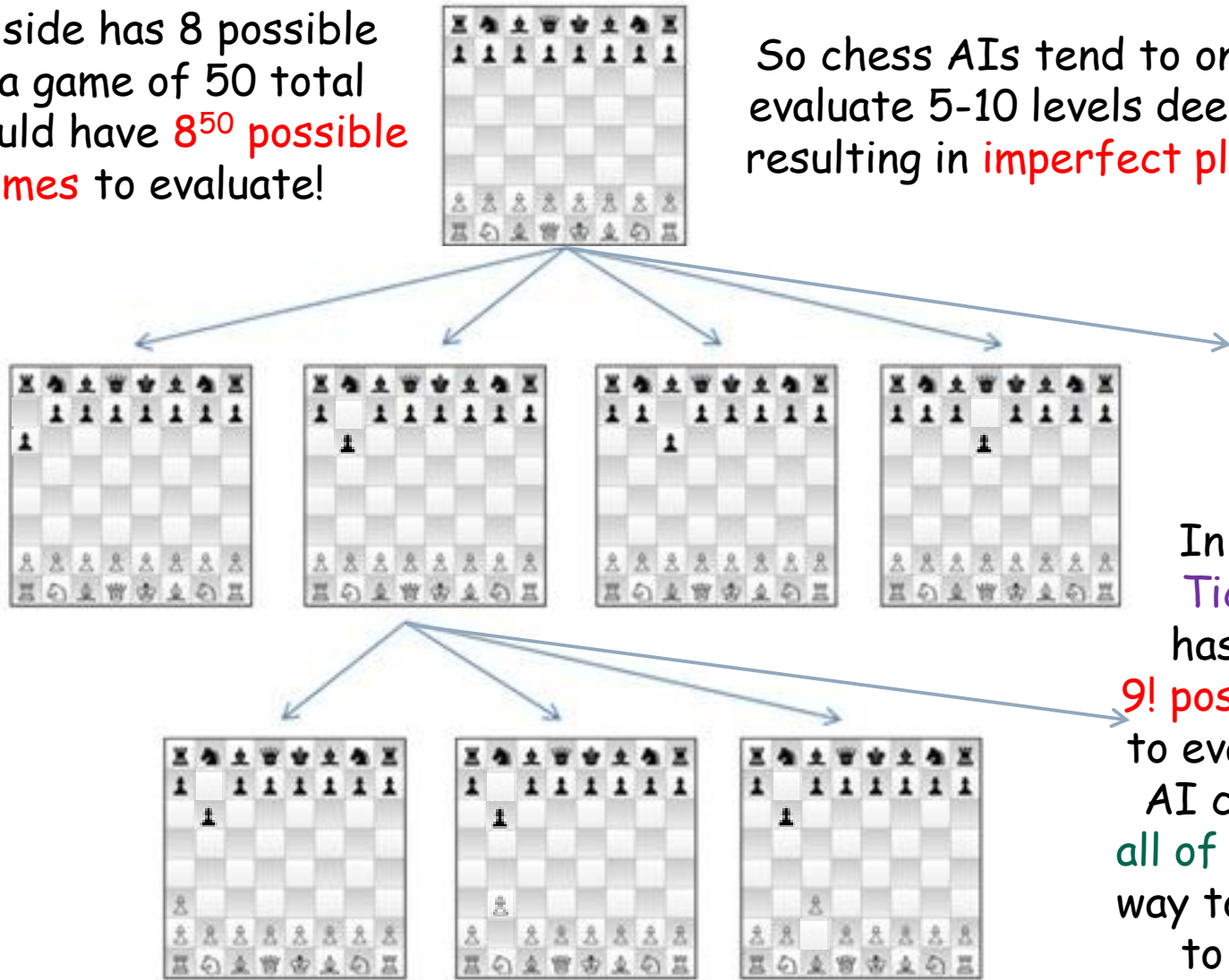
This is called
co-recursion!



Chess Is The Same... But Much Deeper!

If each side has 8 possible moves, a game of 50 total moves would have **8^{50} possible outcomes** to evaluate!

So chess AIs tend to only evaluate 5-10 levels deep... resulting in **imperfect play**.



