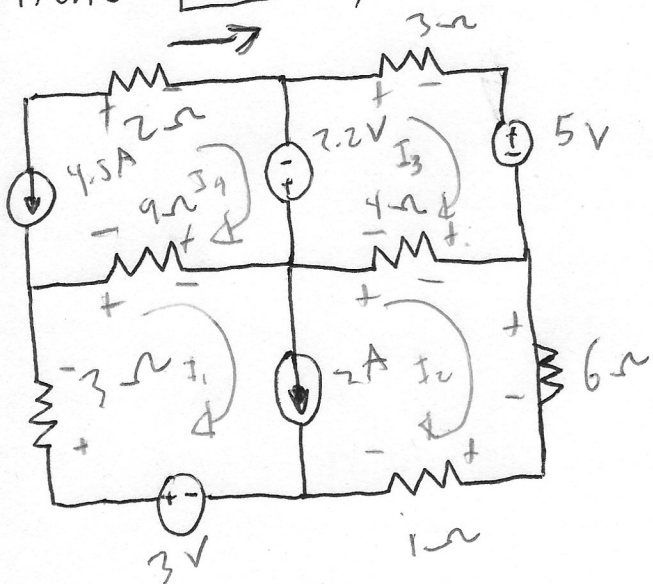


Nota: el signo se tomara negativo si el elemento analizado tiene $\begin{array}{|c|c|} \hline + & - \\ \hline \end{array}$, en caso contrario $\begin{array}{|c|c|} \hline - & + \\ \hline \end{array}$ será Positivo



Para resolver el circuito hacemos uso de supermalla y retiramos la fuente de 2A

Entonces tendríamos que

$$I_1 - I_2 = 2A$$

despejando I_1 ,

$$I_1 = 2A + I_2 \dots \dots \textcircled{3}$$

Para I_1 e I_2

$$-3\Omega \cdot I_1 + 9\Omega \cdot I_4 - 9\Omega I_1 + 4\Omega \cdot I_3 - 4\Omega \cdot I_2 - 6\Omega \cdot I_2 - 1\Omega \cdot I_2 + 3V = 0$$

$$\Rightarrow -12\Omega \cdot I_1 - 11\Omega I_2 + 4\Omega I_3 + 9\Omega I_4 = -3V \dots \textcircled{0}$$

Para I_3

$$-3\Omega \cdot I_3 - 5V + 4\Omega \cdot I_2 - 4\Omega I_3 - 2.2V = 0$$

$$\Rightarrow -7\Omega I_3 + 4\Omega \cdot I_2 = 7.2V \dots \dots \textcircled{1}$$

Para I_4 podemos suponer que $I_4 = -4.5A \dots \dots \textcircled{2}$

ahora sustituyendo $\textcircled{2}$ en $\textcircled{0}$ además $\textcircled{3}$

$$-12\Omega (2A + I_2) - 11\Omega I_2 + 4\Omega I_3 + 9\Omega (-4.5A) = -3V$$

$$-24V - 12\Omega I_2 - 11\Omega I_2 + 4\Omega I_3 - 40.5V = -3V$$

$$\Rightarrow -23\Omega \cdot I_2 + 4\Omega I_3 = 61.5V \dots \dots \textcircled{4}$$

Resolviendo el sistema de 2×2

$$\begin{pmatrix} 4 & -7 \\ -23 & 4 \end{pmatrix} \begin{pmatrix} \frac{36}{5} \\ \frac{123}{2} \end{pmatrix} \left(\frac{1}{4}\right) = \begin{pmatrix} 1 & -\frac{7}{4} \\ -23 & 4 \end{pmatrix} \begin{pmatrix} \frac{9}{5} \\ \frac{123}{2} \end{pmatrix} (23) = \begin{pmatrix} 1 & -\frac{7}{4} \\ 0 & -\frac{145}{4} \end{pmatrix} \begin{pmatrix} \frac{9}{5} \\ \frac{1029}{10} \end{pmatrix}$$

