

Review

Automatic extraction of retinal features from colour retinal images for glaucoma diagnosis: A review

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ABSTRACT

Glaucoma is a group of eye diseases that have common traits such as, high eye pressure, damage to the Optic Nerve Head and gradual vision loss. It affects peripheral vision and eventually leads to blindness if left untreated. The current common methods of pre-diagnosis of Glaucoma include measurement of Intra-Ocular Pressure (IOP) using Tonometer, Pachymetry, Gonioscopy; which are performed manually by the clinicians. These tests are usually followed by Optic Nerve Head (ONH) Appearance examination for the confirmed diagnosis of Glaucoma. The diagnoses require regular monitoring, which is costly and time consuming. The accuracy and reliability of diagnosis is limited by the domain knowledge of different ophthalmologists. Therefore automatic diagnosis of Glaucoma attracts a lot of attention.

This paper surveys the state-of-the-art of automatic extraction of anatomical features from retinal images to assist early diagnosis of the Glaucoma. We have conducted critical evaluation of the existing automatic extraction methods based on features including Optic Cup to Disc Ratio (CDR), Retinal Nerve Fibre Layer (RNFL), Peripapillary Atrophy (PPA), Neuroretinal Rim Notching, Vasculature Shift, etc., which adds value on efficient feature extraction related to Glaucoma diagnosis.

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1. Introduction

Early detection and treatment of retinal eye diseases is critical to avoid preventable vision loss. Conventionally, retinal disease identification techniques are based on manual observations. Patients are imaged using a fundus camera or Scanning Laser Ophthalmoscope (SLO). Optometrists and ophthalmologists often rely on image operations such as change of contrast and zooming to interpret these images and diagnose results based on their own experience and domain knowledge. If specific abnormalities are observed, ophthalmologists may perform Fluorescein Angiography or Optical Coherence Tomography (OCT) for further investigation. These diagnostic techniques are time consuming and invasive. Automating procedures of diagnosis expect more patients to be screened and more consistent diagnoses can be given in a time efficient manner.

Glaucoma is one of the most common and leading cause of blindness [1] among retinal diseases with 13% of the cases being affected [2]. The changes occur in retinal structures, which gradually leads to peripheral vision loss and eventually causes blindness if left untreated. There is no cure for Glaucoma but its early diagnosis and treatment can prevent the vision loss. Since the manual based diagnostic process is costly and prone to error, therefore some efforts have been made on automatic detection of Glaucoma at an early stage. In this paper, we have conducted a comprehensive review on existing methods for automatic identification of anatomical features related to Glaucoma from retinal images, which provides insights for future directions on automatic detection of Glaucoma and other eye diseases from retinal images.

The rest of the sections is organized as follows: Section 2 briefly describes Glaucoma and the changes in retinal structures associated with Glaucoma. In Section 3, we discuss the current clinical methods for Glaucoma diagnosis. Section 4 overviews the existing methods on automatic detection of retinal features associated with Glaucoma in a systematic way. Section 7 concludes the work.

2. Retinal symptoms of glaucoma

Glaucoma is a group of eye diseases which is associated with simultaneous functional failure of the visual field. The structural changes are manifested by a slowly diminishing neuroretinal rim

indicating a degeneration of axons and astrocytes of the Optic Nerve. As lost capabilities of the Optic Nerve cannot be recovered, early detection and subsequent treatment are essential for affected patients to preserve their vision [3].

There are two main types of Glaucoma (i) Primary Open Angle Glaucoma (POAG) and (ii) Angle Closure Glaucoma (ACG). POAG is the most common form of Glaucoma accounting for at least 90% of all Glaucoma cases [4]. The Intra-Ocular Pressure (IOP), which maintains a permanent shape of the human eye and protects it from deformation, rises because the correct amount of fluid cannot drain out of the eye. With POAG, the entrances to the drainage canals work properly but a clogging problem occurs inside the drainage canals [5]. This type of Glaucoma develops slowly and sometimes without noticeable sight loss for many years. It can be treated with medications if diagnosed at the earlier stage. ACG happens when the drainage canals get blocked. The iris is not as wide and open as in the normal case. The outer edge of the iris bunches up over the drainage canals, when the pupil enlarges too much or too quickly. Treatment of this type of Glaucoma usually involves surgery to remove a small portion of the outer edge of the iris. There are four main changes in the retinal structures which are associated with Glaucoma and are explained as follows:

2.1. Optic Nerve Head variance

The Optic Nerve Head (ONH) is the location where the Optic Nerve enters the back of the eye. It is also known as blind spot since this area of retina cannot respond to light stimulation due to lack of photoreceptors. In a typical 2D retinal image, the Optic Nerve Head is a bright elliptic region with a distinguishable cup-like area called Optic Cup surrounded by rest of the area of Optic Disc, as shown in Fig. 1. There are several ways to quantify the Optic Cup to Disc Ratio (CDR) [6]. For instance, the ratio can be defined with respect to area, vertical length and horizontal length of both Optic Disc and Optic Cup. The CDR can be used to compare Glaucoma patients with Normal subjects, and it is an important measurement for the diagnosis of Glaucoma [6]. When more Optic Nerve Fibres disappear, the Optic Cup becomes larger with respect to the Optic Disc, which corresponds to increase in CDR value. In current clinical practice, the CDR is measured manually by an ophthalmologist and is subjective due to differences in the intra-observer experiences and training [7].

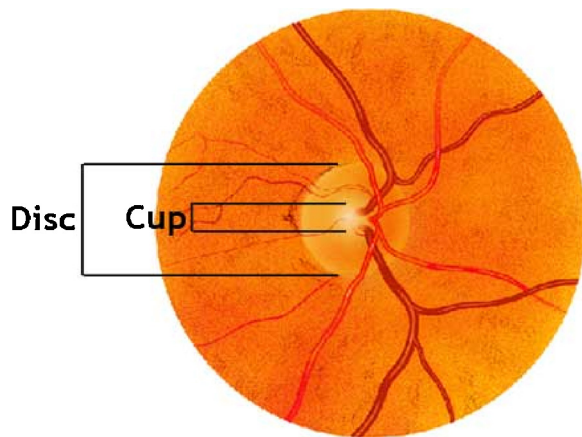


Fig. 1. Optic Disc and Optic Cup in fundus image.

2.2. Neuroretinal Rim loss determination

In Normal eyes, the Neuroretinal Rim usually follows a characteristic pattern as shown in retinal image taken from the right eye in Fig. 2. It is the broadest in the Inferior region followed by the Superior, then Nasal and finally the Temporal regions, which is called the ISNT rule [8]. In case of Glaucoma, the Neuroretinal Rim disobeys the earlier mentioned rule. Although this is not the case with all Glaucoma patients [9], it is still a useful clinical method to aid in diagnosing Glaucoma. For the left eye, the position of Temporal and Nasal region will swap each other.

2.3. Retinal Nerve Fibre Layer (RNFL) defects

According to clinical reports, RNFL defects, if detected, serve as the earliest sign of Glaucoma [10]. The RNFL appears as bright

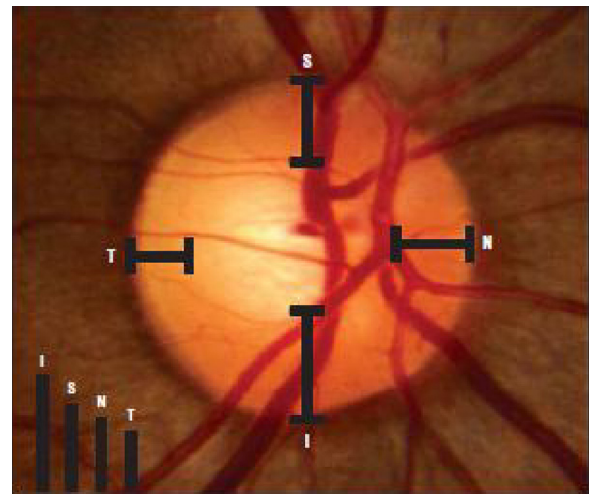


Fig. 2. Clinical assessment based on the ISNT rule obtained from Normal optic nerves. I, S, N and T represent Inferior, Superior, Nasal and Temporal regions separately. The image is taken from the right eye.

bundle striations that are unevenly distributed in Normal eyes. It can be assessed ophthalmoscopically on wide-angle, red-free photographs or by using sophisticated techniques such as Scanning Laser Ophthalmoscope (SLO) and Laser Polarimetry. In Normal eyes, the RNFL striations are most visible in the Temporal Inferior region, followed by the Temporal Superior, the Nasal Superior and the Nasal Inferior regions. There are two types of RNFL defects associated with Glaucomatous eyes. A localised RNFL defect appears as a wedge-shaped dark area in the RNFL with its tip touching the Optic Disc border [10] as shown in Fig. 3. They are often found in the Temporal Inferior region followed by the Temporal Superior

