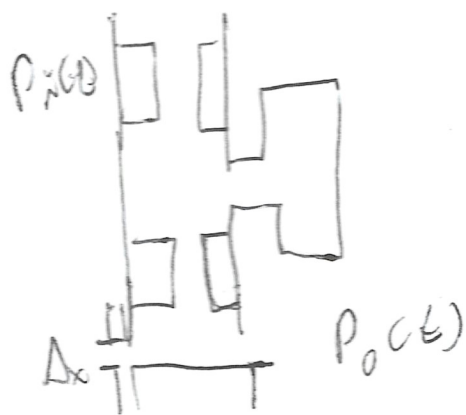


# Problema no 1



Nota:

Problema 3

$$M = 0.5 \text{ Kg}$$

$$R_v = 2.2 \text{ K}$$

$$C = 4.7 \text{ uF}$$



$$V_0(t) = R_f \dot{x}_1(t) + R_v(\dot{x}_1(t) - \dot{x}_2(t)) \dots (1)$$

$$0 = R_v(\dot{x}_2(t) - \dot{x}_1(t)) + \frac{1}{C} \int \dot{x}_2(t) dt \dots (2)$$

$$V_0(t) = \frac{1}{C} \int \dot{x}_2(t) dt \dots (3)$$

Aplicando la transformada de Laplace

$$V_0(s) = R_f I_1(s) + R_v(I_1(s) - I_2(s)) \dots (4)$$

$$0 = R_v I_2(s) - R_v I_1(s) + \frac{1}{sC} I_2(s) \dots (5)$$

$$V_0(s) = \frac{1}{sC} I_2(s) \dots (6)$$

$\uparrow$   
V.S

$\uparrow$   
V.E

Resolviendo variables dependientes

$$V_1(s) = I_1(s)(R_F + R_V) - R_V I_2(s)$$

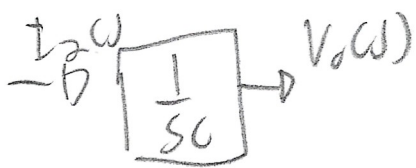
$$V_1(s) + R_V I_2(s) = I_1(s)(R_F + R_V)$$

$$\underbrace{\frac{V_1(s)}{R_F + R_V}}_{V.E} + \underbrace{\frac{R_V}{R_F + R_V} I_2(s)}_{V.E} = \underbrace{I_1(s)}_{V.S} \dots (7)$$

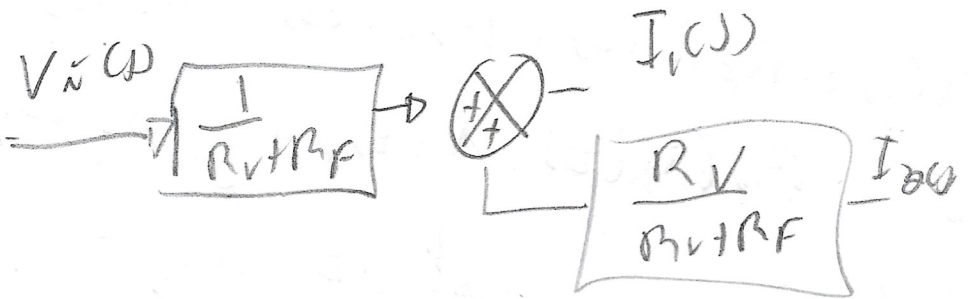
$$R_V I_1(s) = I_2(s)(R_V + \frac{1}{sC}) = I_2(s) \left( \frac{sCR_V + 1}{sC} \right)$$

$$\frac{sCR_V}{sCR_V + 1} I_1(s) = I_2(s) \dots (8)$$

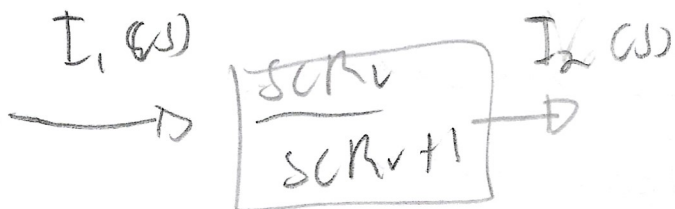
Para (6)



