

Práctica #5 Perceptrón Multicapa

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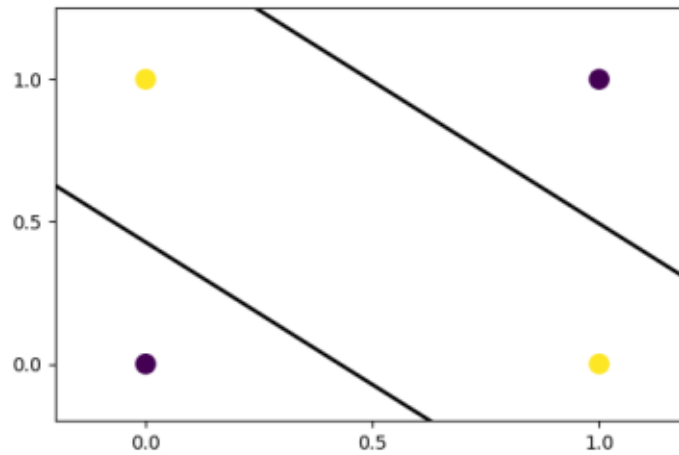
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1. Introducción

Un perceptrón multicapa es tipo de red neuronal artificial compuesta de varias neuronas y varias capas, puede resolver problemas que un perceptrón simple puede. El clásico ejemplo es el de la compuerta XOR:

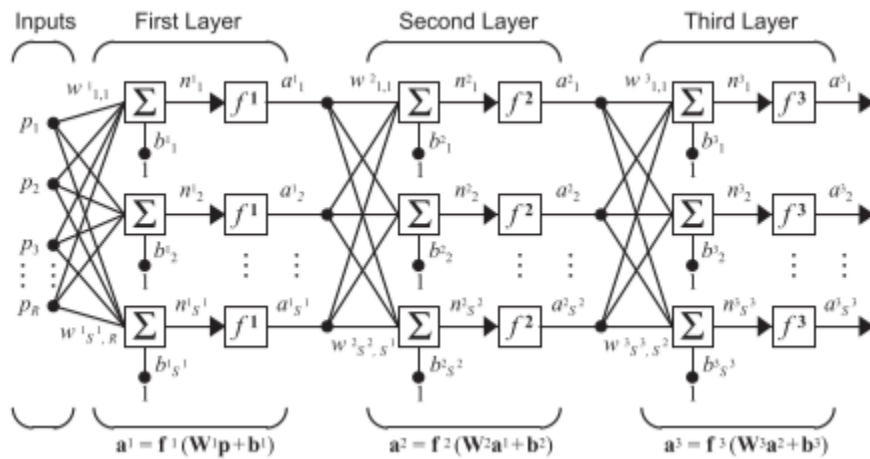
En este caso se necesitan dos fronteras de decisión, por ende dos neuronas y se necesita otra capa para “combinar los resultados”. La manera la cual se actualizan los pesos y bias del MLP es usando un algoritmo para propagar los resultados a las neuronas de la capa actual y de las anteriores, es algoritmo es llamado backpropagation, el cual es un algoritmo de minimización basado en el descenso en gradiente el cual encuentra los mínimos locales de una función. En esta práctica se usan MLP's para aproximar señales leyendo datos de archivos de texto.

Figura 1: Compuerta XOR



1.1. Modelo

Figura 2: Modelo



1.1.1. Forward Propagation

$$a^0 = p$$

$$a^{m+1} = f^{m+1}(W^{m+1} \cdot a^m + b^{m+1}), m = 0, 1, 2, 3, \dots, M - 1$$

$$a = a^M$$

donde M es el número de capas.

1.1.2. Forward Propagation

Para poder usar backpropagation se necesita que las funciones de activación en cada capa sean continuas y derivables. El algoritmo es el siguiente:

1. Calcular las sensitividades de cada capa desde la última capa hasta la primera:

$$s^M = -2\dot{F}^M(n^M)(t - a)$$

$$s^m = \dot{F}^m(n^m)(W^{m+1})^T s^{m+1}$$

2. Actualizar los pesos y bias:

$$w^m(k+1) = W^m(k) - \alpha s^m (a^m - 1)^T$$

$$b^m(k+1) = b^m(k) - \alpha s^m$$

2. Diagrama de Flujo

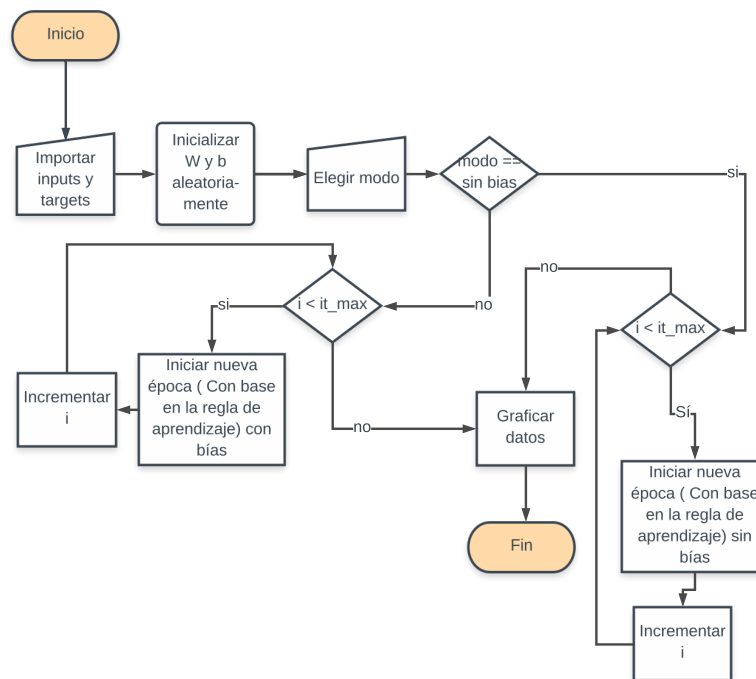


Figura 3: Diagrama de Flujo

3. Resultados

3.1. Polinomio 1

3.2. Inputs

1. -2.0000	27. -0.9600	53. 0.0800	79. 1.1200
2. -1.9600	28. -0.9200	54. 0.1200	80. 1.1600
3. -1.9200	29. -0.8800	55. 0.1600	81. 1.2000
4. -1.8800	30. -0.8400	56. 0.2000	82. 1.2400
5. -1.8400	31. -0.8000	57. 0.2400	83. 1.2800
6. -1.8000	32. -0.7600	58. 0.2800	84. 1.3200
7. -1.7600	33. -0.7200	59. 0.3200	85. 1.3600
8. -1.7200	34. -0.6800	60. 0.3600	86. 1.4000
9. -1.6800	35. -0.6400	61. 0.4000	87. 1.4400
10. -1.6400	36. -0.6000	62. 0.4400	88. 1.4800
11. -1.6000	37. -0.5600	63. 0.4800	89. 1.5200
12. -1.5600	38. -0.5200	64. 0.5200	90. 1.5600
13. -1.5200	39. -0.4800	65. 0.5600	91. 1.6000
14. -1.4800	40. -0.4400	66. 0.6000	92. 1.6400
15. -1.4400	41. -0.4000	67. 0.6400	93. 1.6800
16. -1.4000	42. -0.3600	68. 0.6800	94. 1.7200
17. -1.3600	43. -0.3200	69. 0.7200	95. 1.7600
18. -1.3200	44. -0.2800	70. 0.7600	96. 1.8000
19. -1.2800	45. -0.2400	71. 0.8000	97. 1.8400
20. -1.2400	46. -0.2000	72. 0.8400	98. 1.8800
21. -1.2000	47. -0.1600	73. 0.8800	99. 1.9200
22. -1.1600	48. -0.1200	74. 0.9200	100. 1.9600
23. -1.1200	49. -0.0800	75. 0.9600	101. 2.0000
24. -1.0800	50. -0.0400	76. 1.0000	
25. -1.0400	51. 0	77. 1.0400	
26. -1.0000	52. 0.0400	78. 1.0800	

3.3. Targets

1. 1.0000	27. 1.2487	53. 1.4818	79. 1.6845
2. 1.2487	28. 1.4818	54. 1.6845	80. 1.8443
3. 1.4818	29. 1.6845	55. 1.8443	81. 1.9511
4. 1.6845	30. 1.8443	56. 1.9511	82. 1.9980
5. 1.8443	31. 1.9511	57. 1.9980	83. 1.9823
6. 1.9511	32. 1.9980	58. 1.9823	84. 1.9048
7. 1.9980	33. 1.9823	59. 1.9048	85. 1.7705
8. 1.9823	34. 1.9048	60. 1.7705	86. 1.5878
9. 1.9048	35. 1.7705	61. 1.5878	87. 1.3681
10. 1.7705	36. 1.5878	62. 1.3681	88. 1.1253
11. 1.5878	37. 1.3681	63. 1.1253	89. 0.8747
12. 1.3681	38. 1.1253	64. 0.8747	90. 0.6319
13. 1.1253	39. 0.8747	65. 0.6319	91. 0.4122
14. 0.8747	40. 0.6319	66. 0.4122	92. 0.2295
15. 0.6319	41. 0.4122	67. 0.2295	93. 0.0952
16. 0.4122	42. 0.2295	68. 0.0952	94. 0.0177
17. 0.2295	43. 0.0952	69. 0.0177	95. 0.0020
18. 0.0952	44. 0.0177	70. 0.0020	96. 0.0489
19. 0.0177	45. 0.0020	71. 0.0489	97. 0.1557
20. 0.0020	46. 0.0489	72. 0.1557	98. 0.3155
21. 0.0489	47. 0.1557	73. 0.3155	99. 0.5182
22. 0.1557	48. 0.3155	74. 0.5182	100. 0.7513
23. 0.3155	49. 0.5182	75. 0.7513	101. 1.0000
24. 0.5182	50. 0.7513	76. 1.0000	
25. 0.7513	51. 1.0000	77. 1.2487	
26. 1.0000	52. 1.2487	78. 1.4818	

