# CSCI 3022

# intro to data science with probability & statistics

August 31, 2018

- 1. InterQuartile Range
- 2. Histograms
- 3. Boxplots



Bookkeeping

002

1st ake 1st quizlet

Moodle: if you are not in a section, unenroll then reenroll using csci3022-Dan

*Piazza:* be on it, because no more emails! https://piazza.com/colorado/fall2018/csci3022

**Get Jupyter notebook / Anaconda Python**: make sure you have a working install and check out the Numpy/Pandas tutorial (github/notebooks) <a href="https://www.anaconda.com/downloads">https://www.anaconda.com/downloads</a>

# Last time on CSCI 3022:

Numerical summaries & summary statistics:

• Mean: 
$$\sqrt{\frac{1}{k}} \times k = \overline{X}$$

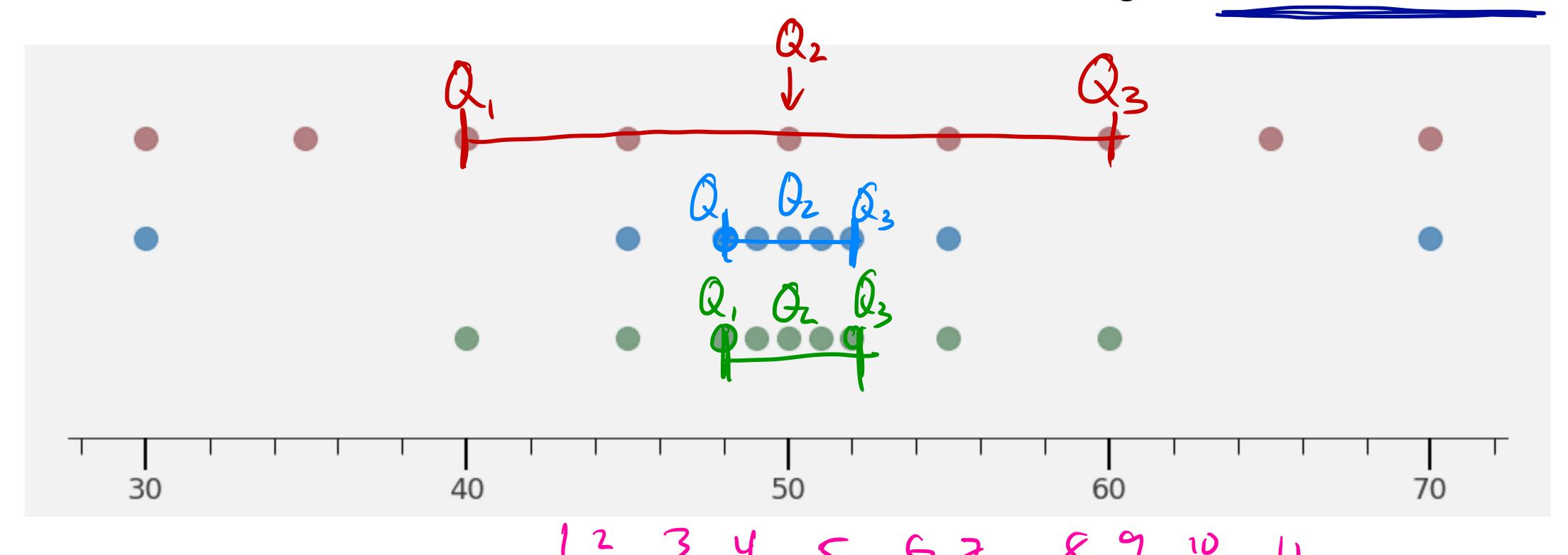
• Mean: 
$$n \times k = x$$
  
• Median:  $n \text{ odd}$ ,  $\binom{n+1}{2}^{th} \text{ value}$ ,  $n \text{ even}$ ,  $\binom{n+2}{2}^{th} + \binom{n}{2}^{th} / 2$ 

• Mode: 
$$Most$$
 common value  
• Sample Variance:  $(x_k - \overline{x})^2$ 

symbol ~

### InterQuartile Range (IQR)

**Definition**: IQR the difference between Q<sub>3</sub> and Q<sub>1</sub>. It's the 'range' of 50% of the data.



**Example**: Compute the IQR of {6, 7, 15, 36, 39, 40, 41, 42, 43, 47, 49}

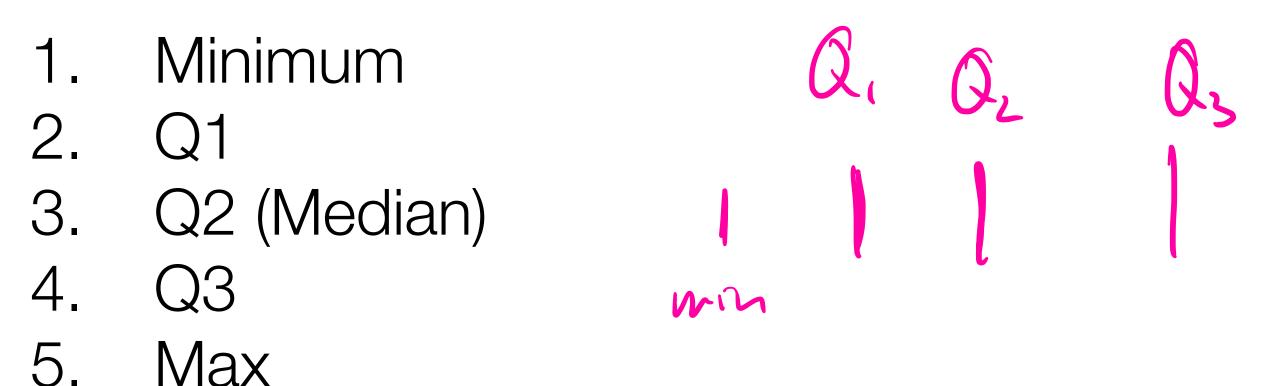
$$|QR - Q_3 - Q_1|^2$$

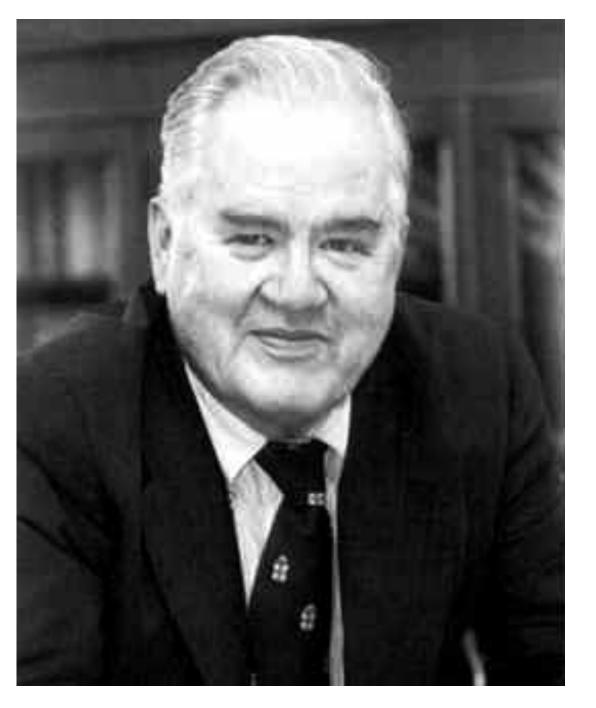
$$|QR - Q_1|^2$$

$$|$$

# Tukey's 5 number summary.

John Tukey advocated that we summarize datasets with 5 values.





John Wilder Tukey

invented FFT, coined the term "bit" = "binary digit" up there with Grace Hopper and the other demigods

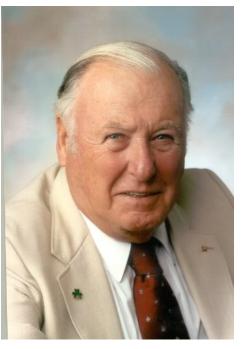
Max

#### Why we like this:

Gives the center of the data

Gives the spread through the easily computable IQR and range

Gives an idea of skewness



James Willian Cooley

What about Graphical Summaries of data?

Two key types that we'll dig into today:

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**Histogram**: FYI, not the same as #throwbackthursday. A histogram is a great way to visually understand a single distribution.

### What about Graphical Summaries of data?

Two key types that we'll dig into today:

**Histogram**: FYI, not the same as #throwbackthursday. A histogram is a great way to visually understand a *single distribution*.