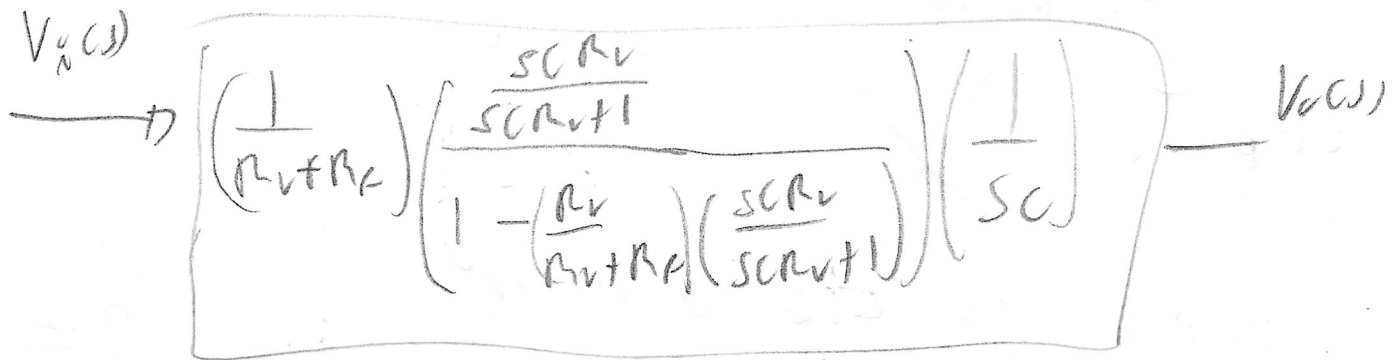
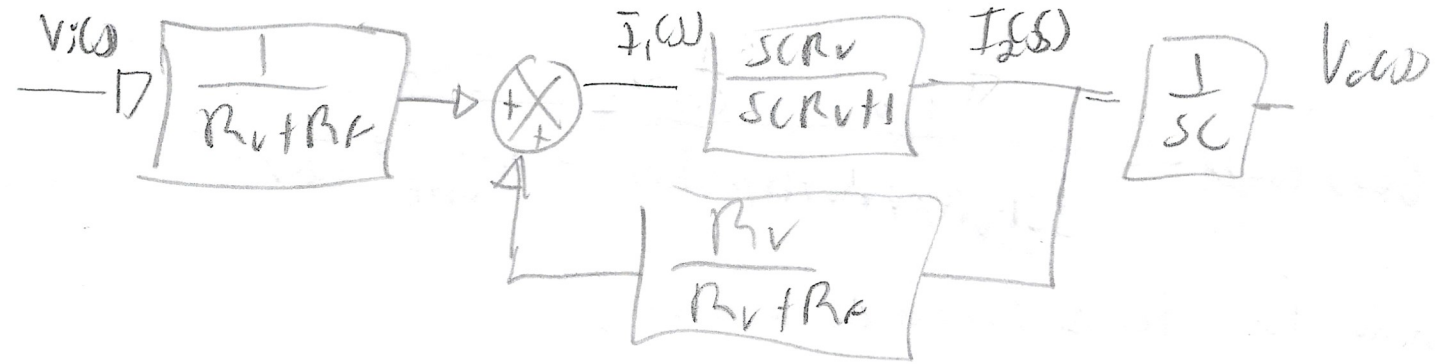
Para (7)



Para (8)



Unimos los diagramas



$$\frac{V_o(s)}{V_i(s)} = \left( \frac{1}{R_v + R_F} \right) \left( \frac{sC R_v \cdot (R_v + R_F) (sC R_v + 1)}{(R_v + R_F)(sC R_v + 1) - sC R_v^2} \right) \frac{1}{sC}$$

$$\frac{V_o(s)}{V_i(s)} = \frac{R_v (R_v + 1)}{sC R_v^2 + R_v + sC R_v R_F + R_F - sC R_v^2}$$

$$\frac{V_o(s)}{V_i(s)} = \frac{R_v}{sC R_v R_F + R_v + R_F}$$

Para una entrada impulso

$$R(s) = 1$$

$$C(s) = G(s) \cdot R(s) = \frac{1}{s + \frac{1}{\tau}} \cdot 1 = \frac{1}{s + \frac{1}{\tau}}$$