In contrast, **Tic Tac Toe** has less than **$9!$ possible boards** to evaluate, so an AI can **evaluate all of them**, all the way to the bottom to make the perfect move!

Object Oriented Design

(for on-your-own study)



Object Oriented Programming Design

Why should you care?

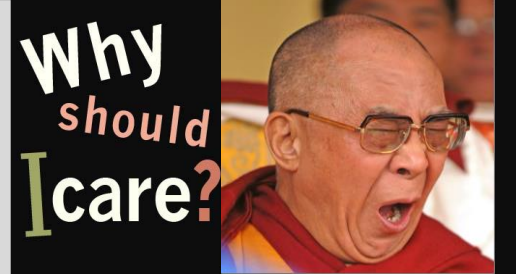
Good software design can dramatically reduce bugs, reduce development time, and simplify team programming.

So far, you've learned the basics of OOP.

But you haven't learned how properly design OOP programs.

It's like the difference between writing simple sentences and writing a great novel.

So go learn this stuff!



Object-Oriented Design

So, how does a computer scientist go about designing a program?

How do you figure out all of the **classes**, **methods**, **algorithms**, etc. that you need for a program?

At a high level, its best to tackle a design in two phases:



First, determine the classes you need, what data they hold, and how they interact with one another.

Second, determine each class's data structures and algorithms.



(Well, it's not easy! Many senior engineers are **horrible** at it!)

Class Design Steps

1. Determine the **classes** and **objects** required to solve your problem.



2. Determine the **outward-facing functionality** of each class. How do you interact with a class?

3. Determine the **data** each of your classes holds and...

4. How they **interact** with each other.



An Example

Often, we start with a **textual specification** of the problem.

For instance, let's consider a spec for an **electronic calendar**.

Each user's calendar should contain appointments for that user. There are two different types of appointments, one-time appts and recurring appts. Users of the calendar can get a list of appointments for the day, add new appointments, remove existing appointments, and check other users' calendars to see if a time-slot is empty. The user of the calendar must supply a password before accessing the calendar. Each appointment has a start-time and an end-time, a list of participants, and a location.

Step #1: Identify Objects

Start by identifying
potential classes.

The easiest way to do this is
identify all of the **nouns** in the
specification!

Each **user's** calendar should contain **appointments** for that user. There are two different types of appointments, **one-time appts** and **recurring appts**. Users of the calendar can get a list of appointments for the day, add new appointments, remove existing appointments, and check other users' calendars to see if a **time-slot** is empty. The user of the calendar must supply a **password** before accessing the calendar. Each appointment has a **start-time** and an **end-time**, a list of **participants**, and a **location**.

Step #1b: Identify Objects

Now that we know our nouns,
let's identify potential classes.

We don't need classes for every
noun, just for those key
components of our system...

Which nouns should we turn
into classes?

Calendar

Appointment

Recurring Appointment

One-time Appointment

user

calendar

password

time-slot

start-time

appointments

recurring appts

one-time appts

participants

location

end-time

Step #2a: Identify Operations

Next we have to determine what actions need to be performed by the system.

To do this, we identify all of the **verb phrases** in the specification!

Each user's calendar should contain appointments for that user. There are two different types of appointments, one-time appts and recurring appts. Users of the calendar can get a list of appointments for the day, add new appointments, remove existing appointments, and check other users' calendars to see if a time-slot is empty. The user of the calendar must **supply a password** before accessing the calendar. Each appointment has a **start-time** and an **end-time**, a list of participants, and a location.

Step #2b: Associate Operations w/Classes

Calendar

```
list getListOfAppts(void)
bool addAppt(Appointment *addme)
bool removeAppt(string &apptName)
bool checkCalendars(Time &slot,
                    Calendar others[])
bool login(string &pass)
bool logout(void)
```

Appointment

```
bool setStartTime(Time &st)
bool setEndTime(Time &st)
bool addParticipant(string &user)
bool setLocation(string &location)
```

Next we have to determine **what actions** go with **which classes**.
(let's just look at the first two)

Verbs

get a list of appointments

add new appointments

remove existing

check other users' calendars

supply a password

has a start-time

has an end-time

has a list of participants

has a location

Step #2b: Associate Operations w/Classes

Calendar

```
Calendar() and ~Calendar()
list getListOfAppts(void)
bool addAppt(Appointment *addme)
bool removeAppt(string &apptName)
bool checkCalendars(Time &slot,
                    Calendar others[])
bool login(string &pass)
bool logout(void)
```

So, do we need all
of our classes?

