Attitude estimation from an ideal accelerometer

Suppose our IMU/Accelerometer in Fig. 1 is only rotating (negligible accelerations). Then, we may

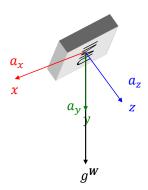


Figure 1: IMU acceleration measurements

estimate its attitude in Euler angles $\begin{bmatrix} \phi & \theta & \psi \end{bmatrix}^T$ using the measured accelerations $\begin{bmatrix} a_x & a_y & a_z \end{bmatrix}^T$ by recognizing that the gravity vector points down.

$$\phi = \tan^{-1} \left(\frac{a_y}{\sqrt{a_x^2 + a_z^2}} \right) \tag{1}$$

$$\theta = \tan^{-1} \left(\frac{a_x}{\sqrt{a_y^2 + a_z^2}} \right) \tag{2}$$

$$\psi = \tan^{-1} \left(\frac{\sqrt{a_x^2 + a_y^2}}{a_z} \right), \tag{3}$$

where (3) is not as robust an estimate as the other two.