(9) for the scalar
$$f^n f(u,y,z) = u^2 + 3y^2 + 2z^2$$
 than gradient at point $\rho(1,2,-1)$

$$\Rightarrow \nabla f = \frac{\partial f}{\partial x} \hat{i} + \frac{\partial f}{\partial y} \hat{j} + \frac{\partial f}{\partial z} \hat{k}$$

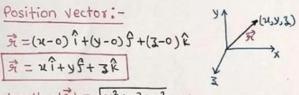
$$\Rightarrow 2x \hat{i} + 6y \hat{j} + 4z \hat{k}$$

$$\nabla f \Big|_{4.2.-1} = 2\hat{i} + 12\hat{j} - 4\hat{k}$$

$$\Rightarrow \nabla \cdot \overrightarrow{F} = \frac{\partial}{\partial x} u^3 y - \frac{\partial}{\partial y} u^2 y^2 + \frac{\partial}{\partial 3} (-u^2 y_3)$$

$$\Rightarrow \nabla \times \vec{f} = \begin{vmatrix} \hat{i} & \hat{f} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial 3} \\ y_3 & x_3 & x_y \end{vmatrix} \Rightarrow 0$$

· Position vector:-



1)
$$\frac{\partial x}{\partial u} = \frac{u}{x}$$
 frost: $\frac{\partial x}{\partial u} = \frac{\partial}{\partial x} \sqrt{u^2 + y^2 + z^2} \Rightarrow \frac{\partial x}{\partial x} = \frac{x}{x}$

$$2 \frac{\partial x}{\partial y} = \frac{y}{x}$$

②
$$\frac{\partial x}{\partial y} = \frac{y}{x}$$

③ $\frac{\partial x}{\partial z} = \frac{z}{x}$
④ $\nabla x \vec{x} = \text{curl } \vec{x} = 0$
③ $\frac{\partial x}{\partial z} = \frac{z}{x}$
④ $\nabla f x = f(x) \nabla x$
④ $\nabla f x = \frac{\vec{x}}{x}$
⑤ $\nabla k \vec{x} = \frac{\vec{x}}{x} = 0$
④ $\nabla f x = f(x) \nabla x$
⇒ $\frac{1}{x} \times \nabla x \Rightarrow \frac{1}{x} \times \frac{\vec{x}}{x} \Rightarrow \frac{\vec{x}}{x^2}$
⑧ Laplace operators

$$\nabla^2 = \nabla \nabla = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial y^2} \Rightarrow \boxed{\nabla^2 f = 0}$$

(9)
$$\varphi^2 f(x) = f''(x) + \frac{2}{x} f'(x)$$

①
$$\nabla \cdot x^n \vec{x} = 0$$
 than, $n = -3$ $\nabla \cdot \frac{\vec{x}}{x^3} = 0$

· Property: -[2 operator together]

① unit surface normal vector
$$(\hat{N}) = \frac{\nabla f}{|\nabla f|}$$

•
$$DD_{mqx} = At \cdot \frac{\Delta t}{\Delta t} = \frac{|\Delta t|}{|\Delta t|} = |\Delta t|$$

$$\Rightarrow \int_{-\infty}^{2} \left[\frac{\chi^{2}}{2} \right] y dy \qquad \Rightarrow 1 \text{ Ans}$$

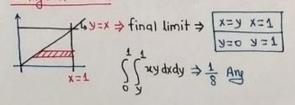
$$\Rightarrow \int_{2}^{2} dy \Rightarrow \left[\frac{y^{2}}{4}\right]^{2} \Rightarrow 1 \text{ Ans} \quad \text{order of integration} \\ \text{doesn't matter.}$$

@ Variable limit:-

(9.)
$$\int_{0}^{1} \int_{0}^{x} uy \, dy \, dx \Rightarrow \text{Initial limit} \Rightarrow \boxed{\begin{array}{c} x = 0 & x = 1 \\ y = 0 & y = x \end{array}}$$

$$\Rightarrow \int_{0}^{1} u \cdot \frac{u^{2}}{3} \, dx$$

change of order :-



"SUMIT KUMAR"