3.3.1. Datos

$$V1 = [1116101]$$

$$V2 = [321]$$

epochmax = 10000

Múltiplo para las épocas de validación = 500

numval = 7

alpha=.0701

error de validación = .0000000000000001

Configuración: 80-15-15

3.4. Resultado

3.5. Imágenes

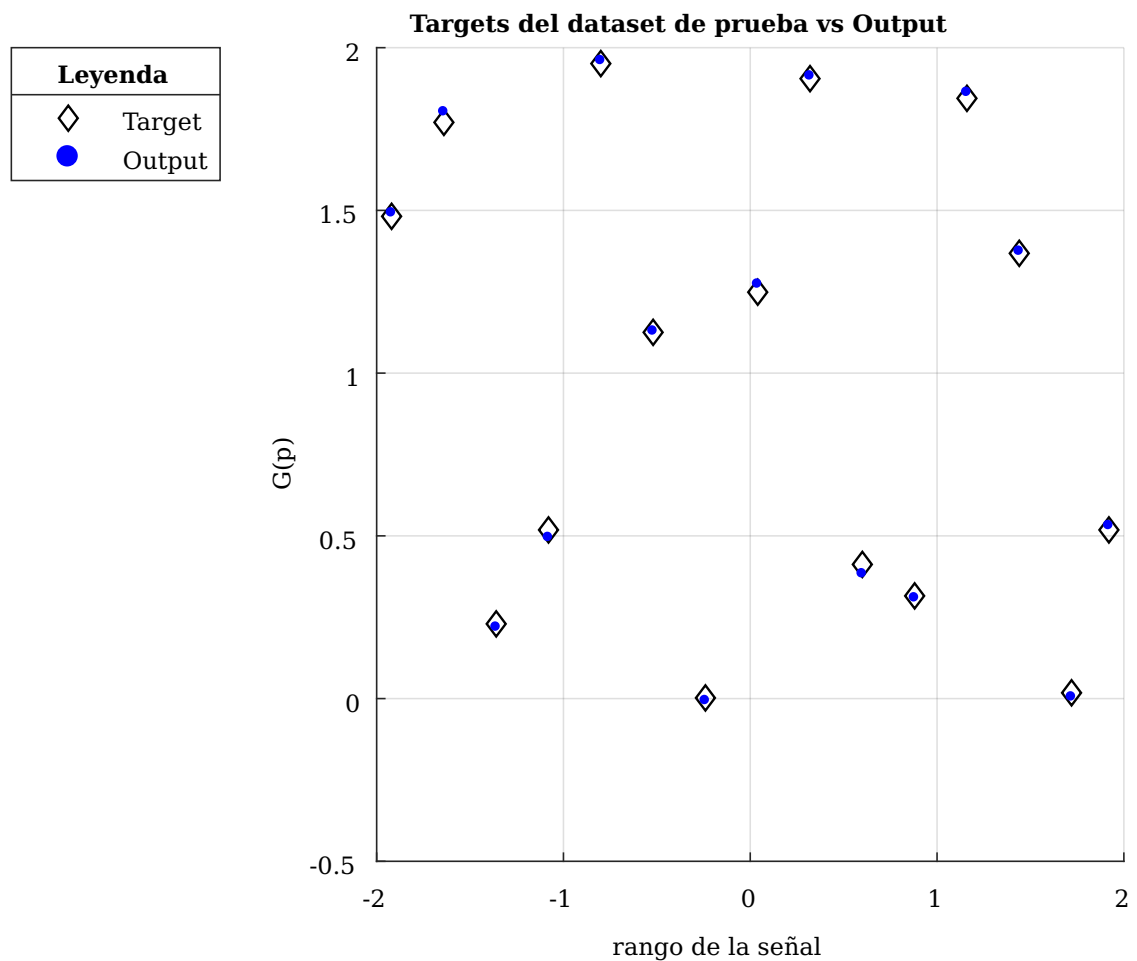


Figura 4: Gráfica 1.1

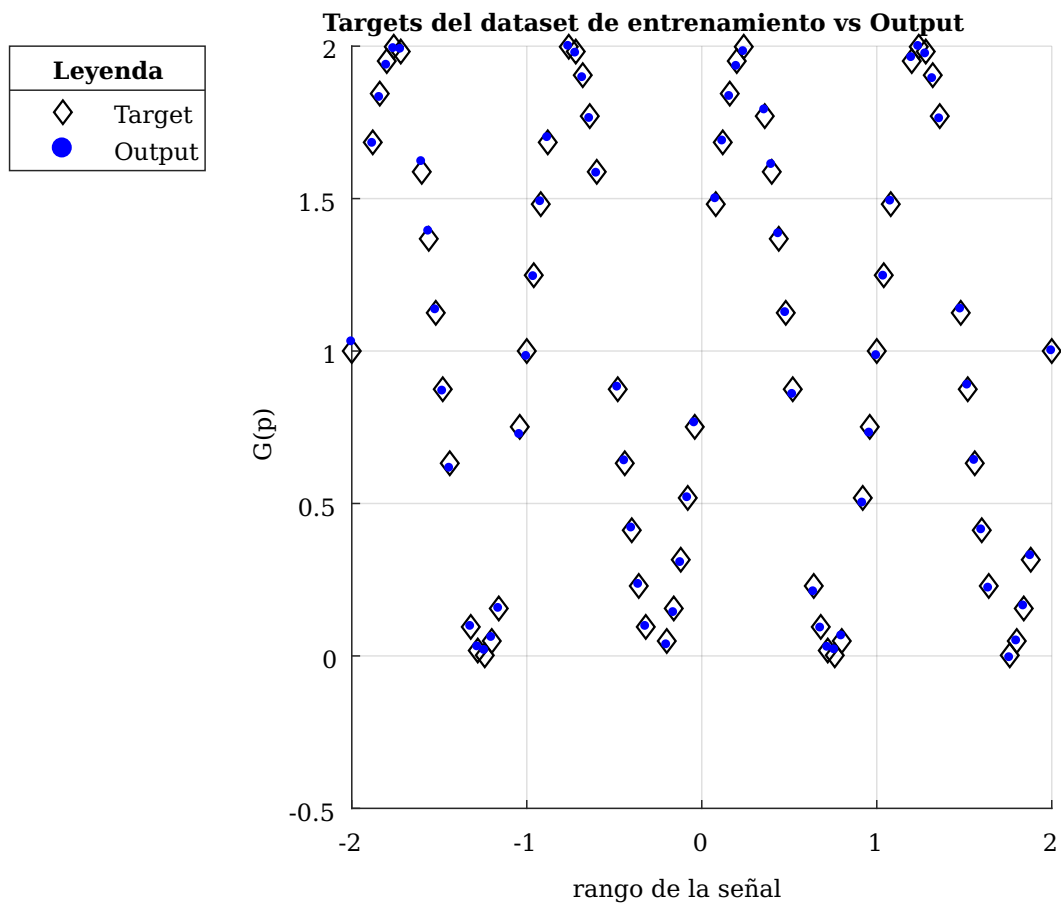


Figura 5: Gráfica 1.2

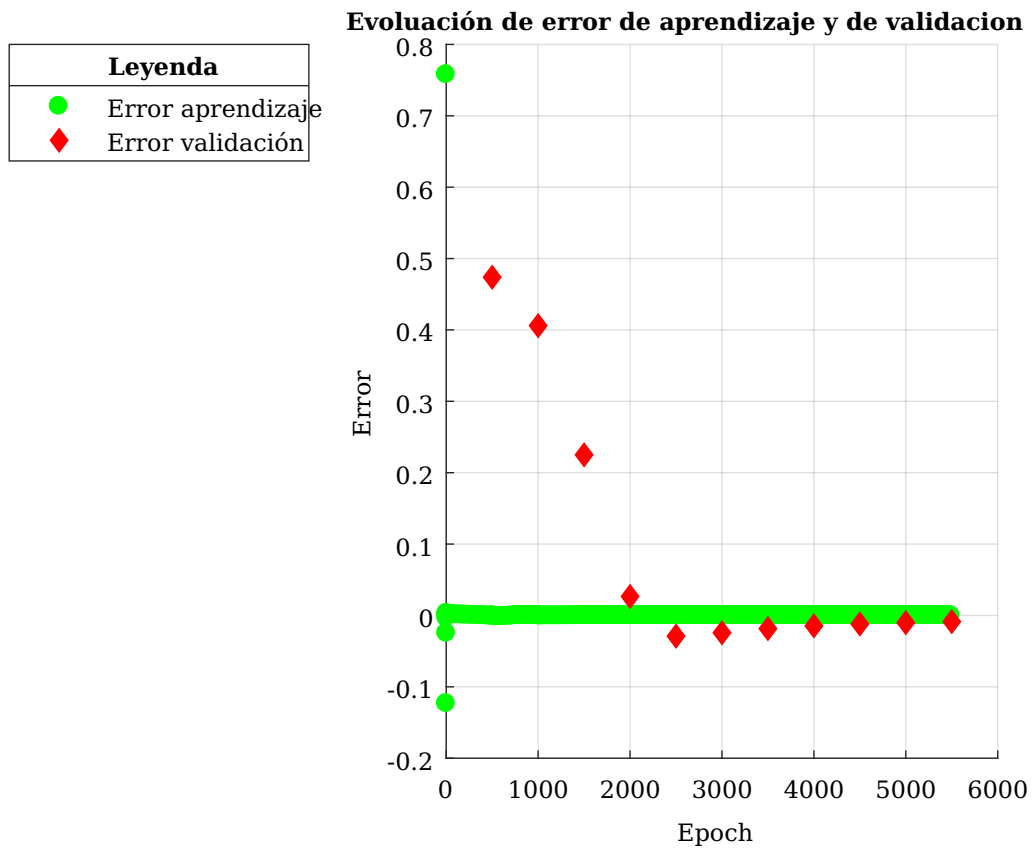


Figura 6: Gráfica 1.3

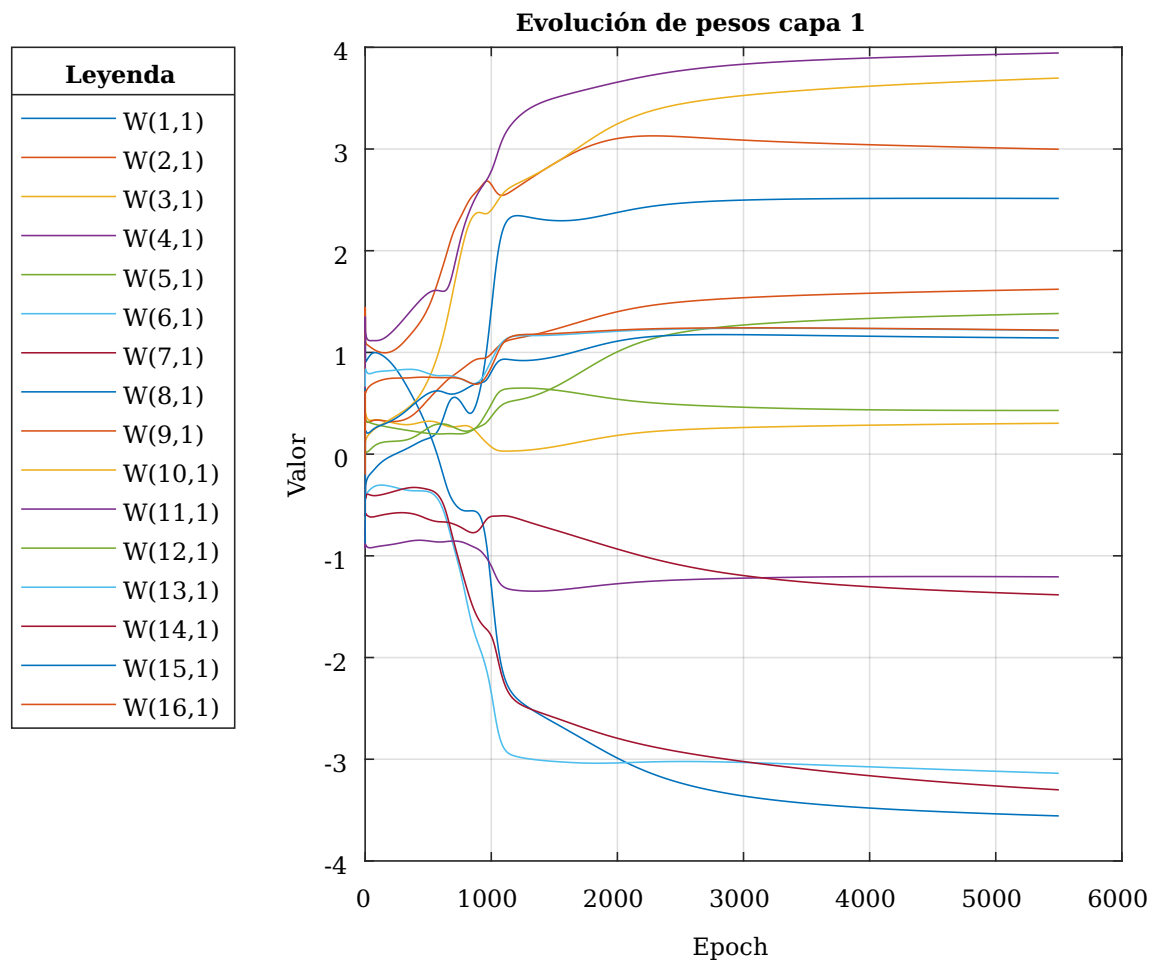


Figura 7: Gráfica 1.4

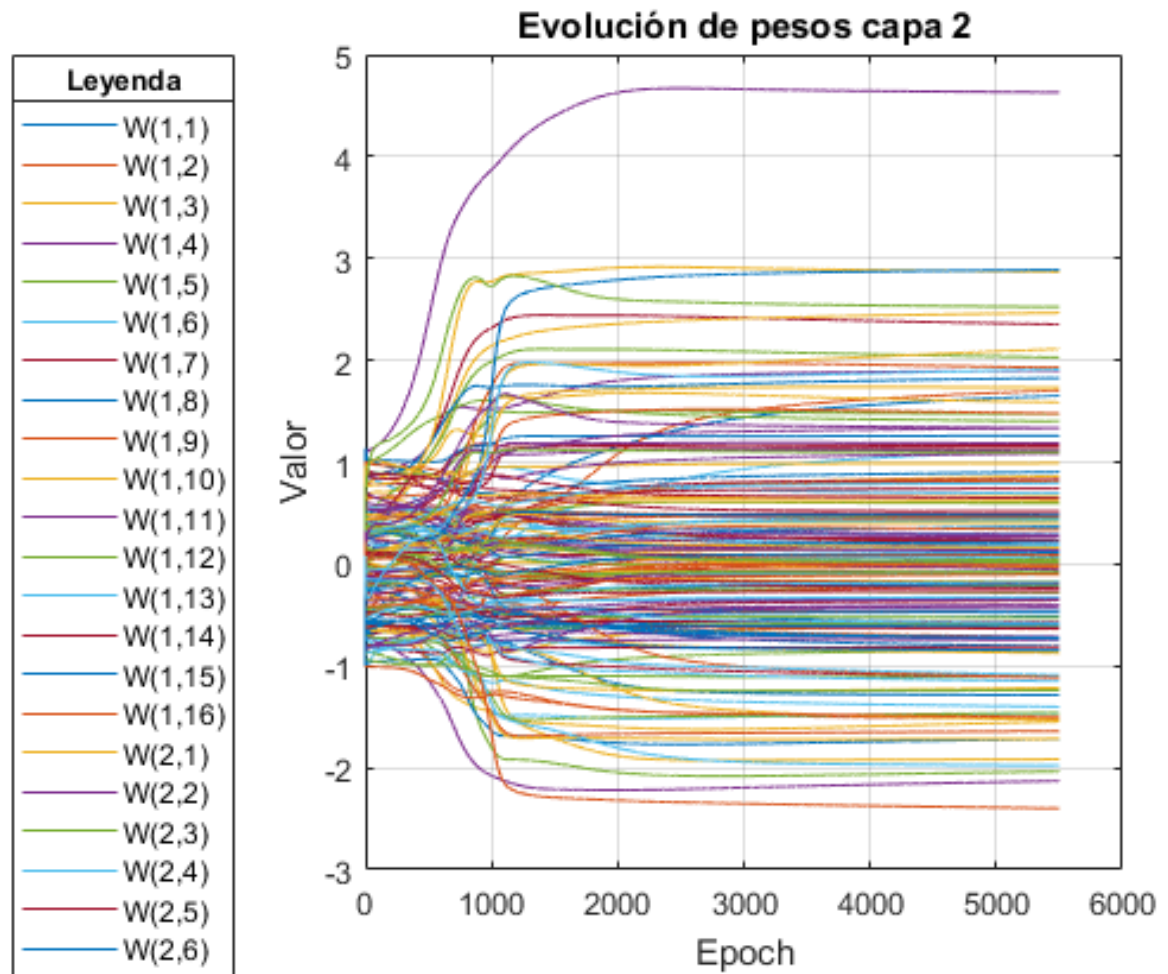


Figura 8: Gráfica 1.5

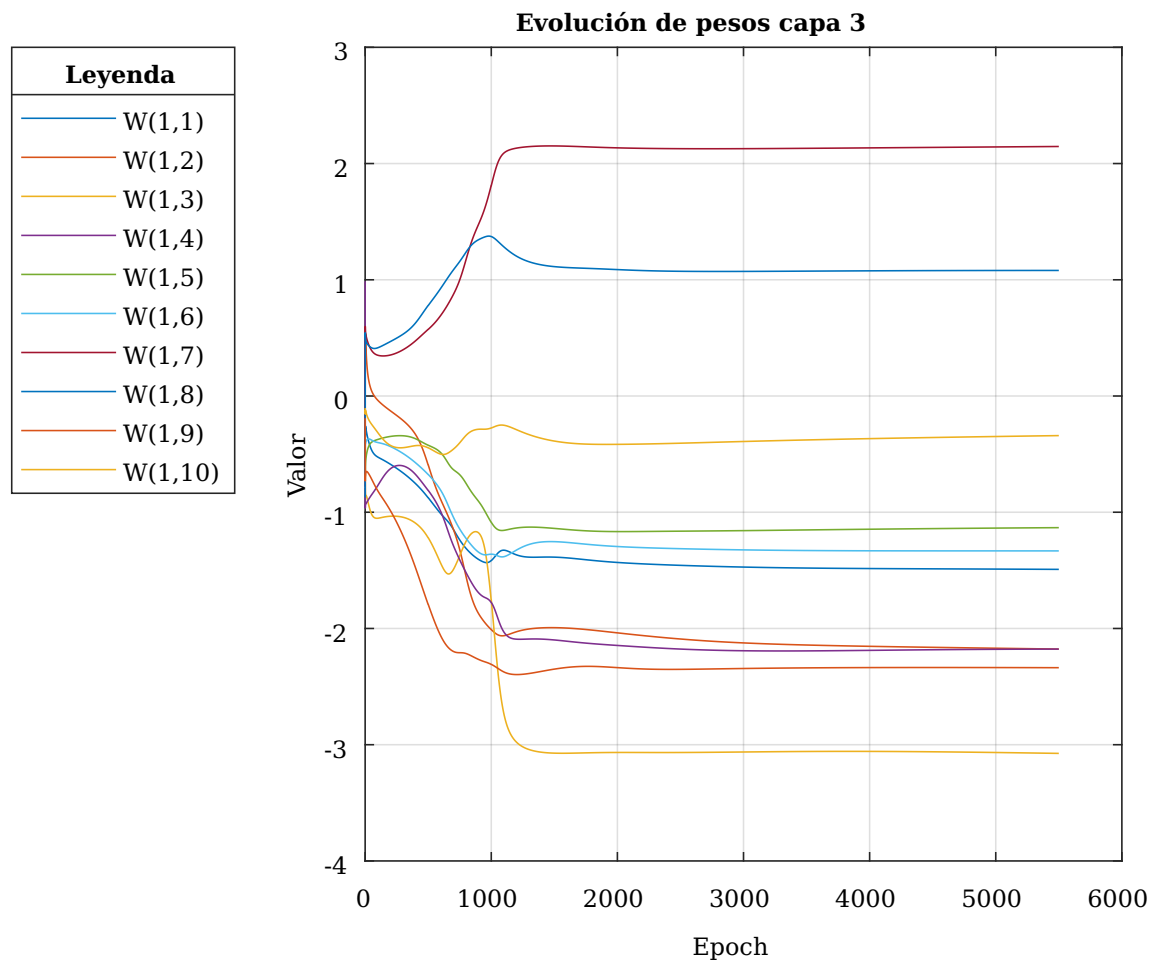


Figura 9: Gráfica 1.6

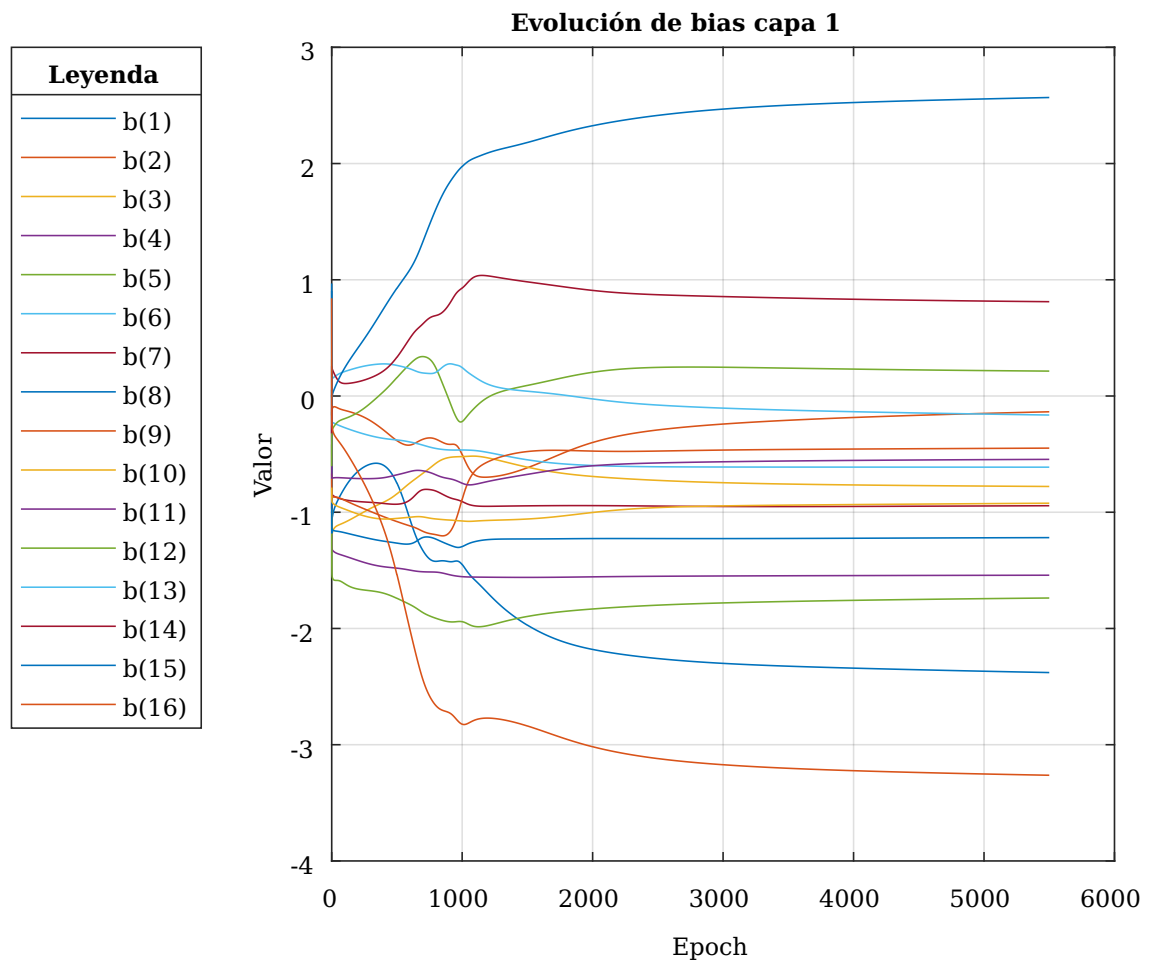


Figura 10: Gráfica 1.7

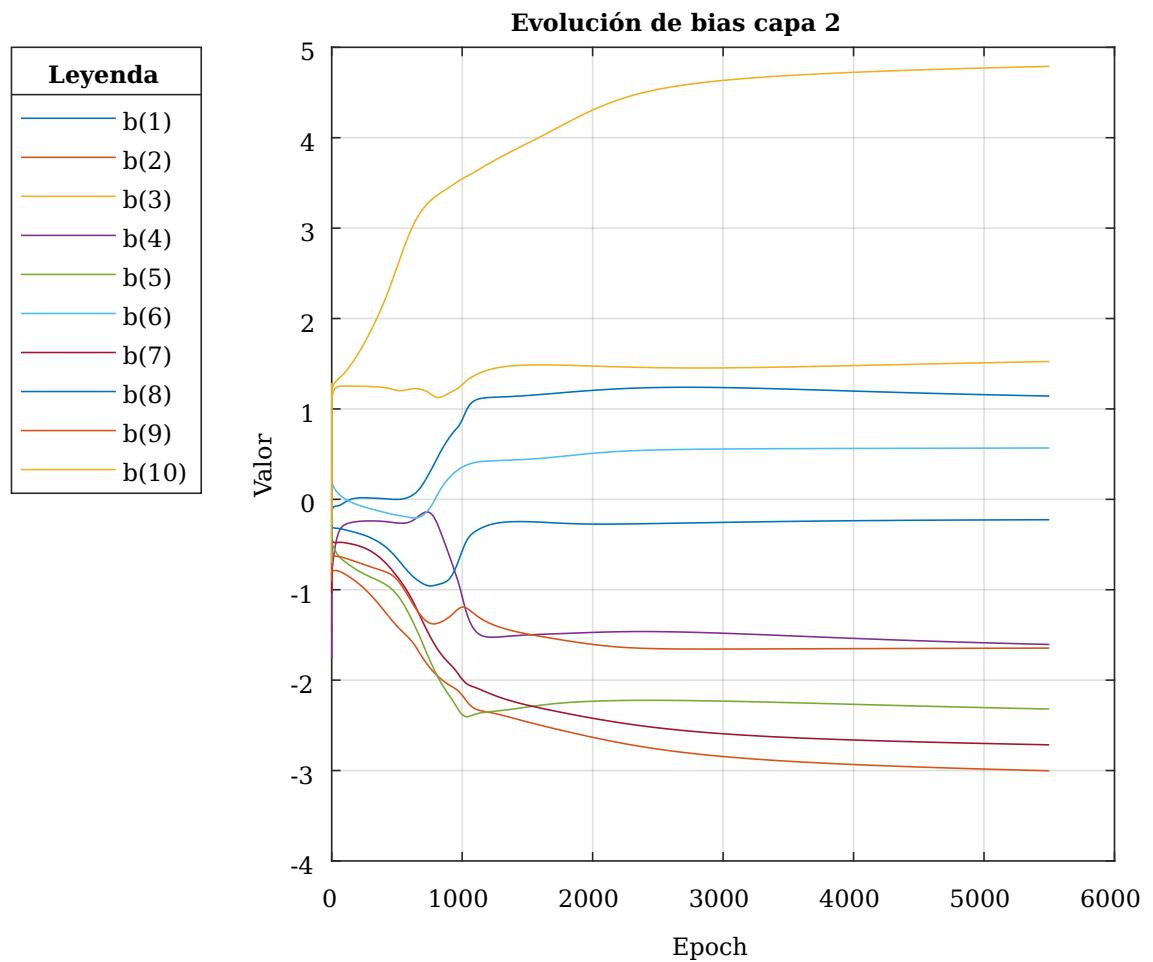


Figura 11: Gráfica 1.8

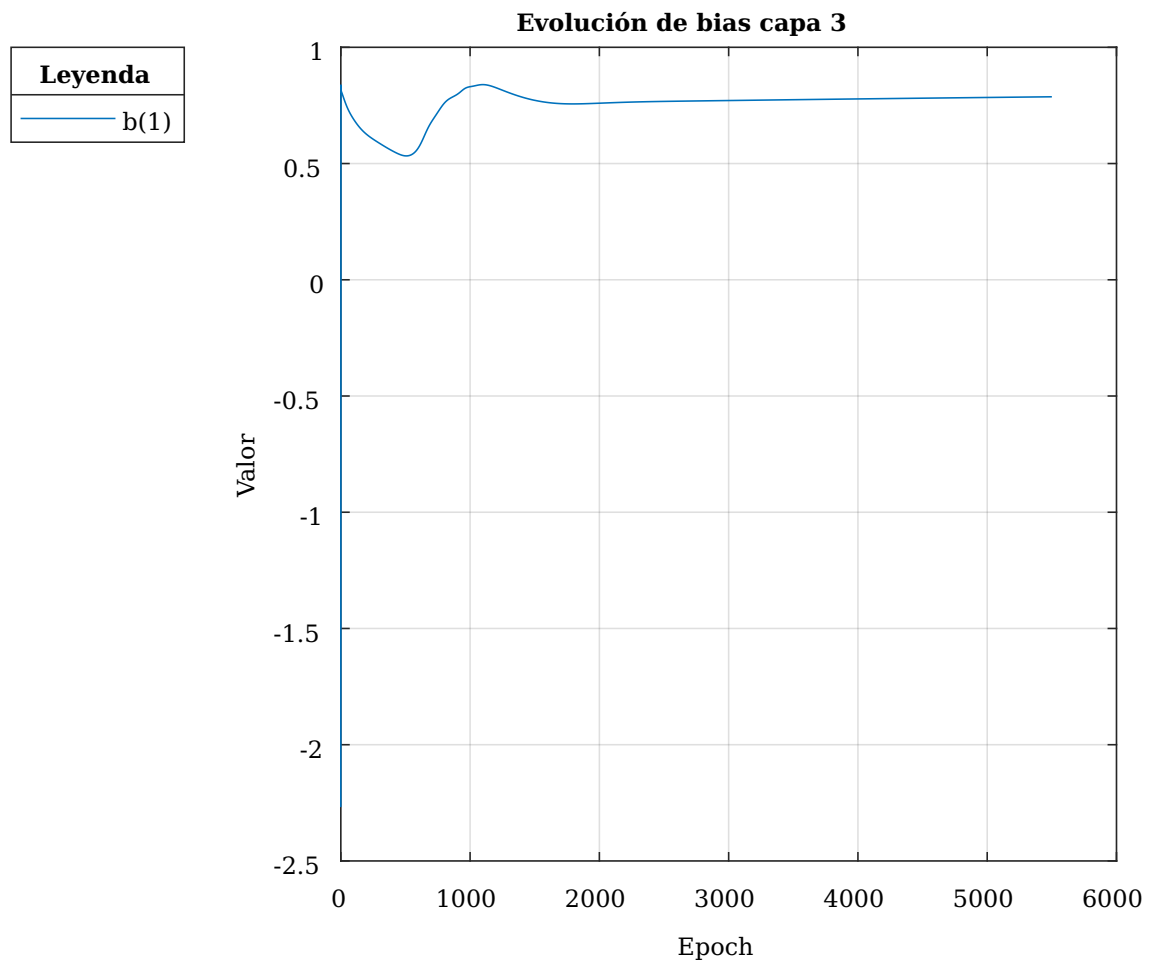


Figura 12: Gráfica 1.9

3.6. Polinomio 2

3.7. Inputs

1. 4.0000	30. 3.0333	59. 2.0667	88. 1.1000
2. 3.9667	31. 3.0000	60. 2.0333	89. 1.0667
3. 3.9333	32. 2.9667	61. 2.0000	90. 1.0333
4. 3.9000	33. 2.9333	62. 1.9667	91. 1.0000
5. 3.8667	34. 2.9000	63. 1.9333	92. 0.9667
6. 3.8333	35. 2.8667	64. 1.9000	93. 0.9333
7. 3.8000	36. 2.8333	65. 1.8667	94. 0.9000
8. 3.7667	37. 2.8000	66. 1.8333	95. 0.8667
9. 3.7333	38. 2.7667	67. 1.8000	96. 0.8333
10. 3.7000	39. 2.7333	68. 1.7667	97. 0.8000
11. 3.6667	40. 2.7000	69. 1.7333	98. 0.7667
12. 3.6333	41. 2.6667	70. 1.7000	99. 0.7333
13. 3.6000	42. 2.6333	71. 1.6667	100. 0.7000
14. 3.5667	43. 2.6000	72. 1.6333	101. 0.6667
15. 3.5333	44. 2.5667	73. 1.6000	102. 0.6333
16. 3.5000	45. 2.5333	74. 1.5667	103. 0.6000
17. 3.4667	46. 2.5000	75. 1.5333	104. 0.5667
18. 3.4333	47. 2.4667	76. 1.5000	105. 0.5333
19. 3.4000	48. 2.4333	77. 1.4667	106. 0.5000
20. 3.3667	49. 2.4000	78. 1.4333	107. 0.4667
21. 3.3333	50. 2.3667	79. 1.4000	108. 0.4333
22. 3.3000	51. 2.3333	80. 1.3667	109. 0.4000
23. 3.2667	52. 2.3000	81. 1.3333	110. 0.3667
24. 3.2333	53. 2.2667	82. 1.3000	111. 0.3333
25. 3.2000	54. 2.2333	83. 1.2667	112. 0.3000
26. 3.1667	55. 2.2000	84. 1.2333	113. 0.2667
27. 3.1333	56. 2.1667	85. 1.2000	114. 0.2333
28. 3.1000	57. 2.1333	86. 1.1667	115. 0.2000
29. 3.0667	58. 2.1000	87. 1.1333	116. 0.1667

117. 0.1333	149. -0.9333	181. -2.0000	213. -3.0667
118. 0.1000	150. -0.9667	182. -2.0333	214. -3.1000
119. 0.0667	151. -1.0000	183. -2.0667	215. -3.1333
120. 0.0333	152. -1.0333	184. -2.1000	216. -3.1667
