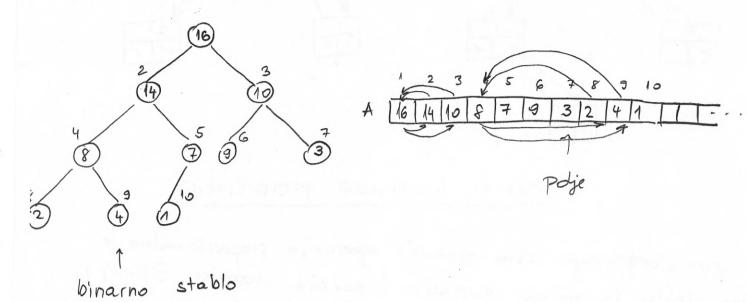
BINARNE HRPE

struktura podataka koja se może promatrati kao "skoro" potpuno binarno stablo (svaki čvor, osim nekolicine, ima točno dva djeteta)

koristi polje kao spremnik



length - olulina potra A
heap-size - broj elemenata u hrpi

\$\int 0 \leq A.heap-size \leq A.length

[1] - Korijen stabla

(skoro potpuno)

FRENT (i) - indeks roditeljskog čvora od čvora s indeksom i u A FT (i) - indeks lijevog djeteta od čvora s indeksom i u polju A light (i) - indeks deshog djeteta od čvora s indeksom i u polju A

PARENT (i)

if i=1
error: "Korijen nema roditelja"
else then
return [1/2]

end if

= razlikujemo dvije vrste binarnih hrpa:

- * maksimalno origentirane hrpe
- * minimalno origentirane hope

Svojstvo maksimalno orijentirane hrpe:

Za svaki 1=2,---, A. heap-site
A[PARENT (i)] Z A Ti)

=) Največi element u svakom podstablu nalazi se u kori jem tog podstabla

Svojstvo minimalno orijentirane hrpe! Za svaki i= 2,---, A. heap-size A [PARENT (i)] < A [i]

=> Najmanji element u svakom podstablu nalazi se u korijemu tog podstabla

visina binarnog stabla kojim je implementirana binarna) hrpa od n elemenata iznosi O(lyn) e Zadafa

l'azmotrit cemo skedece operacije maksimalno orijentirane

hrpe: * Max - HEAPIFY - Služi za očuvanji svojstva Maksimalno orijentirane hrpe . ()

* BUILD-MAX-HEAP-služi za izgradnju maksimalno-Orijentirane hrpe iz nesortiranog polja A

Vrijeme: O(n)

* HEAPSORT - Sortira polje A "in-place" (\$ "konstantuo "mnego" dodatne memorije)

Vrijeme: O(n lyn)

* MAX-HEAP-INSERT - Ubacironje novog elementa Vrijeme: Olyn)

* HEAP- EXTRACT- MAX hirbrisange najverez

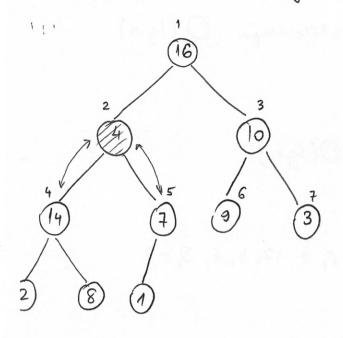
elementa Vrijeme: Olyn) * HEAD- INCREASE-KEY - poveravanje rrijednosti kynča nekog elementa

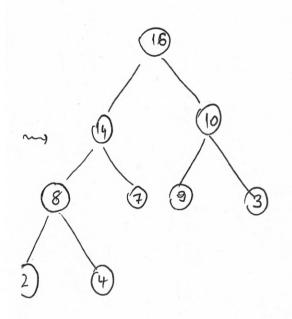
Vrijeme: O(lgn)

: HEAD- MAXIMUM uzimanje najvećeg elementa Vrijeme: O(lgn)

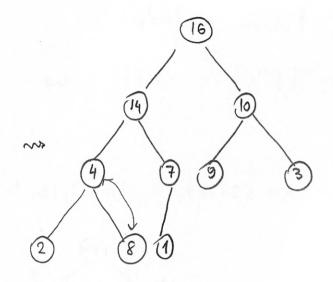
Održavanje svojstva hrpe

- ordin leuro implementirati funkcipi MAX-HEAPIFY (A,i)
- pretpostavljamo da Evigistro može briti narusenomini.