Aplicando la transformada inversa

$$c(t) = \frac{1}{\tau} e^{-\frac{t}{\tau}}$$

Para su constante en el tiempo

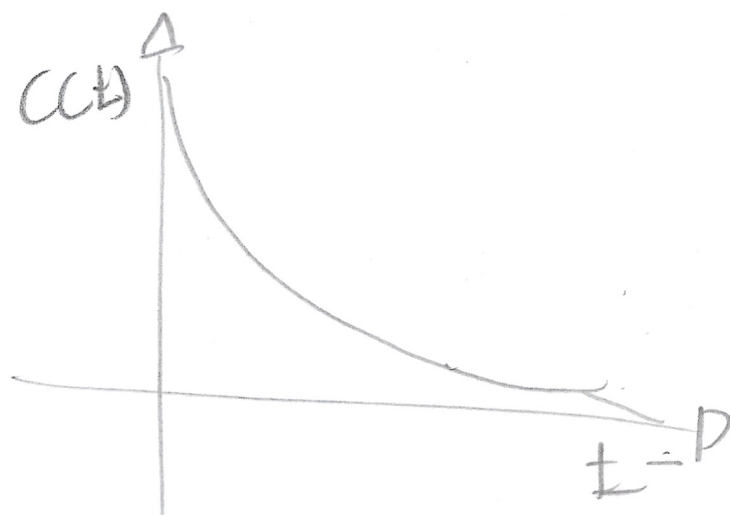
$$\frac{V_o(s)}{V_i(s)} = \frac{R_v}{s C_v R_f + R_v + R_f} \cdot \frac{1}{C_v R_f} = \frac{\frac{1}{C_v R_f}}{s + \frac{1}{C_v R_f} + \frac{1}{C_v R_v}}$$

$$= \frac{\frac{R_f + R_v}{C_v R_v} \left( \frac{R_v}{R_f + R_v} \right)}{s + \frac{R_f + R_v}{C_v R_v}} \Rightarrow \frac{1}{\tau} = \frac{R_f + R_v}{C_v R_v}$$

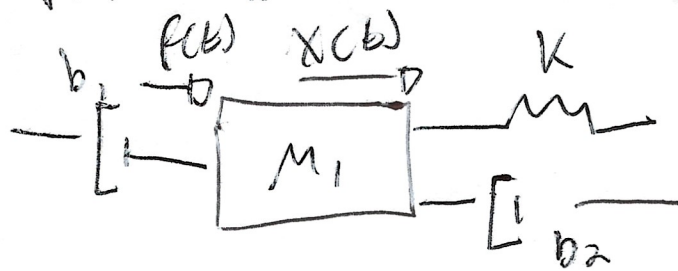
$$\Rightarrow \tau = \frac{C_v R_v R_f}{R_f + R_v} = 0.00323$$

$$c(t) = \left( \frac{1}{0.00323} e^{-\frac{t}{0.00323}} \right) \cdot 5 \cdot (0.3125) \leftarrow \text{Ganancia}$$

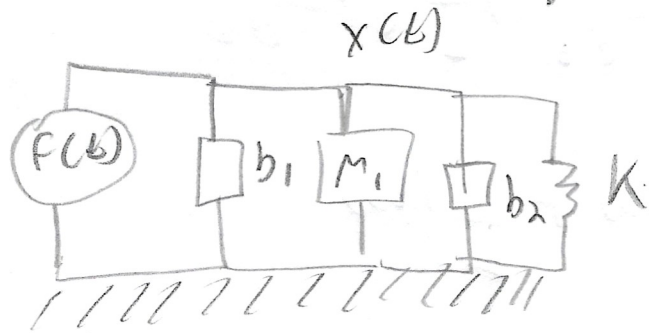
$t$	$C(t)$
0	483.55
$T/2$	<del>293.29</del>
$T$	177.89
$2T$	165.44
$3T$	521.07
$4T$	28.185
$5T$	3.125
$6T$	27.19



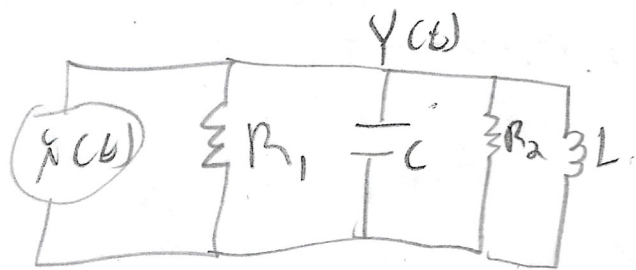
### Problema 3



Establezcamos tierra y conectemos las masas



Sustituimos los componentes con la analogía Fza-corriente



El número de ecuaciones es igual al número de nodos o desplazamientos

$$\dot{x}(t) = \frac{1}{b_1} x(t) + C \dot{x}(t) + \frac{1}{b_2} x(t) + L \ddot{x}(t)$$