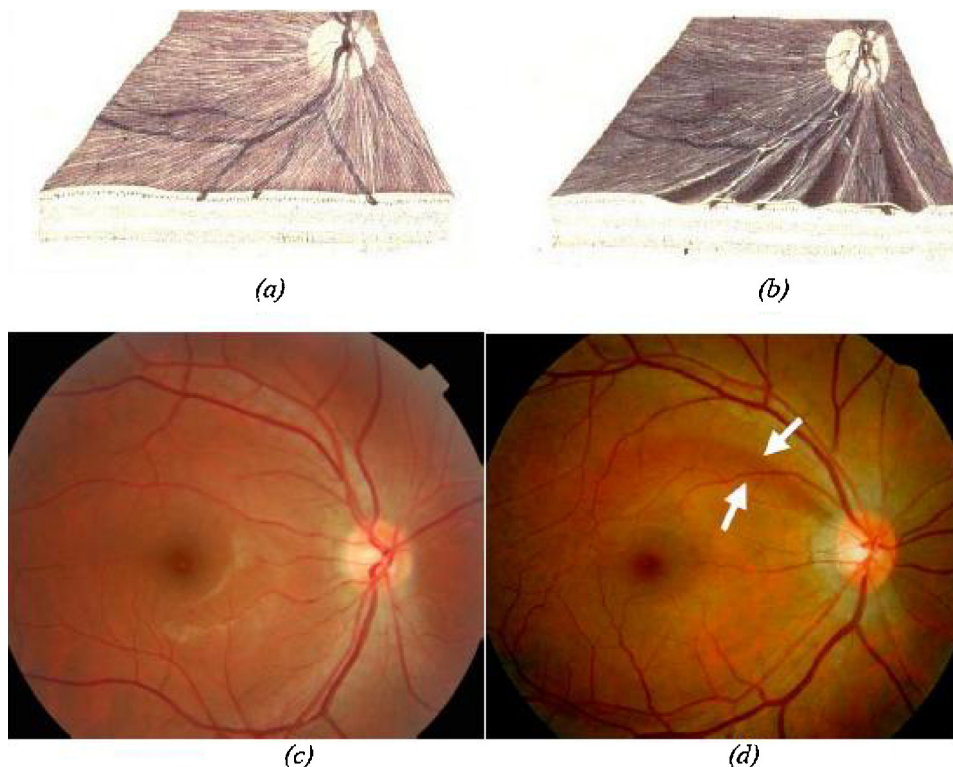


Fig. 3. Example of Localized RNFL in the right eye: (a) cross section view of Normal RNFL; (b) cross section view of RNFL defect; (c) Normal RNFL in fundus image; (d) RNFL defect in fundus image (white arrows pointed) [11].

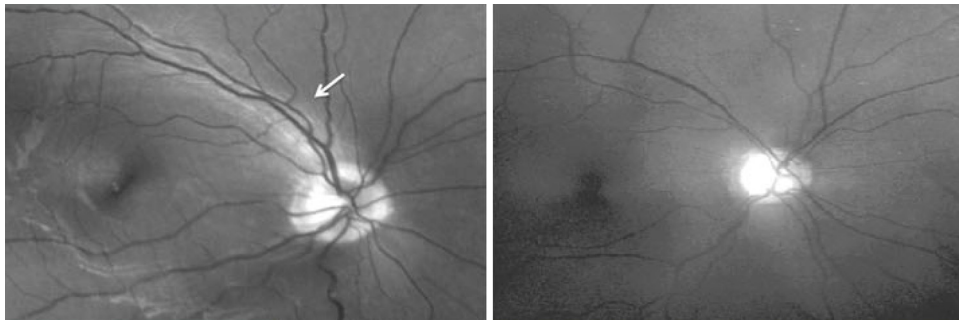


Fig. 4. Example of Diffuse RNFL in the right eye: (a) Normal RNFL in Scanning Laser Ophthalmoscope (SLO) image (white arrow pointed); (b) Diffuse RNFL Defect in SLO image [12].

region. Diffuse RNFL defect results in a decrease in appearance of RNFL due to loss of ganglion cells as shown in Fig. 4.

2.4. Peripapillary Atrophy

Peripapillary Atrophy (PPA) is an important risk factor and its progression can lead to Disc Haemorrhage and thus Glaucoma [13]. It is the degeneration of the retinal pigment epithelial layer, photoreceptors and underlying choriocapillaries in the region surrounding the ONH [14]. PPA is divided into two zones namely central β -zone and peripheral α -zone as shown in Fig. 5. α -zone is characterized by irregular hypopigmentation, hyperpigmentation and intimated thinning of the chorioretinal tissue layer. On its outer side it is adjacent to retina and on its inner side it is in touch with β -zone characterized by visible sclera and visible large choroidal vessels. In Normal eyes, both α -zone and β -zone are frequently located in the Temporal region followed by Inferior region and Superior region. In Glaucomatous eyes, β -zone occurs more frequently in the Temporal region [15] and its extent correlates with the RNFL thinning.

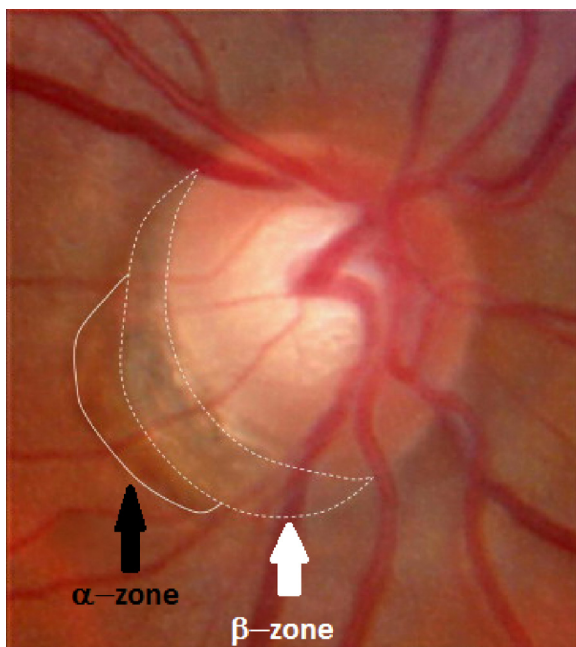


Fig. 5. PPA with α -zone and β -zone [16]. β -Zone occurs more frequently in the Temporal region of the right eye.

3. Clinical methods for diagnosing glaucoma

Glaucoma is usually realized by a patient after a long time of disease progression. This is because Glaucoma usually damages the outer edge of the eye and works slowly inwards [17]. Therefore, it is important to have regular eye tests so that any symptoms can be detected and treated as early as possible. According to UK's National Institute of Health and Clinical Excellence (NICE) guidelines [18], the tests which should be offered for suspecting Glaucoma or Ocular Hypertension are eye pressure test (Tonometry), corneal thickness (Pachymetry), Gonioscopy, visual field test (Perimetry) and ONH appearance.

Tonometry uses an instrument called a tonometer to measure IOP. Glaucoma is suspected if IOP value exceeds 21Hg. There are several techniques for tonometry. Among those techniques, Goldmann Applanation is considered the gold standard among other tests [19] as inter and intra-observer variability is between 2–3 mmHg. However, high pressures of IOP are not an accurate indication for Glaucoma [20] as different patients have different cornea thickness. Therefore, Pachymetry is the test used to determine thickness of cornea and it is important because actual IOP may be underestimated in the patients with thinner cornea, and overestimated in the patients with thicker cornea [21]. Gonioscopy can help to determine whether this angle is open or closed (blocked). It is an examination of the front outer edge of the eye, between the cornea and the iris. This is the area where the fluid should drain out of the eye. As peripheral vision is usually the first to deteriorate in Glaucoma, Perimetry is a systematic measurement of light sensitivity in the visual field by detection of targets presented on defined background. It checks for missing areas of peripheral vision. It may take three examinations before an accurate baseline is obtained and moreover long-term fluctuations in the field tests can often occur. Therefore the accuracy of this method is still questioned [22,23].

Glaucoma leads to alterations in the ONH, neuroretinal rim and vasculature structure. By analyzing retinal images, anatomical changes in retina due to Glaucoma can be observed. However, manual observation of ONH is time consuming and subject to inter-observer variability. Therefore efforts are being conducted to determine the anatomical changes in the retinal structures due to Glaucoma from the retinal images automatically. Also because changes observed in RNFL are also one of the early signs of Glaucoma, ophthalmologists usually go for 3D imaging in order to determine the thickness of RNFL. These imaging modalities include Scanning Laser Polarimetry (SLP), Confocal Scanning Laser Ophthalmoscopy (CSLO) and Optical Coherence Tomography (OCT) [24]. SLP utilizes the birefringent properties of the RNFL to measure its thickness by measuring the phase-shift of the polarized light through the layer. CSLO employs the principle of light reflection. Here a laser is projected through a pinhole towards the area of interest and the reflections are picked up through another pinhole

in front of light detector. OCT, based upon interferometry, is a non-invasive, non-contact method of producing high-resolution images utilizing coherence property of light reflected from a scanned area [25]. Its working principle is like ultrasound but OCT has higher resolution and it discriminates quite well between Normal and Glaucomatous eyes. Nevertheless, its role in detecting any Glaucomatous progression is uncertain [26].

