

1. Given matrix A as the product of the following 3 matrices, what is the value of A_{32} ?

$$A = \begin{bmatrix} 3 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & -5 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \begin{bmatrix} -2 & 0 & 0 \\ 0 & -3 & 0 \\ 0 & 0 & -4 \end{bmatrix}$$

(a) 120 (b) 36 (c) 32 (d) none of the above

2. If A is an invertible lower triangular matrix, then $(A^T)^{-1}$ is which of the following matrices.

(a) Diagonal (b) lower triangular (c) upper triangular (d) symmetric

3. If A^{-1} is the product of the following 3 matrices,

$$\begin{bmatrix} 1 & 0 & 0 \\ -2 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 3 & 1 \end{bmatrix} \begin{bmatrix} 1/2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

What is the value of the A_{31} ?

(a) 1 (b) 2 (c) -1 (d) -2

4. If A is an invertible matrix, which one of the following is false ?

- (a) A is a square matrix
- (b) $Ax=b$ has exactly one solution
- (c) A^T is also invertible
- (d) $Ax=0$ has nontrivial solutions.