$$\begin{pmatrix} 1 & -\frac{7}{4} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \frac{9}{5} \\ \frac{2058}{725} \end{pmatrix} \left(\frac{7}{4}\right) = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \frac{9813}{1450} \\ \frac{2058}{725} \end{pmatrix}$$

$$\Rightarrow I_2 = 6.7675$$

$$I_3 = 2.8386$$

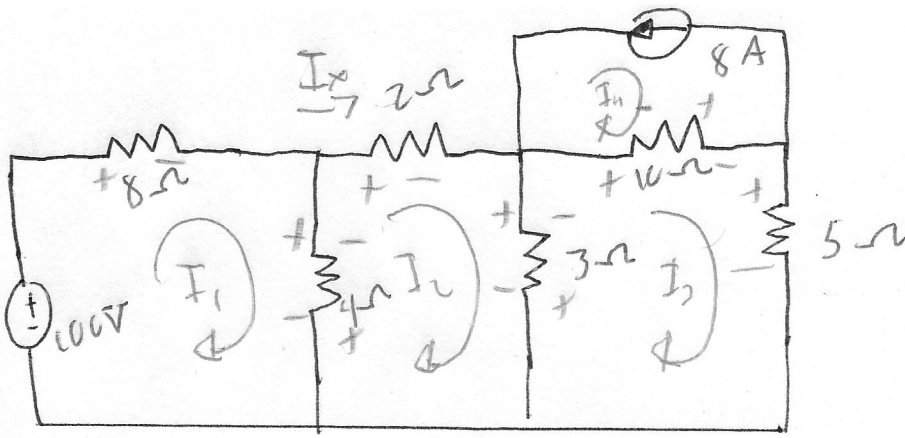
Para determinar la potencia de la fuente de 2.2 V

$$P = (I) \cdot \bar{V}$$

pero $I = I_4 - I_3$

$$P = (4.5 \text{ A} - 2.8386) (2.2 \text{ V})$$

$$P = 3.6550$$



Podemos suponer que $I_4 = -8A$ y $I_x = I_2$

para I_1

$$-8\Omega \cdot I_1 + 4\Omega I_2 - 4\Omega I_1 + 100V = 0$$

$$-12\Omega I_1 + 4\Omega I_2 = -100V \dots\dots (0)$$

para I_2

$$-2\Omega I_2 + 3\Omega I_3 - 3\Omega I_2 + 4\Omega I_1 - 4\Omega I_2 = 0$$

$$4\Omega I_1 - 9\Omega I_2 + 3\Omega I_3 = 0 \dots\dots (1)$$

para I_3

$$3\Omega I_2 - 3\Omega I_3 - 5\Omega I_3 - 10(I_3 + 8) = 0$$

$$3\Omega I_2 - 18\Omega I_3 = -80V \dots\dots (2)$$

Resolviendo el sistema de 3×3

$$\begin{pmatrix} -12 & 4 & 0 & | & -100 \\ 4 & -9 & 3 & | & 0 \\ 0 & 3 & -18 & | & 80 \end{pmatrix} \left(-\frac{1}{12}\right) = \begin{pmatrix} 1 & -\frac{1}{3} & 0 & | & \frac{25}{3} \\ 4 & -9 & 3 & | & 0 \\ 0 & 3 & -18 & | & 80 \end{pmatrix} \left(-4\right) \rightarrow \begin{pmatrix} 1 & -\frac{1}{3} & 0 & | & \frac{25}{3} \\ 0 & -\frac{23}{3} & 3 & | & -\frac{100}{3} \\ 0 & 3 & -18 & | & 80 \end{pmatrix}$$