**Boxplot**: sometimes called *box-and-whisker-plot*. A boxplot is a great way to visually compare *multiple distributions*.

### Histograms. Why?



Yellowstone National Park

O.F. erupts every 44 to 125 mins

for a ~2 to 5 mins.

```
184
                                118
                                     290
               105
                     272
                          199
                                230
                                     126
          274
                290
                     104
                          293
          110
                                223
                                      100
                288
                     109
                                      282
          105
                                250
                     119
                                121
               240
          246
               158
                     244
                          296
          112
               289
                     110
                          258
                                     225
                     243
                     102
                                139
                265
               118
                     276
                          226
                                115
                                     270
          168
                260
                     110
                          263
                                      296
                289
                     260
                          119
                                278
                                      121
               276
                          240
                                270
                                     245
          120
               230
                     210
                                142
                                      300
                          260
                                      145
                246
                     238
                          254
                                210
                                     262
          248
               112
                                262
                     276
                          107
                                     231
               230
                     205
               269
                     240
          105
                                     256
                133
          251
                     267
                                111
                                      257
               270
                     249
                                     267
                                          120
          214
286 \quad 272 \quad 111 \quad 255 \quad 119 \quad 135 \quad 285 \quad 247 \quad 129 \quad 265
```

#### 272 eruption durations!

Histograms. Why?

And yet! Not particularly useful? Let's dig in...

```
252
              105
                   282
                        130
                                  288
                                        96
                                            255
    105
         207
              184
                   272
                        216
                             118
                                  245
              242
                   230
                        121
                             112
                                  290
         274
              105
                   272
                        199
                             230
                                  126
                                            120
              290
                   104
                        293
                             223
         110
                                  100
         105
              288
                   109
                        264
                                  282
                             250
         270 \quad 240
                   119
                        304
                             121
                                  274 \quad 233
                   244
         246
              158
                        296
     260
         112
              289
                   110
                        258
                             280
                                  225
         126
              270
                   243
                             282
         294
              265
                   102
                        278
                             139
                                  276
                                       109
         255 118
                   276 \quad 226
                             115
                                  270
    250
         168
              260
                   110
                        263
                             113
                                  296
              289
                   260 119
                             278
                                  121
                   214
         144
              276
                        240
                             270
                                  245
         120 230
    249
                   210 275
                             142
                                  300
              200
                   250
                        260
                             270
                                  145
         255
              226
                   122
                        266
                             245
                                  110
                                            131
         288
              246
                   238
                        254
                             210
                                  262
    261
              112
         248
                   276
                        107
                             262
                                  231
                                            270
         112 \ \ 230
                   205
                        254
                             144
                                  288
                                       120
         105
              269
                   240
                        247
                                  256
                             245
    145
         251 \quad 133
                   267
                                  257 \quad 237
                       113
                             111
                        230
                                            261
         214 \quad 270
                   249
                        229
                             235
                                  267
                                       120
286 272 111 255 119 135 285 247 129 265
109 268
```

272 eruption durations!

Histograms. Why? n = 272 136,137

And yet! Not particularly useful? Let's dig in...

min: 76

max: 306

mean: 209.3

Q1: (29,5

Q2: 737

Q3: 767.5

```
102 104 105 105
                    223
               230 \quad 230
                         231
                             231 233
                    250
                    260
                         260
                              261
                                   261
                         264 \quad 265
                    263
                                         265
                                                   280
               288
                    288
                         288
                              288
                                   288
                                         289
              293 294 294 296
27 29028 304
```

df.sort\_values(...)

Histograms. Why?

A histogram shows us how the data are *distributed*.

Easy to compute.
Easy to understand.

```
120
               120
               132
               140
                   141
          157
               158
                    168
               207
                                  235
          230
               230
               247
                   248
                                  249
     250
          250
               250
                    251
                        252
               256
     260
          260
               260
                    260
                         261
                             261
                                  261
               263
                    264
                              265
                                  265
                                            280
                                            286
     288
          288
               288
                    288
                         288
                             288
                                  289
                                       289
     291 293 294 294 296 296 296 300 302
304 306
```

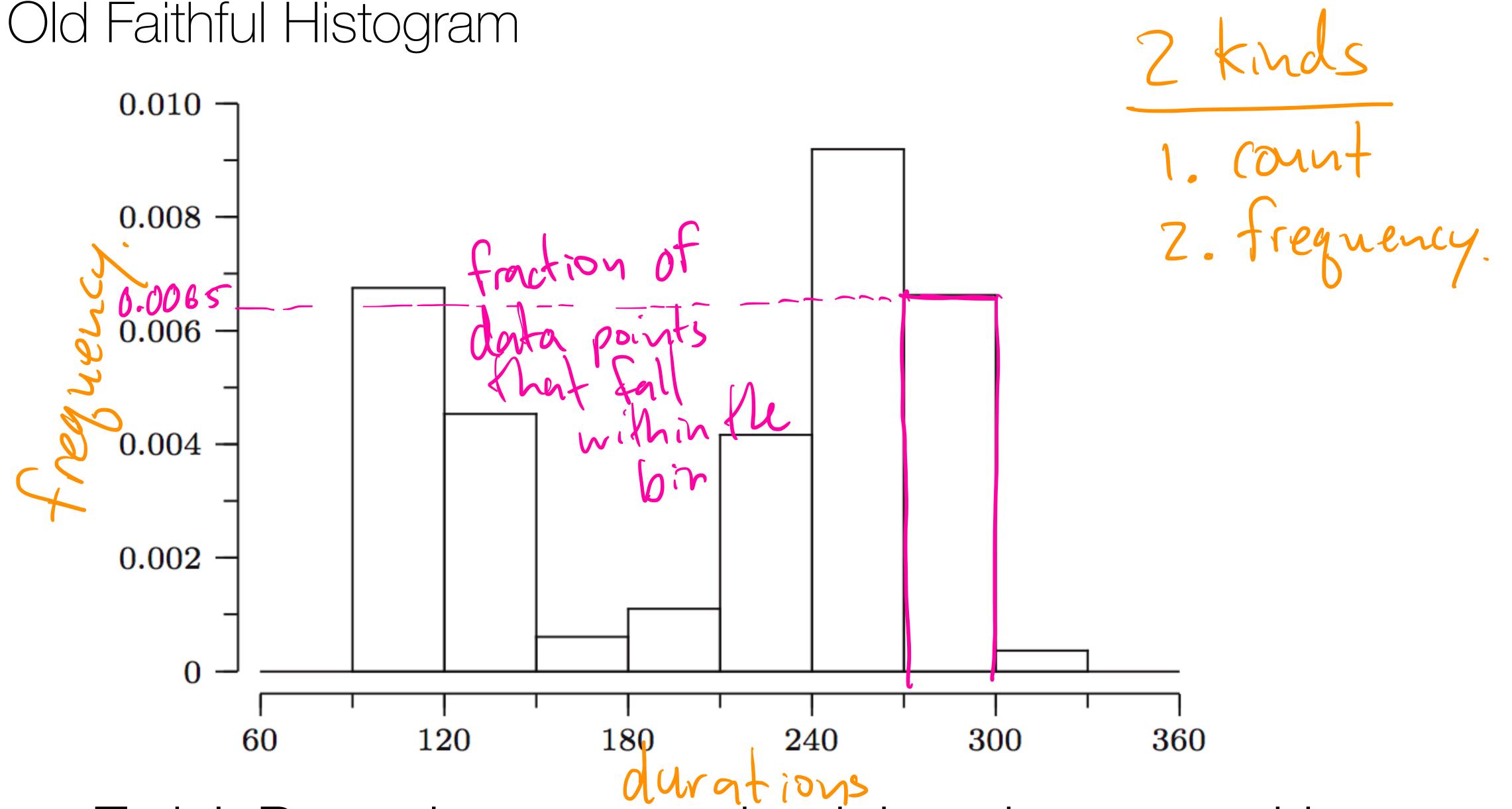
df.sort\_values(...)