4. Segmentation based automatic feature detection methods of retinal structures symptomatic for glaucoma

Since the current clinical methods for the diagnosis of Glaucoma are mostly based on manual observations and sometimes invasive, therefore the use of automatic detection of features related to Glaucoma can aid their diagnosis in a time effective and non-invasive manner. There is no cure for Glaucoma but its diagnosis and treatment at earlier stage can slow down the progression of the disease. There are some segmentation and non-segmentation (discussed in the Section 5) based automatic methods used to determine features of the retinal structures that reflect changes due to Glaucoma. Since most of segmentation based need ONH analysis, therefore, most of the existing methods for analysis of the Glaucoma are related to extraction of ONH and its anatomical structures. Still, there are some methods of detecting RNFL defect which aid in diagnosing Glaucoma and do not require Optic Disc detection and segmentation. The methods described in this section are classified in terms of image processing techniques and are mentioned in the form of hierarchy as shown in Fig. 6. Their results are summarized in Tables 1–5. The results which were applied on common datasets are grouped together so as to compare different methods on a common benchmark. Moreover the evaluation measures used in Literature Survey are defined in A and the public databases used for experimentation are briefed in B.

4.1. Localization of ONH

The Localization of ONH is the initial step in order to locate other anatomical structures, vessel tracking and registering changes within Optic Disc region. If any pixel within the Optic Disc boundary is located, then it can facilitate the extraction of the Optic Disc boundary. There are three main categories for the localization methods of the Optic Disc boundary which are discussed in the following paragraphs and a summary of the methods is shown in Table 1.

4.1.1. Optic disc detection as the brightest region

The first category is based on calculating the intensity of pixels in coloured and grayscale image. Under normal circumstances, the Optic Disc region is the brightest region on the retinal image. Therefore it can be detected by thresholding out the pixels with the intensity values below the certain level [27].

Sinthanayothin et al. [28] localized the Optic Disc using Local Contrast Colour Enhancement in Intensity-Hue-Saturation space. The variance image after converting back to RGB space will intensify the Optic Disc as compared to rest of the image. The algorithm resulted in high accuracy in their local dataset however, others have found its high failure rate in the images with a large number of white lesions, light artifacts or strongly visible choroidal vessels [29]. The use of pre-processing steps such as image filtering for removing artifacts brighter than the Optic Disc may result in improvement of the results. Walter et al. [30] localized the Optic Disc center with the proposal to select the brightest two percent of the image pixels to determine a threshold. After thresholding the image, the region with the largest area is likely to be Optic Disc region. The algorithm was applied on a set of 30 retinal images however, it failed on a low contrast image. Sekhar et al. [31] improved

the method by utilizing mathematical morphology to apply the shade correction on the retinal image. The mathematical morphology is the process of analyzing the geometrical structures present in the image by affecting their shape and form [32]. The largest area of the shape corrected retinal image was considered as Optic Disc region. The shade correction although improved the localization accuracy as compared to the previous method, its role in locating the Optic Disc region is uncertain. In order to locate the Optic Disc automatically, both methods used Circular Hough Transform [33] which aims to find circular patterns within an image.

In spite of assuming the Optic Disc as the brightest region of the retinal image is the straightforward approach to localize the region, the method is unreliable. The technique usually fails to localize the Optic Disc in the retinal images having artifacts and the bright regions in the diseased retina. Moreover, this assumption is not a guaranteed way to determine the center of the Optic Disc.

4.1.2. Center localization by matching of the Optic Disc template

The second category is based on formation of template representing the Optic Disc and matching the template in a test image. The results were comparatively accurate as compared to first category at the expense of the computational time. Later on, the computational time was reduced by introducing efficient algorithmic procedure.

Li et al. [40] modeled the Optic Disc texture using Principal Component Analysis (PCA). The Optic Disc in a test image was localized by dividing the test image into sub-images and Euclidean distance from the PCA-model was calculated for each sub-image. The sub-image with the Optic Disc at the center will have least Euclidean distance from the PCA model. The results were accurate but the search procedure was computationally inefficient. Computational time may be reduced if the image resolution is reduced as less number of pixels will allow to execute the task earlier but consequently, it might skip some of the textural information resulting in decrease in accuracy of the localization. Osareh et al. [37] evaluated the normalized correlation coefficient in order to compare the template image and the region of consideration. The template was generated after averaging the 16 colour-normalized retinal images. The method only detected the location based on highest value of normalized correlation coefficient which does not necessarily mean the Optic Disc center. They further improved their template by dividing the Optic Disc into smaller segments and selecting the largest segment which is approximate to a half circle and the region is not occluded by blood vessels. The algorithm followed the iterative procedure for minimizing the error between the set of pixels in the arc points and the estimated arc. The center of the circular arc is the approximate location of Optic Disc center. These template based matching algorithms were less computationally efficient therefore some pre-processing steps were introduced in order to improve the computational time.

Lalonde et al. [38] proposed an Optic Disc center detection method based on Pyramidal Decomposition and circular template matching. Pyramidal Decomposition reduces the image resolution to one-fourth at each iteration level. At the fifth level, bright regions of retina other than Optic Disc are vanished. The localization of the brightest pixel led to the determination of Optic Disc area for determining the edges of anatomical structures. The edge map was thresholded based on the strongest edges in the retinal image and the circular template was then compared along the pixels having strong edges. This made the computational time smaller as the template did not need to be compared pixel by pixel in the retinal image. Then pixel with the lowest degree of mismatch (Hausdorff distance) with the circular template and the highest confidence value was regarded as Optic Disc center. The author reported the failure cases when pyramidal decomposition sometimes localized the brightest pixel very far from Optic Disc due to artifacts in the retinal

Table 1
Accuracy of several methods of optic disc detection/center localization.

Localization method	Image database	Colour space	Image dimension	Number of test images	Accuracy	Citation
ONH as brightest region						
Local Contrast Colour Enhancement	STARE [34]	24-Bit RGB to IHS space	605 × 700	81	42% within ONH	[28,35]
Thresholding Highest Pixel Intensities	STARE [34]	24-Bit RGB to HLS space	605 × 700	81	58% within ONH	[30,35]
Shade Correction using Morphology	STARE [34]	24-Bit RGB	605 × 700	17	82.3% within ONH	[31]
	DRIVE [36]	8-Bit RGB	768 × 584	38	94.7% within ONH	
ONH template matching						
Least Squares Regression Arc Estimation	STARE [34]	24-Bit RGB	605 × 700	81	58% within ONH	[37,35]
Pyramidal Decomposition and Circular Template Matching	STARE [34]	24-Bit RGB	605 × 700	81	71.6% within ONH	[38,35]
Vasculature Detection using matched filter	STARE [34]	24-Bit RGB	605 × 700	81	98.7% within 60 pixels	[39]
	DRIVE [36]	8-Bit RGB	768 × 584	40	100% within 60 pixels	
Principal Component Analysis	National University Hospital Singapore	24-Bit RGB	512 × 512	40	–	[40]
Averaging Optic Disc Region	Bristol Eye Hospital	24-Bit RGB	760 × 570	60	–	[37]
Vasculature convergence point						
Fuzzy Convergence of Blood Vessels	STARE [34]	24-Bit RGB	605 × 700	81	89% within 60 pixels	[41]
Mathematical modeling of Vasculature Structure	STARE [34]	24-Bit RGB	605 × 700	81	98% within ONH	[42]
Tensor Voting and Mean-Shift procedure	STARE [34]	24-Bit RGB	605 × 700	81	92% within ONH	[43]
Horizontal and Vertical Edge Mapping	STARE [34]	24-Bit RGB	605 × 700	81	97% within 60 pixels	[44]
	DRIVE [36]	8-Bit RGB	768 × 584	40		
Fractal Dimension Analysis	DRIVE [36]	8-Bit RGB	768 × 584	40	–	[45]
Gabor Filter Vessel Detection	MESSIDOR [46]	8-Bit RGB to CIE space	1440 × 960	1200	98.3% within ONH	[47]
			2240 × 1488 2304 × 1536			

Table 2
Results of different methods of optic disc extraction.