121. 0.0000	153. -1.0667	185. -2.1333	217. -3.2000
122. -0.0333	154. -1.1000	186. -2.1667	218. -3.2333
123. -0.0667	155. -1.1333	187. -2.2000	219. -3.2667
124. -0.1000	156. -1.1667	188. -2.2333	220. -3.3000
125. -0.1333	157. -1.2000	189. -2.2667	221. -3.3333
126. -0.1667	158. -1.2333	190. -2.3000	222. -3.3667
127. -0.2000	159. -1.2667	191. -2.3333	223. -3.4000
128. -0.2333	160. -1.3000	192. -2.3667	224. -3.4333
129. -0.2667	161. -1.3333	193. -2.4000	225. -3.4667
130. -0.3000	162. -1.3667	194. -2.4333	226. -3.5000
131. -0.3333	163. -1.4000	195. -2.4667	227. -3.5333
132. -0.3667	164. -1.4333	196. -2.5000	228. -3.5667
133. -0.4000	165. -1.4667	197. -2.5333	229. -3.6000
134. -0.4333	166. -1.5000	198. -2.5667	230. -3.6333
135. -0.4667	167. -1.5333	199. -2.6000	231. -3.6667
136. -0.5000	168. -1.5667	200. -2.6333	232. -3.7000
137. -0.5333	169. -1.6000	201. -2.6667	233. -3.7333
138. -0.5667	170. -1.6333	202. -2.7000	234. -3.7667
139. -0.6000	171. -1.6667	203. -2.7333	235. -3.8000
140. -0.6333	172. -1.7000	204. -2.7667	236. -3.8333
141. -0.6667	173. -1.7333	205. -2.8000	237. -3.8667
142. -0.7000	174. -1.7667	206. -2.8333	238. -3.9000
143. -0.7333	175. -1.8000	207. -2.8667	239. -3.9333
144. -0.7667	176. -1.8333	208. -2.9000	240. -3.9667
145. -0.8000	177. -1.8667	209. -2.9333	241. -4.0000
146. -0.8333	178. -1.9000	210. -2.9667	
147. -0.8667	179. -1.9333	211. -3.0000	
148. -0.9000	180. -1.9667	212. -3.0333	

3.8. Targets

1. -0.01292	31. -0.24440	61. -1.33982	91. -1.33437
2. -0.01451	32. -0.26413	62. -1.38403	92. -1.26546
3. -0.01628	33. -0.28507	63. -1.42719	93. -1.19232
4. -0.01825	34. -0.30725	64. -1.46909	94. -1.11519
5. -0.02043	35. -0.33070	65. -1.50947	95. -1.03433
6. -0.02284	36. -0.35544	66. -1.54811	96. -0.95005
7. -0.02550	37. -0.38150	67. -1.58477	97. -0.86267
8. -0.02844	38. -0.40891	68. -1.61920	98. -0.77252
9. -0.03167	39. -0.43767	69. -1.65116	99. -0.67999
10. -0.03523	40. -0.46778	70. -1.68040	100. -0.58546
11. -0.03914	41. -0.49926	71. -1.70668	101. -0.48934
12. -0.04342	42. -0.53210	72. -1.72976	102. -0.39205
13. -0.04812	43. -0.56628	73. -1.74941	103. -0.29402
14. -0.05325	44. -0.60178	74. -1.76541	104. -0.19569
15. -0.05886	45. -0.63858	75. -1.77754	105. -0.09754
16. -0.06497	46. -0.67663	76. -1.78559	106. 0.00000
17. -0.07162	47. -0.71589	77. -1.78938	107. 0.09646
