

### ENSE452 Assignment 3

1. Consider a system that has three tasks with periods: 10 millisecond, 39 millisecond, and 1 second. If the WCETs have been estimated at 4 milliseconds, 12 milliseconds, and 98 milliseconds, respectively, what is the total time-loading of the system? (We are ignoring context switch time) Is the task set guaranteed to have a feasible schedule, by the RMS criterion? If not, what would be the easiest rewrite that would make the three tasks schedulable? Explain your answer

Time loading of the system:  $U_i = C_i / P_i$  where  $C_i$  is the WCET and  $P_i$  is the period

- $4 \text{ ms} / 10 \text{ ms} = 0.4$
- $12 \text{ ms} / 39 \text{ ms} = 0.3077$
- $98 \text{ ms} / 1000 \text{ ms} = 0.098$

Total time loading of the system =  $0.4 + 0.3077 + 0.098 = \mathbf{0.8057}$

RMS criterion for utilization with  $n$  tasks:  $n(2^{1/n} - 1) = 3(2^{1/3} - 1) = 0.7798 < 0.8057$  therefore, the task set is not guaranteed to have a feasible schedule by the RMS criterion.

The easiest rewrite would be to change the 39 millisecond period to be 40 milliseconds which would make this a harmonic set and  $U < 100\%$  so it is now guaranteed to be a feasible schedule.

2. A preemptive system has three concurrent tasks, described by the table below (context switch time is ignored). The background, or idle task is assumed to be nonessential and is fully preemptable by all higher priority tasks.

| Task  | Cycle        | Execution Time | Priority    |
|-------|--------------|----------------|-------------|
| TaskA | 10ms         | 4ms            | 3 (highest) |
| TaskB | 20ms         | 5ms            | 1           |
| TaskC | 40ms         | 10ms           | 2           |
| Idle  | (continuous) | 5ms            | —           |

(a) Answer the following:

- i. What is the system utilization?

$$U_i = \text{Sum of } (C_i/P_i) = (4 \text{ ms} / 10 \text{ ms}) + (5 \text{ ms} / 20 \text{ ms}) + (10 \text{ ms} / 40 \text{ ms}) = 0.4 + 0.25 + 0.25 = 0.9 = \mathbf{90\%}$$

- ii. Is this task set RMS scheduled?

Max allowable utilization =  $n (2^{(1/n)} - 1) = 3 (2^{(1/3)} - 1) = 0.7798 < 0.9$  so the **task set is not RMS scheduled**

iii. What is the response time for each task?

WCET + (roundUp(previous result / period of previous task)) \* previous WCET  
 Task A response time = **4 ms**

Task C response time  $10\text{ms} + (0\text{ms} / 10\text{ms}) * 4 = 10\text{ms}$   
 $10\text{ms} + (10\text{ms}/10\text{ms}) * 4\text{ms} = 14\text{ms}$   
 $10\text{ms} + (14\text{ms}/10\text{ms}) * 4\text{ms} = 10 + 2 * 4 = 18\text{ms}$   
 $10\text{ms} + (18/10) * 4 = 10 + 2 * 4 = \mathbf{18\text{ms Converged}}$

Task B response time =  $5\text{ms} + (5\text{ms} / 40\text{ms}) * 10\text{ms} + (5/10) * 4 = 5 + 10 + 4 = 19\text{ms}$   
 $5\text{ms} + (19\text{ms} / 40) * 10 + (19/10) * 4 = 5 + 10 + 8 = 23\text{ms}$   
 $5 + (19/40) * 10 + (23/10) * 4 = 5 + 10 + 12 = 27\text{ms}$   
 $5 + (27/40) * 10 + (27/10) * 4 = 5 + 10 + 12 = \mathbf{27\text{ms Converged}}$