Localization method	Image database	Colour space	Image dimension	Number of test images	Accuracy	Citation
Non-model based approach						
Morphological Operation	Kasturba Medical College India	8-Bit RGB to grayscale	560 × 720	24 Normal and 37 Glaucoma	90% Neural Network [49] classification	[48]
Fuzzy Histogram	Kasturba Medical College India	8-Bit RGB to Lab space	560 × 720	30 Normal, 31 Retinopathy and 39 Glaucoma	93.4% Overlapping Score	[50]
Circular Hough Transform on gradient map	MESSIDOR [46]	8-Bit RGB	1440 × 960 2240 × 1488 2304 × 1536	1200	86% Overlapping Score	[51]
Genetic Algorithm for elliptical approximation	DRION-DB [52]	8-Bit RGB	600 × 400	110	96% images have ≤5 pixel MAD	[52]
K-Means Clustering	Aravind Eye Hospital India	YUV space	1504 × 1000	20 Normal and 25 Glaucoma	91.7% CDR Correlation Coefficient	[53]
Watershed Transformation	Mines ParisTech	8-Bit RGB to HLS space	640 × 480	30	–	[30]
Hough Transform on Edge Map	DRIVE [36]	8-Bit RGB to Y channel	768 × 584	40	73% Overlapping Score	[54]
Thresholding	STARE [34]	24-Bit RGB	605 × 700	81	93% of OD diameter	[55]
Freeform modeling						
Morphological Preprocessing	New York Library	8-Bit RGB to YIQ space	285 × 400	9	–	[56,58]
Morphological Preprocessing	Bristol Hospital	24-Bit RGB to Lab space	760 × 570	16	90.3% Overlapping Score	[58]
Circular Hough Transform Initialization	National University Hospital Singapore	24-Bit RGB have ≤3 pixel	512 × 512	100	93% images MAD	[59]
Level Set Approach	Aravind Eye Hospital India	8-Bit RGB	2896 × 1944	33 Normal and 105 Glaucoma	97% Overlapping Score	[60]
Fast Level-Set Approach	MESSIDOR [46]	8-Bit RGB	1440 × 960 2240 × 1488 2304 × 1536	1200	89.5% 1 – (MAD/OD radius)	[47]
Statistical shape modeling						
Image Gradient Based Landmark Search	National University Hospital Singapore	24-Bit RGB	512 × 512	35	82% images have ≤3 pixel MAD	[61]
RANSAC approach	Seoul University Korea	8-Bit RGB	2896 × 1944	53 Normal and 30 Glaucoma	84.5% Overlapping Score	[62]
Minimum Mahalanobis distance Method	ORIGA ^{light} [63]	8-Bit RGB	3072 × 2048	482 Normal and 168 Glaucoma	89% Overlapping Score	[11]
Search Space Restriction along Normal Lines	DRION-DB [52]	8-Bit RGB	600 × 400	110	92% Overlapping Score	[65]

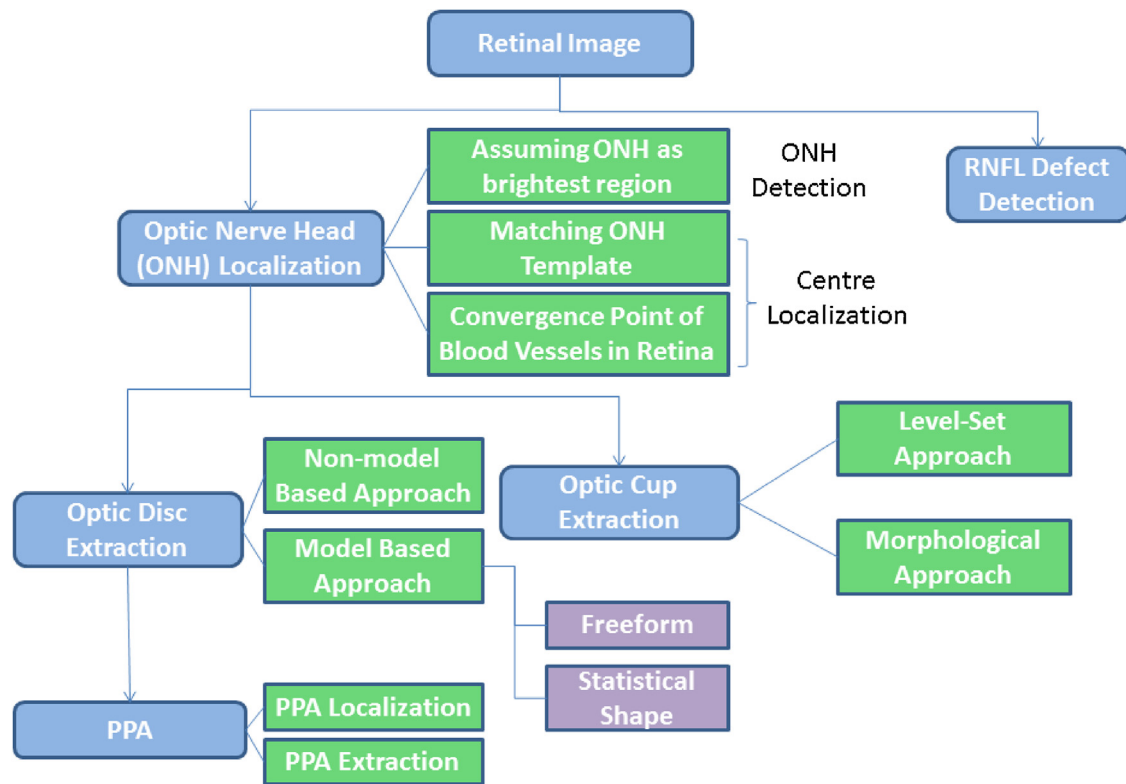


Fig. 6. A hierarchy of methodologies for segmentation based automatic feature extraction from digital retinal images.

Table 3

Results of different methods of optic cup extraction.

Localization method	Image database	Colour space	Image dimension	Number of test images	Accuracy	Citation
Morphological approach						
Fuzzy C-means Clustering	Aravind Eye Hospital India	RGB space	1504 × 1000	20 Normal and 25 Glaucoma	91.7% CDR Correlation Coefficient	[53]
Morphological Operations	Kasturba Medical College India	8-Bit RGB converted to grayscale	560 × 720	24 Normal and 37 Glaucoma	90% Neural Network [49] classification	[48]
Level-set approach						
Vessel Kink Interpolation in 3D	Aravind Eye Hospital India	8-Bit RGB	2896 × 1944	33 Normal and 105 Glaucoma	82% Overlapping Score	[60]
Gradient Vector Flow Modeling	ORIGA ^{light} [63]	8-Bit RGB	3072 × 2048	94 Normal and 10 Glaucoma	90.85% CDR Correlation Coefficient	[73]
Blood Vessel Kinks Edge Detection	ORIGA ^{light} [63]	8-Bit RGB	3072 × 2048	17 Normal and 10 Glaucoma	95.2% CDR Correlation Coefficient	[74]

Table 4

Results of different methods of PPA localization/extraction.

Extraction method	Image database	Colour space	Image dimension	Number of test images	Accuracy	Citation
PPA detection						
Disc Difference Method	SCORM [75]	RGB converted to HSV space	800 × 800	20 Normal and 20 Glaucoma	95% within PPA	[76]
GLCM Based Texture Analysis	SCORM [75]	RGB converted to HSV space	800 × 800	20 Normal and 20 Glaucoma	92.5% within PPA	[77]
PPA extraction						
GLCM Based Texture Analysis	Gifu University Hospital Japan	8-Bit RGB	1600 × 1200	26	73% LDA Segmentation Overlapping Score	[78]

Table 5
Results of different methods of RNFL detection.

Extraction method	Image database	Colour space	Image dimensions	Number of test images	Accuracy	Citation
Directional Gabor Filters	Gifu University Japan	RGB space converted to grayscale	768 × 576	52	71%	[81]
Intensity Profile Plotting	Regional Institute of Ophthalmology, India	Green plane of RGB	768 × 576	300 Normal and 529 Glaucoma	91.5%	[82]
Markov Random Fields	Eye Clinic Zlin, Czech Rep	Green and Blue Channels of RGB space	3504 × 2336	18 Normal and 10 Glaucoma	89.3%	[83,84]

image, and Hausdorff distance based circular template matching was failed when Optic Disc was highly occluded by blood vessels. As discussed earlier, the use of image filtering e.g. Directional Gabor Filters as a preprocessing step can improve the results. Yousiff et al. [39] applied directional matched filter in order to determine the vasculature structure. Then a window of 9x9 from the test image was compared on the pixels belonging to the vasculature structure which can be resized based on size of the image. The pixel with least accumulative distance was regarded as Optic Disc center. Yu et al. [47] used binary template to define the search region for the Optic Disc. They further applied the Directional Gabor Filters and calculated the standard deviation of the Optic Disc pixel candidates. The pixel candidates were determined after sorting the pixels of the search region using Pearson's correlation coefficient. The pixel candidates with maximum standard deviation was regarded as Optic Disc center.

Center localization of the Optic Disc using template matching proved to be more accurate as compared to the methods based on assumption of highest pixel intensity values within Optic Disc region due to non-uniform illumination in the retinal image. PCA and circular arc based template matching were the initial steps towards the Optic Disc center localization. In spite of they were more accurate as compared to pixel intensity based techniques, they were still not able to distinguish among artifacts across the retinal image. Moreover, the removal of blood vessel occlusion reduced the quality of template to be compared. Pyramidal Decomposition improved the center detection in terms of computational time however, the misguidance by artifacts remained. The use of directional filters for vasculature segmentation were then introduced which not only reduced the search region for the best candidate of the Optic Disc center but also improved the detection accuracy. But the use of directional filters may be less applicable to the images diseased with glaucoma as the atrophy around the Optic Disc would also be segmented out as the part of the vasculature structure which may affect the detection accuracy based on template matching.

4.1.3. ONH center as convergence point of retinal blood vessels

The third category regards the convergence point of blood vessels in retina to be the center of the ONH. This assumption avoided mis-localization of the Optic Disc as most of the retinal blood vessels converge within the ONH region. Moreover if the retinal vasculature structure is segmented out accurately, it can also avoid the detection failure of Optic Disc center due to template matching.

