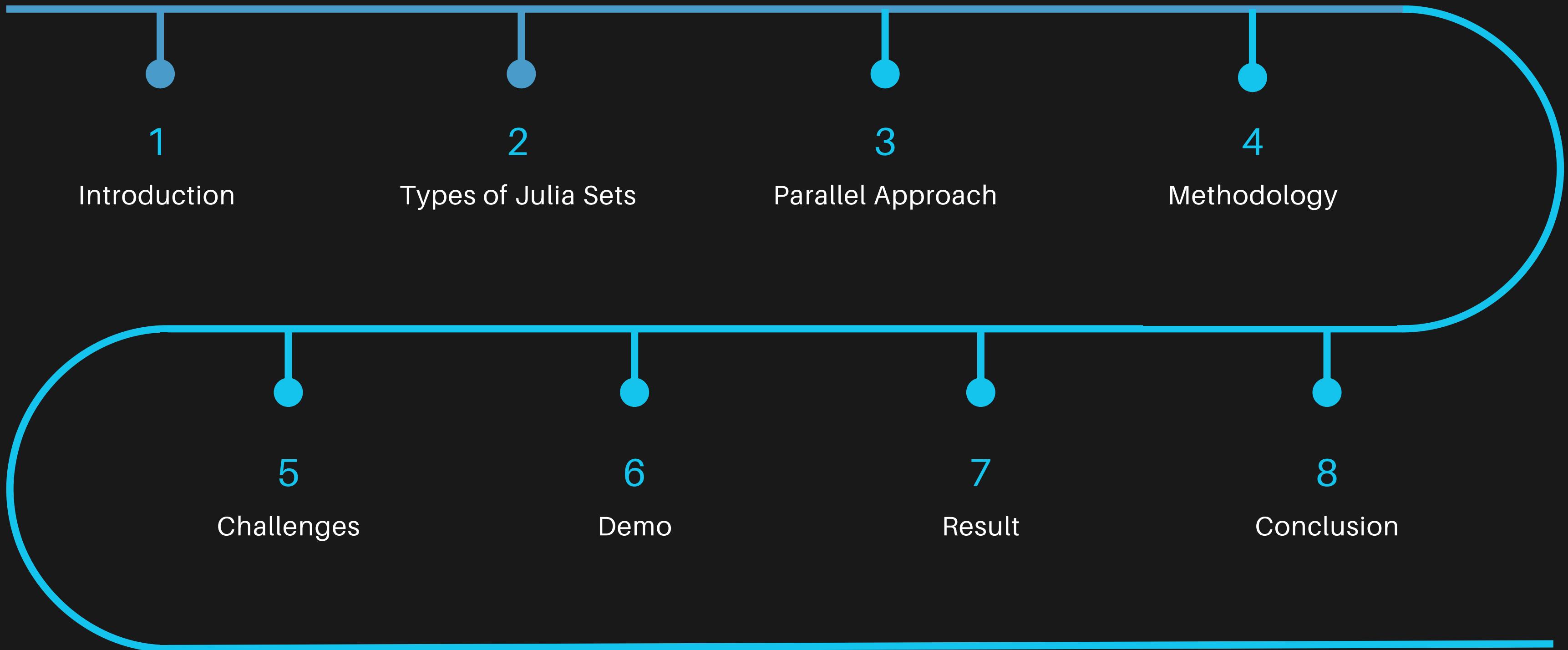


Group 1

Parallel Programming
Julia Sets
Generation

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Outline



Introduction to Julia Sets

Definition:

Fractals generated by iterating complex numbers

Visualization:

Colour-coded images or animations illustrate intricate patterns

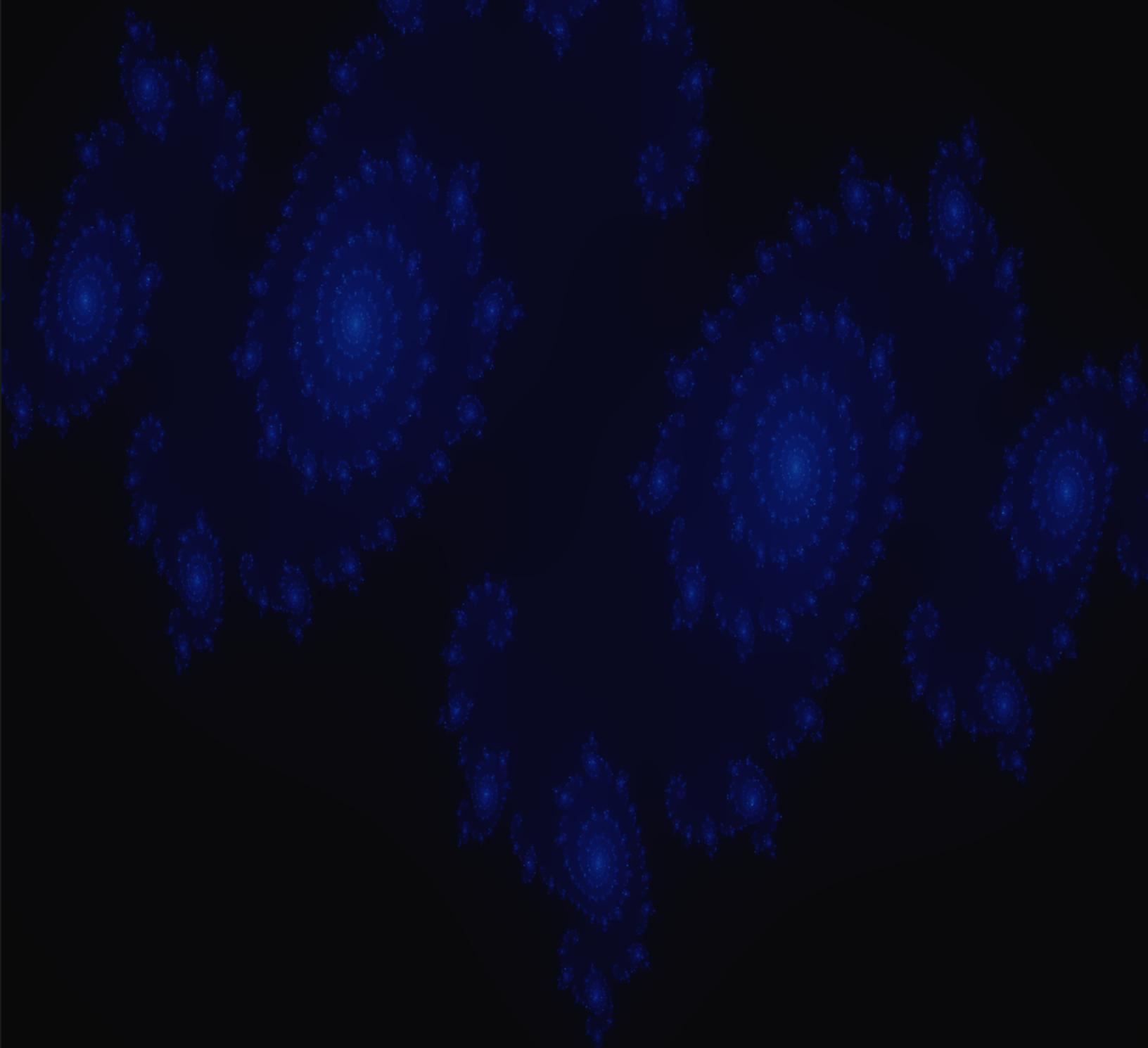
Properties:

Self-similarity, infinite complexity, and non-repeatability

Mandelbrot Set:

Each point in the Mandelbrot set corresponds to a different Julia set

Visualizing Julia sets provides insights into the complex dynamics of mathematical functions and fractals