Imagine all these data points on an axis...

```
104 105 105 105
                               105, 105, 105
         108
                  108 108
             108
         110
             110
                  110
                      110
                           111
112 112 112 112 112 113 113 113
                 117
                      118
         116
            116
                          118
                               118
    120
         120
             120
                  120
                      121
                                121
             126
                  126
                      126
             132
                  133
                      134
         132
                           134 \ 135
         139
             140
                      142
                  141
         157
             158
                  168
                                184
             207
         221
             223
                  224
                      225
                                226
    230
         230
             230
                  231
                      231
                           233
                                235
         238
             238
                  240
                                240
                      240
             244
         247
             247
                  248
                      248
                                249
    250
         250
             250
                  251
                      252
                           254
             256
                  256
                      257
    260
         260
             260
                  260
                       261
                           261
                                261
         262
             263
                  264
                      265
                           265
                                265
         267
             267
                  268
                      268
                                         280
                                         286
                           288
                                    289
             288
                  288
                                289
290 291 293 294 294 296 296 296 300 302
```

Then, divide the line into "bins" and count.

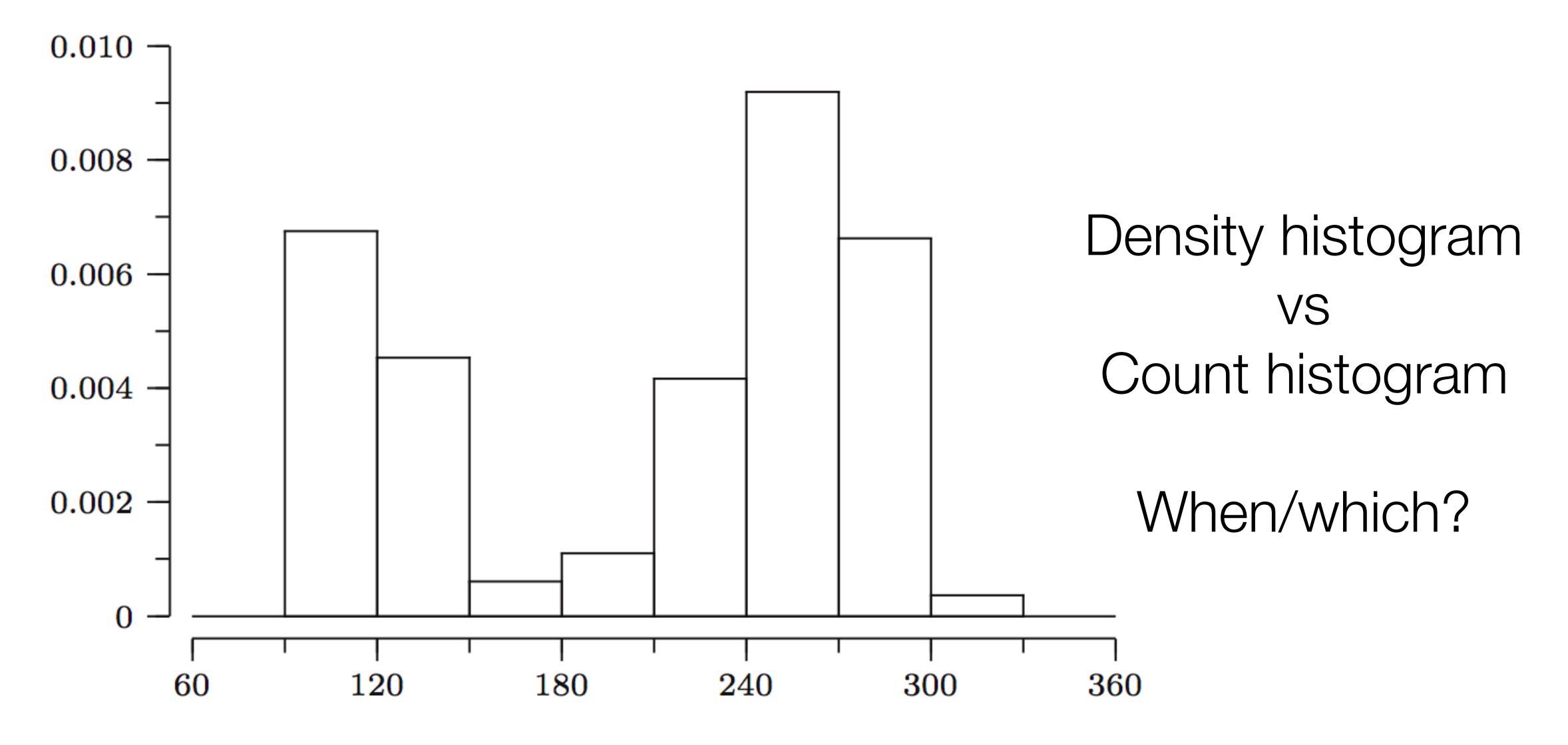
df.sort\_values(...)



Tada! But wait... your textbook has done something peculiar.

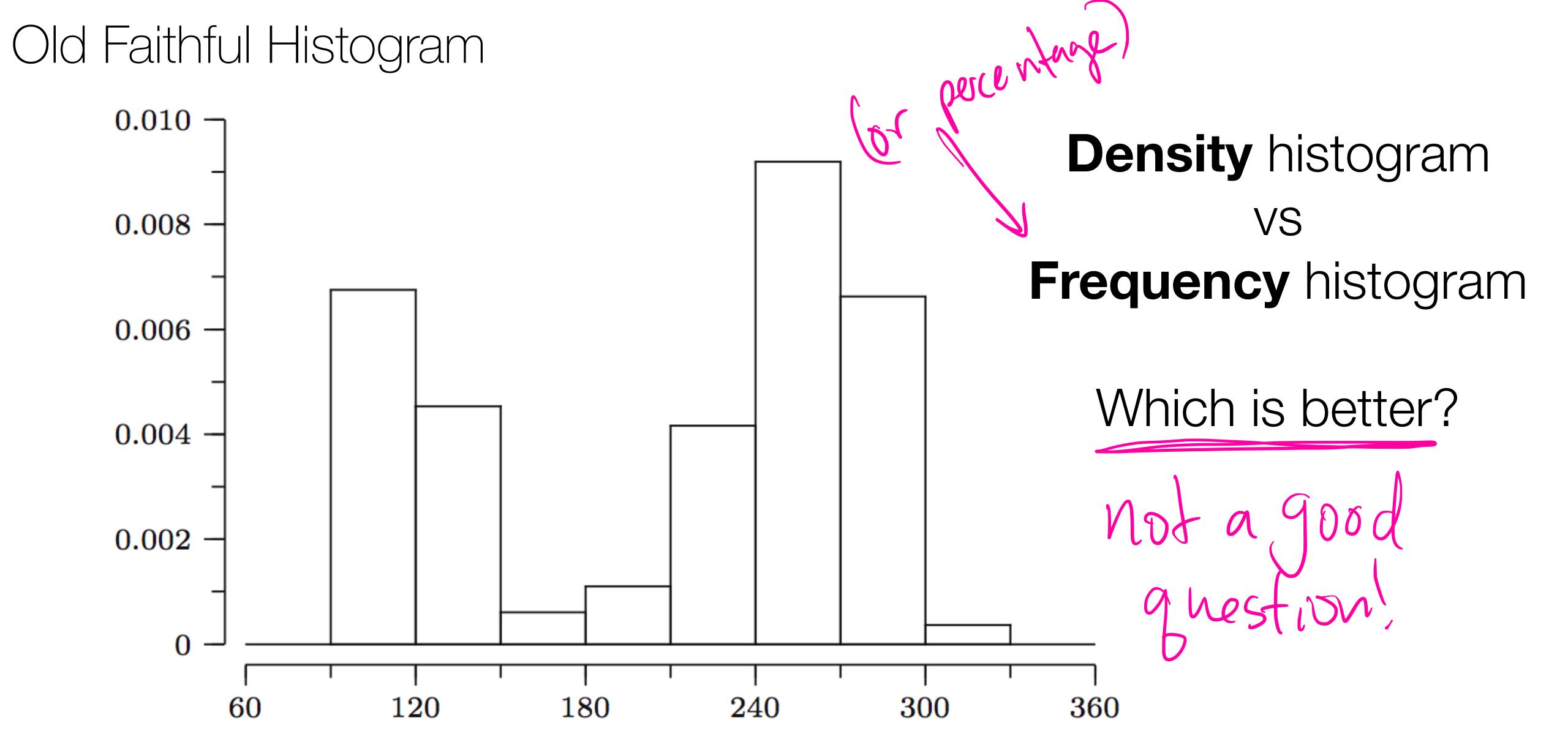
Can you spot it?

## Old Faithful Histogram



Tada! But wait... your textbook has done something peculiar.