Hoover et al. [41] segmented out the blood vessels in order to determine the point of intersection. A voting process was introduced in order to find out points where a large number of blood vessels combine and the point with maximum votes was regarded as ONH center. Then, illumination equalization was applied in order to determine the different region in retinal image as the method was also applied to retinal images having diseases such as Diabetic Retinopathy (DR) and Age-Related Macular Degeneration (AMD) which shows different bright spots on retina. Finally, hypothesis

was developed based on region size and if only one region was classified out, it was considered as Optic Disc region. The hypothesis testing might involve parameters other than region size such as region circularity in order to improve the accuracy. Foracchia et al. [42] not only localized the ONH center as the main convergence point of blood vessels but also approximated the entire vasculature structure by fitting it with a mathematical model. The algorithm does not require accurate vasculature segmentation although it may not converge in the retinal images with low contrast ONH regions. Ying et al. [45] differentiated ONH from other bright regions, including exudates and artifacts, based on fractal dimension of blood vessels. A fractal dimension is a ratio providing a statistical index of complexity comparing how detail in a pattern changes with the scale at which it is measured. The fractal dimension of vasculature structure within ONH area is approximately 1.7 and it is higher as compared to fractal dimension of other bright areas. The method was applied on DRIVE database but no overall accuracy of the method was reported. Besides, the authors suspected the algorithm failure on low quality images. Park et al. [43] extracted out vasculature structure based on tensor voting. Tensor voting is the voting process of the expected candidates based on geometrical features. The image was initially contrast enhanced before application of tensor voting process. The Optic Disc was detected using mean shift procedure which points towards direction of maximum increase in the density (convergence point of blood vessels). The algorithm had higher failure rate on diseased images with white lesions. Mahfouz et al. [44] used the horizontal and vertical edge maps to locate the ONH center. These maps can be used to accurately localize the ONH center based upon a simple observation that the central retinal artery and vein emerge from the ONH mainly in the vertical direction and then progressively branch into the main horizontal vessels. The highest projection amplitude along both directions will result in center localization in a computationally efficient manner. The accuracy of the method was highly dependent on horizontal localization process.

The determination of convergence point of vasculature structure is the most efficient way to localize the Optic Disc in terms of accuracy, robustness and computational time. The methods can be applied to most of the fundus retinal images. The proved the high accuracy in case of healthy images however, the algorithms were misguided due to presence of white lesions. Retinal images diseased with Glaucoma may not have white lesions but the presence PPA may misguide the center detection of Optic Disc which is usually required for Optic Disc and Cup segmentation followed by their measurements for Glaucoma diagnosis. Therefore, combining the best features of different vasculature convergence point based algorithms may improve the center detection accuracy in the case of diseased images.

4.2. Optic disc extraction

The literature divides the different methods of Optic Disc Extraction in two main parts: non-model based approaches and model

based approaches. In the non-model based approaches, the Optic Disc is extracted using different image processing algorithms such as Morphological Operations and Pixel Clustering. In the Model based approaches, the Optic Disc boundary is represented in the form of mathematical model. Both Model-based as well as Non-model based approaches are discussed as follows.

4.2.1. Non-model based approaches

For a non-model based approaches, the Optic Disc was either segmented out using different thresholding techniques or morphological operations; or approximated as an circular or elliptical area. Initially, morphological approach was introduced for Optic Disc segmentation as it required basic image processing techniques. Since the shape of Optic Disc is in the form of closed curve, therefore the structure was approximated with circular and elliptical shapes.

Walter and Klein [30] described an approach in which the RGB image was converted to Hue-Luminance-Saturation (HLS) space and a thresholding was applied to approximately localize the Optic Disc center in the luminance channel. Then the precise boundary of the Optic Disc was determined using the red channel of the RGB image via the Watershed transform [65] involving morphological pre-processing of the gradient image and region growing image segmentation. After Watershed Transform, the image is divided into small regions called superpixels. The red channel was selected as Optic Disc boundary is more prominent here. To determine the Optic Disc, the Watershed transform is constrained by markers derived from a previously calculated Optic Disc center. The identification process of the Optic Disc boundary had some problems due to blood vessels occlusion. This problem might be solved if the superpixels are generated using Simple Linear Iterative Clustering (SLIC) [66]. Nayak et al. [48] applied the morphological operations in the red channel of the RGB image in order to segment out Optic Disc. They then segmented out the Optic Cup in the green channel and calculated Cup to Disc ratio from the vertical lengths of the segmented areas. The training dataset should include larger dataset to improve generalization. Since these algorithms had the tendency to segment out the pixels other than Optic Disc therefore it led to shape approximation of the anatomical structure. Even though, Mookiah et al. [50] with their fuzzy histogram approach improved the segmentation accuracy which in their local dataset was even better than Model based Gradient Vector Flow (GVF) technique. The histogram was then correlated with roughness index to represent Optic Disc region. The authors suggested use of more diverse images and appropriate fuzzy membership functions for increase in accuracy as the algorithm over segmented PPA regions.

Zhu et al. [54] applied the Hough Transform on edge map obtained after applying morphological operations on the Luminance gray scale of the image. The Luminance grayscale can be obtained after normalizing each component of the RGB space. This method is loosely connected to main convergence point of retinal blood vessels. The authors warned about their method failure on low quality images as circular hough space might be misguided due to weak edge information. Aquino et al. [51] approximated the Optic Disc boundary using Circular Hough transform on the gradient image obtained after removal of blood vessels. The results were compared with 'Circular Gold Standards' (benchmarks) obtained from the ophthalmologists. They suspected that performance of elliptical approximation and deformable approaches could outperform circular approximation. Carmona et al. [52] obtained a set of hypothesis points that represented geometric properties and intensity levels similar to ONH contour pixels. Then a genetic algorithm was applied in order to find an ellipse approximating the boundary of ONH. The method was applied on DRION-DB database and the accuracy was reported in terms of pixel difference. The authors also reported its computational inefficiency and failure cases on the images having PPA. It might be improved if the hypothesis

also involve statistical properties such as entropy and homogeneity which can be able to distinguish among PPA and ONH pixels.

In [55], various statistical criteria for thresholding have been employed, such as 1) percentage of higher pixel intensity values; 2) Comparative value of pixel intensity as compared to the total intensity values of the extended background image which is other than Optic Disc area. The overall accuracy was determined in terms of measuring vertical diameter of the Optic Disc. This method is applicable to both healthy images and images with AMD. Babu and Shenbagadevi [53] used *k*-means clustering after converting the image into YUV color space (one luma Y and two chrominance UV components) based on *Commission Internationale de l'Éclairage* (CIE) format. They calculated the CDR by taking the rectangular area measurements of both the Optic Disc and Optic Cup. The overall accuracy of the method was determined by comparing CDR values with those obtained from Gold Standard values from the Ophthalmologists.

In the non-model based approaches for extracting out Optic Disc, the measures such as vertical length or horizontal length were used in determining CDR after extracting out Optic Cup. CDR, although one of the important aspect in diagnosing Glaucoma, it is not crucial for Glaucoma documentation [10] as some of the patients can have large size of ONH. Therefore it is sufficient to determine other symptoms such as neuroretinal rim loss and PPA which require exact segmentation of Optic Disc and Optic Cup. Therefore, Model based approaches can be used in determining out exact boundaries of Optic Disc and are explained in the following sections.

4.2.2. Freeform modeling based approaches

The model based approaches were characterized as either freeform modeling or statistical shape modeling [67]. In the freeform modeling, there is no explicit structure of template except some constraints. In this category, Active Contour Modeling (ACM) [68] has been widely investigated for extraction of Optic Disc boundaries. ACM is fundamentally a deformable contour. It changes its shape corresponding to the properties of an image based contour properties and/or knowledge based constraints. The behavior of classical parametric active contours is typically controlled by internal and external energy functions. The external energies determine the region of the model and could be derived from image features such as edges. Internal energies, such as elasticity and rigidity determine the curvature of the model and could serve as smoothness constraints to resist any deformation. The minimization of a total energy function moves the contour towards the target shape.

Mendels et al. [56,58] applied morphological operations on retinal images in YIQ (*Luminance In-phase Quadrature*) followed by an active contour to segment the Optic Disc. In the morphological process, a Dilation operator was first applied followed by an Erosion operator in order to retain the Disc contour whilst remove the blood vessels. Having removed the blood vessels crossing the Disc boundary, an active contour was initialized as a circle centered inside the Optic Disc. The contour was fitted to the rim of the Disc using the Gradient Vector Flow (GVF) derived from edge maps [69]. The final location of the contour was independent of initialization values. This technique was tested on nine retinal images. The morphological preprocessing has been proven effective compared to directly use of original grayscale images, however a quantitative comparison was not presented. Osareh et al. [58] applied the same method on different color spaces and found the *Lab* space to be more suitable for the application of ACM. Xu et al. [59] modified the contour energy function by defining the vector of control points with regards to smoothness, gradient orientation and median intensity. The contour was initialized using Circular Hough Transform. Moreover, the contour points were grouped into edge point clusters and uncertain point clusters using a weighted

k-means algorithm where the position of the contour points were updated automatically. This operation retains the edge points close to their original positions and updates the uncertain points to their correct positions. The overall accuracy of Optic Disc extraction was high but the authors reported the algorithm failure on the images having Peripapillary Atrophy (PPA) as the energy function did not converge.