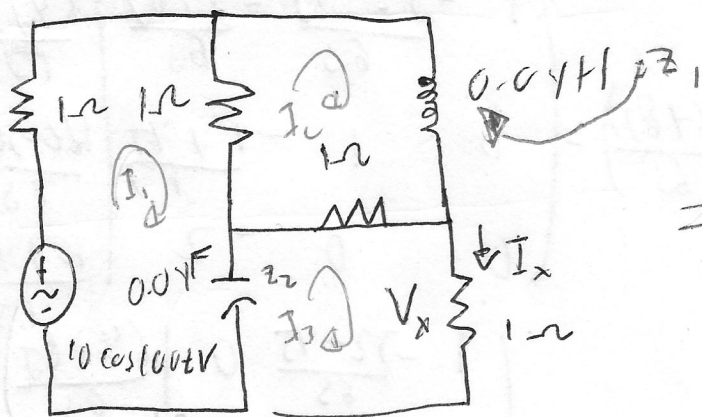
$$\begin{pmatrix} 1 & -\frac{1}{3} & 0 & | & \frac{25}{3} \\ 0 & 1 & -\frac{9}{23} & | & \frac{100}{23} \\ 0 & 3 & -18 & | & 80 \end{pmatrix} \left(-3\right) = \begin{pmatrix} 1 & -\frac{1}{3} & 0 & | & \frac{25}{3} \\ 0 & 1 & -\frac{9}{23} & | & \frac{100}{23} \\ 0 & 0 & -\frac{387}{23} & | & \frac{1540}{23} \end{pmatrix} \left(-\frac{23}{387}\right)$$

$$= \left(\begin{array}{ccc|c} 1 & -\frac{1}{3} & 0 & 25/3 \\ 0 & 1 & -\frac{9}{23} & 100/23 \\ 0 & 0 & 1 & \frac{1540}{387} \end{array} \right) \left(\frac{9}{23} \right) = \left(\begin{array}{ccc|c} 1 & -\frac{1}{3} & 0 & 25/3 \\ 0 & 1 & 0 & 120/23 \\ 0 & 0 & 1 & \frac{1540}{387} \end{array} \right)$$