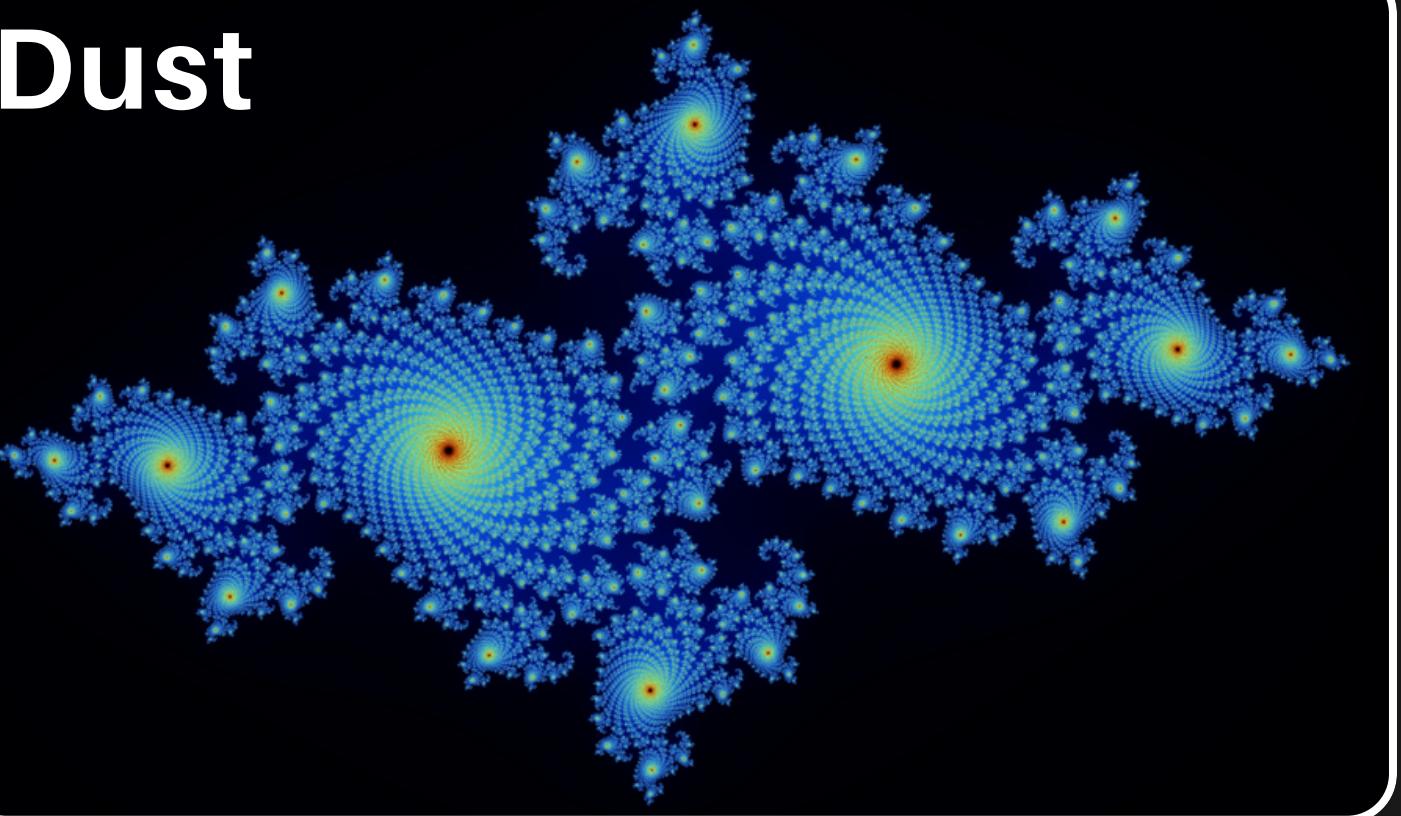


Types of Julia Sets

Filled



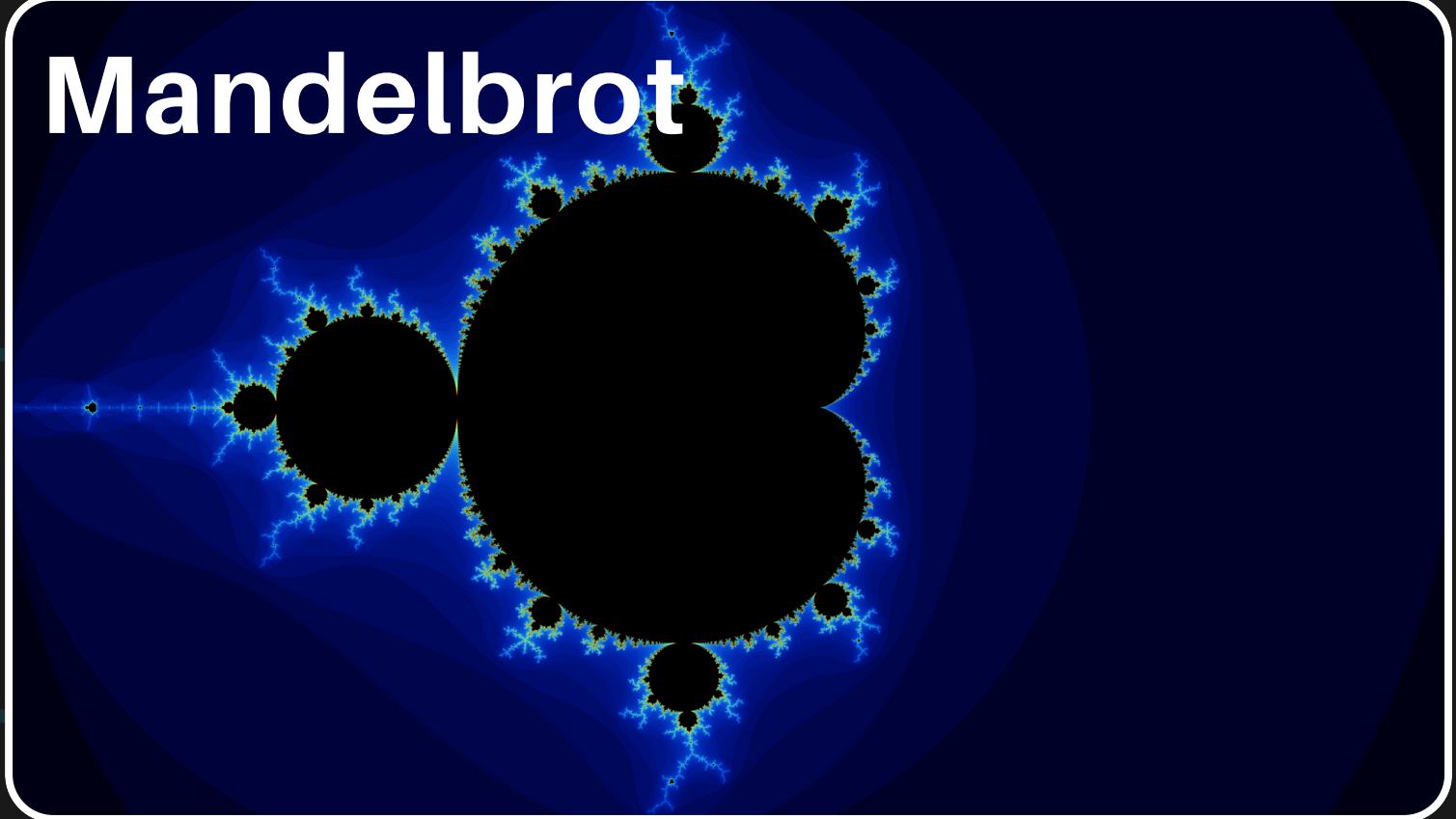
Dust



Mandelbrot vs Julia Set

$$z = z^2 + c$$

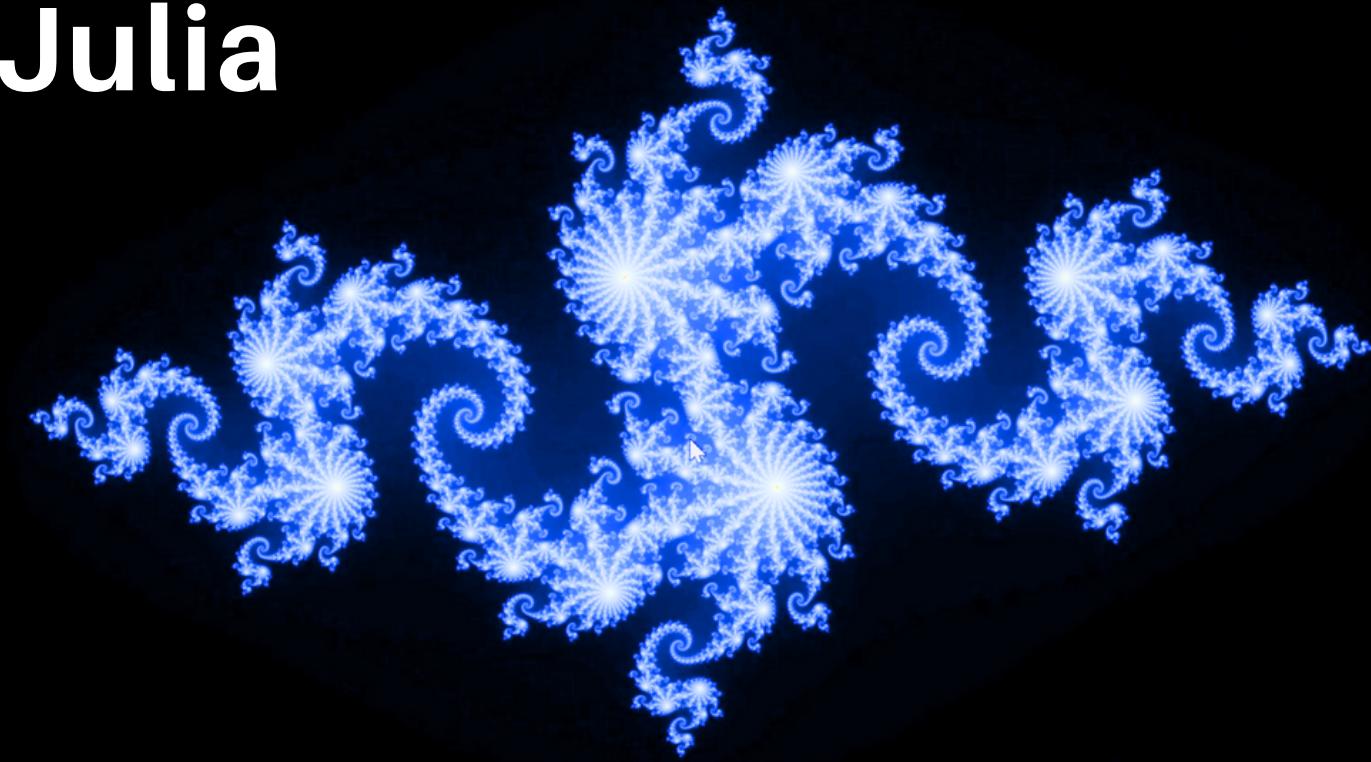
Mandelbrot



$z = 0$

$c = \text{pixel location}$

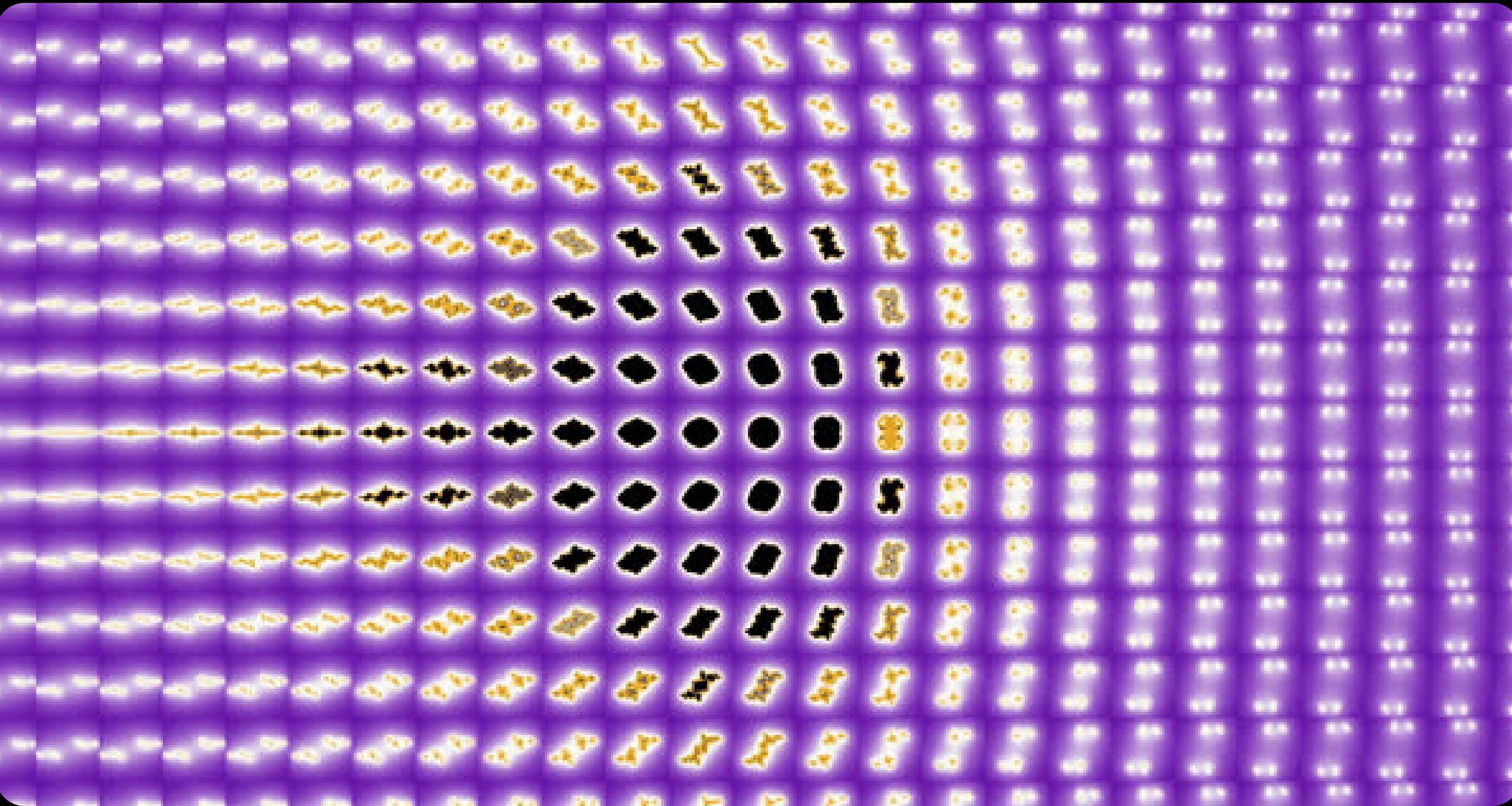
Julia



$z = \text{pixel location}$

$c = \text{constant}$

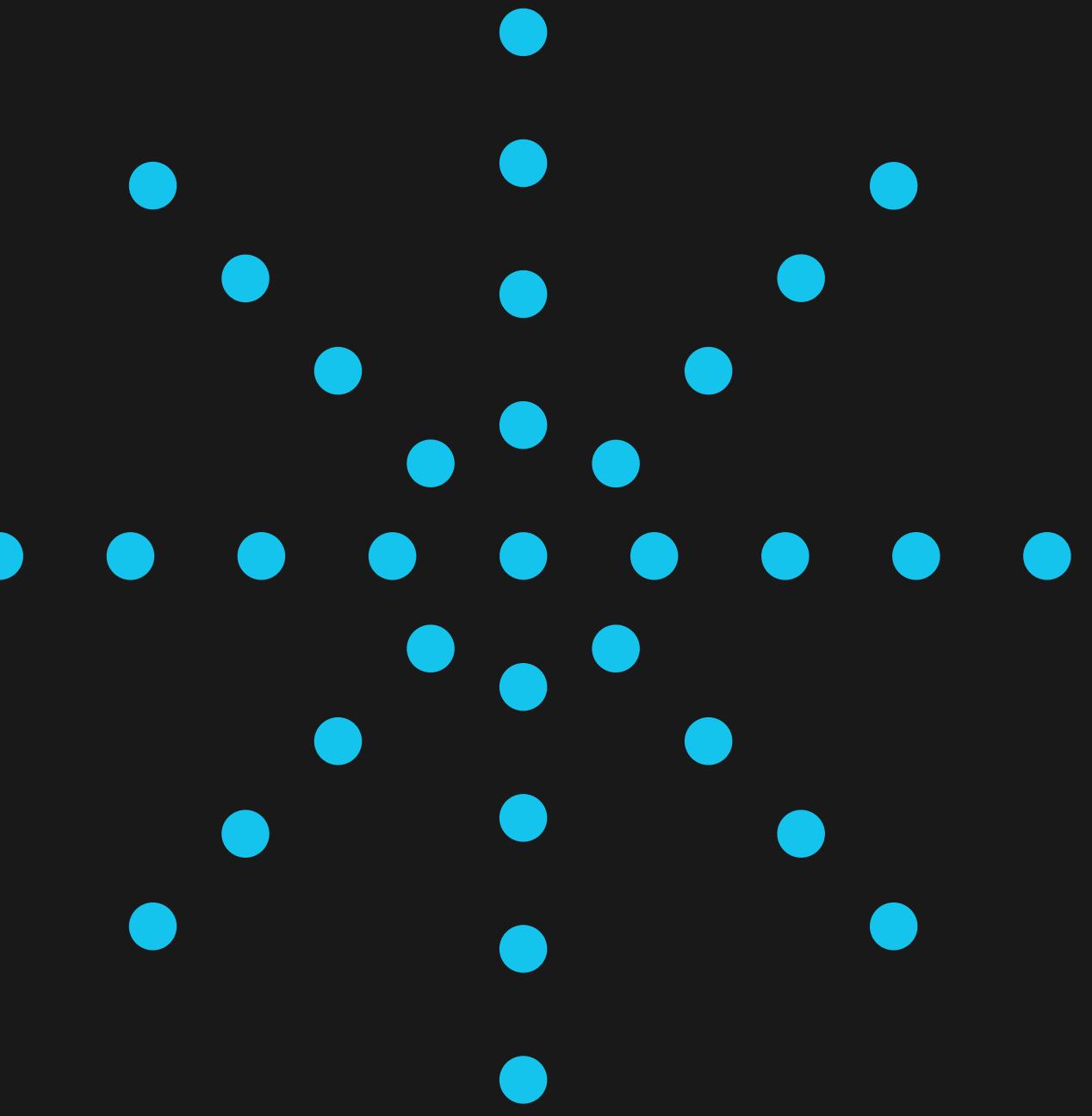
Mandelbrot and Julia Set