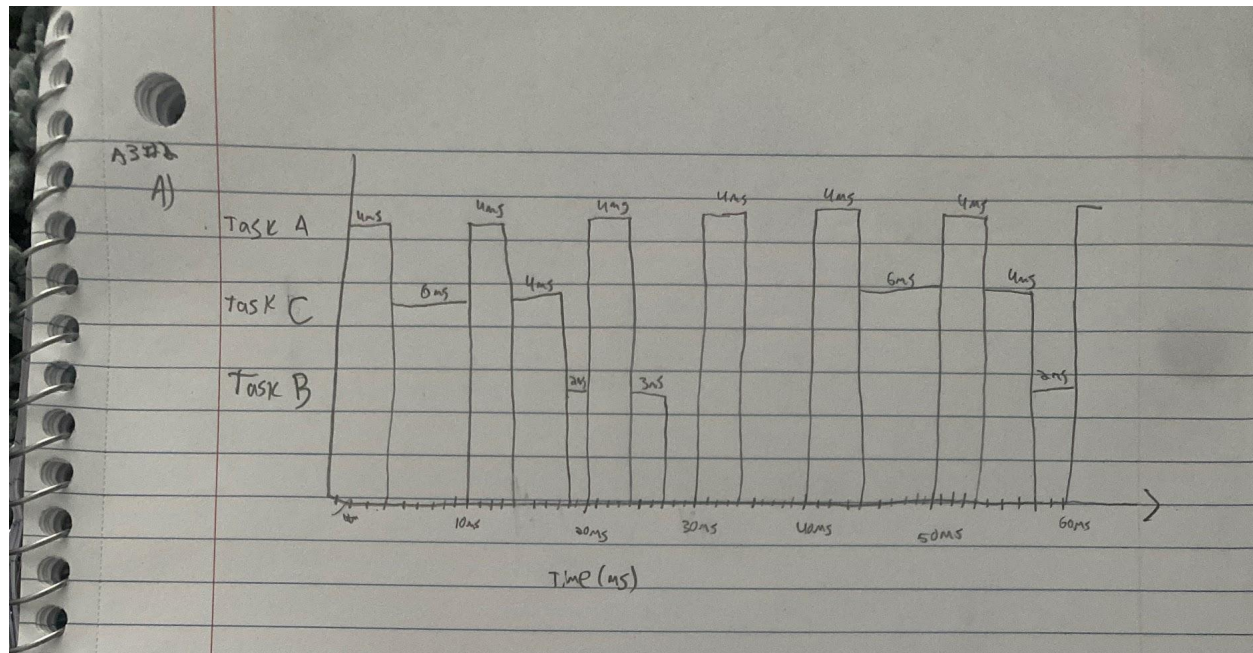
iv. Do all the tasks meet their deadlines? By how much does each task beat, or miss, its deadline.

**Task A: 4 ms < 10ms Deadline beat by 6 ms**

**Task B: 27 ms > 20 ms Deadline missed by 7 ms**

**Task C: 18 ms < 40ms Deadline beat by 22 ms**

v. Draw an execution time line for this system.



(b) Now suppose the priorities of Task B and C are interchanged, that is, TaskB has priority 2 and TaskC has priority 1. Answer the following:

i. What is the system utilization?

System utilization is still **90%**

ii. What is the response time for each task?

Task A response time = **4 ms**

Task B response time =  $5 \text{ ms} + (0/10) * 4 = 5 \text{ ms}$

$5 \text{ ms} + (5/10) * 4 = 5 + 1 * 4 = 9 \text{ ms}$

$5 \text{ ms} + (9/10) * 4 = 5 + (1 * 4) = \mathbf{9 \text{ ms Converged}}$

Task C response time =  $10 \text{ ms} + (9/20) * 5 = 10 + (1 * 5) = 15 \text{ ms}$

$10 \text{ ms} + (10/10) * 4 + (10/20) * 5 = 10 + 4 + 5 = 19 \text{ ms}$

$10 \text{ ms} + (19/10) * 4 + (19/20) * 5 = 10 + 8 + 5 = 23 \text{ ms}$

$10 \text{ ms} + (23/10) * 4 + (23/20) * 5 = 10 + 12 + 10 = 32 \text{ ms}$

$10 \text{ ms} + (32/10) * 4 + (32/20) * 5 = 10 + 16 + 10 = 36 \text{ ms}$

$10 \text{ ms} + (36/10) * 4 + (36/20) * 5 = 10 + 16 + 10 = \mathbf{36 \text{ ms Converged}}$

iii. Do all the tasks meet their deadlines? By how much does each task beat, or miss, its deadline.

**Task A:  $4 \text{ ms} < 10 \text{ ms}$  Deadline beat by 6 ms**

**Task B:  $9 \text{ ms} < 20 \text{ ms}$  Deadline beat by 11 ms**

**Task C:  $36 \text{ ms} < 40 \text{ ms}$  Deadline beat by 4 ms**

iv. Draw an execution time line for this system.