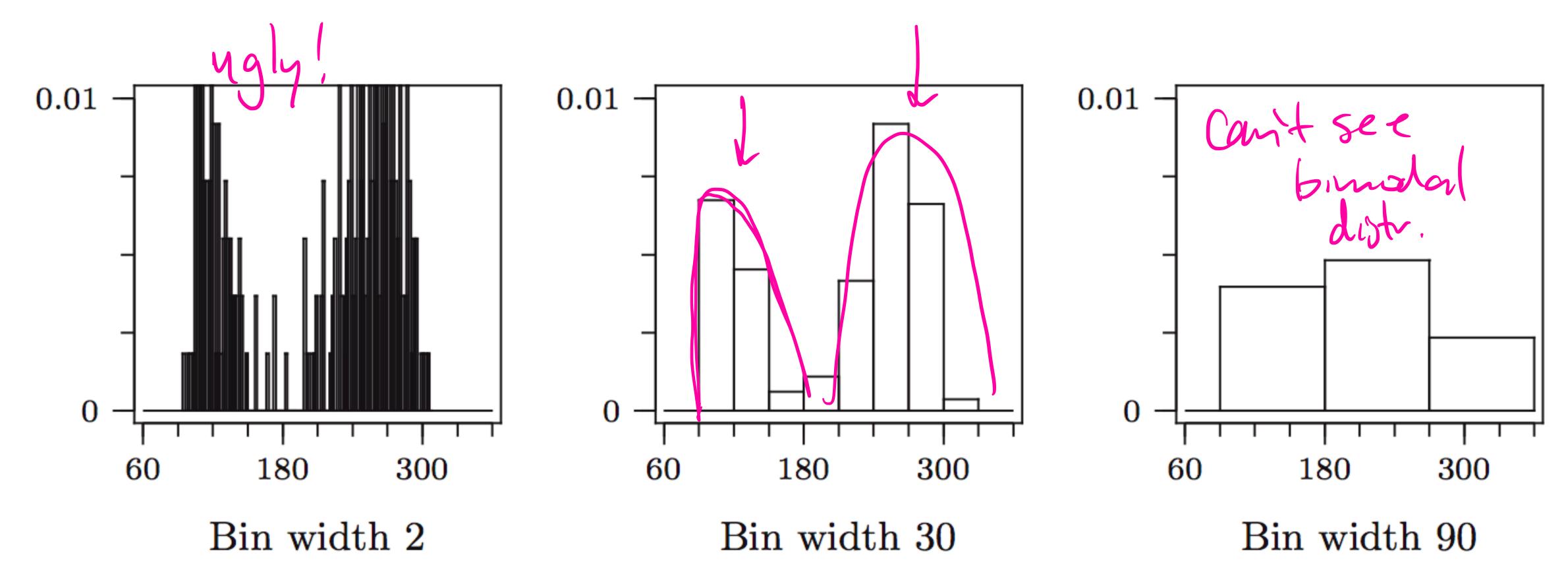
Can you spot it?



Tada! But wait... your textbook has done something peculiar.

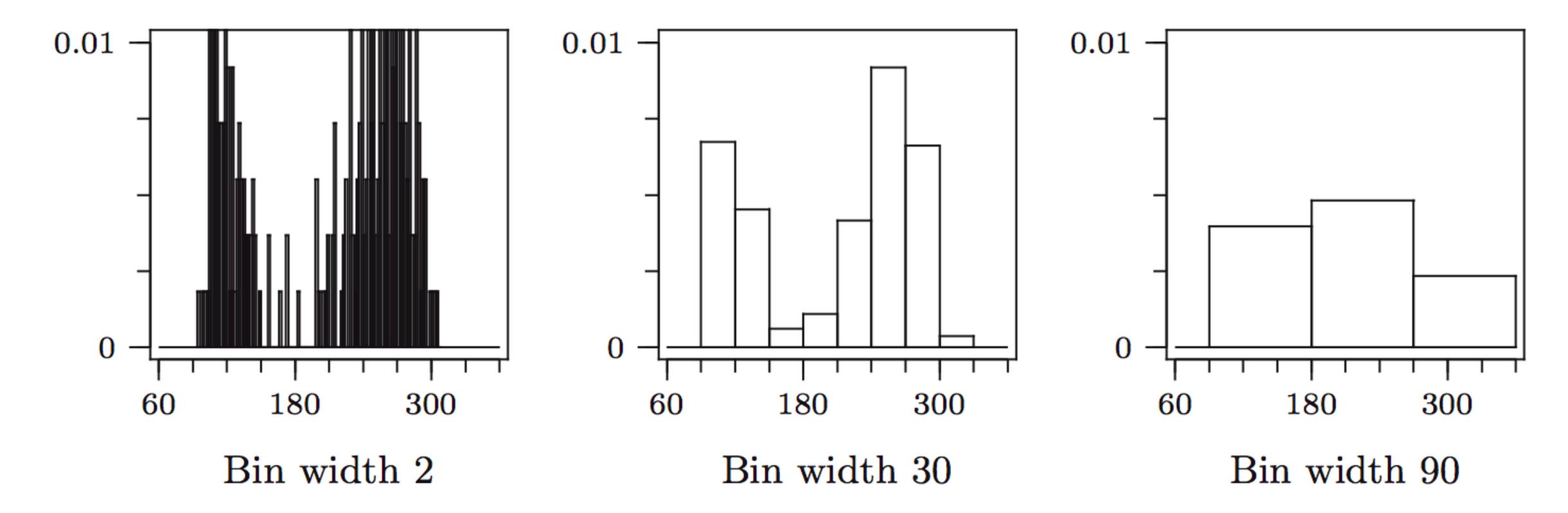
Can you spot it?

Bins, Bins, Bins...



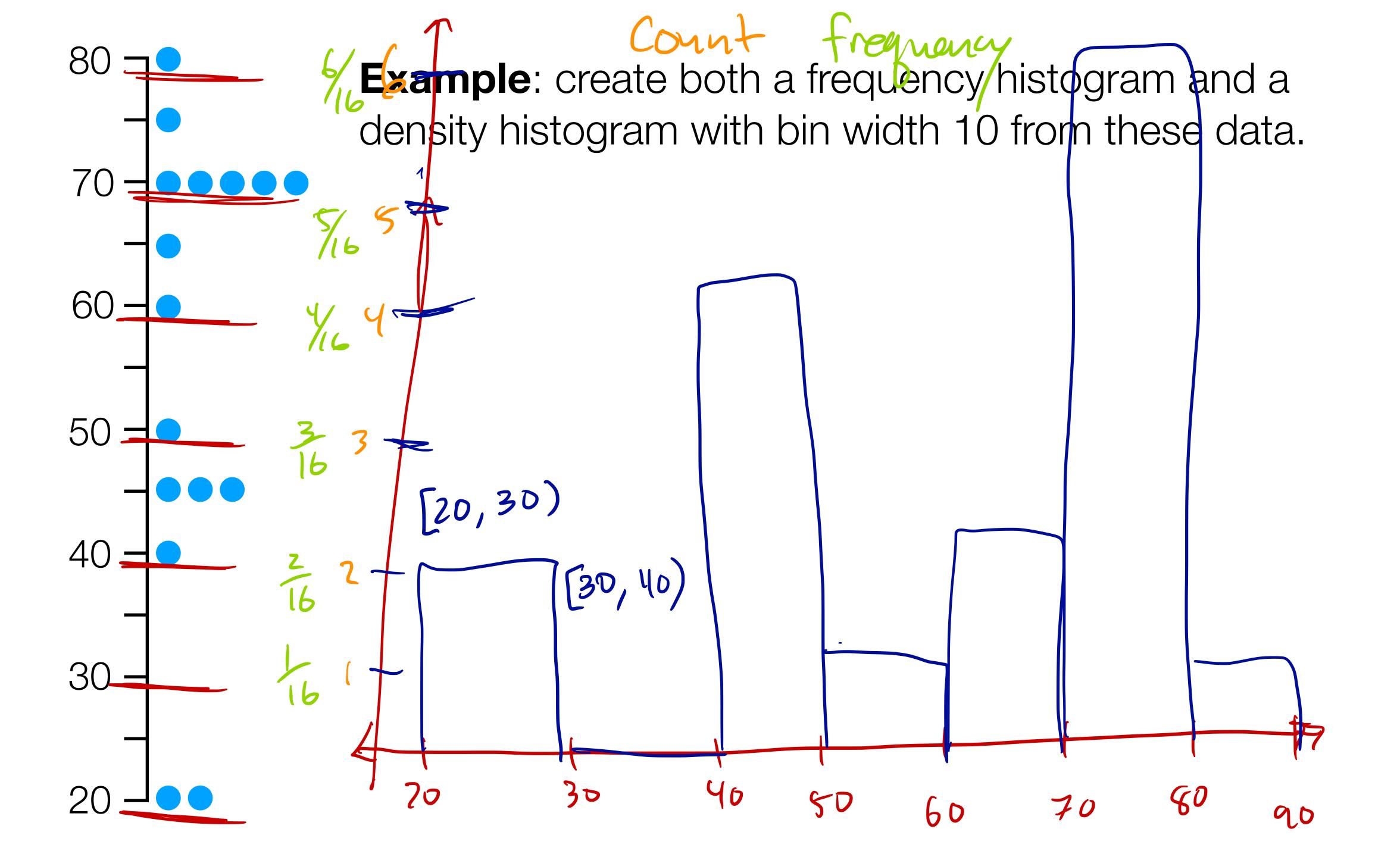
These are all histograms. They're all correct. However, the one in the middle is more useful. Why?