Parallel MPI Approach to Julia Set Rendering

Our goal is to use the capabilities of parallel programming with MPI to efficiently generate high-resolution images of Julia sets.

- Julia sets are **fractals** produced from complex quadratic polynomials
- Fractal creation is resource-intensive, making it a perfect candidate for parallelization





Methodology

- Project executed on **SHARCnet** high-performance computing cluster with strict adherence to computational etiquette
- Programmed in **C** for MPI which enabled the distribution of computations across multiple processes
- **PNG library** used for rendering computed Julia sets into high-resolution images that show intricate details of fractals



Methodology



ALGORITHM OVERVIEW

We used a Message Passing Interface (MPI) to distribute the computation of the Julia and Mandelbrot sets across multiple processes.



PARALLELIZATION STRATEGY

We divided the computational task among various MPI processes, assigning each a portion of the grid representing the complex plane.



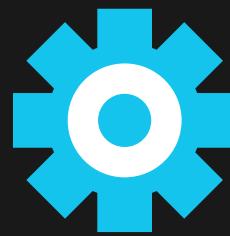
VISUALIZATION TECHNIQUE

We mapped iteration counts or divergence tests from the computation to the colours in the fractals. This lets us generate detailed images that reveal the intricate patterns of both the Julia and Mandelbrot sets.