Joshi et al. [60] used a level set approach in which a contour is represented by a zero-level set of the Lipschitz function [70]. A good accuracy has been achieved based on appropriately selected initialization parameters, but the computational efficiency was low. Yu et al. made its fast implementation on the expense of accuracy by using region intensity information in level set module. The method was applied on MESSIDOR after blood vessel removal by morphological pre-processing.

ACM achieved higher accuracy in segmenting out Optic Disc as compared to Non-model based approaches however, it was prone to error when a testing image involves any textural changes or atrophy associated with any retinal diseases around the Optic Disc boundary [71]. Moreover, since these techniques were applied in their local dataset therefore their robustness is questionable. Therefore, these techniques need to be tested on public available databases in order to improve their generalization.

4.2.3. Statistical shape modeling based approach

Statistical shape modeling involves an offline training process in order to determine a shape model parameterizing the diverse of characteristics of the shape. In this category, ASM has been explored for the extraction of Optic Disc boundary. ASM represents shape approximation of an object using a statistic based model. The ASM deforms to reflect the boundary shape of the Optic Disc in ways that are consistent with shapes presented in the training set.

Li and Chutatape [61] proposed the use of ASM to model the boundary of Optic Disc. They differentiated the Optic Disc edges from other edges on the basis of image gradient. They compared their results with the landmarks obtained from ophthalmologists using Mean Distance to the Closest Point (MDCP). Fengshou et al. [11] used minimum Mahalanobis distance from the mean profile vector to choose the best candidate point during the local edge search. Gradient information was added as a weight into the Mahalanobis distance function. They applied their shape deformation procedure on the image composed of weighted combination of the colour channels and evaluated their results with the benchmark using other evaluation measures as well along with MDCP. We constrained the search space by defining the search boundary on the image gradient for determining the edges of Optic Disc [65]. Restricting the search space on the image improved the results as compared to original ASM. The method needs to be improved by reducing the blood vessel occlusion. Kim et al. [62] defined the imaginary circle after selecting ONH as brightest point. The random sample consensus technique [72] was applied in which the imaginary circle was first warped into a rectangle and then inversely warped into a circle to find the boundary of ONH. The shape warping was applied on the thresholded binary image in which boundary pixels were highly dependent on thresholding value. The author predicted more accuracy after adding constraint condition into the model selection of Random Sample Consensus (RANSAC).

The reason of Statistical shape Modeling of not achieving higher segmentation accuracy as compared to Freeform Modeling is that there were less number of parameters trained during construction of training set. The training set might include statistical measures, and even contour energy information in order to improve the segmentation accuracy. Adding prior information in the training set can be quite useful in distinguishing between PPA and Optic Disc area. Moreover, reducing blood vessel occlusion can also aid to improve segmentation accuracy.

4.3. Optic cup extraction

After the segmentation of Optic Disc boundary, the next step is to find out the boundary of Optic Cup in order to determine the features such as Cup to Disc Ratio and Neuroretinal Rim Loss for the diagnosis of Glaucoma. Since we know that Optic Nerve is a 3-Dimension structure of which the fundus image is in 2-Dimension, therefore a 3-Dimension view of the Optic Cup from stereo fundus images was obtained [59]. Similar to boundary extraction of Optic Disc, ACM was used to determine the Optic Cup boundary and they also incorporated depth analysis to minimize the energy function with regards to intensity, smoothness and shape. Automatic extraction of Optic Cup boundary using 2-Dimension fundus image have also been proposed in the literature discussed as follows.

4.3.1. Morphology based cup segmentation

Nayak et al. [48] used morphological operations in the green channel of RGB images to segment Optic Cup. As mentioned in Section 4.2.1, the results were used in order to classify between Normal and Glaucoma images after measuring Cup to Disc Ratio, Neuroretinal Rim Loss and vasculature shift. The classification accuracy is shown in Table 3. Babu et al. [53] applied Fuzzy C-means clustering on the Wavelet transformed green plane image after the removal of blood vessels. They compared the Cup to Disc Ratio values with those of Gold Standard obtained from the ophthalmologists. In both of the methods, the segmentation accuracy of Optic Cup was not reported

4.3.2. Level-set approach for cup boundary detection

Wong et al. [73] proposed a level-set approach to represent the boundary of Optic Cup in the form of gradient flow equation. The gradient flow equation was initialized by a particular threshold value. The threshold value was selected according to higher 66.7% of the normalized cumulative intensity values of the image in green channel based on the fact that Optic Cup is more prominent in Green channel. The boundary of the Optic Cup was smoothened by ellipse fitting. They applied the same approach on the red channel to obtain the Optic Disc boundary. Their later studies proposed the concept of blood vessel kinks at the edge of the Optic Cup for boundary extraction [74]. They used Canny edge detection and Wavelet transform to determine the edges of the Optic Cup. The bending of blood vessels at the angle of more than 20 degrees were empirically determined to be at the edge of Optic Cup. Joshi et al. [60] used the same information of blood vessel kinks at the edge of Optic Cup to determine the Optic Cup boundary by interpolating the vessels kinks and the Optic Cup boundary in the 3rd dimension using spline interpolation. Clinical knowledge of ophthalmologists obtained from direct 3D cup examination was utilized to approximate the cup boundary.

Up till recent, there are very limited report on Optic Cup segmentation algorithms available, and the results for the existing methods are preliminary. Since the edge between Optic Disc and Optic Cup is not usually visible in normal contrast of colour fundus images, therefore there is need to determine certain parameters which can distinguish between Optic Cup and Optic Disc. Optic Cup extraction may also require segmenting out vasculature structure and in-painting with neighborhood for accurate dimension measurement.

4.4. Peripapillary atrophy

In this section, we review the automatic PPA detection and segmentation methods for diagnosing Glaucoma discussed as follows:

4.4.1. PPA localization

Tan et al. [76] detected PPA for determining pathological myopia. They proposed the variational level set method [79] to

extract the PPA boundary. The variational level set method is initialized with a horizontal elliptical contour within Optic Disc boundary whereas a vertical elliptical contour is initialized outside the boundary. The horizontal elliptical contour is initialized in order to reduce the influence of the edges of the retinal vessels and allow the level set function to grow and seek for the correct Optic Disc boundary. Conversely, a vertical elliptical contour is set externally as it best represents the physiological shape of the Optic Disc. The difference of these two Optic Discs is taken and thresholding in the HSV (Hue Saturation Value) color space is used to roughly segment the PPA area. They claimed the PPA localization accuracy of 95% however, they did not consider the cases if PPA is present in both temporal and nasal sides. Moreover, no PPA segmentation was done. The Test Images were taken from Singapore Cohort study Of the Risk factors for Myopia (SCORM) [75]. The same authors [77] proposed a fusion of two decision methods. Gray Level Covariance Matrix (GLCM) based texture analysis was used to generate a degree of roughness which is then compared for the temporal side and nasal side. The higher degree of roughness in the temporal side compared to nasal side indicates PPA presence. Statistical analysis around the Optic Disc boundary, including average intensity and standard deviation were also used to detect PPA. However, like previous method, no PPA segmentation was performed.

4.4.2. PPA extraction

The statistical textural features, such as contrast, correlation and variance were determined in [78,80] and a feature vector of 63 features was constructed. The PPA and non-PPA pixel values were classified based on the feature vector. The training set was based on stereo images which were obtained by taking the retinal pictures of both Normal and Glaucoma patients from different angles in order make the 3D projection. The classification was performed using Linear Discriminant Analysis (LDA) [49]. The testing dataset consists of 58 Glaucoma patients out of which, 26 images have moderate to severe PPA the images with moderate to severe PPA were tested.

The segmentation of PPA is an important step not only because it is one of main indications in Glaucoma diagnosis but also it can improve the segmentation accuracy of Optic Disc if it is segmented out first. Therefore textural based properties can be used in order to classify among Optic Disc region, PPA and other retinal areas. Moreover there is need to use accurate classification algorithm which can distinguish among these regions.

4.5. Retinal nerve fibre layer defect detection

Several attempts had been made in order to detect RNFL based on the fact that RNFL defect detection serves as earliest signs of Glaucoma. Initially images from the modalities such as OCT or Scanning Laser Polarimetry (SLP) were used to scan the 3-Dimensional view of the retina so that RNFL was detected from these images [85–87]. Later on several Image Processing techniques were applied to detect the RNFL defect on 2-Dimensional image. Lee et al. [88] used the green plane of the fundus retinal image to detect the intensity decrease around the Optic Disc for RNFL detection. The method contributes to quantify RNFL defect and provide an objective method for Glaucoma evaluation. Hayashi et al. [81] used directional Gabor filters [89] to determine the RNFL defect. They initially removed the blood vessels and then applied the directional filter on the grayscale image. The method was prone to error as vasculature removal also erased some narrow RNFL. Moreover the false positive rate was high [90]. Prageeth et al. [82] classified the retinal images between Glaucomatous and non-Glaucomatous images using the information of RNFL defect along with CDR. They determined the RNFL defect after plotting the intensity profile of the retinal area at the edges of the retina and around the Optic Disc.

