

## Quiz10

1. What's the nullity of A with

$$\text{ref}(A) = \begin{bmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

- (a) 1      (b) 2      (c) 3      (d) 4

(a)

2. If  $A\mathbf{x}=\mathbf{0}$ , with

$$\text{rref}(A) = \begin{bmatrix} 1 & -3 & 0 & 1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Null (A) is spanned by

(a)  $\begin{pmatrix} -3 \\ 1 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} 1 \\ 2 \\ 0 \\ 1 \end{pmatrix}$  (b)  $\begin{pmatrix} 3 \\ 1 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} -1 \\ -2 \\ 0 \\ 1 \end{pmatrix}$  (c)  $\begin{pmatrix} 3 \\ 1 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} -1 \\ 0 \\ -2 \\ 1 \end{pmatrix}$  (d)  $\begin{pmatrix} -3 \\ 1 \\ 0 \\ 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 2 \\ 1 \end{pmatrix}$

(c)

3. If A is 3x4 matrix, then rank(A) is at most \_\_\_\_\_.

- (a) 1      (b) 2      (c) 3      (d) 4

(c)

4. True or False

If  $\mathbf{u}_1, \mathbf{u}_2, \dots, \mathbf{u}_n \in \mathbb{R}^n$  are linear independent, then  $M\mathbf{u}_1, M\mathbf{u}_2, \dots, M\mathbf{u}_n$

are also linearly independent.

False

5. True or False

If A is  $m \times n$  matrix, then  $\text{Rank}(A^T) + \text{Nullity}(A^T) = m$ .

True

