

1. Give the 2×2 symmetric matrix which has eigenvalues $\lambda_1 = 3$ and $\lambda_2 = 2$ with corresponding eigenvectors $\begin{bmatrix} 1 \\ -3 \end{bmatrix}$ and $\begin{bmatrix} 3 \\ 1 \end{bmatrix}$

$$\begin{bmatrix} -21/10 & -3/10 \\ -3/10 & 29/10 \end{bmatrix}$$

2. Consider Q : $13x^2 - 10xy + 13y^2 - 72 = 0$, what is the quadratic form with no cross terms by performing a rotation ? (note : not need to show the rotation)

$$\begin{bmatrix} x & y \end{bmatrix} \begin{bmatrix} 13 & -5 \\ -5 & 13 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = 72 \quad \text{or} \quad 18'^2 + 8y'^2 = 72 \quad \text{or} \quad x'^2/4 + y'^2/9 = 1$$