Odstrčilík et al. [83,84] analyzed the RNFL defect using Markov Random Fields (MRF). MRF is the image modeling whose parameters are estimated using Expected Maximization Algorithm [91]. The RNFL striations of Normal and Glaucomatous patients are classified on the basis of feature vector composed of MRF parameters. Despite these attempts, there is little work done to analyze the RNFL defect using 2-Dimension retinal images and the results are preliminary.

5. Non-segmentation based classification between normal and glaucomatous retinal images

Although there are few efforts available reflecting the classification between Normal and Glaucomatous patients based on features that do not require segmentation of retinal structures, these methods can serve as prior knowledge for measuring different Glaucomatous symptoms associated with retinal segmentation. Some of those methods are discussed as follows and their results are summarized in Table 6.

In non-segmentation based methods, Bock has major contribution [95,96,92]. Initially they used Pixel Intensity Values on which they applied Principal Component Analysis (PCA) [97] for dimensionality reduction. As a pre-processing step, they corrected illumination and intensity inhomogeneity then in-painted vasculature area after segmenting them out. Later on they added features such as Image Texture, FFT Coefficients, Histogram Models and B-Spline coefficients. Based on these features they calculated Glaucoma Risk Index (GRI). They used classifiers such as Naive Based Classifier, *k*-Nearest Neighbor Classifier and Support Vector Machines (SVM) [49] to classify between healthy and Glaucomatous images and they found SVM to be less prone to sparsely sampled feature space. Dua et al. [94] used Wavelet-Based Energy Features and compared the performance of different classifiers including the previously mentioned classifiers, Random Forests [98] and Sequential minimal optimization (SMO) [99]. From SMO they obtained the maximum classification accuracy.

Unlike segmentation based methods, there are few methods available based on non-segmentation analysis for the retinal images associated with Glaucoma. One of the main reason is that non-segmentation based methods are not validated by the ophthalmologists in order to distinguish among Normal and Glaucomatous images as in the case of segmentation based methods. If they are used in conjunction with segmentation based methods, they can not only be quite effective in increasing the classification accuracy among different stages of Glaucoma but also can serve as a benchmark for development of further automatic classification methods.

6. Discussion

Glaucoma causes changes in retinal structures which lead to peripheral vision loss if left untreated. The latest clinical information suggests observation of ONH area and the retinal changes around it in order to diagnose Glaucoma. Therefore after IOP measurement, the retinal exam is mostly based on measuring ONH related measurements such as Optic Disc size, Optic Cup size, their ratio, Neuroretinal Rim observation and PPA.

It is very difficult to determine the Optic Cup boundary from 2-D retinal image as there is no sharp edge indicating it. Moreover, the occlusion of blood vessels make the extraction difficult of not only Optic Cup but also Optic Disc boundary which can become even tougher if PPA is present. Also, the detection of RNFL has been quite challenging because it is not easy to distinguish between RNFL striations and vasculature structure on retina. Like fingerprint, every subject has different ONH structure therefore we need to have robust algorithms to determine the retinal changes related to Glaucoma diagnosis.

Table 6

Results of different methods of non-segmentation based classification between normal and glaucomatous retinal images.

Extraction method	Image database	Colour space	Image dimensions	Number of test images	Accuracy	Citation
Glaucoma Risk Index	Pattern Recognition Lab Germany	8-Bit RGB	1600 × 1216	336 Normal and 239 Glaucoma [93]	80% on 5-fold cross validation (SVM)	[92]
Wavelet Coefficients	Kasturba Medical College India	8-Bit RGB	560 × 720	24 Normal and 37 Glaucoma	93% on 10-fold cross validation (SMO)	[94]

The survey has been categorized into two types of algorithms i.e. segmentation based methods and non-segmentation based method. The algorithms which were applied on same datasets are grouped together so as to present their results on a common benchmark. As far as segmentation based methods are concerned, they involve series of steps; each of which can be performed using specific algorithm. It is important to observe the overall accuracy of each step from ONH localization to extraction of boundaries of Optic Disc, Optic Cup and PPA which are needed to be high to ensure the effectiveness of the overall process maintained at satisfactory level.

ONH localization has been the initial step in determination of Glaucoma as well as other retinal diseases such as Diabetic Retinopathy. The reason is that ONH has been considered the brightest region in the retinal image and therefore can serve as a way to locate other retinal structures. But, the presence of artifacts in the retinal image brighter than ONH led to vasculature segmentation as all the retinal blood vessels converge in ONH. The vasculature segmentation not only localized the ONH accurately but also the researchers who worked on Optic Disc and Optic Cup segmentation found comparatively accurate results after segmenting out retinal blood vessels. However, the accurate segmentation of vasculature structure has itself been a challenging task.

Current vasculature segmentation methods are mostly applied and therefore quite efficient on public datasets. These datasets are composed of healthy images and the images diseased with Diabetic Retinopathy which consists of small lesions and are usually observed away of ONH. But they often segmented out PPA as well which is usually present in the images diseased with Glaucoma as shown in Fig. 7. Based on our research, textural analysis could help to distinguish among PPA and non PPA regions and incorporating them along with vasculature segmentation methods can

increase their efficiency on Glaucoma images. Moreover, accurate in-painting methods by neighborhood pixels after segmenting out vasculature structure can be used to remove blood vessel occlusion problem which can lead to accurate segmentation of Optic Disc and Optic Cup. 3-D scans obtained from modalities; such as OCT, can simplify the Optic Cup boundary detection problem but these modalities are not available in every hospital. Therefore we have to limit ourselves to 2-D scans.

Apart of image processing and computer vision based techniques, pattern recognition based methods have also been applied in order to locate and extract out ONH boundary and Optic Cup. Although they were not up to the mark as they were expected; by increasing the training parameters such as texture parameters, statistical based parameters and design of accurate classifier will not only improve the results in terms of accuracy but also it will make the algorithms more robust and generalized. Huge diverse training data will significantly improve the classification efficiency. Another key issue in pattern recognition techniques is that there are few available public dataset of Glaucoma based retinal images. Although there are contributions from some of the hospitals and research labs even though, there are not enough number of retinal images diseased with Glaucoma as in the case of Diabetic Retinopathy. Since Glaucoma progresses slowly and its symptoms occur gradually, therefore it is required to develop a retinal image database of different stages of Glaucoma with annotations around different retinal structures associated with Glaucoma. The database will serve as a benchmark to test and validate algorithms related to Glaucoma based feature extraction. Detection of non-ONH anatomical structures such as RNFL can be improved by applying non-segmentation based methods on retinal images in the database. Since any of the single symptom mentioned earlier is not

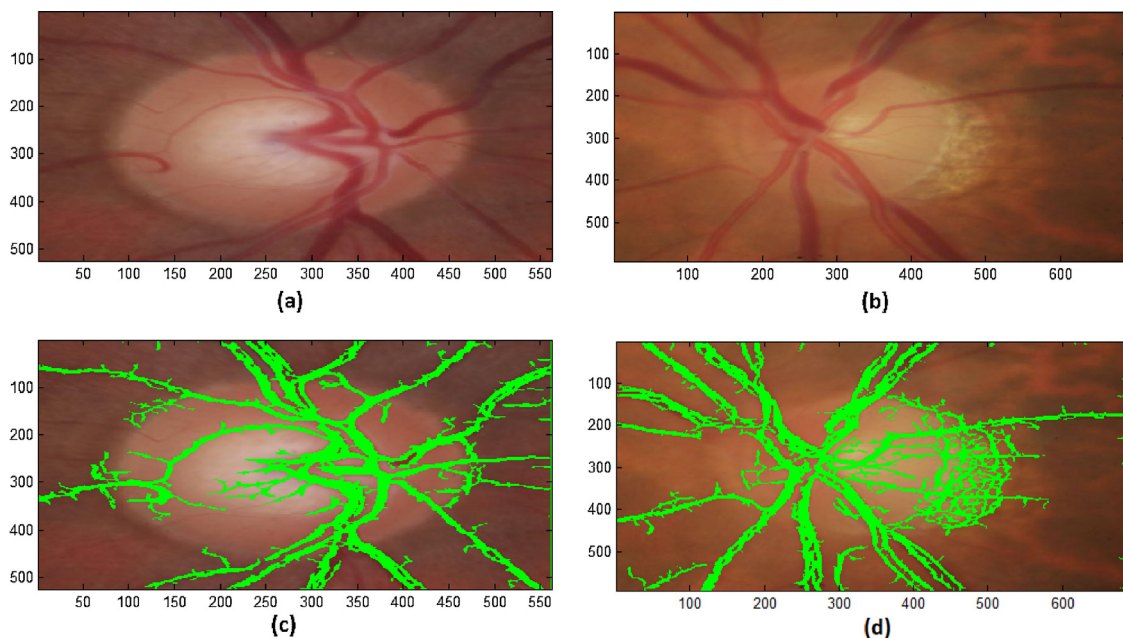


Fig. 7. Comparison of vasculature when (a) no PPA and (b) when PPA is present. (c) vasculature segmentation output of (a) and (d) vasculature segmentation output of (b).

the guaranteed sign of Glaucoma, the combination of all features is required for the accurate diagnosis. If the automatic methods are improved in terms of accuracy and generalization; they will serve as a benchmark for the clinicians to diagnose the disease based on measurements obtained by using those methods.

