

$$Q2) \quad x = \begin{bmatrix} 1 & 2 \end{bmatrix} \quad w^{(1)} = \begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix} \quad w^{(2)} = \begin{bmatrix} 1 & 2 \\ 1 & 2 \end{bmatrix}$$

$$T = \begin{bmatrix} 0 & 0 \end{bmatrix}$$

$$\frac{\partial L}{\partial w^{(2)}} = \sum - (y_n - \hat{y}_n) \cdot \frac{\partial \hat{y}_n}{\partial s^{(3)}} \cdot \frac{\partial s^{(3)}}{\partial w^{(2)}}$$

$$= y_2^T \times (-T + y_3) \odot \begin{bmatrix} 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 \\ 3 \end{bmatrix} \times \begin{bmatrix} 5 & 10 \end{bmatrix} \odot \begin{bmatrix} 1 & 1 \end{bmatrix}$$

$$\boxed{\frac{\partial L}{\partial w^{(2)}} = \begin{bmatrix} 10 & 20 \\ 15 & 30 \end{bmatrix}}$$

$$\frac{\partial L}{\partial w^{(1)}} = x^T \times (y_3 - T) \times w^{(2)T}$$

$$= \begin{bmatrix} 1 \\ 2 \end{bmatrix} \times \begin{bmatrix} 5 & 10 \end{bmatrix} \times \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 1 \\ 2 \end{bmatrix} \times \begin{bmatrix} 25 & 25 \end{bmatrix}$$

$$\boxed{\frac{\partial L}{\partial w^{(1)}} = \begin{bmatrix} 25 & 25 \\ 50 & 50 \end{bmatrix}}$$