18. -0.07886	48. -0.75630	78. -1.78873	108. 0.19138
19. -0.08671	49. -0.79779	79. -1.78348	109. 0.28432
20. -0.09522	50. -0.84028	80. -1.77349	110. 0.37483
21. -0.10442	51. -0.88368	81. -1.75865	111. 0.46247
22. -0.11437	52. -0.92790	82. -1.73885	112. 0.54683
23. -0.12510	53. -0.97281	83. -1.71402	113. 0.62751
24. -0.13666	54. -1.01829	84. -1.68412	114. 0.70412
25. -0.14909	55. -1.06421	85. -1.64912	115. 0.77632
26. -0.16243	56. -1.11042	86. -1.60902	116. 0.84375
27. -0.17674	57. -1.15676	87. -1.56387	117. 0.90613
28. -0.19204	58. -1.20305	88. -1.51372	118. 0.96317
29. -0.20839	59. -1.24912	89. -1.45866	119. 1.01463
30. -0.22583	60. -1.29478	90. -1.39883	120. 1.06030
			121. 1.10000
			122. 1.13359
			123. 1.16097

124. 1.18207	154. -0.19222	184. -0.69370	214. -0.13619
125. 1.19687	155. -0.25207	185. -0.67457	215. -0.12586
126. 1.20536	156. -0.30943	186. -0.65456	216. -0.11614
127. 1.20760	157. -0.36409	187. -0.63383	217. -0.10702
128. 1.20367	158. -0.41589	188. -0.61251	218. -0.09847
129. 1.19368	159. -0.46467	189. -0.59073	219. -0.09048
130. 1.17779	160. -0.51031	190. -0.56861	220. -0.08302
131. 1.15617	161. -0.55272	191. -0.54628	221. -0.07607
132. 1.12905	162. -0.59180	192. -0.52384	222. -0.06961
133. 1.09666	163. -0.62752	193. -0.50140	223. -0.06360
134. 1.05928	164. -0.65983	194. -0.47905	224. -0.05804
135. 1.01720	165. -0.68874	195. -0.45688	225. -0.05288
136. 0.97075	166. -0.71424	196. -0.43498	226. -0.04812
137. 0.92025	167. -0.73636	197. -0.41341	227. -0.04373
138. 0.86605	168. -0.75517	198. -0.39224	228. -0.03969
139. 0.80854	169. -0.77072	199. -0.37153	229. -0.03597
140. 0.74809	170. -0.78309	200. -0.35132	230. -0.03256
141. 0.68508	171. -0.79239	201. -0.33168	231. -0.02943
142. 0.61990	172. -0.79871	202. -0.31262	232. -0.02656
143. 0.55296	173. -0.80218	203. -0.29419	233. -0.02395
144. 0.48465	174. -0.80293	204. -0.27640	234. -0.02156
145. 0.41536	175. -0.80109	205. -0.25928	235. -0.01938
146. 0.34547	176. -0.79682	206. -0.24285	236. -0.01741
147. 0.27537	177. -0.79027	207. -0.22710	237. -0.01561
148. 0.20543	178. -0.78158	208. -0.21205	238. -0.01398
149. 0.13599	179. -0.77093	209. -0.19770	239. -0.01250
150. 0.06741	180. -0.75846	210. -0.18405	240. -0.01117
151. 0.00000	181. -0.74434	211. -0.17108	241. -0.00996
152. -0.06593	182. -0.72874	212. -0.15879	
153. -0.13009	183. -0.71180	213. -0.14717	

