

# Tarea 3

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## 1. Ejercicio 1

$ssso + sssso$   
 $s(ssso + sssso)$   
 $s(s(ssso + sso))$   
 $s(s(s(ssso + so)))$   
 $s(s(s(s(ssso + o))))$   
 $s(s(s(s(s(so + o))))))$   
 $s(s(s(s(s(s(o)))))))$   
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## 2. Ejercicio 2

Caso Base

Por axiomas pasados, se sabe que cualquier número multiplicado por cero es igual a cero.

Caso Inductivo

$a \otimes b = a + (a * (b - 1))$   
 $a \otimes b = a + (ab - a)$   
 $a \otimes b = a + ab - a$   
 $a \otimes b = ab$   
 $a \otimes b = a \otimes b$

## 3. Ejercicio 3

$s(s(s(0))) \otimes 0$

Axioma = n por cero es 0

$$\begin{aligned}
& s(s(s(0))) \otimes s(0) \\
s(s(s(0))) \otimes s(0) &= sss0 + (sss0 * (s0-s0)) \\
s(s(s(0))) \otimes s(0) &= sss0 + (sss0 * (0)) \\
s(s(s(0))) \otimes s(0) &= sss0
\end{aligned}$$

$$\begin{aligned}
& s(s(s(0))) \otimes s(s(0)) \\
s(s(s(0))) \otimes s(s(0)) &= sss0 + (sss0 * (ss0-s0)) \\
s(s(s(0))) \otimes s(s(0)) &= sss0 + (sss0 * s0) \\
s(s(s(0))) \otimes s(s(0)) &= sss0 + sss0 \\
s(s(s(0))) \otimes s(s(0)) &= ssssss0
\end{aligned}$$

#### 4. Ejercicio 4

$$\begin{aligned}
a \oplus s(s(0)) &= s(s(a)) \\
a \oplus s(s(0)) &= s(0) + s(a) \\
a \oplus s(s(0)) &= s(s(0)) + a \\
a \oplus s(s(0)) &= a \oplus s(s(0))
\end{aligned}$$

$$\begin{aligned}
a \otimes b &= b \otimes a \\
sa \otimes sb &= sb \otimes sa \\
s(a \otimes b) &= s(b \otimes a) \\
s(a \otimes b)/s &= s(b \otimes a)/s \\
a \otimes b &= b \otimes a
\end{aligned}$$

$$\begin{aligned}
& \text{Caso base } C=0 \\
a \otimes (b \otimes 0) &= (a \otimes b) \otimes 0 \\
a \otimes 0 &= (a \otimes b) \otimes 0 \\
& \text{Axioma = n por cero es 0} \\
0 &= 0
\end{aligned}$$

$$\begin{aligned}
& \text{Caso Inductivo} \\
a \otimes (b \otimes c) &= (a \otimes b) \otimes c \\
a \otimes bc &= ab \otimes c \\
abc &= abc
\end{aligned}$$