OneTimeAppointment

```
OneTimeAppointment()
~OneTimeAppointment()
bool setStartTime(Time &st)
bool setEndTime(Time &st)
bool addParticipant(string &user)
bool setLocation(string &location)
```

Appointment

```
Appointment() and ~Appointment()
bool setStartTime(Time &st)
bool setEndTime(Time &st)
bool addParticipant(string &user)
bool setLocation(string &location)
```

RecurringAppointment

```
RecurringAppointment()
~RecurringAppointment()
bool setStartTime(Time &st)
bool setEndTime(Time &st)
bool addParticipant(string &user)
bool setLocation(string &location)
bool setRecurRate(int numDays)
```

Step 3: Determine Relationships & Data

Now you need to figure out how the classes **relate to each other** and what data they hold.

There are three relationships to consider:

1. **Uses**: Class X **uses** objects of class Y, but may not actually hold objects of class Y.
2. **Has-A**: Class X **contains** one or more instances of class Y (composition).
3. **Is-A**: Class X **is a specialized version** of class Y.

This will help you figure out what **private data** each class needs, and will also help determine **inheritance**.

Step 3: Determine Relationships & Data

Calendar

`Calendar()` and `~Calendar()`

`list getListOfAppts(void)`

`bool addAppt(Appointment *addme)`

`bool removeAppt(string &apptName)`

`bool checkCalendars(Time &slot,`

`Calendar others[])`

`bool login(string &pass)`

`bool logout(void)`

private:

`Appointment m_app[100];`

`String m_password;`

A Calendar contains **appointments**

A Calendar must have a **password**

A Calendar uses other **calendars**,
but it doesn't need to hold them.

In general, if a class **naturally**
holds a piece of data, your
design should place the data in
that class.

Of course, you might not get
it right the first time.

In this case, it helps to
"re-factor" your classes.
(i.e. iterate till you get it right)

Step 3: Determine Relationships & Data

Appointment

```
Appointment()
virtual ~Appointment()
bool setStartTime(Time &st)
bool setEndTime(Time &st)
bool addParticipant(string &user)
bool setLocation(string &location)
private:
    Time m_startTime;
    Time m_endTime;
    string m_participants[10];
    string m_location;
```

Now, how about our
RecurringAppointment?

It's shares all of the attributes of an Appointment. So should a Recurring Appointment contain an Appointment or use inheritance?

An Appointment has a **start time**

An Appointment has an **end time**

An Appointment is associated with a set of **participants**.

An Appointment is held at a **location**.

RecurringAppointment

```
: public Appointment
RecurringAppointment()
~RecurringAppointment()
```

private:

```
int m_numDays;
bool setRecurRate(int numDays)
```

Step 4: Determine Interactions

Here, we want to determine how each class **interacts** with the others.

The best way to determine the interactions is by coming up with **use cases**...



Use Case Examples

1. The user wants to add an appointment to their calendar.
2. The user wants to determine if they have an appointment at 5pm with Joe.
3. The user wants to locate the appointment at 5pm and update it to 6pm.

Use Case #1

1. The user wants to add an appointment to their calendar.

A. The user creates a new Appointment object and sets its values:

```
Appointment *app = new Appointment ("10am","11am","Dodd",...);
```

B. The user adds the Appointment object to the Calendar:

```
Calendar c;  
c.addAppointment(app);
```

It looks like we're OK here. Although it might be nicer if we could set the Appointment's values during construction

Use Case #2

2. The user wants to determine if they have an appointment at 5pm with Joe.

Hmm... Can we do this with our classes?