7. Conclusion

Glaucoma is an evasive and dangerous eye disease and is the second leading cause of blindness globally. Since Glaucoma can not be cured, the diagnosis at their early stage can help clinicians to treat it accordingly and to prevent the patient from leading to the blindness. In this paper, we have provided a systematic review on Glaucoma, its types, current clinical methods to diagnose Glaucoma, and the methods based on automatic detection of retinal features which can be employed to assist diagnosis of Glaucoma at an early stage. The accuracy and reliability of the current clinical diagnosis are subject to inter-observer variability and every ophthalmologist determine those measurements based on their own experience. As far as retinal scans are concerned, there are significant differences among observations of different clinicians which are highly specific to the image. Moreover, 3-D scanning modalities such as OCT are not available in every hospital. Therefore, with the advent of 2-D retinal scan based automatic retinal feature methods to diagnose Glaucoma, an accurate diagnosis can be given in a time and cost effective manner.

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Appendix A. Evaluation functions

A.1. Overlapping Score

The *Overlapping Score* evaluates the degree of overlap of two regions and is used to determine the extent to which the segmented objects match. The Overlapping Score can be defined as in equation A.1:

$$S(A, B) = \frac{|A \cap B|}{|A \cup B|}, \quad (\text{A.1})$$

where A and B are the segmented images surrounded by model boundary and annotations from the ophthalmologists respectively, \cap denotes the intersection and \cup denotes the union. Its value varies between 0 and 1 where a higher value, indicates an increased degree of overlap.

A.2. Mean Absolute Difference

The *Mean Absolute Difference* (MAD) is the mean difference between the extracted boundary and the average boundary obtained from the ophthalmologists as shown below:

$$\text{textrm{MAD}} = \frac{1}{n} \sum_{i=1}^n \sqrt{e_{x_i}^2 + e_{y_i}^2}, \quad (\text{A.2})$$

where e_{x_i} and e_{y_i} are the error values at the particular point.

A.3. Correlation Coefficient

The *Correlation Coefficient* is defined as:

$$\rho_{X,Y} = \frac{E(XY) - E(X)E(Y)}{\sqrt{E(X^2) - (E(X))^2} \sqrt{E(Y^2) - (E(Y))^2}}, \quad (\text{A.3})$$

where X and Y represent the datasets whereas $E()$ defines mean of dataset.

Appendix B. Public databases used for experimentation

A brief explanation of the public databases used in the literature review are explained as in this section. Most of the public databases were constructed for automatic feature extraction of Diabetic Retinopathy but they were used for extraction of anatomical structures such as Optic Disc used in Glaucoma diagnosis. Some of the public databases were constructed particularly for automatic feature extraction of Glaucoma.

B.1. STARE (STructured Analysis of the REtina)

The STARE database [34] is the part of STARE project initiated by Michael Goldbaum at University of California, San Diego in 1975 for the analysis of retinal images. It is being funded by National Institute of Health, USA since 1986. Uptil now, the database is composed of 81 in which 31 of them are from healthy retinas and 50 images show the symptoms of the retinal diseases such as exudates and haemorrhages that completely obscure the Optic Nerve Head. All these images were acquired using a TopCon TRV-50 fundus camera at 35° field-of-view, and subsequently digitized at 605 × 700 pixels in resolution, 24 bits per pixel.

B.2. DRIVE (Digital Retinal Images for Vessel Extraction)

The photographs for the DRIVE database [36] were obtained from a diabetic retinopathy screening program in The Netherlands. The screening population consisted of 400 diabetic subjects between 25–90 years of age. 40 photographs have been randomly selected, 33 do not show any sign of diabetic retinopathy and 7 show signs of mild early diabetic retinopathy. The images were acquired using a Canon CR5 non-mydratic (which does not cause dilation to eye pupil) camera with a 45° field of view (FOV). Each image was captured using 8-bits per color plane at 768 by 584 pixels. Each image has the manual segmentation of the vasculature structure.

B.3. DIARETDB0 (Standard Diabetic Retinopathy Database Calibration Level 0)

This is a public database [100] for benchmarking diabetic retinopathy detection from digital images. It consists of 130 color fundus images of which 20 are Normal and 110 contain signs of the diabetic retinopathy (hard exudates, soft exudates, microneurysms, hemorrhages and neovascularization). Images, obtained from Kuopio University Hospital, were captured with a 50° field-of-view digital fundus camera at 1500 × 1152 pixels. The dataset can be used to evaluate the general performance of diagnostic methods. This dataset is referred to as “calibration level 0 fundus images” as it corresponds to the situation where no calibration is performed and the imaging was performed with unknown amount of imaging parameters.

B.4. DIARETDB1 (Standard Diabetic Retinopathy Database Calibration Level 1)

The images of the database [101] are obtained from same hospital and used for benchmarking diabetic retinopathy. It consists of 89 colour fundus images of which 84 contain at least mild non-proliferative signs (Microaneurysms) of the diabetic retinopathy, and 5 are considered as Normal which do not contain any signs of the diabetic retinopathy according to all experts who participated in the evaluation. Images were captured using the same 50° field-of-view digital fundus camera at 1500 × 1152 with varying imaging settings. This data set is referred to as “calibration level 1 fundus images” as the images are captured after encountering different amounts imaging noise and optical aberrations.

B.5. MESSIDOR (Méthodes d'Evaluation de Systèmes de Segmentation et d'Indexation Dédiées à l'Ophthalmologie Rétinienne)

MESSIDOR [46] is a project funded by the French Ministry of Research and Defense within a 2004 TECHNO-VISION program for implementing and testing segmentation algorithms. It contains 1200 eye fundus color images of the posterior pole acquired by the Hôpital Lariboisière Paris, the Faculté de Médecine St. Etienne and the LaTIM-CHU de Brest (France). 800 of these images were captured with pupil dilation (one drop of Tropicamide at 10%) and 400 without dilation, using a Topcon TRC NW6 non-mydratic retinograph with a 45° field of view. The images are 1440 × 960, 2240 × 1488, or 2304 × 1536 pixels in size and 8-bits per color plane and are provided in TIFF format. 540 images are from patients not affected by Diabetic Retinopathy and 660 images correspond to patients affected by the illness. To prevent the inclusion of any kind of skew, although some images are not suitable for processing (i.e., images too blurred or with severe enough cataract), no exclusion criteria was applied. To make evaluation of the algorithm performance on this database possible, the Optic Disc rim was manually delimited by experts producing by this way a gold standard set.

B.6. DRION-DB (Digital Retinal Images for Optic Nerve Segmentation Database)

This database [52] is composed by joint collaboration of three Spanish organizations, i.e. Universidad Complutense, Hospital Miguel Servet and Universidad Nacional de Educación a Distancia. It has 110 retinal images with each image having the resolution of 600 × 400 pixels and the Optic Disc annotated by two experts with 36 landmarks. The images were acquired with a colour analogical fundus camera, approximately centered on the ONH and they were stored in slide format. In order to have the images in digital format, they were digitized using a HP-PhotoSmart-S20 high-resolution scanner, RGB format, resolution 600 × 400 and 8-bits/pixel. Independent contours from 2 medical experts were collected by using a software tool provided for image annotation. A person with medical education and solid experience in ophthalmology was considered as an expert. In each image, each expert traced the contour by selecting the most significant papillary contour points and the annotation tool connected automatically adjacent points by a curve.

B.7. RIM-ONE (An Open Retinal Image Database for Optic Nerve Evaluation)

RIM-ONE [102] is exclusively focused on ONH segmentation, it has 169 high-resolution images and 5 manual reference segmentations and a gold standard of each one. The high number of expert segmentations enables the creation of reliable gold standards and the development of high accurate segmentation algorithms. The

designed database is composed of 169 ONH images obtained from 169 full fundus images of different subjects. These retinographs have been captured in the three hospitals cited before which are located in different Spanish regions. Compiling images from different medical sources guarantee the acquisition of a representative and heterogeneous image set. All the retinographs are non mydratic retinal photographs captured with specific flash intensities, avoiding saturation. The images are classified in different subsets, as domain experts have indicated:

- Normal eye (non-glaucomatous): 118 images.
- Early glaucoma: 12 images.
- Moderate glaucoma: 14 images.
- Deep glaucoma: 14 images.
- Ocular hypertension (OHT): 11 images

B.8. ORIGA-light (An Online Retinal Fundus Image Database for Glaucoma Analysis and Research)

The database [63] is based on retinal images collected in a population based study, Singapore Malay Eye Study. It contains 650 annotated retinal images. Each image is tagged with grading information of different features related to Glaucoma. This database is not available publically now.

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