# Fluïdummechanica Grenslagen en turbulentie

#### Brecht Baeten<sup>1</sup>

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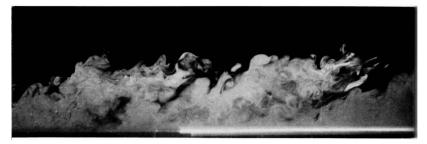
18 oktober 2016

#### Inhoud

1 Inleiding

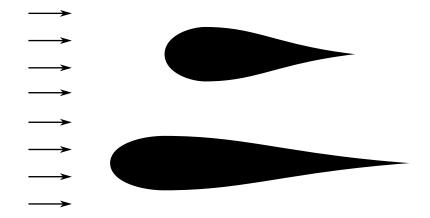
2 Grenslagen

#### Voorbeeld



Bron: An Album of Fluid Motion (Van Dyke)

### Voorbeeld

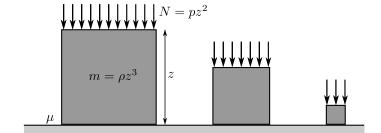


#### Inhoud

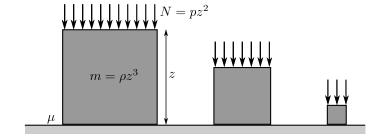
Inleiding

2 Grenslagen

# No-slip randvoorwaarde

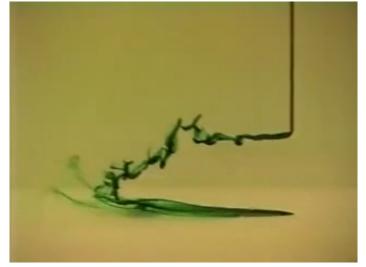


# No-slip randvoorwaarde



$$m\frac{\mathrm{d}v}{\mathrm{d}t} = -\mu N$$

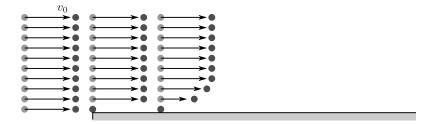
# No-slip randvoorwaarde

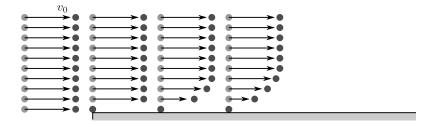


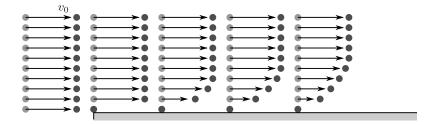
Bron: https://www.youtube.com/watch?v=cUTkqZeiMow

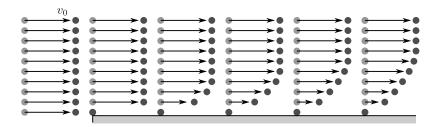


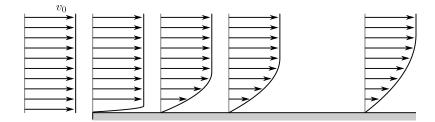


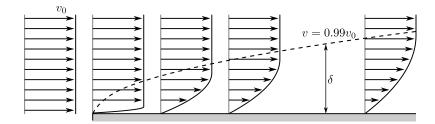


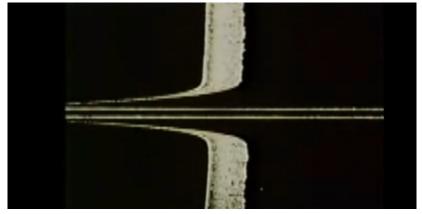












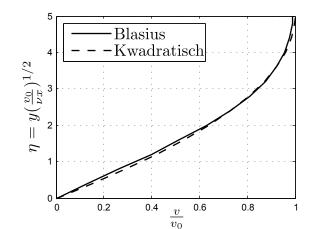
Bron: https://www.youtube.com/watch?v=7SkWxEUXIoM

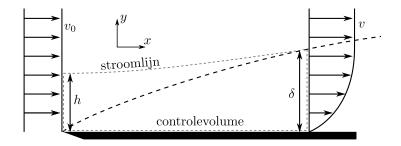
### Snelheidsprofiel

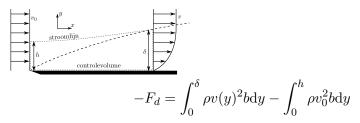
$$v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} = \nu \left( \frac{\partial^2 v_x}{\partial x^2} \right)$$