A[PARENT(i)] > A[i)



MAX- HEAPIFY (A,i)

L← LEFT(i)

F ← RIGHT(i)

If L ⊆ A. heap-size and A[L] > A[T]

Hen largest ← L

else largest ← i

end if

if r ⊆ A. heap-size and A[T] > A[largest]

Then largest ← r

end if

then largest ← r

end if

Hen A[T] ← A[largest] (Zamjena)

MAX-HEAPIFY (A, largest)

tipeme izvršavanija:

- sratujerno visini binarnog stabla - O(n)

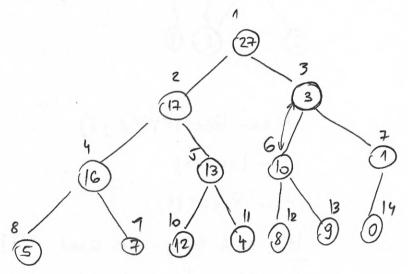
... kako je visina bin. stabla O(lgn)

Zakegningemo da je vrijeme izvršavanja O(lgn)

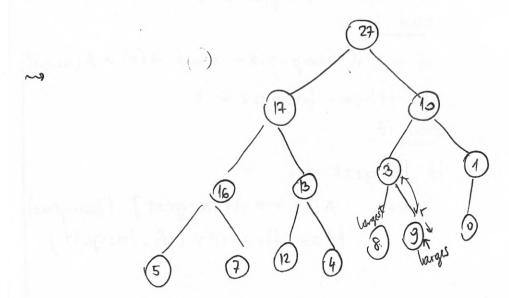
i preko Master metode

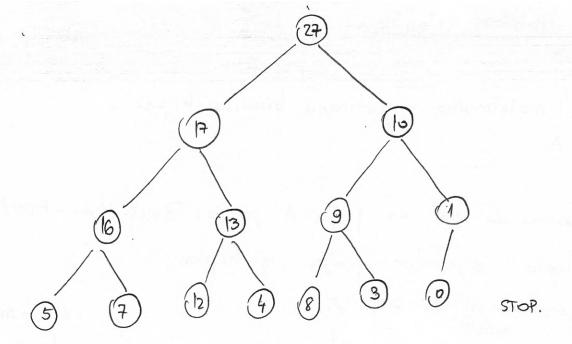
$$T(n) = T(\frac{n}{2}) + \Theta(1)$$
 my $\Theta(\lg n)$

Primjer: A = <27, 17, 3, 16, 13, 10, 1, 5, 7, 12, 4, 8, 9,0>



MAX-HEAPIFY (A13)





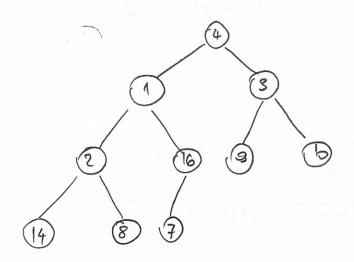
Izgraduja maksimalno orijentinane hrpe

Problem: Pretvoriti polje A[1,-..,n), n=A.length n maksimalno orijentiramu hrpu

*Listori se nalaze u potpolju A[(["/2]+1),...,n]

* Hrpa od n elemenata ima visinu Llgn]

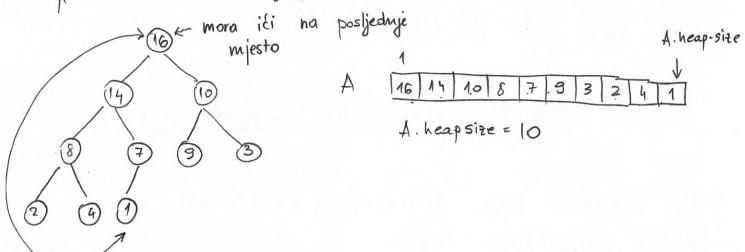
Primjer: A = [4 | 1 | 3 | 2 | 16 | 9 | 10 | 14 | 8 | 7 |

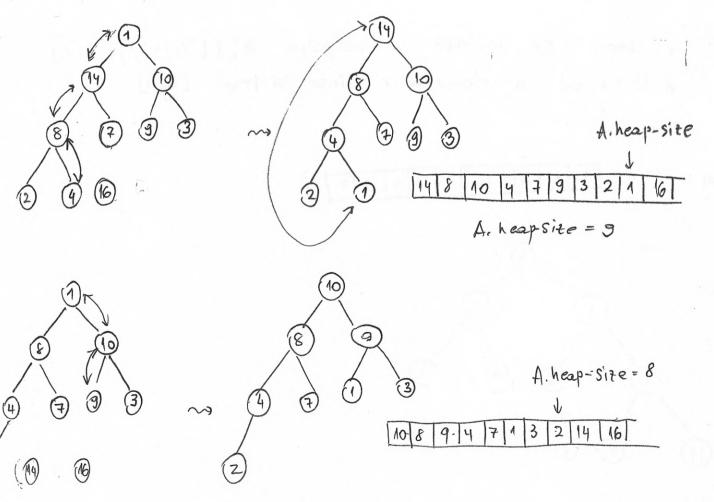


HEAPSORT algoritam

deja:
- izgraditi maksimalno origentiranu binarnu hrpu
12 polja A

rimje: pretpostavimo da smo na posju A pozvali BULD-MAX-HEAP
to je rezultiralo stjedećim posjem, tj. hrpom