3.8.1. Datos

$$V1 = [1116101]$$

$$V2 = [321]$$

epochmax = 2200

alpha=.0103

Múltiplo para las épocas de validación = 500

numval = 7

error de validación = .000000000001

Configuración: 80-10-10

3.9. Resultado

3.10. Imágenes

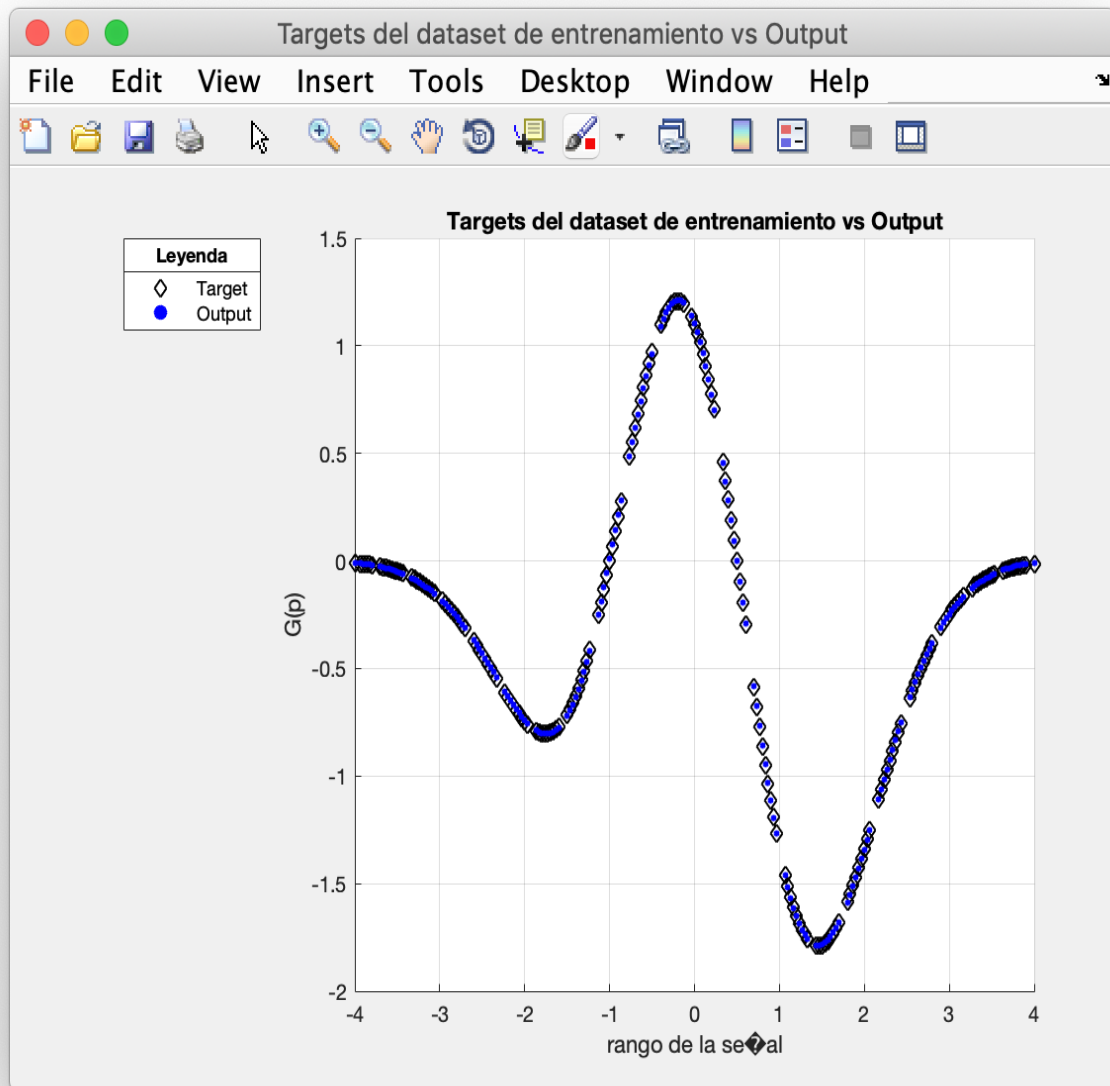


Figura 13: Gráfica 1.1

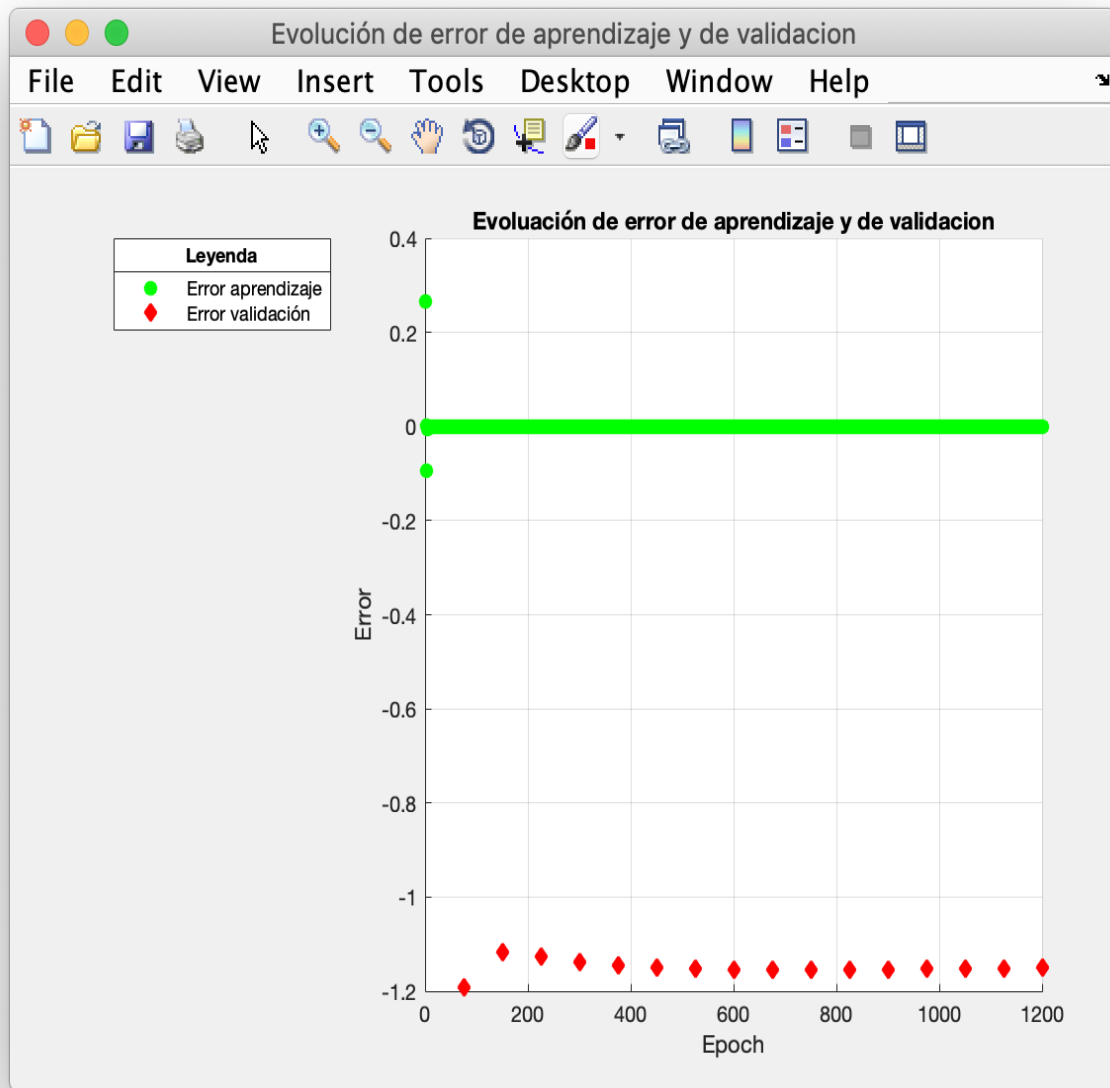


Figura 14: Gráfica 1.2

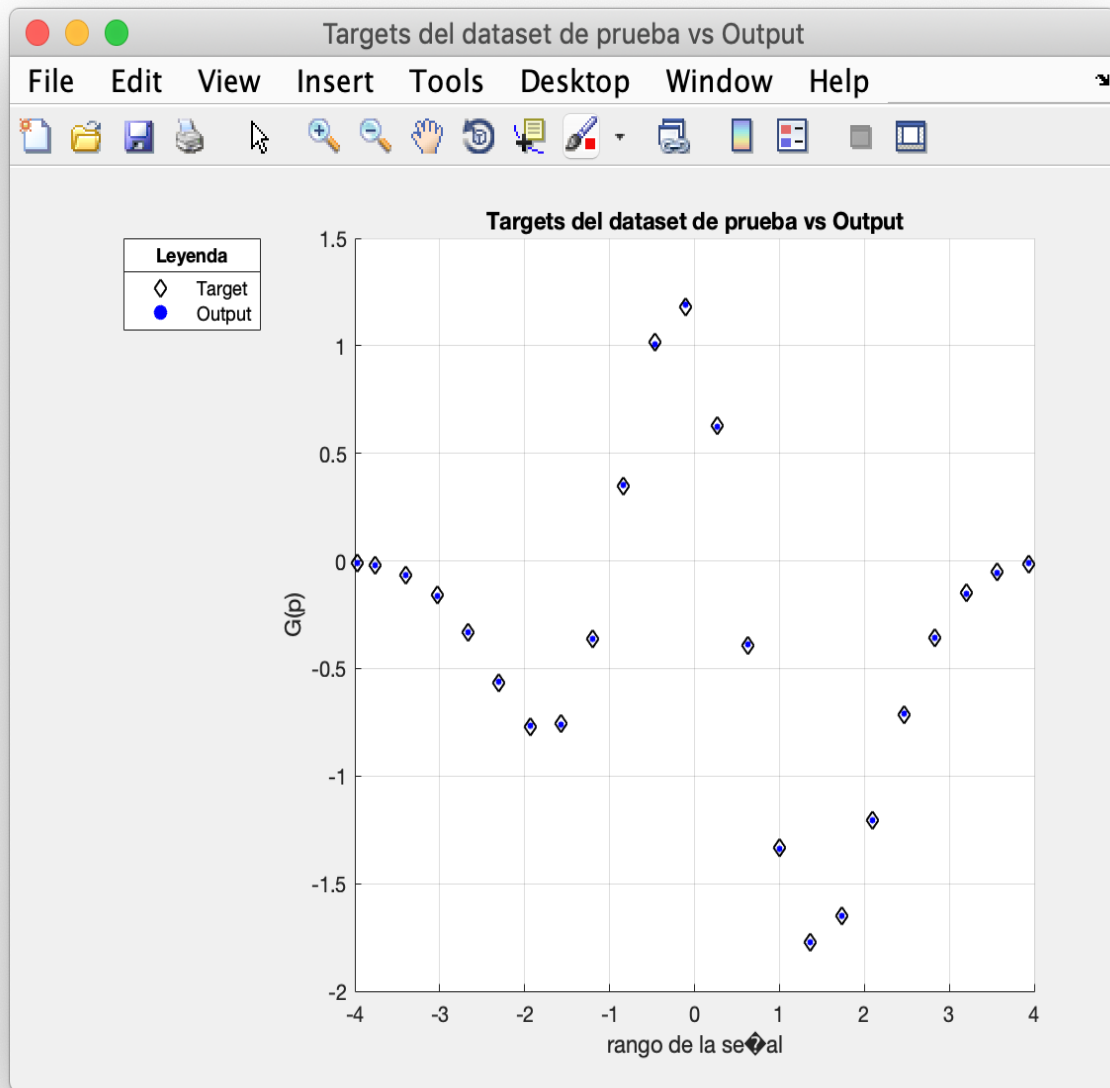


Figura 15: Gráfica 1.3

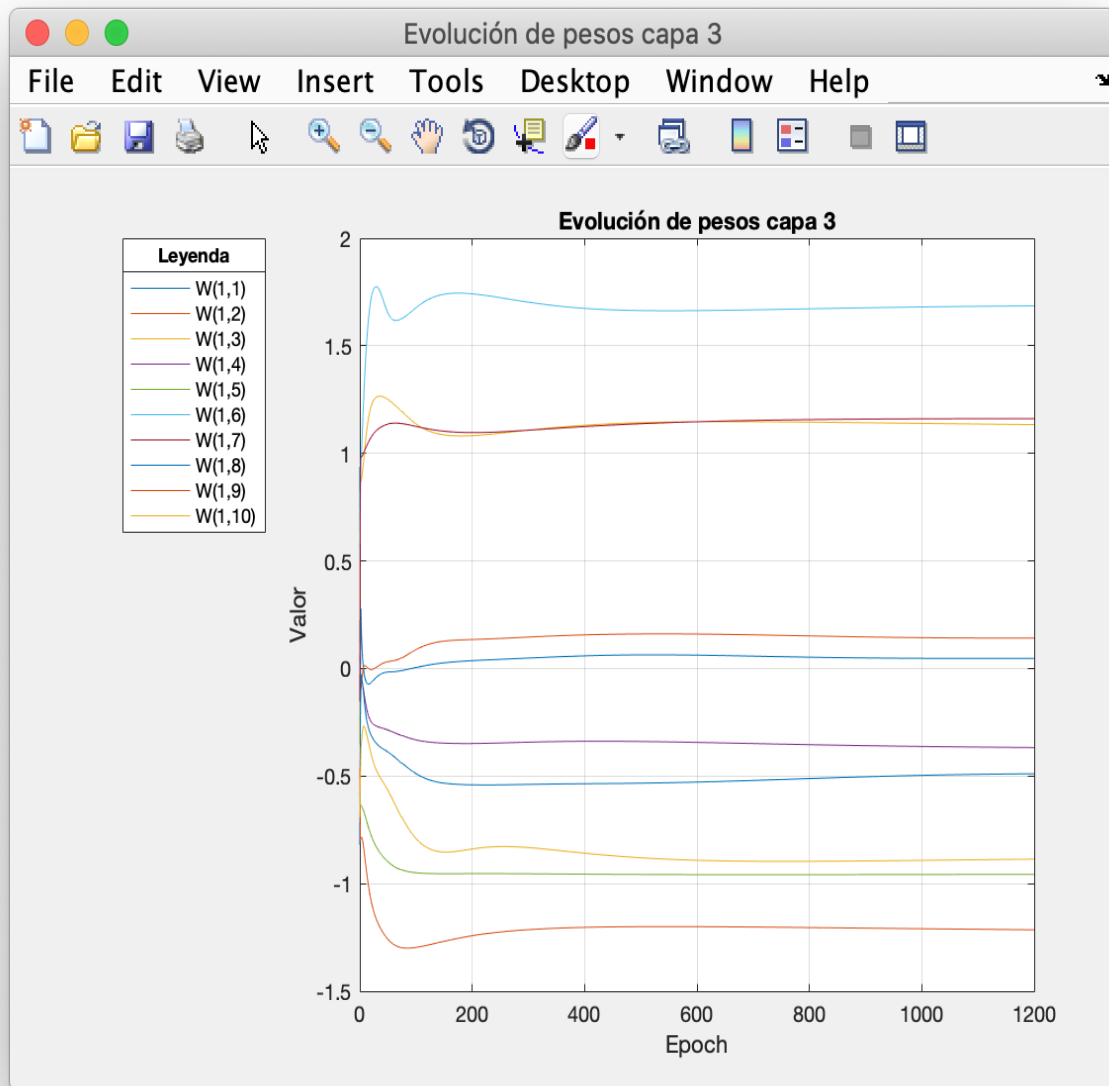


Figura 16: Gráfica 1.4