HOW WE DID IT

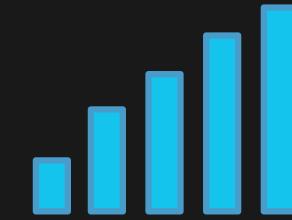


Challenges



MEMORY MANAGEMENT

A chunk-based approach deals with high memory demands



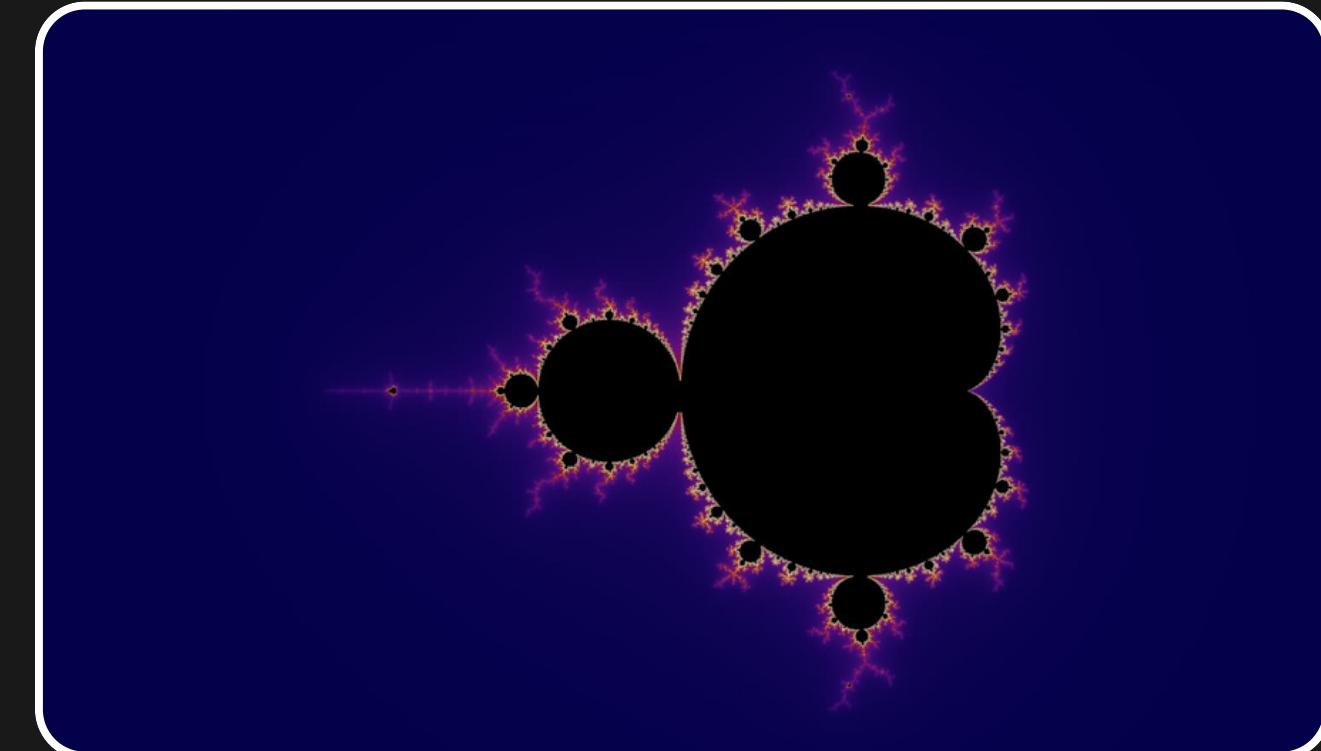
POSITION AND ALIGNMENT

Adjusted scale and translation parameters allows for precise alignment

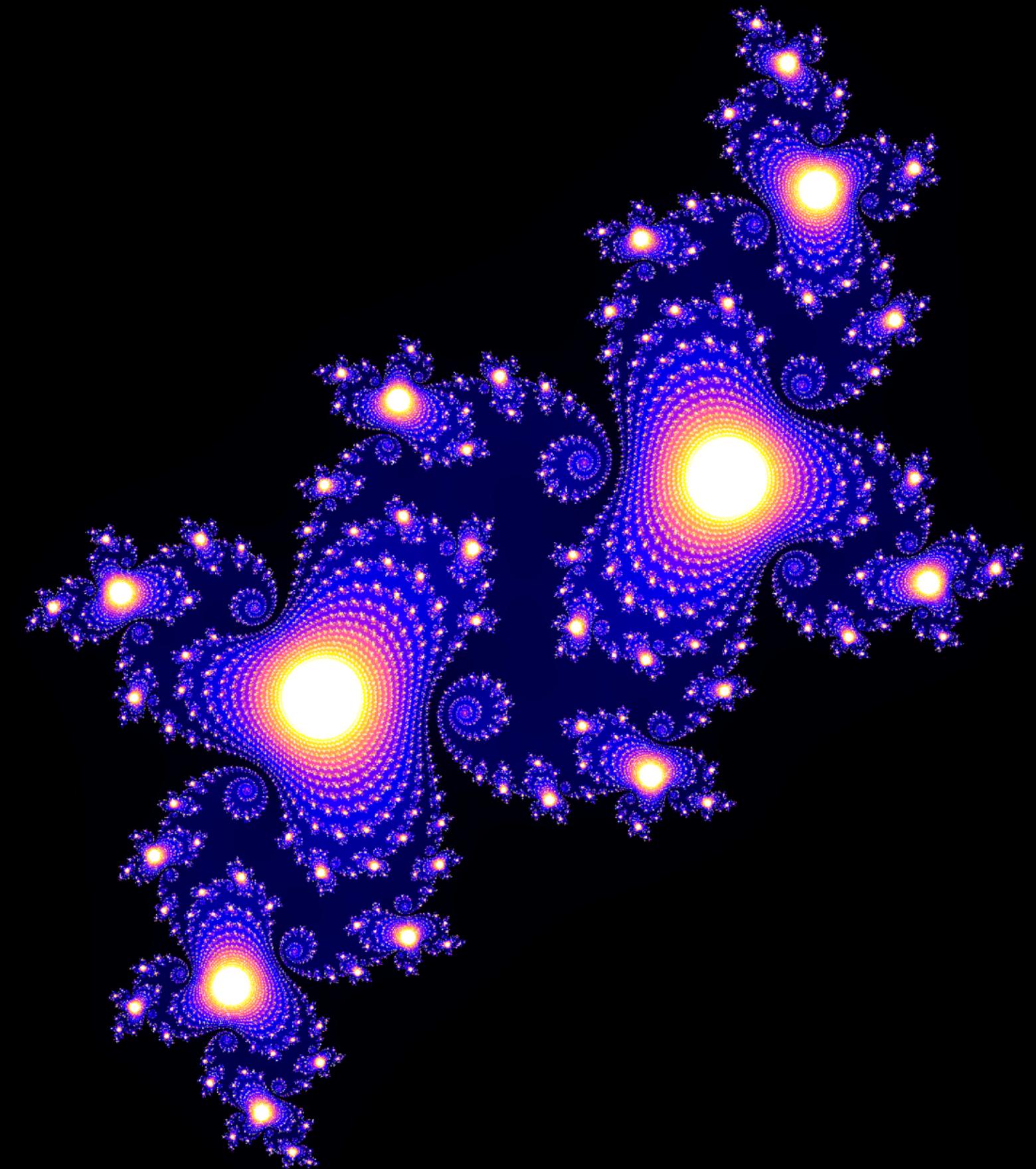


COLOUR MAPPING

Iterative testing helps identify colour schemes that balance aesthetics and clarity