Nope. We'll need to add this to our Appointment class!

```
Calendar c;
```

```
...
```

```
Appointment *appt;
```

```
appt = c.checkTime("5pm");
```

```
if (appt == NULL)
```

```
    cout << "No appt at 5pm";
```

```
else if (appt->isAttendee("Joe"))
```

```
    cout << "Joe is attending!";
```

Calendar

```
Calendar() and ~Calendar()  
list getListOfAppts(void)
```

Appointment

```
Appointment() & virtual ~Appointment()  
bool setStartTime(Time &st)  
bool setEndTime(Time &st)  
bool addParticipant(string &user)  
bool setLocation(string &location)  
bool isAttendee(string &person)
```

private:

```
Time m_startTime;  
Time m_endTime;  
string m_participants[10];  
string m_location;
```

Class Design Conclusions

First and foremost, **class design is an iterative process.**

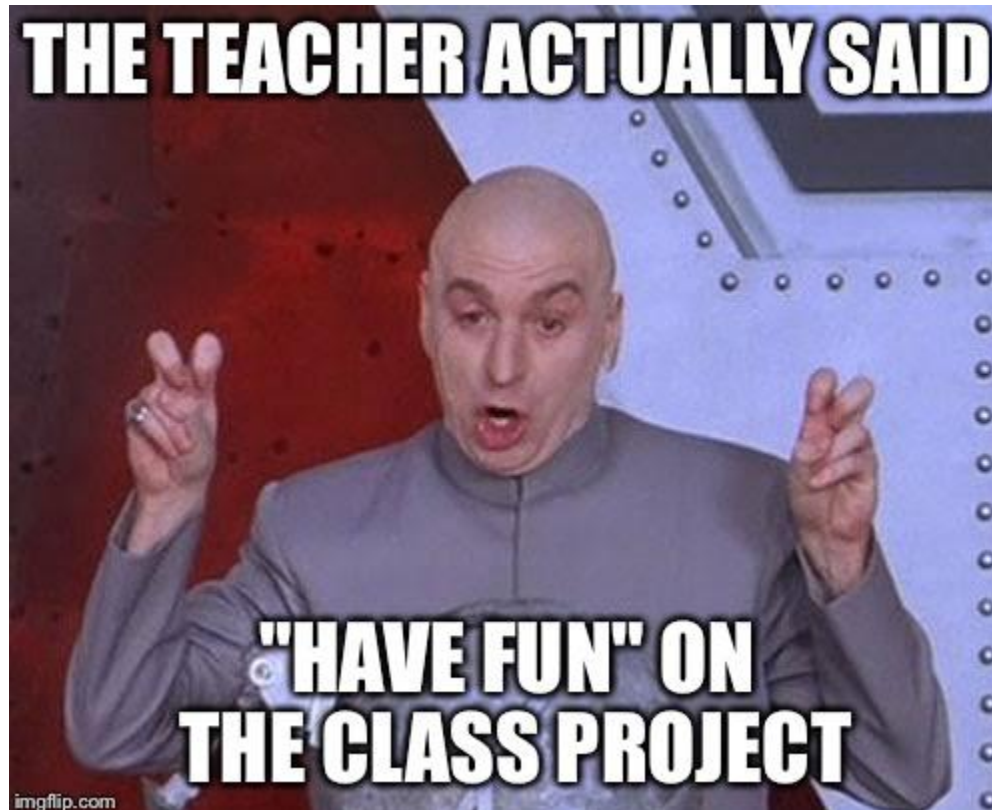
Before you ever start to program your class implementations, it helps to determine your **classes**, their **interfaces**, their **data**, and their **interactions**.

It's important to go through all of the **use cases** in order to make sure you haven't forgotten anything.

This is something that you only get better at with **experience**, so **don't feel bad** if its difficult at first!

Class Design Tips

Helpful tips for Project #3!



Tip #1

Avoid using dynamic cast to identify common types of objects. Instead add methods to check for various classes of behaviors:

Don't do this:

```
void decideWhetherToAddOil(Actor *p)
{
    if (dynamic_cast<BadRobot *>(p) != nullptr ||
        dynamic_cast<GoodRobot *>(p) != nullptr ||
        dynamic_cast<ReallyBadRobot *>(p) != nullptr ||
        dynamic_cast<StinkyRobot *>(p) != nullptr)
        p->addOil();
}
```

Do this instead:

```
void decideWhetherToAddOil (Actor *p)
{
    // define a common method, have all Robots return true, all biological
    // organisms return false
    if (p->requiresOilToOperate())
        p->addOil();
}
```