nastavljamo sve dok ne ispratnimo hrpu

56

Vrijeme izvršavanja T(n) = O(n) + n. O(lgn) = O(nlgn)

PRIORITETHI REDOVI

najvaznija primjena prioritetnog reda razlikujemo olva tipa:

- * maksimalno origentirani prioritetni red
- * minimalno origentirani prioritetni red

prioritetni real: - red u kojem svaki element ima kyuč

- kynë predstanja prioritet chementa u reslu

maksimalno orijentirani prioritetni red:

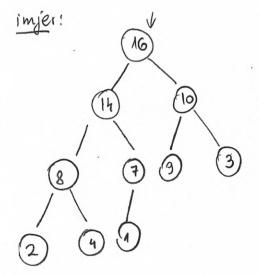
=) element s najvecim kynčem prvi ide van"

minimalno origenticani prioritetni red:

=) element s najmanjim kyntem prvi "ide van"

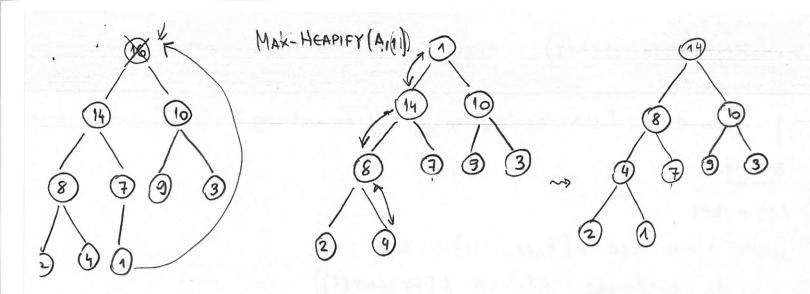
peacije: * MAXIMUM

- * EXTRACT MAX
- + HICREASE-KEY
- * | HSERT



MAXIMUM (S)

return A[1]



EXTRACT-MAX (A) A. heap-size < 1

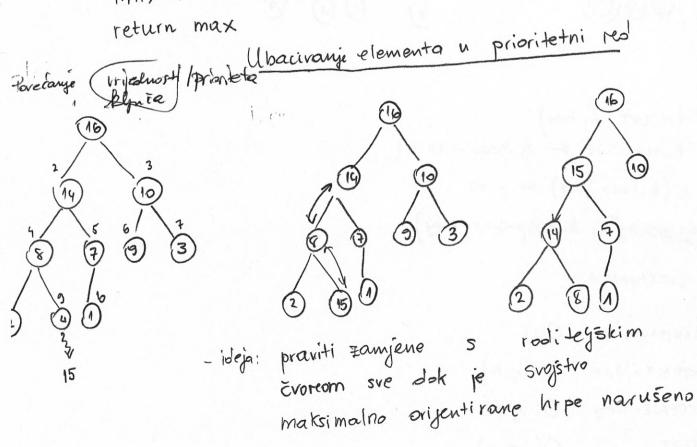
then error "heap underflow" end is

max + A[1]

A[1] A[A. heap-size]

A. heap-size - A. heap-size -1

MAX-HEAPIFY (A,1)



INCREASE-KEY(A, i, key)

if key < A[i]

| then error: "Novi kyut je manji od trenutnog"

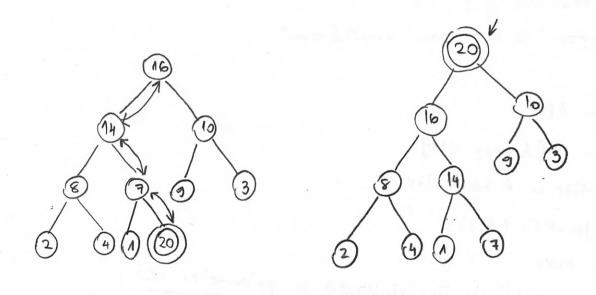
end if

A[i] ← key

while i > 1 and A[PARENT(i)] < A[i)

do exchange A[i] ↔ A[PARENT(i)]

i ← PARENT(i)



| HSERT (A, key)

A. heap-size
A. heap-size + 1

A [A. heap-size]
-
NO

INCREMENTAL A. heap-size, key)

PIJEME PURSAVANIA:

MAXIMUM O(1)

EXTRACT-MAX O(lgn)

INCREASE- Key O(lgn)

INSERT O(lgn)

Primjeri: visualgo.net

Zadatak ti. Neka je A binarna hrpa maksimalnog usujerenja koja koja je inicipalno prazna.