Bins, Bins, Bins...



These are all histograms. They're all correct. However, the one in the middle is more useful. Why?

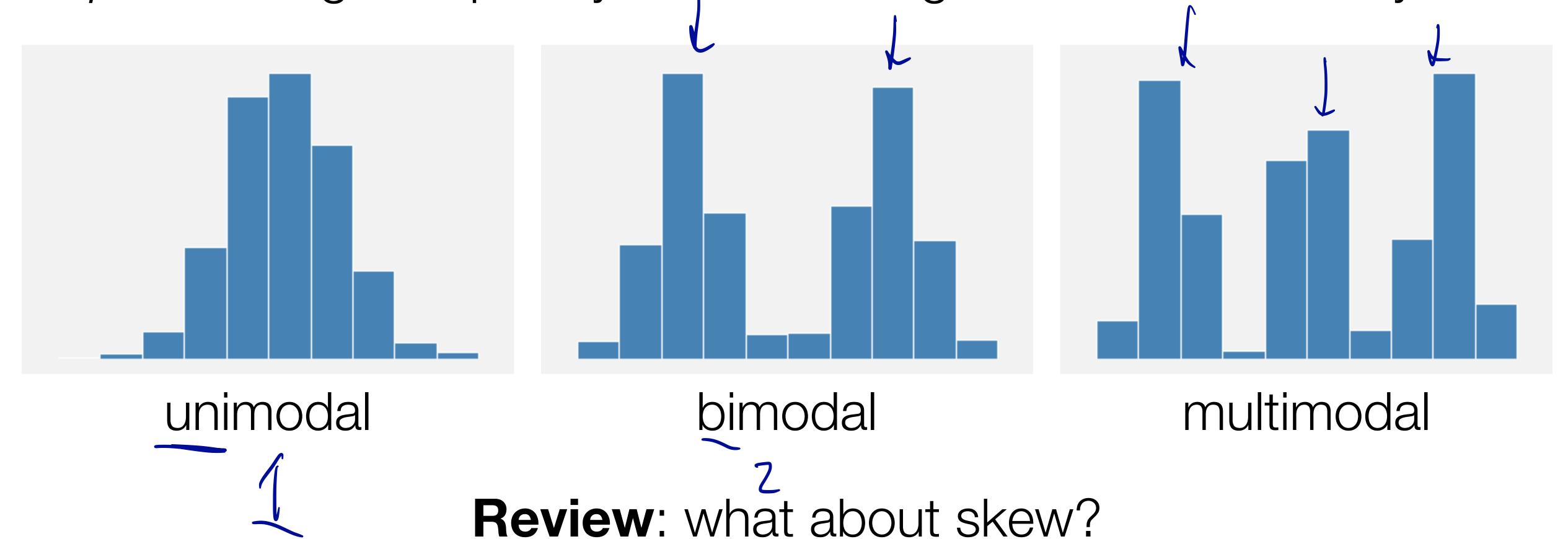
Goldilocks bin sizes, Freedman & Diaconis =  $2 \frac{IQR}{n^{1/3}} = 2 \frac{Q_3 - Q_1}{n^{1/3}}$ 



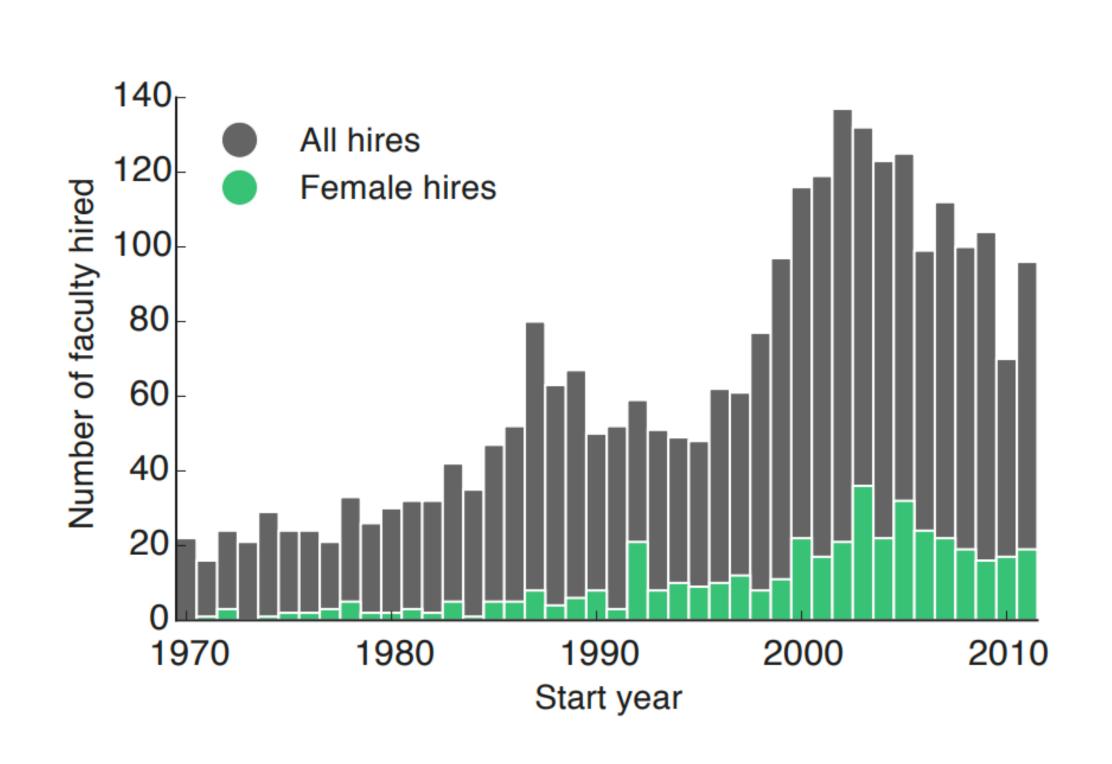
#### Modes..

We talked before about "the" mode, i.e. the most frequent value.

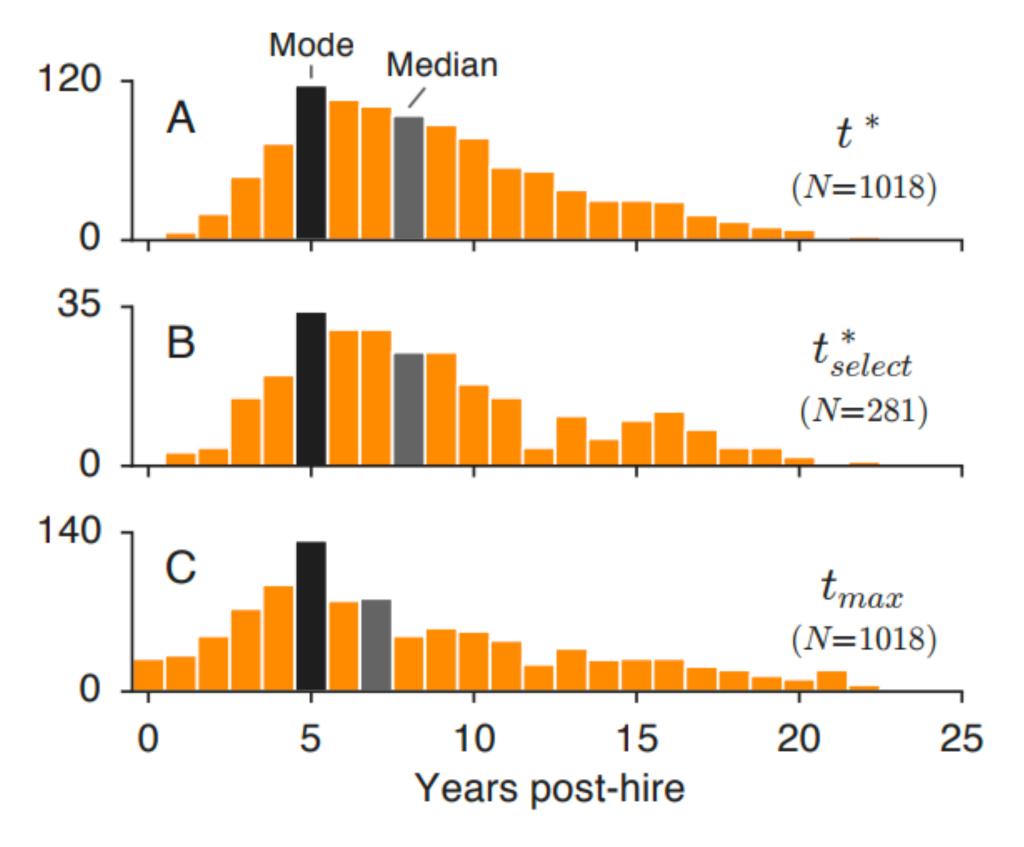
Often, it's useful to describe whether a distribution has multiple separated high frequency values. Histograms make this easy:



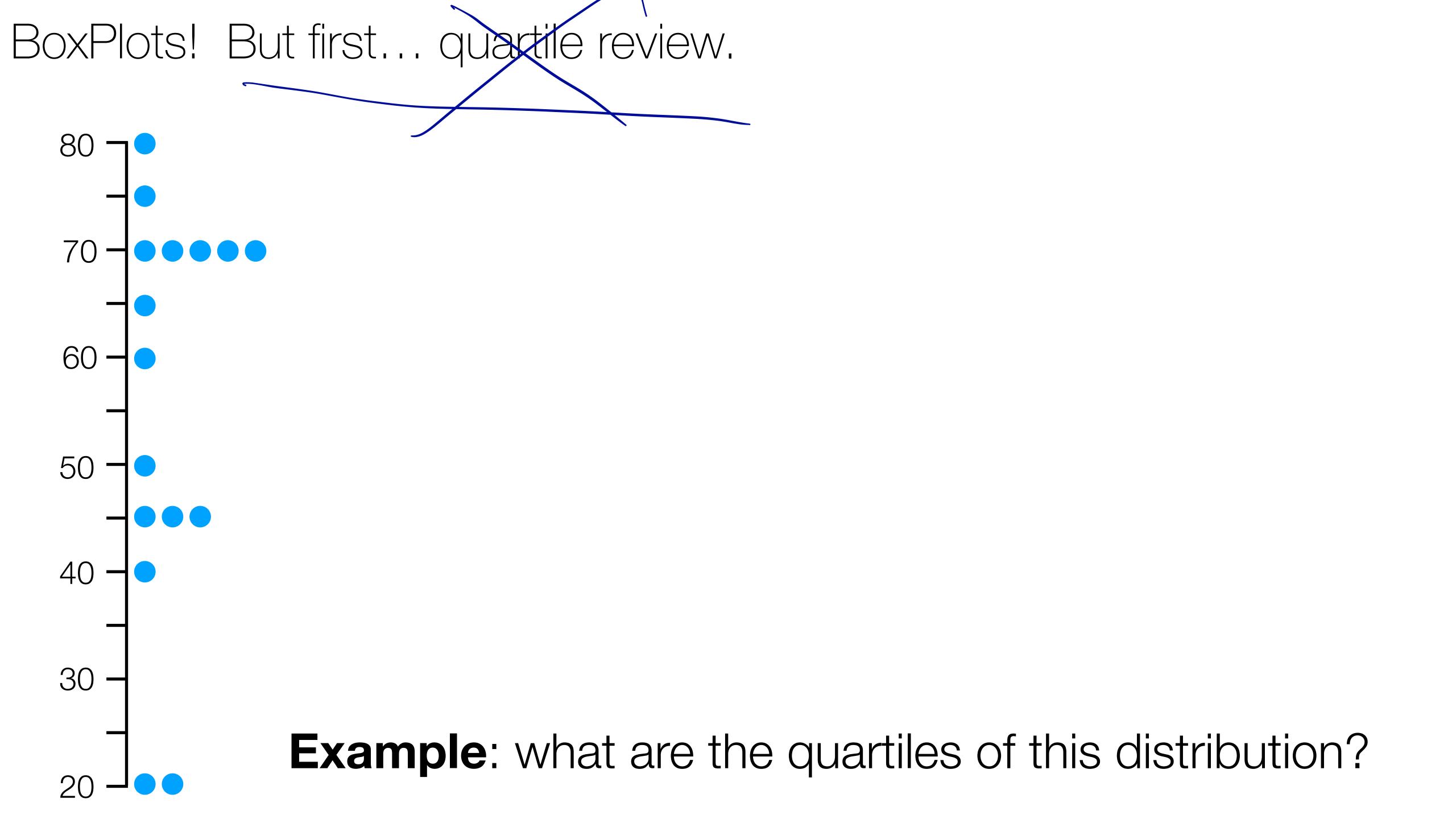
#### Histograms in the wild!



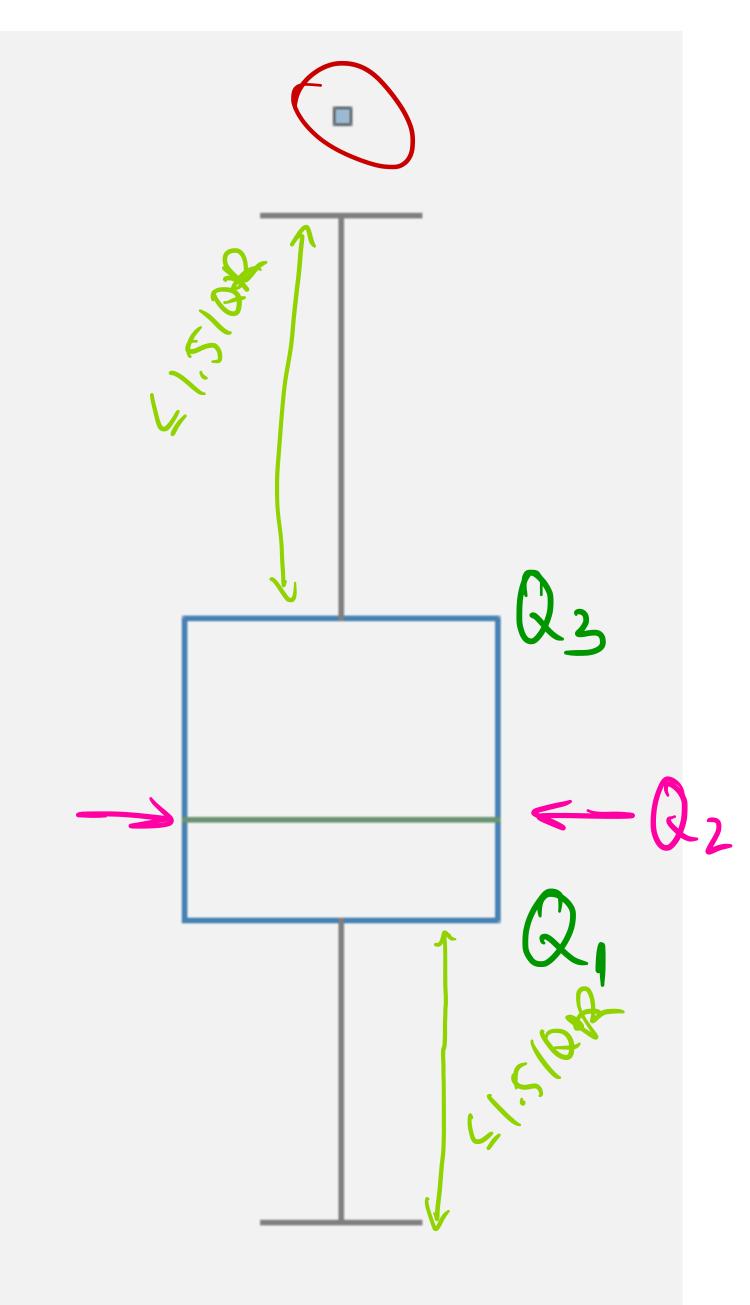
"Gender, Productivity, and Prestige in Computer Science Faculty Hiring Networks" Samuel F. Way, Daniel B. Larremore, and Aaron Clauset. Proc. 2016 World Wide Web Conference (WWW), 1169-1179 (2016).