Tip #2

Always avoid defining specific `isParticularClass()` methods for each type of object. Instead add methods to check for various common behaviors that span multiple classes:

Don't do this:

```
void decideWhetherToAddOil (Actor *p)  
{  
    if (p->isGoodRobot() || p->isBadRobot() || p->isStinkyRobot())  
        p->addOil();  
}
```

Do this instead:

```
void decideWhetherToAddOil (Actor *p)  
{  
    // define a common method, have all Robots return true, all biological  
    // organisms return false  
    if (p->requiresOilToOperate())  
        p->addOil();  
}
```

Tip #3

If two related subclasses (e.g., `BadRobot` and `GoodRobot`) each directly define a member variable that serves the same purpose in both classes (e.g., `m_amountOfOil`), then move that member variable to the common base class and add accessor and mutator methods for it to the base class. So the `Robot` base class should have the `m_amountOfOil` member variable defined once, with `getOil()` and `addOil()` functions, rather than defining this variable directly in both `BadRobot` and `GoodRobot`.

Don't do this:

```
class SmellyRobot: public Robot
{
    ...
private:
    int m_oilLeft;
};

class GoofyRobot: public Robot
{
    ...
private:
    int m_oilLeft;
};
```

Do this instead:

```
class Robot
{
public:
    void addOil(int oil)
        { m_oilLeft += oil; }
    int getOil() const
        { return m_oilLeft; }
private:
    int m_oilLeft;
};
```

Tip #4

Never make any class's data members public or protected. You may make class constants public, protected or private.

Tip #5

Never make a method public if it is only used directly by other methods within the same class that holds it. Make it private or protected instead.

Tip #6

Your StudentWorld methods should never return a vector, list or iterator to StudentWorld's private game objects or pointers to those objects. Only StudentWorld should know about all of its game objects and where they are. Instead StudentWorld should do all of the processing itself if an action needs to be taken on one or more game objects that it tracks.

Don't do this:

```
class StudentWorld
{
    public:
        vector<Actor *> getZappableActors (int x, int y)
        {
            ... // creates a vector with
                // actor pointers and return it
        }
};
```

```
class NastyRobot
{
    public:
        virtual void doSomething()
        {
            ...
            vector<Actor *> v;
            vector<Actor *>::iterator p;

            v = studentWorldPtr-> getZappableActors(getX(), getY());
            for (p = actors.begin(); p != actors.end(); p++)
                p->zap();
        }
};
```

Do this instead:

```
class StudentWorld
{
    public:
        void zapAllZappableActors(int x, int y)
        {
            for (p = actors.begin(); p != actors.end(); p++)
                if (p->isAt(x,y) == true && p->isZappable())
                    p->zap();
        }
};
```

```
class NastyRobot
{
    public:
        virtual void doSomething()
        {
            ...
            studentWorldPtr-> zapAllZappableActors (getX(), getY());
        }
};
```

Tip #7

If two subclasses have a method that shares some common functionality, but also has some differing functionality, use an auxiliary method to factor out the differences:

Don't do this:

```
class StinkyRobot: public Robot
{
...
protected:
    virtual void doDifferentiatedStuff()
    {
        doCommonThingA();
        doCommonThingB();

        passStinkyGas();
        pickNose();
    }
};

class ShinyRobot: public Robot
{
...
protected:
    virtual void doDifferentiatedStuff()
    {
        doCommonThingA();
        doCommonThingB();

        polishMyChrome();
        wipeMyDisplayPanel();
    }
};
```

Do this instead:

```
class Robot
{
public:
    virtual void doSomething()
    {
        // first do all the common things that all robots do:
        doCommonThingA();
        doCommonThingB();

        // then call out to a virtual function to do the differentiated stuff
        doDifferentiatedStuff();
    }

protected:
    virtual void doDifferentiatedStuff() = 0;
};

class StinkyRobot: public Robot
{
...
protected:
    // define StinkyRobot's version of the differentiated function
    virtual void doDifferentiatedStuff()
    {
        // only Stinky robots do these things
        passStinkyGas();
        pickNose();
    }
};

class ShinyRobot: public Robot
{
...
protected:
    // define ShinyRobot's version of the differentiated function
    virtual void doDifferentiatedStuff()
    {
        // only Shiny robots do these things
        polishMyChrome();
        wipeMyDisplayPanel();
    }
};
```

Appendix

Tracing Through Recursion (on Paper)

You're taking a CS exam and see this:

How do you solve it quickly?