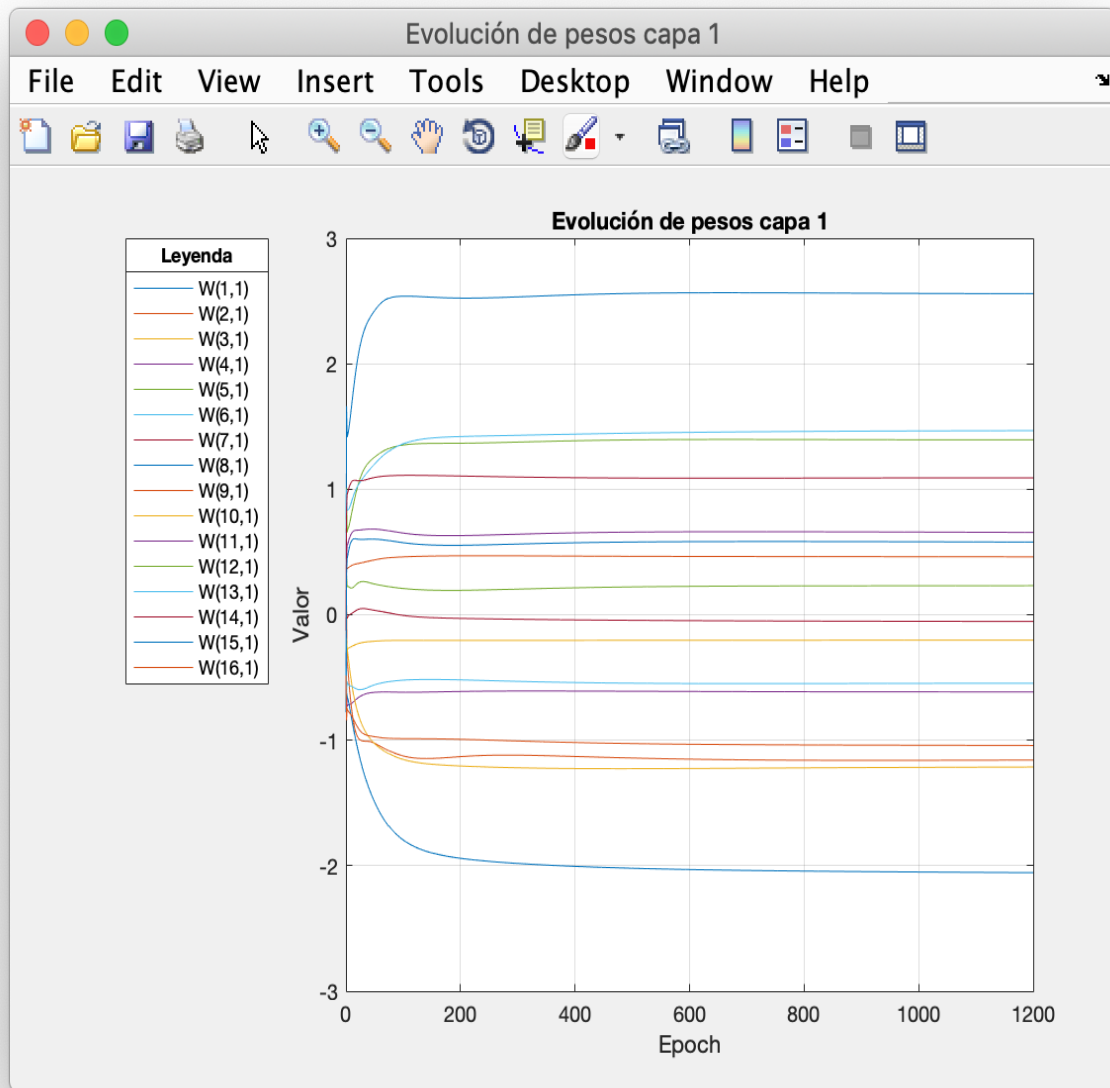


Figura 17: Gráfica 1.5

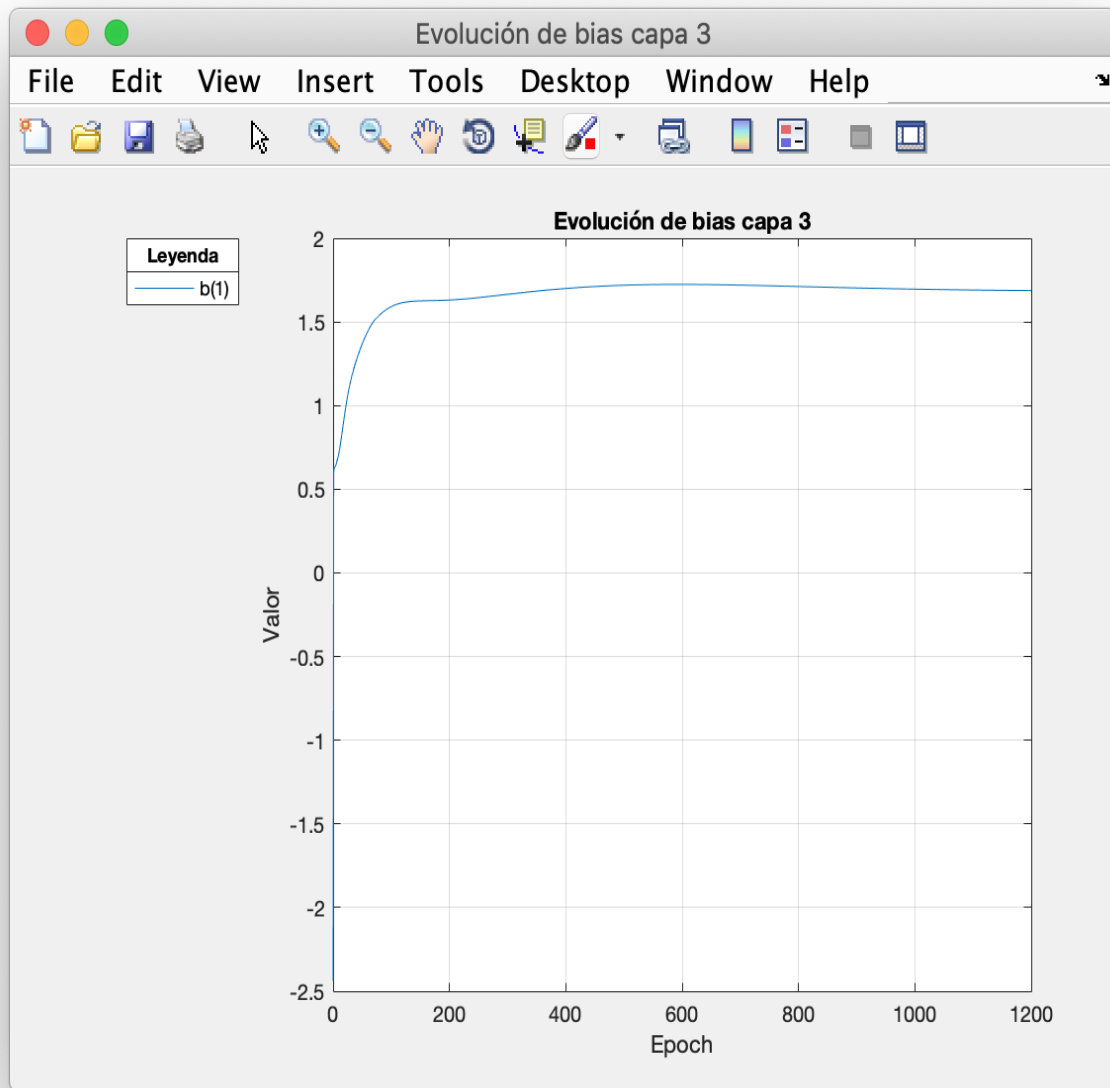


Figura 18: Gráfica 1.6

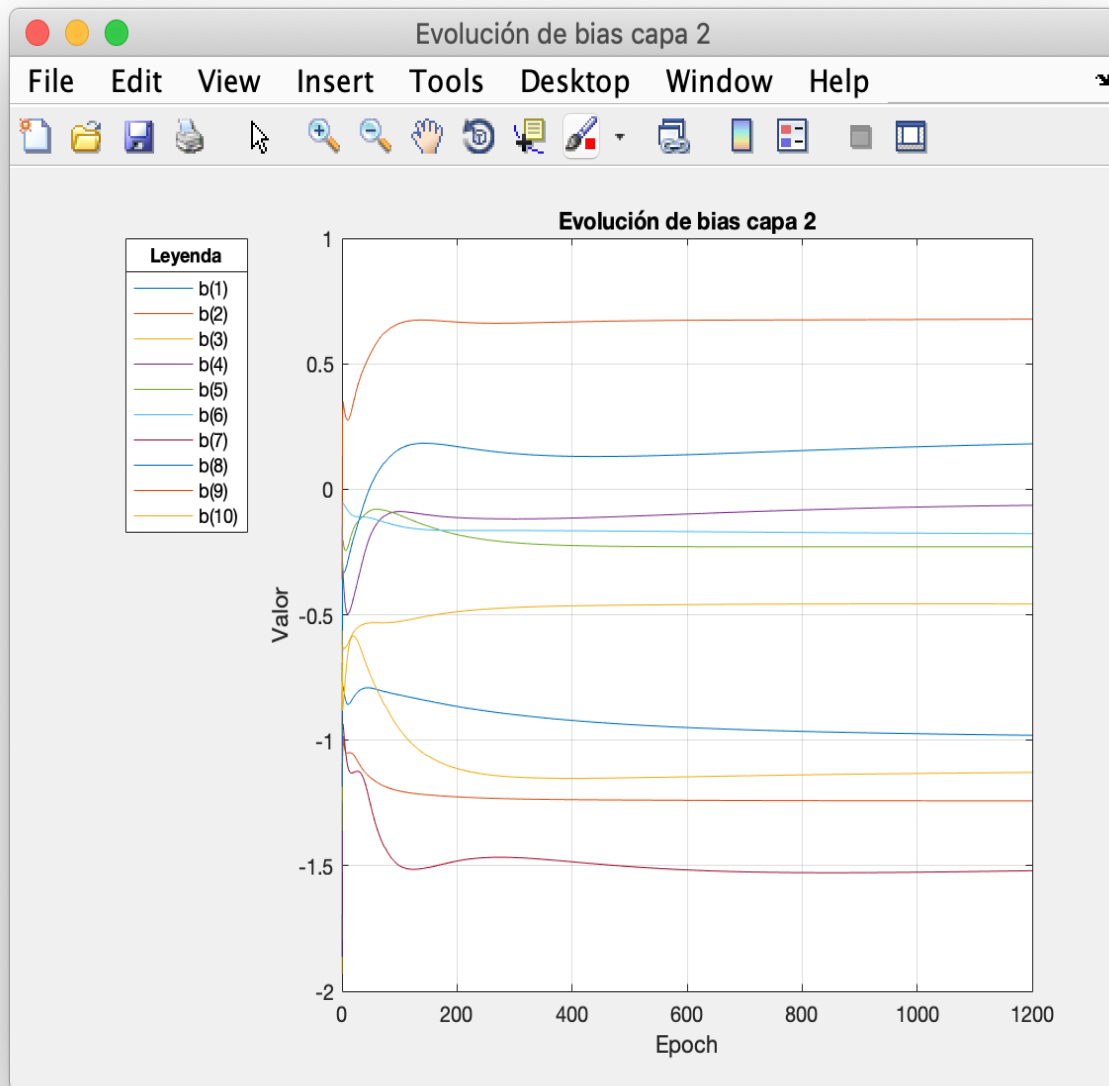


Figura 19: Gráfica 1.7

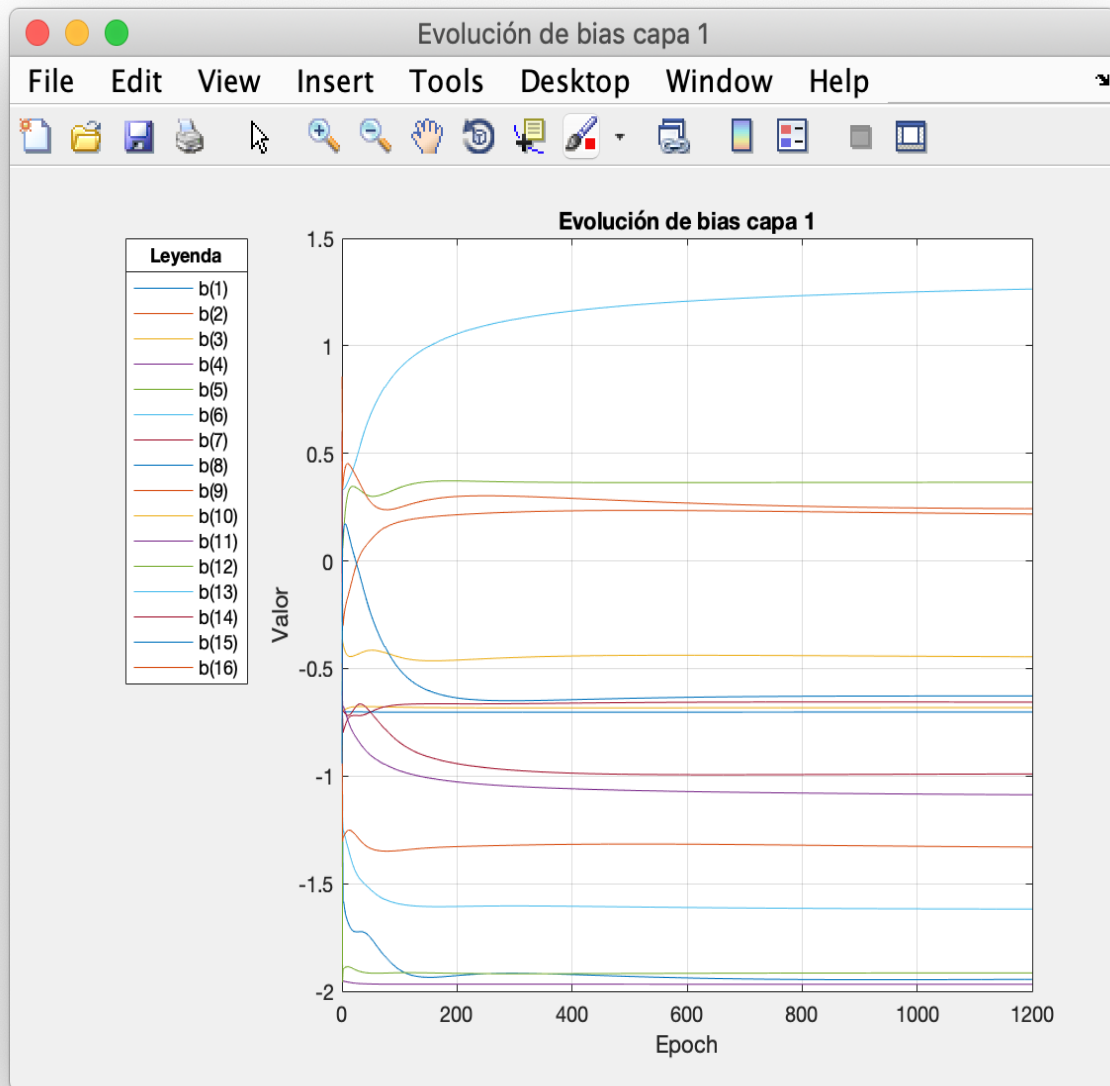


Figura 20: Gráfica 1.8

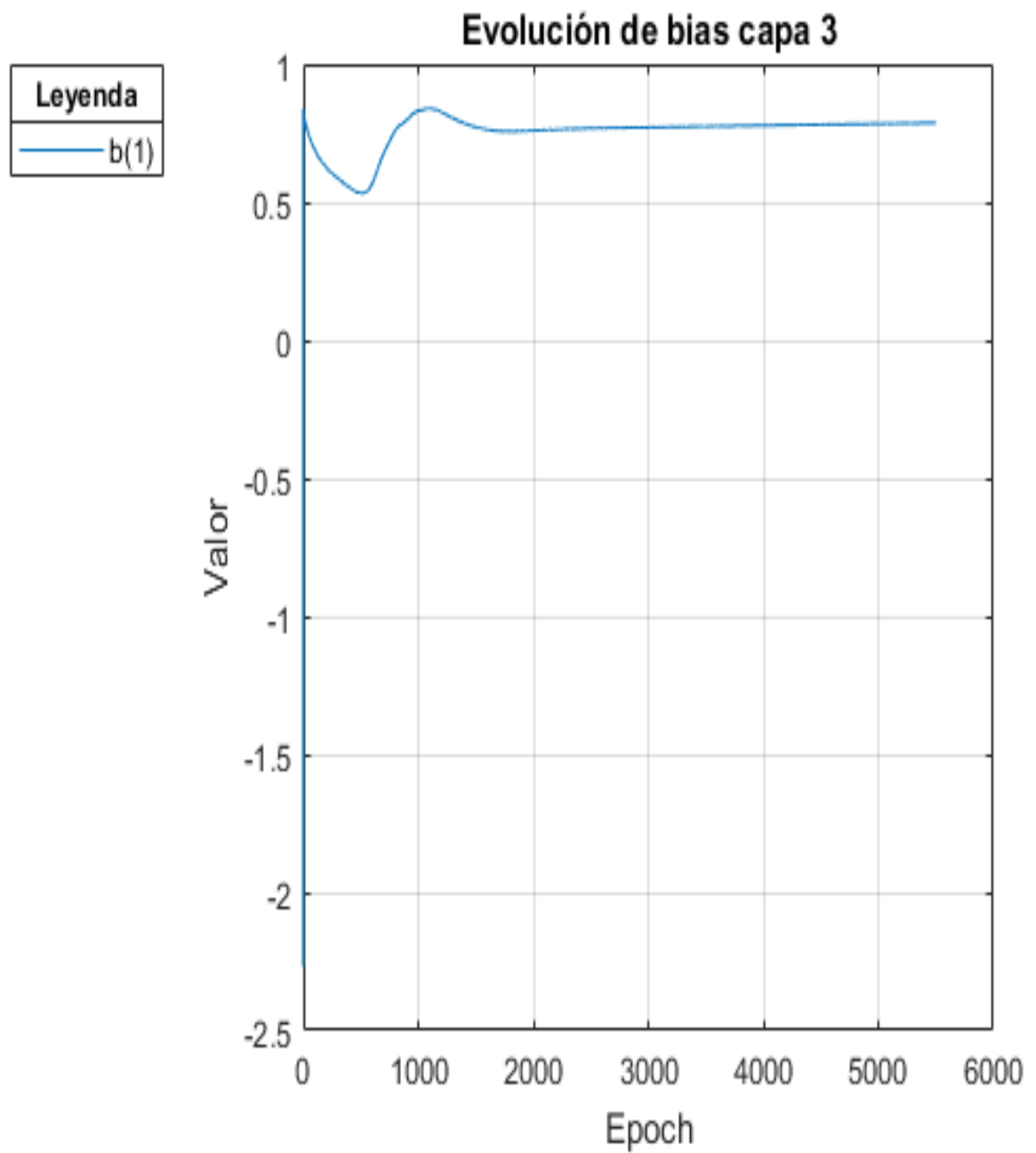


Figura 21: Gráfica 1.9

4. Discusión de Resultados

Para cada uno de los resultados se muestra:

1. Los datos con los cuales fue realizado el ejemplo.
2. Los pesos y bias iniciales.
3. La gráfica del “historial” de la evolución de los parámetros del perceptrón
4. La gráfica de los vectores de entrada con su target y la frontera de desición final.

5. Conclusiones

El perceptrón es la unidad básico de las redes neuronales que se usan hoy en día, su creador, Frank Rosenblatt, hizo una muy importante aportación para el campo de las redes neuronales artificiales. La práctica estuvo mucho más corta de lo que esperaba, la regla de aprendizaje es “magia”.

6. Referencias

Martin T Hagan. Machine Learning, Neural Network Design (2nd Edition), 2014.