- a) Utinite stjedete operacije nad binarnom hrpom A.
 - 1. INSERT (A120), INSERT (A126), INSERT (A13), INSERT (A15), INSERT (A15), INSERT (A13)

 INSERT (A14), INSERT (A12), INSERT (A17), INSERT (A13)
 - 2. EXTRACT MAX (A), EXTRACT MAX (A)
 - 3. IHCREASE KEY (A4,11), IHCREASE KEY (A,1,31)
- 4. EXTRACT MAX (A)
- b) Objasnite kako možemo sortirati u O(nlgn) vremenu koristeći operacije na binarnoj hrpi.

Rjesenje:

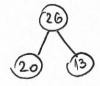
1 HSERT (A120) (20)

| NIERT (A126)

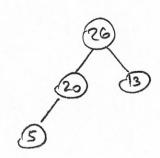




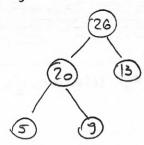
| NJERT (A, 13)



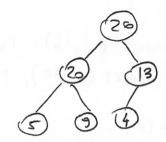
INVERT (A, 5)



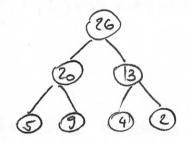
HJERT (A,9)



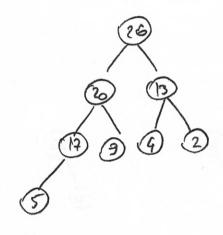
45ERT (A, 4)



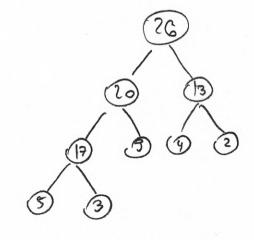
SERT (A,2)



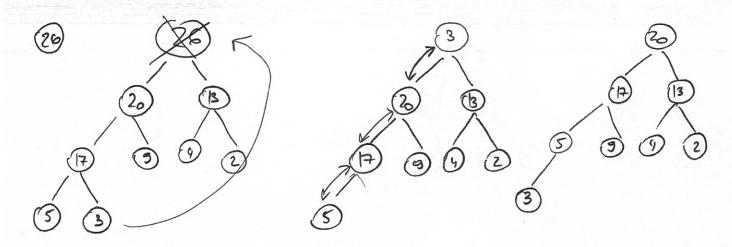
JERT (A, 17) 26 (B) (B) (V) (Z)



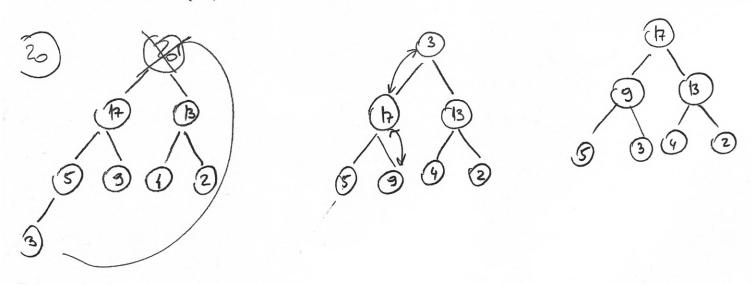
15 ERT (4,3)



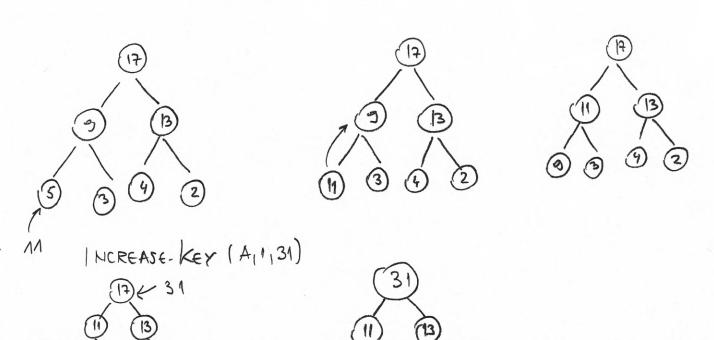
2. EXTRACT-MAX (A)



EXTRACT MAX (A)



3. | NCREASE-KEY (A,4,11)



EXTRACT-MAX (A)