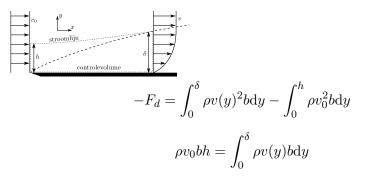
#### **Snelheidsprofiel**

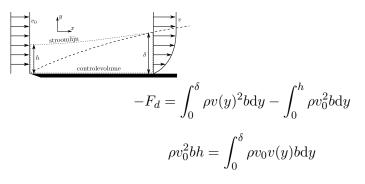
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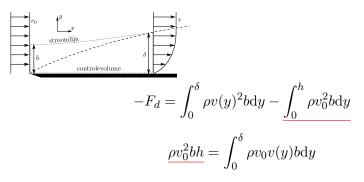


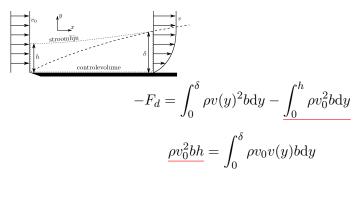










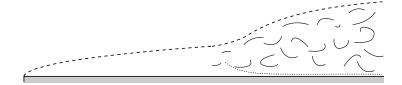


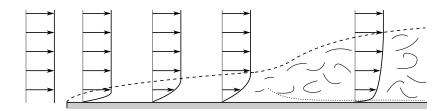
$$F_d = \rho b \int_0^\delta v(y)(v_0 - v(y)) dy$$

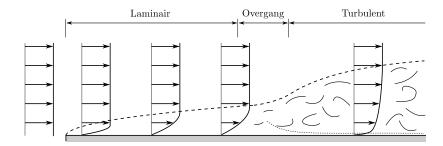
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1 Inleiding

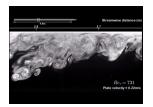
2 Grenslagen



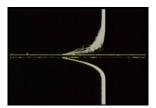












Bron: https://www.youtube.com/watch?v=1\_oyqLOqwnl
Bron: https://www.youtube.com/watch?v=e1TbkLIDWys Bron:
https://www.youtube.com/watch?v=wMxK2GtFFq0

Schijnbaar willekeurig

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- Zeer gevoelig aan begincondities

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- Variatie in tijd en lengte schalen
- 3 dimensionaal

### Laminaire stroming



Bron: https://www.youtube.com/watch?v=p08\_KITKP50

$$\rho \left( \frac{\partial v_x}{\partial t} + v_x \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \right) =$$

$$- \frac{\partial p}{\partial x} + \rho g_x + \mu \left( \frac{\partial^2 v_x}{\partial x^2} + \frac{\partial^2 v_x}{\partial y^2} + \frac{\partial^2 v_x}{\partial z^2} \right)$$

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Stel:

$$v_x = \sin \omega x$$

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$$v_x = \sin \omega x$$

Dan:

$$v_x \frac{\partial v_x}{\partial x} = \omega \sin(\omega x) \cos(\omega x) = \frac{1}{2} \omega \sin(2\omega x)$$

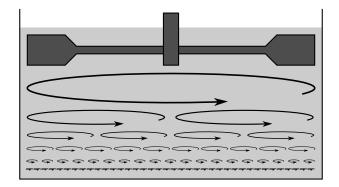
$$\rho \left( \frac{\partial v_x}{\partial t} + \underline{v_x} \frac{\partial v_x}{\partial x} + v_y \frac{\partial v_x}{\partial y} + v_z \frac{\partial v_x}{\partial z} \right) = \frac{\partial p}{\partial x} + \rho g_x + \mu \left( \frac{\partial^2 v_x}{\partial x^2} + \frac{\partial^2 v_x}{\partial y^2} + \frac{\partial^2 v_x}{\partial z^2} \right)$$

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### Turbulentie en het Reynoldsgetal

$$\mathrm{Re} = \frac{vx}{\nu} = \frac{\mathrm{traagheidskracht}}{\mathrm{viskeuze\ krachten}}$$

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Re klein 
$$\Longrightarrow$$
 Laminair

### Turbulentie en het Reynoldsgetal

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Dus

Re klein 
$$\Longrightarrow$$
 Laminair

$$Re groot \Longrightarrow Turbulent$$