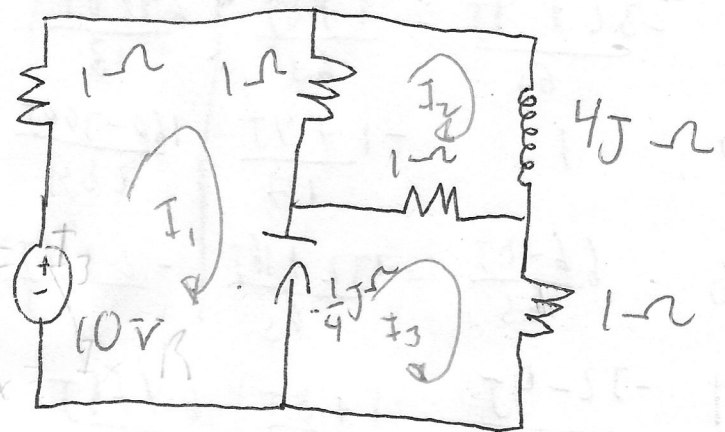
$$\Rightarrow I_2 = 2.7906$$

Como $I_x = I_2$, entonces

$$I_x = 2.7906$$



\Rightarrow



$$Z_1 = 10^2 (0.04 + j1) = 4j \Omega$$

$$I_x = I_3$$

$$Z_2 = -\frac{1}{10^2 (0.04F)} = -\frac{1}{4} j \Omega$$

$$(I_1) -I_1 -I_1 + I_2 + \frac{1}{4} j I_1 - \frac{1}{4} j I_3 + 10 = 0$$

$$\Rightarrow (\frac{1}{4} j - 2) I_1 + I_2 - \frac{1}{4} j I_3 = -10$$

$$(I_2) -4j I_2 - I_2 + I_3 - I_2 + I_1 = 0$$

$$\Rightarrow I_1 + (-7 - 4j) I_2 + I_3 = 0$$

$$(I_3) -I_3 + \frac{1}{4} j I_3 - \frac{1}{4} j I_1 - I_2 + I_2 = 0$$

$$\Rightarrow -\frac{1}{4} j I_1 + I_2 + (\frac{1}{4} j - 2) I_3 = 0$$

$$\begin{pmatrix} \frac{-8+j}{4} & 1 & -\frac{j}{4} & -10 \\ 1 & -2-4j & 1 & 0 \\ -\frac{j}{4} & 1 & \frac{-8+j}{4} & 0 \end{pmatrix} \xrightarrow{(\frac{-2-4j}{6j})} \begin{pmatrix} 1 & \frac{-32-4j}{6j} & \frac{-1+j}{6j} & \frac{64+8j}{6j} \\ 1 & -2-4j & 1 & 0 \\ -\frac{j}{4} & 1 & \frac{-8+j}{4} & 0 \end{pmatrix}$$

$$= \begin{pmatrix} 1 & \frac{-32-4j}{6j} & \frac{-1+j}{6j} & \frac{64+8j}{6j} \\ 0 & \frac{-98-28j}{6j} & \frac{66-8j}{6j} & \frac{-(4-8j)}{6j} \\ -\frac{j}{4} & 1 & \frac{-8+j}{4} & 0 \end{pmatrix} \xrightarrow{(\frac{4}{j})} \begin{pmatrix} 1 & \frac{-32-4j}{6j} & \frac{-1+j}{6j} & \frac{64+8j}{6j} \\ 0 & \frac{-98-28j}{6j} & \frac{66-8j}{6j} & \frac{-64-8j}{6j} \\ 0 & \frac{66-8j}{6j} & \frac{-132+16j}{6j} & \frac{-2+16j}{6j} \end{pmatrix}$$

$$\begin{aligned}
 & \begin{pmatrix} 1 & \frac{-32+4j}{65} & \frac{-1+8j}{65} & \frac{64+8j}{13} \\ 0 & 1 & \frac{-1+4j}{17} & \frac{160-300j}{289} \\ 0 & \frac{66-8j}{65} & \frac{-132+16j}{65} & \frac{-2+16j}{13} \end{pmatrix} \begin{pmatrix} (-66+8j)/65 \\ (-66+8j)/65 \\ (-66+8j)/65 \end{pmatrix} = \begin{pmatrix} 1 & \frac{-32-4j}{65} & \frac{-1+8j}{65} & \frac{64+8j}{13} \\ 0 & 1 & \frac{-1+4j}{17} & \frac{160-300j}{289} \\ 0 & 0 & -2 & \frac{-10+40j}{13} \end{pmatrix} \\
 & \begin{pmatrix} 1 & \frac{-32-4j}{65} & \frac{-1+8j}{65} & \frac{64+8j}{63} \\ 0 & 1 & \frac{-1+4j}{17} & \frac{160-300j}{289} \\ 0 & 0 & 1 & \frac{5-20j}{17} \end{pmatrix} \begin{pmatrix} (1-4j)/17 \\ (1-4j)/17 \\ (1-8j)/65 \end{pmatrix} = \begin{pmatrix} 1 & \frac{-32-4j}{65} & 0 & \frac{64+8j}{65} \\ 0 & 1 & 0 & \frac{5-20j}{17} \\ 0 & 0 & 1 & \frac{5-20j}{17} \end{pmatrix}
 \end{aligned}$$

$$= \begin{pmatrix} 1 & 0 & 0 & 5 \\ 0 & 1 & 0 & \frac{5-20j}{17} \\ 0 & 0 & 1 & \frac{5-20j}{17} \end{pmatrix}$$

$$\Rightarrow I_x = I_y = \frac{5-20j}{17} A = 0.294 - 1.1764j A$$

$$I_x(t) = \frac{5\sqrt{2}}{17} \cos(100t - 75.963^\circ) A$$