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Calibration Output

Fit to \$B\$:

```
[[15.38259852 16.32376991 22.79136017 0.69473671]]
Reduced \chi^2:
9.773087679348862
Hessian:
[[ 1.46254840e+07 -2.61266489e+06 -4.77996000e+05 -8.02105155e+07]
 [-2.61266489e+06 4.73145331e+05 8.36924668e+04 1.41052105e+07]
 [-4.77996000e+05 8.36924668e+04 1.91219697e+04 2.58462153e+06]
 [-8.02105155e+07 \quad 1.41052105e+07 \quad 2.58462153e+06 \quad 4.51684397e+08]]
Covariance Matrix:
[[2.02545829e-03 6.26923449e-03 4.57864379e-03 1.37707037e-04]
 [6.26923449e-03 1.97238413e-02 1.39523498e-02 4.17521734e-04]
 [4.57864379e-03 1.39523498e-02 1.27571234e-02 3.04376715e-04]
 [1.37707037e-04 4.17521734e-04 3.04376715e-04 9.69569673e-06]]
Matrix of Correlation:
             0.99187538 0.90073871 0.98266383]
 [0.99187538 1. 0.87957976 0.95475914]
 [0.90073871 0.87957976 1.
                                   0.865457081
 [0.98266383 0.95475914 0.86545708 1.
Conditioned Hessian:
         -0.99318764 -0.90386345 -0.98686703]
 [-0.99318764 1.
                          0.87987864 0.96486099]
 [-0.90386345 \quad 0.87987864 \quad 1.
                                      0.879453941
 [-0.98686703 \quad 0.96486099 \quad 0.87945394 \quad 1.
Conditioned Hessian Eigenvalues:
[3.80597516e+00 1.58273488e-01 2.26022377e-04 3.55253288e-02]
```

Since the largest eigenvalue for the conditioned Hessian is \$\sim 1\$, and the next largest is four orders of magnitude less, the effective number of parameters is one, while the other three are negligible, comparatively.

Fit to \$B/A\$:

```
Best fit parameters (manual):  [[14.99186197\ 15.40430709\ 21.08623433\ 0.66223486]]  Reduced \chi^2:  0.0017192739342586434  Hessian:  [[6.290000000e+02\ -1.30445310e+02\ -1.79661613e+01\ -2.90292230e+03]   [-1.30445310e+02\ 2.84197186e+01\ 3.65562462e+00\ 5.67114157e+02]   [-1.79661613e+01\ 3.65562462e+00\ 7.60102675e-01\ 7.97080129e+01]   [-2.90292230e+03\ 5.67114157e+02\ 7.97080129e+01\ 1.45727189e+04]]  Covariance Matrix:  [[1.15748945e-03\ 2.97892312e-03\ 2.36811060e-03\ 1.01693794e-04]   [2.97892312e-03\ 7.98472891e-03\ 5.55109757e-03\ 2.52311365e-04]   [2.36811060e-03\ 5.55109757e-03\ 1.10776908e-02\ 1.95114882e-04]
```

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```
[1.01693794e-04 2.52311365e-04 1.95114882e-04 9.48943640e-06]]
Matrix of Correlation:
[[1. 0.97987502 0.66133094 0.97032164]
[0.97987502 1.
                        0.59023391 0.91661406]
[0.66133094 0.59023391 1.
                                    0.601790831
[0.97032164 0.91661406 0.60179083 1.
                                         ]]
Conditioned Hessian:
             -0.97564823 -0.82166321 -0.95882599]
                           0.78653051 0.8812321 ]
[-0.97564823 1.
[-0.82166321 \quad 0.78653051 \quad 1.
                                        0.75734813]
 [-0.95882599 \quad 0.8812321 \quad 0.75734813 \quad 1.
                                                ]]
Conditioned Hessian Eigenvalues:
[3.59663476e+00 2.83928814e-01 1.59108187e-03 1.17845342e-01]
```

The result from fitting to \$B/A\$, compared to \$B\$ is similar, but not quite the same. The difference is most obvious in the reduced \$\chi^2\$ value.