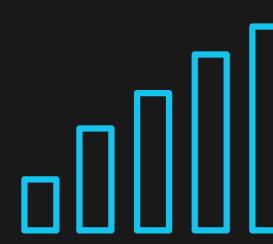


Demo



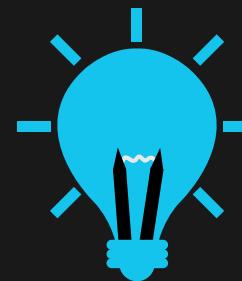


Results



PERFORMANCE IMPROVEMENT

Faster results thanks to parallelization



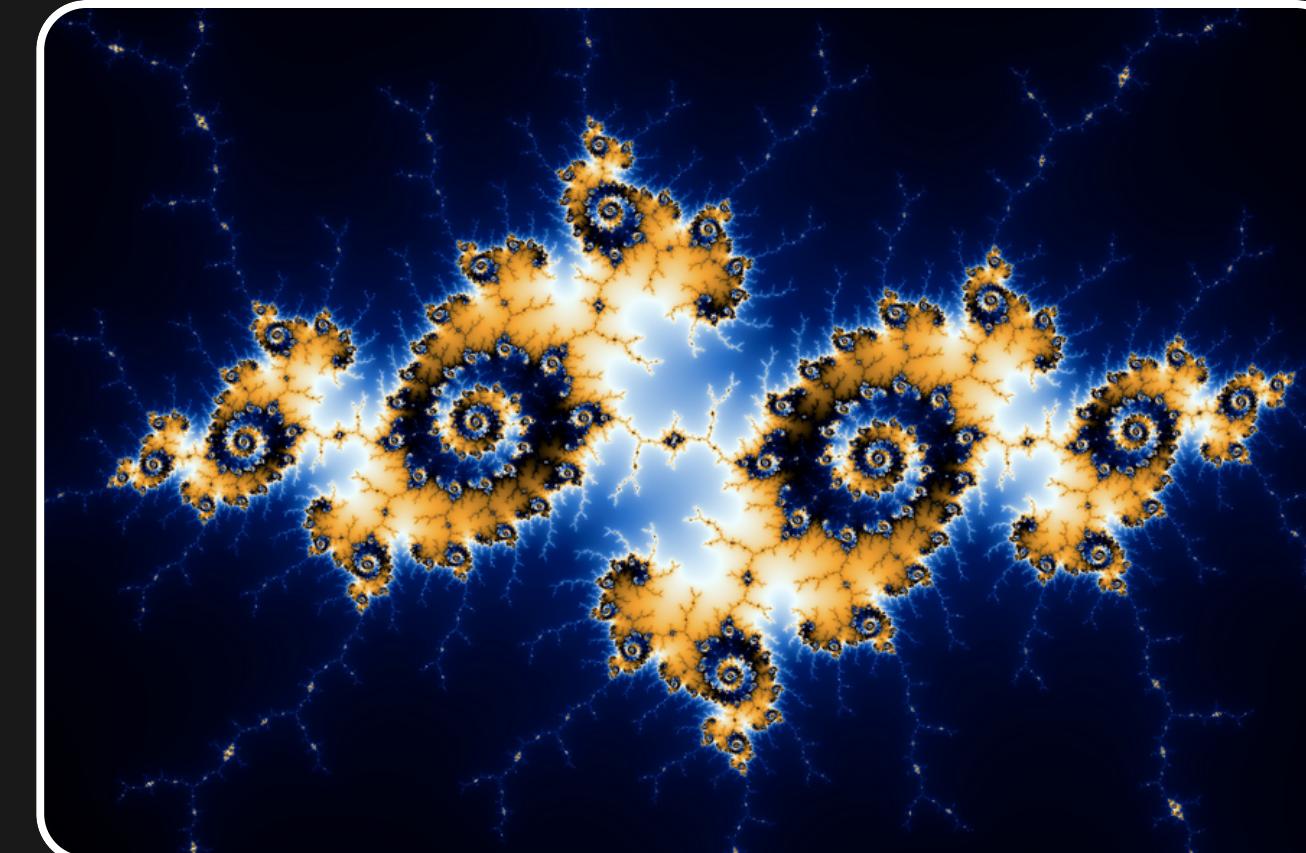
INSIGHTS

Deeper understanding of how fractal geometry works and the self-similarity principle of fractals



GENERATED IMAGES

Generate sets that display clear images and are intuitive to use and explore



THE POWER OF VISUALIZATIONS

Conclusion

Thank you! Any questions?

GROUP 1