<https://medium.com/@thomascountz/calculate-the-decision-boundary-of-a-single-perceptron-visualizing>

7. Apéndice

Listing 1: Código

```
1 clc
2 clear
3
4 % Read the inputs file
5 inputs_path = strcat(input('Ingrese el nombre del archivo de inputs sin la extensión:
    ','s'), '.txt');
6 %inputs_path = 'inputs.txt';
7 inputs = importdata(inputs_path);
8
9 % Read the targets
10 targets_file = strcat(input('Ingrese el nombre del archivo de targets sin la extensión
    : ','s'), '.txt');
11 %targets_path = 'targets.txt';
12 targets = importdata(targets_path);
13
14 data_size = size(inputs, 1);
15
16 % Enter MLP architecture
17 architecture = str2num(input('Ingrese el vector de la arquitectura: ','s'));
18 % Calculate layer parameters
19 %architecture = str2num('1 16 10 1');
20 num_layers = length(architecture) - 1;
```

```
21 R = architecture(1);
22 functions_vector = str2num(input('Ingrese el vector de las funciones de activación: 1)
    purelin()\n2) logsig()\n3) tansig()\n\n: ','s'));
23 %functions_vector = str2num('3 2 1');
24
25 %Enter the learning factor
26 alpha = input('Ingresa el valor del factor de aprendizaje(alpha): ');
27 %alpha = .01;
28
29 epochmax = input('Ingresa el número máximo de épocas: ');
30 % epochmax = 10000;
31 %validation_iter = 500;
32 %numval = 7;
33 %error_epoch_validation = .0000000000000001;
34 numval = input('Numero maximo de incrementos consecutivos del error de validacion (
    numval): ');
35 error_epoch_validation = input('Ingrese el valor minimo del error de epoca (
    error_epoch_validation): ');
36 validation_iter = input('Ingrese el múltiplo de épocas para realizar una época de
    validación (validation_iter): ');
37
38 % Dataset Slicing
39 config_option = input('Elija una configuración de distribución de datasets: \n1:
    80-10-10\n2: 70-15-15\n');
40 %config_option = 2;
41 [training_ds, test_ds, validation_ds] = dataset_slices(config_option, inputs, targets)
    ;
42 validation_ds_size = size(validation_ds, 1);
43 test_ds_size = size(test_ds, 1);
44 training_ds_size = size(training_ds, 1);
45
46 disp('Dataset de entrenamiento:');
47 disp(training_ds);
48 disp('Dataset de validacion:');
49 disp(validation_ds);
50 disp('Dataset de prueba:');
51 disp(test_ds);
52
53 % Open the files for weights and bias
54 total_weight_files = 0;
55 total_bias_files = 0;
56 for i=1:num_layers
57 % For neurons
58 for j=1:architecture(i + 1)
59 % For weights
60 for l=1:architecture(i)
61 total_weight_files = total_weight_files + 1;
62 end
63 end
```

```
64 total_bias_files = total_bias_files + 1;
65 end
66
67 W_files = zeros(total_weight_files, 1);
68 b_files = zeros(total_bias_files, 1);
69
70 current_file = 1;
71 for i=1:num_layers
72     path = strcat(pwd, '/historico/capa_', num2str(i), '/pesos/');
73     if ~exist(path, 'dir')
74         mkdir(path);
75     end
76     % For layers
77     for j=1:architecture(i + 1)
78         % For neurons
79         for k=1:architecture(i)
80             archivo_pesos = strcat(path, '/pesos', num2str(j), '_', num2str(k), '.txt');
81             W_files(current_file) = fopen(archivo_pesos, 'w');
82             current_file = current_file + 1;
83         end
84     end
85 end
86
87 current_file = 1;
88 for i=1:num_layers
89     path = strcat(pwd, '/historico/capa_', num2str(i), '/bias/');
90     if ~exist(path, 'dir')
91         mkdir(path);
92     end
93     for j=1:architecture(i+1)
94         archivo_bias = strcat(path, '/bias', num2str(j), '.txt');
95         b_files(current_file) = fopen(archivo_bias, 'w');
96         current_file = current_file + 1;
97     end
98 end
99
100 % Initialize MLP parameters and Print them
101
102 num_w_files = 1;
103 num_b_files = 1;
104 W = cell(num_layers, 1);
105 b = cell(num_layers, 1);
106 % Output of each layer
107 a = cell(num_layers + 1, 1);
108 % Sentitivities
109 S = cell(num_layers, 1);
110 % Derivatives of each layer
111 F_m = cell(num_layers, 1);
112
```



```
113 % For each layer
114 for i=1:num_layers
115 % Random value
116 W_r_value = 2 * rand(architecture(i + 1), architecture(i)) - 1;
117 b_r_value = 2* rand(architecture(i + 1), 1) - i;
118 W{i} = W_r_value
119 b{i} = b_r_value
120 % For each neuron
121 for j=1:architecture(i + 1)
122 %For each weight
123 for k=1:architecture(i)
124 % Print wights value
125 fprintf(W_files(num_w_files), '%f\r\n', W_r_value(j, k));
126 num_w_files = num_w_files + 1;
127 end
128 end
129 % For each neuron
130 for j=1:architecture(i + 1)
131 %print bias value
132 fprintf(b_files(num_b_files), '%f\r\n', b_r_value(j));
133 num_b_files = num_b_files + 1;
134 end
135 end
136
137 % Learning algorithm
138 num_validation_epoch = 0;
139 early_stopping_increment = 0;
140 validation_error = 0;
141 learning_error = 0;
142 early_s_counter = 0;
143
144 % initialize vectors for printing errors
145 learning_err_values = zeros(epochmax, 1);
146 evaluation_err_values = zeros(ceil(epochmax / validation_iter), 1);
147 for epoch=1:epochmax
148 l_error = 0;
149 % Reset the values
150 num_w_files = 1;
151 num_b_files = 1;
152 % if isn't a validation epoch
153 if(mod(epoch ,validation_iter) ~= 0)
154 for t_data=1:training_ds_size
155 % initial condition
156 a{1} = training_ds(t_data, 1);
157 % Foward propagation
158 for t_p=1:num_layers
159 W_aux = cell2mat(W(t_p));
160 b_aux = cell2mat(b(t_p));
161 a_aux = cell2mat(a(t_p));
```

```
162 n_f = W_aux * a_aux + b_aux;
163 a{t_p + 1} = get_activation_function(n_f, functions_vector(t_p));
164 end
165 a_aux = cell2mat(a(num_layers + 1));
166 t_error = training_ds(t_data, 2) - a_aux;
167 l_error = l_error + (t_error / data_size);
168 % Sensitivities calculation
169 F_m{num_layers} = get_F_matrix(functions_vector(num_layers), architecture(num_layers +
    1), a_aux);
170 F_m_temp = cell2mat(F_m(num_layers));
171 S{num_layers} = F_m_temp * (t_error)*(-2);
172 % Backpropagation
173 for m = num_layers-1:-1:1
174     W_aux = cell2mat(W(m+1));
175     s_aux = cell2mat(S(m+1));
176     a_aux = cell2mat(a(m+1));
177     F_m{m} = get_F_matrix(functions_vector(m),architecture(m+1),a_aux);
178     F_m_temp = cell2mat(F_m(m));
179     S{m} = F_m_temp * (W_aux')*s_aux;
180 end
181 % Learning Rules
182 for k = num_layers:-1:1
183     W_aux = cell2mat(W(k));
184     b_aux = cell2mat(b(k));
185     s_aux = cell2mat(S(k));
186     a_aux = cell2mat(a(k));
187     W{k} = W_aux - (alpha * s_aux * a_aux');
188     b{k} = b_aux - (alpha * s_aux);
189     W_aux = cell2mat(W(k));
190     b_aux = cell2mat(b(k));
191 end
192 end
193 learning_error = l_error;
194 learning_err_values(epoch) = l_error;
195 % This epoch is a validation one
196 else
197     val_error = 0;
198     num_validation_epoch = num_validation_epoch + 1;
199     for t_data = 1:validation_ds_size
200         % Initial Condition
201         a{1} = validation_ds(t_data, 1);
202         % Forward propagation
203         for k=1:num_layers
204             W_aux = cell2mat(W(k));
205             a_aux = cell2mat(a(k));
206             b_aux = cell2mat(b(k));
207             n_f = W_aux * a_aux + b_aux;
208             a{k + 1} = get_activation_function(n_f, functions_vector(k));
209         end
```

```
210 a_aux = cell2mat(a(num_layers+1));
211 val_error = validation_ds(t_data,2)-a_aux;
212 val_error = val_error+(val_error/validation_ds_size);
213 end
214 evaluation_err_values(epoch) = val_error;
215 if early_stopping_increment == 0
216 validation_error = val_error;
217 early_stopping_increment = early_stopping_increment+1;
218 fprintf('Incremento actual para early stopping = %d\n', early_stopping_increment);
219 else
220 if val_error > validation_error
221 validation_error = val_error;
222 early_stopping_increment = early_stopping_increment+1;
223 fprintf('Incremento actual para early stopping = %d\n', early_stopping_increment);
224 if early_stopping_increment == numval
225 %Reset the counter
226 early_s_counter = 1;
227 fprintf('Early stopping en la época: %d\n', epoch);
228 break;
229 end
230 else
231 validation_error = 0;
232 early_stopping_increment = 0;
233 fprintf('Incremento actual para early stopping = %d\n', early_stopping_increment);
234 end
235 end
236 end
237
238 %Print the values on console
239 num_w_files = 1;
240 num_b_files = 1;
241 for k = num_layers:-1:1
242 W_aux = cell2mat(W(k));
243 b_aux = cell2mat(b(k));
244 for j=1:architecture(k+1)
245 for l=1:architecture(k)
246 fprintf(W_files(num_w_files), '%f\r\n', W_aux(j,l));
247 num_w_files = num_w_files +1;
248 end
249 end
250 for j=1:architecture(k + 1)
251 fprintf(b_files(num_b_files), '%f\r\n', b_aux(j));
252 num_b_files = num_b_files + 1;
253 end
254 end
255
256 %Check stopping calculations
257 if mod(epoch,validation_iter) ~= 0 && l_error <= error_epoch_validation && l_error >=
    0
```

```
258 learning_error = l_error;
259 fprintf('Aprendizaje exitoso en la época %d\n', epoch);
260 break;
261 end
262 end
263
264 if epoch == epochmax
265     disp('Se llegó a epochmax');
266 end
267
268 % Print the las final values
269 if early_s_counter == 1
270     num_w_files = 1;
271     num_b_files = 1;
272     for k = num_layers:-1:1
273         W_aux = cell2mat(W(k));
274         b_aux = cell2mat(b(k));
275         for j = 1:architecture(k + 1)
276             for l=1:architecture(k)
277                 fprintf(W_files(num_w_files), '%f\r\n', W_aux(j, l));
278                 num_w_files = num_w_files + 1;
279             end
280         end
281         for j=1:architecture(k + 1)
282             fprintf(b_files(num_b_files), '%f\r\n', b_aux(j));
283             num_b_files = num_b_files + 1;
284         end
285     end
286 end
287
288 % Close all files
289 for i=1:total_weight_files
290     fclose(W_files(i));
291 end
292 for i=1:total_bias_files
293     fclose(b_files(i));
294 end
295
296 % Propagate the test dataset
297 test_error = 0;
298 output = zeros(test_ds_size,1);
299 for i=1:test_ds_size
300     % Initial condition
301     a{1} = test_ds(i,1);
302     for k=1:num_layers
303         W_aux = cell2mat(W(k));
304         a_aux = cell2mat(a(k));
305         b_aux = cell2mat(b(k));
306         n_f = W_aux*a_aux+b_aux;
```

```
307 a{k+1} = get_activation_function(n_f, functions_vector(k));
308 end
309 test_data = cell2mat(a(1));
310 a_aux = cell2mat(a(num_layers + 1));
311 test_error = test_error + (1 / test_ds_size) * (test_ds(i,2) - a_aux);
312 output(i) = a_aux;
313 end
314
315 % Print last errors
316 fprintf('Error de aprendizaje = %f\n', learning_error);
317 fprintf('Error de validación = %f\n', validation_error);
318 fprintf('Error de prueba = %f\n', test_error);
319
320
321 % Output vs test
322 scatter_output_vs_test(test_ds, output);
323 % Propagate the training size for plotting
324
325 output = zeros(training_ds_size,1);
326 for i=1:training_ds_size
327 % Initial Condition
328 a{1} = training_ds(i, 1);
329 for k=1:num_layers
330 W_aux = cell2mat(W(k));
331 a_aux = cell2mat(a(k));
332 b_aux = cell2mat(b(k));
333 a{k+1} = get_activation_function(W_aux*a_aux+b_aux,functions_vector(k));
334 end
335 a_aux = cell2mat(a(num_layers + 1));
336 test_error = test_error + (1 / training_ds_size) * (training_ds(i,2) - a_aux);
337 output(i) = a_aux;
338 end
339
340 scatter_output_vs_training(training_ds, output);
341
342 % Plot the error evolution
343 error_plot(validation_iter, num_validation_epoch, learning_err_values, epoch,
    evaluation_err_values);
344 % Plot weight evolution
345 weight_evolution_plot(architecture, num_layers, epoch);
346 % Plot bias evolution
347 bias_evolution_plot(architecture, num_layers, epoch);
348
349 % Write final values
350 for i=1:num_layers
351 path = strcat(pwd, '/Valores_finales/capa_', num2str(i), '/');
352 if ~exist(path, 'dir')
353 mkdir(path);
354 end
```

```
355 W_aux = cell2mat(W(i));
356 res_pesos = strcat(path, '/pesos.txt');
357 dlmwrite(res_pesos, W_aux, ';');
358 end
359
360 for i=1:num_layers
361 path = strcat(pwd, '/Valores_finales/capa_', num2str(i), '/');
362 if ~exist(path, 'dir')
363 mkdir(path);
364 end
365 b_aux = cell2mat(b(i));
366 res_bias = strcat(path, '/bias.txt');
367 dlmwrite(res_bias, b_aux, ';');
368 end
```