5. What does this print?

```
int mystery(int a)
{
    if (a == 0)
        return a+1;
    cout << a;

    if (a % 2 == 0)
        a = mystery(a/3);
    else
        a = mystery(a-1);
    return a+5;
}

int main()
{
    cout << mystery(3);
}
```

Output: 3

a = 3

a = mystery(2); *

Steps:

1. Put a blank sheet of paper next to the func.
2. Trace the func with your finger.
 - A. When you hit/update a var, write its value down.
 - B. Write all output on your original sheet.
 - C. When you call a func:
 - i. Write its params down
 - ii. Write a * to mark where to continue tracing later
 - iii. Fold the sheet in half and continue tracing

Tracing Through Recursion (on Paper)

You're taking a CS exam and see this:

How do you solve it quickly?

5. What does this print?

```
int mystery(int a)
{
    if (a == 0)
        return a+1;
    cout << a;

    if (a % 2 == 0)
        a = mystery(a/3);
    else
        a = mystery(a-1);
    return a+5;
}

int main()
{
    cout << mystery(3);
}
```

Output: 3 2

a = 2

a = mystery(0); *

Steps:

1. Put a blank sheet of paper next to the func.
2. Trace the func with your finger.
 - A. When you hit/update a var, write its value down.
 - B. Write all output on your original sheet.
 - C. When you call a func:
 - i. Write its params down
 - ii. Write a * to mark where to continue tracing later
 - iii. Fold the sheet in half and continue tracing

Tracing Through Recursion (on Paper)

You're taking a CS exam and see

How do you solve it quickly?

Returning a
value of 1

5. What does this print?

```
int mystery(int a)
{
    if (a == 0)
        return a+1;
    cout << a;

    if (a % 2 == 0)
        a = mystery(a/3);
    else
        a = mystery(a-1);

    return a+5;
}

int main()
{
    cout << mystery(3);
}
```

Output: 3 2

a = 0

Steps:

D. To return from a function:

- i. Determine what value is being returned (if any)
- ii. Unfold your paper once.
- iii. Find the * that points to the line where you were (you'll continue from here)
- iv. Erase the *

Tracing Through Recursion (on Paper)

You're taking a CS exam and see

How do you solve it quickly?

Returning a
value of 6

5. What does this print?

```
int mystery(int a)
{
    if (a == 0)
        return a+1;
    cout << a;

    if (a % 2 == 0)
        a = mystery(a/3);
    else
        a = mystery(a-1);
    return a+5;
}

int main()
{
    cout << mystery(3);
}
```

Output: 3 2

a = 2

¹
~~a = mystery(0); *~~

Steps:

D. To return from a function:

- i. Determine what value is being returned (if any)
- ii. Unfold your paper once.
- iii. Find the * that points to the line where you were (you'll continue from here)
- iv. Erase the *
- v. Write the returned value above your function
- vi. Continue tracing normally.

Tracing Through Recursion (on Paper)

You're taking a CS exam and see:
How do you solve it quickly?

Returning a
value of **11**

5. What does this print?

```
int mystery(int a)
{
    if (a == 0)
        return a+1;
    cout << a;

    if (a % 2 == 0)
        a = mystery(a/3);
    else
        a = mystery(a-1);
    return a+5;
}

int main()
{
    cout << mystery(3);
}
```

Output: 3 2 11

a = 3

⁶
~~a = mystery(2); *~~

Steps:

D. To return from a function:

- i. Determine what value is being returned (if any)
- ii. Unfold your paper once.
- iii. Find the * that points to the line where you were (you'll continue from here)
- iv. Erase the *
- v. Write the returned value above your function
- vi. Continue tracing normally.

Recursion Tracing Exercise

Use the paper tracing technique to determine what the following program prints:

```
int mystery(int a)
{
    cout << a;
    if (a == 0)
        return 1;
    int b = mystery(a/2);
    cout << b;
    return b + 1;
}

int main()
{
    cout << mystery(3);
}
```