"The misleading narrative of the canonical faculty productivity trajectory" Samuel F. Way, Allison C. Morgan, Aaron Clauset, and Daniel B. Larremore. (2016)

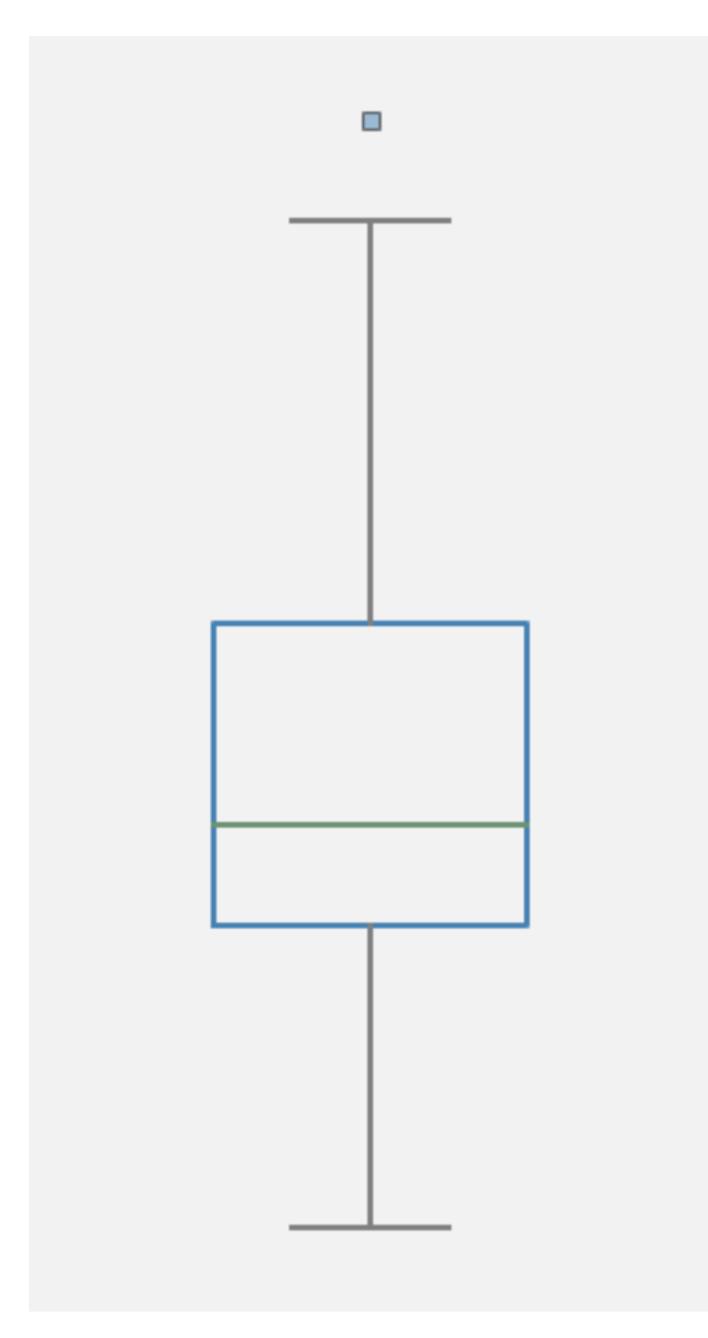


#### BoxPlots!



- The **Box** extends from  $Q_1$  to  $Q_3$ .
- The Median Line goes through median
- The Whiskers extend to farthest point within 1.5 x IQR
- The Fliers or outliers are any points outside of whiskers
- The width of the box is unimportant.