Encontramos el valor de las corrientes

$$\dot{x}(t) = \frac{V(t)}{R_1} + C_1 \frac{dV(t)}{dt} + \frac{V(t)}{R_2} + \frac{1}{L} \int V(t) dt$$



Sustituirlo por su definición formal del voltaje

(como el voltaje Fza-corriente

$$V(\omega) = \frac{dY(\omega)}{dt}$$

$$I(\omega) = \frac{1}{R_1} \frac{dY(\omega)}{dt} + C_1 \frac{d^2 Y(\omega)}{dt^2} + \frac{1}{R_2} \frac{dY(\omega)}{dt} + \frac{1}{L} \int \frac{d(Y(\omega))}{dt} dt$$

$$I(\omega) = \frac{s}{R_1} Y(\omega) + s^2 C_1 Y(\omega) + \frac{s}{R_2} Y(\omega) + \frac{1}{L} Y(\omega)$$

$$I(\omega) = Y(\omega) \left( \frac{s}{R_1} + s^2 C_1 + \frac{s}{R_2} + \frac{1}{L} \right)$$

$$= Y(\omega) \left( \frac{sLR_2 + s^2 R_1 R_2 L + sLR_1 + R_1 R_2 L}{R_1 R_2 L} \right)$$

$$\frac{R_1 R_2 L}{s^2 R_1 R_2 L + s(LR_2 + LR_1) + R_1 R_2 L} = \frac{Y(\omega)}{I(\omega)}$$

Para determinar la cte de amortiguamiento

$$\frac{Y(s)}{I(s)} = \frac{R_1 R_2 L}{s^2 R_1 R_2 L + s(L R_2 + L R_1) + R_1 R_2 \frac{1}{L R_1 R_2}}$$

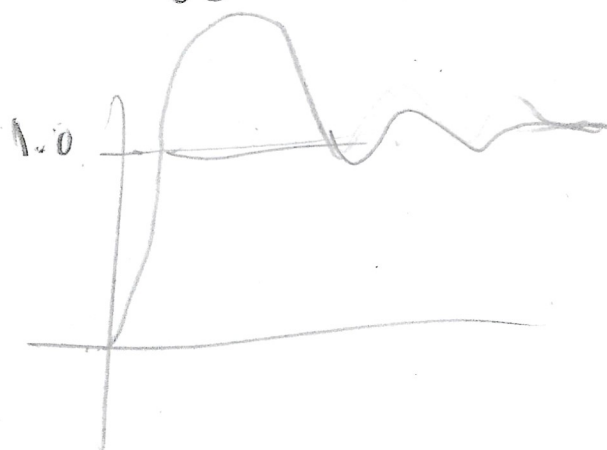
$$\frac{Y(s)}{I(s)} = \frac{4\left(\frac{1}{L}\right)}{s^2 + s\left(\frac{1}{R_1} + \frac{1}{R_2}\right) + \frac{1}{L}}$$

$$\Rightarrow \omega_n^2 = \frac{1}{L} = \sqrt{\frac{1}{L}} = \sqrt{k} = 3.49$$

$$2 \zeta \omega_n = b_1 + b_2$$

$$\zeta = \frac{b_1 + b_2}{2 \omega_n} = \frac{1.2 + 1.7}{2(3.49)} = 0.844$$

$0 < \zeta < 1$



sub amortiguada



Para resolver la ecuación diferencial, utilizando AOP

$$F(s) = s^2 M X(s) + s X(s) (B_1 + B_2) + X(s) K$$

$$F(\omega) = m \frac{d^2 \dot{x}(\omega)}{d\omega} + (b_1 + b_2) \frac{dX(\omega)}{d\omega} + K X(\omega)$$

$$F(\omega) = m \ddot{x} + (b_1 + b_2) \dot{x} + K x$$

$$\ddot{x} = \frac{F(\omega)}{m} + \frac{(b_1 + b_2)}{m} \dot{x} - \frac{K}{m} x$$