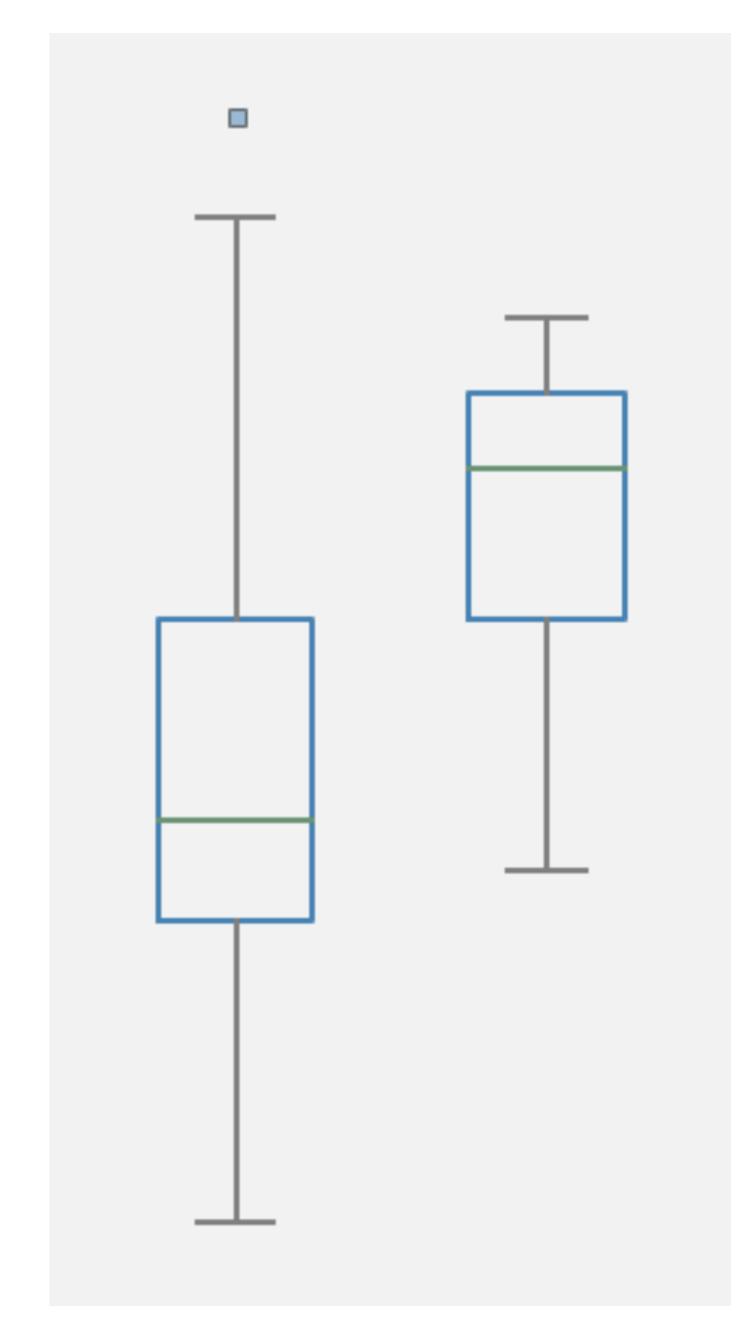
#### BoxPlots



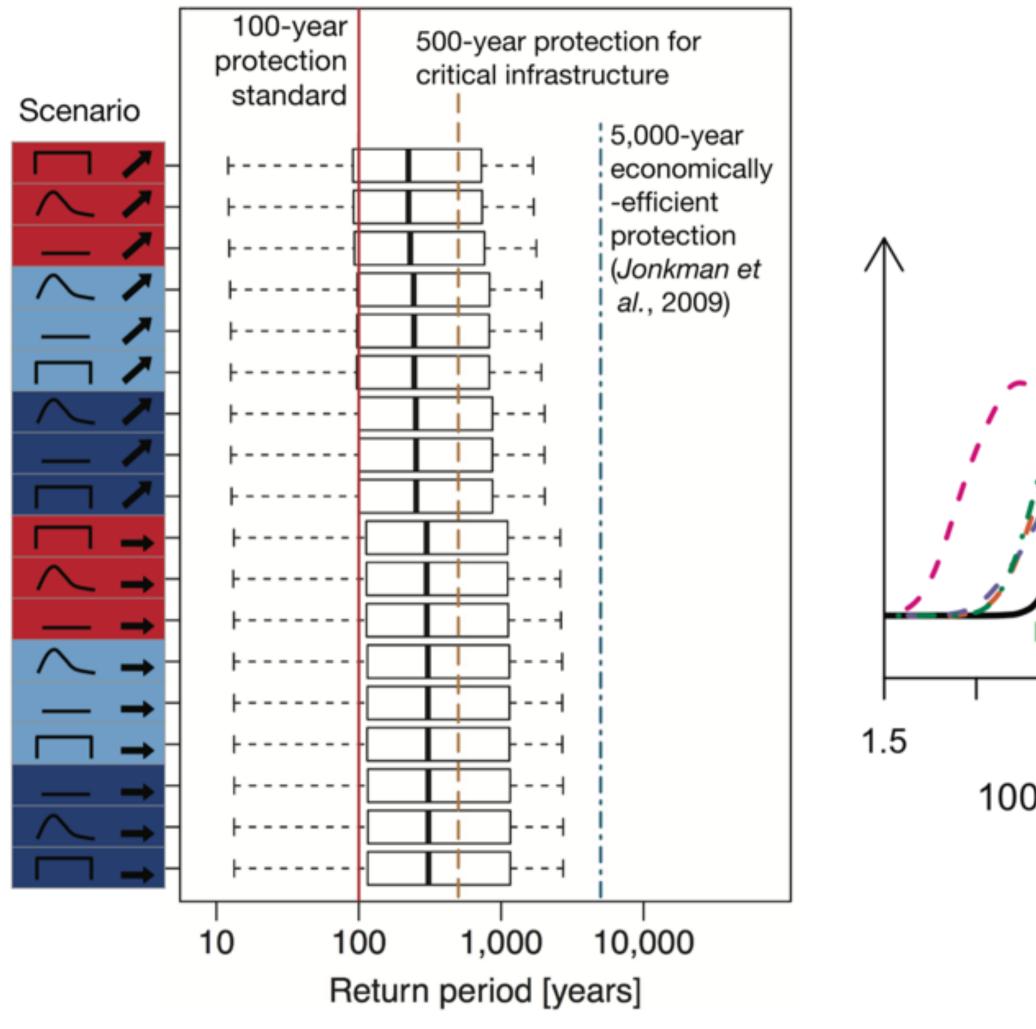
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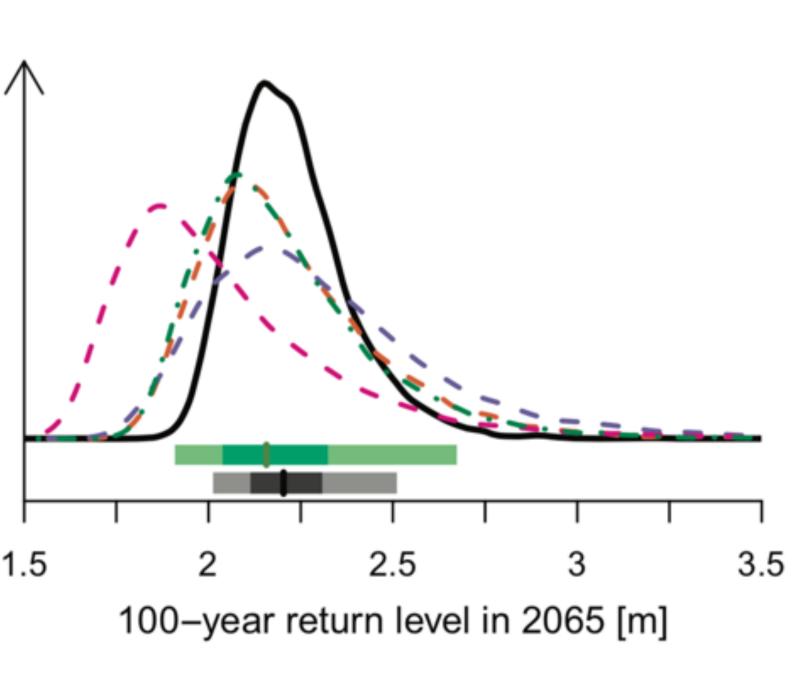
Boxplots are a visualization of Tukey's 5# summary.

#### BoxPlots!



Boxplots are great for comparing multiple datasets or pieces of a dataset.

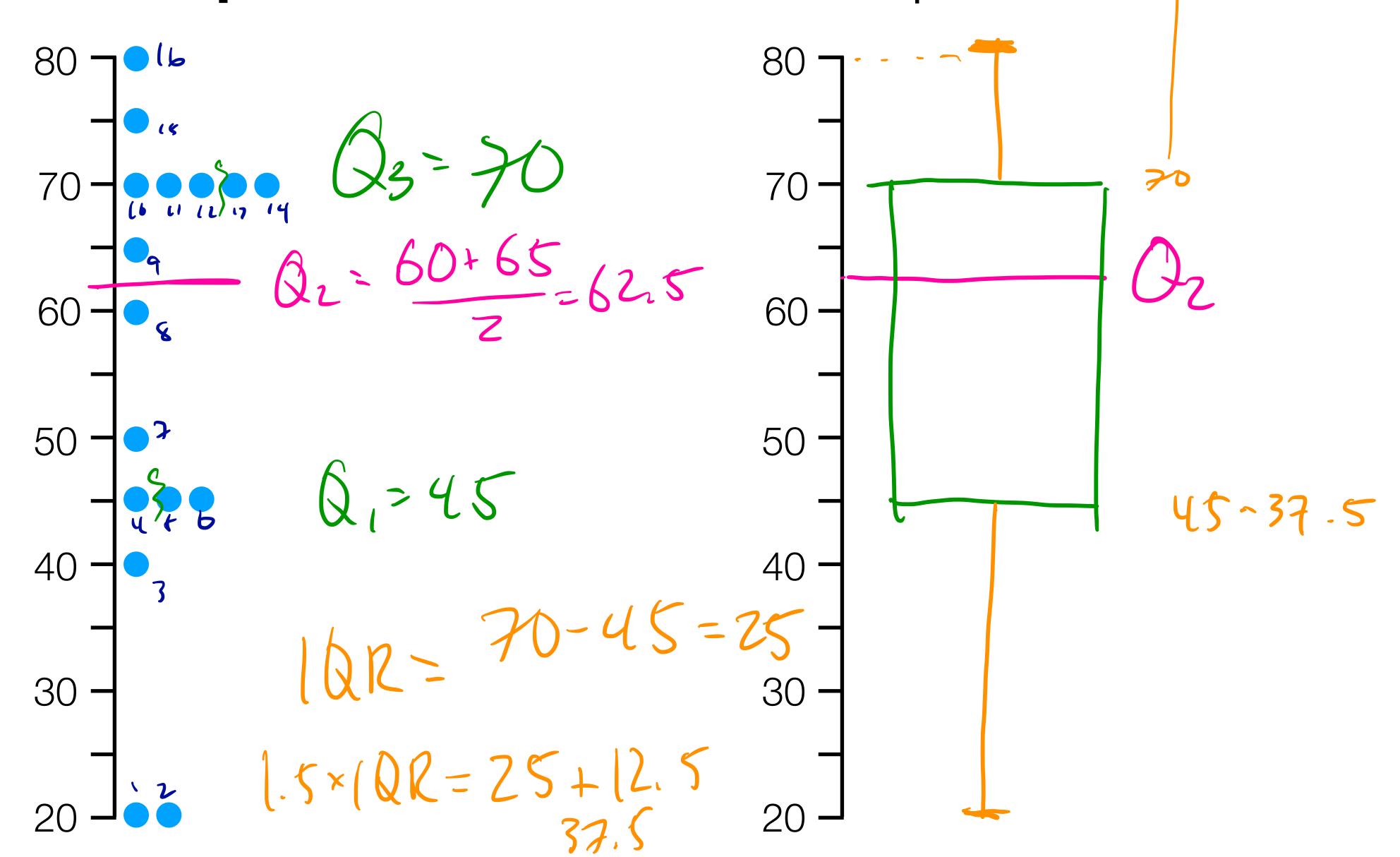




Wong, T.E. and K. Keller (2017), Probabilistic Future Flood Risk Scenarios for New Orleans, *Earth's Future*, DOI: 10.1002/2017EF000607.

Wong, T.E., A. Klufas, V. Srikrishnan, and K. Keller (2018), Neglecting Model Structural Uncertainty Underestimates Upper Tails of Flood Hazard, *Environmental Research Letters*, DOI: 10.1088/1748-9326/aacb3d.

# **Example**: draw a box & whisker plot from this dataset



# Advanced Histogram Thoughts!

it's not just about the bin width...

also important where the bins start!

