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1 Data Structure

1.1 MO with Update [43 lines]

```
//1 indexed
//Complexity:  $O(S \times Q + Q \times \frac{N^2}{S^2})$ 
//S =  $(2 * n^2)^{(1/3)}$ 
const int block_size = 2720; // 4310 for 2e5
const int mx = 1e5 + 5;
struct Query {
    int L, R, T, id;
    Query() {}
    Query(int _L, int _R, int _T, int _id) : L(_L),
        R(_R), T(_T), id(_id) {}
    bool operator<(const Query &x) const {
        if (L / block_size == x.L / block_size) {
            if (R / block_size == x.R / block_size)
                return T < x.T;
            return R / block_size < x.R / block_size;
        }
        return L / block_size < x.L / block_size;
    }
} Q[mx];
struct Update {
    int pos;
    int old, cur;
    Update() {}
    Update(int _p, int _o, int _c) : pos(_p),
        old(_o), cur(_c) {}
} U[mx];
int ans[mx];
inline void add(int id) {}
```

```
inline void remove(int id) {}
inline void update(int id, int L, int R) {}
inline void undo(int id, int L, int R) {}
inline int get() {}
void MO(int nq, int nu) {
    sort(Q + 1, Q + nq + 1);
    int L = 1, R = 0, T = nu;
    for (int i = 1; i <= nq; i++) {
        Query q = Q[i];
        while (T < q.T) update(++T, L, R);
        while (T > q.T) undo(T--, L, R);
        while (L > q.L) add(--L);
        while (R < q.R) add(++R);
        while (L < q.L) remove(L++);
        while (R > q.R) remove(R--);
        ans[q.id] = get();
    }
}

1.2 MO [28 lines]
const int N = 2e5 + 5;
const int Q = 2e5 + 5;
const int SZ = sqrt(N) + 1;
struct qry {
    int l, r, id, blk;
    bool operator<(const qry& p) const {
        return blk == p.blk ? r < p.r : blk < p.blk;
    }
};
qry query[Q];
ll ans[Q];
void add(int id) {}
void remove(int id) {}
ll get() {}
int n, q;
void MO() {
    sort(query, query + q);
    int cur_l = 0, cur_r = -1;
    for (int i = 0; i < q; i++) {
        qry q = query[i];
        while (cur_l > q.l) add(--cur_l);
        while (cur_r < q.r) add(++cur_r);
        while (cur_l < q.l) remove(cur_l++);
        while (cur_r > q.r) remove(cur_r--);
        ans[q.id] = get();
    }
}
/* 0 indexed. */

1.3 Persistent Segment Tree [58 lines]
const int mxn = 1e5 + 5; //CHECK here for every
    problem
int root[mxn], leftchild[25 * mxn],
    rightchild[25 * mxn], value[25 * mxn], a[mxn];
int now = 0, n;

int build(int L, int R) {
    int node = ++now;
```

```

if(L == R){
    return node;
}
int mid = (L+R)>>1;
leftchild[node] = build(L, mid);
rightchild[node] = build(mid+1, R);
//initialize value[node]
return node;
}

int update(int nownode, int L, int R, int val){
    int node = ++now;
    if(L == R){
        //value[node] = value[nownode]+1;
        //update value[node]
        return node;
    }
    int mid = (L+R)>>1;
    leftchild[node] = leftchild[nownode];
    rightchild[node] = rightchild[nownode];

    if(mid <= val){//change condition as required
        leftchild[node] = update(leftchild[nownode],
            L, mid, val);
    }
    else{
        rightchild[node] =
            update(rightchild[nownode], mid+1, R, val);
    }
    //value[node] = value[nownode]+1;
    //update value[node]
    return node;
}

int query(int leftnode, int rightnode, int L, int
    R, int k){
    if(L==R) return L;
    //int leftcnt = value[leftchild[rightnode]]-
        value[leftchild[leftnode]];a
    //change as required
    int mid = (L+R)>>1;
    if(leftcnt >= k){//change condition as required
        return query(leftchild[leftnode],
            leftchild[rightnode], L, mid, k);
    }
    else{
        return query(rightchild[leftnode],
            rightchild[rightnode], mid+1, R, k-leftcnt);
    }
}

void persistentsegtree(){
    root[0] = build(0, mxn);
    for(int i=1; i<=n; i++){
        root[i] = update(root[i-1], 0, mxn, a[i]);
    }
}

```

1.4 SQRT Decomposition [106 lines]

```

struct sqrtDecomposition
{
    static const int sz = 320;//sz = sqrt(N);
    int numberofblocks;

    struct node
    {
        int L, R;
        bool islazy = false;
        ll lazyval=0;
        //extra data needed for different problems

        void ini(int l, int r)
        {
            for(int i=l; i<=r; i++){
                //...initialize as need
            }
            L=l, R=r;
        }

        void semiupdate(int l, int r, ll val){
            if(l>r) return;
            if(islazy){
                for(int i=L; i<=R; i++){
                    //...distribute lazy to everyone
                }
                islazy = 0;
                lazyval = 0;
            }
            for(int i=l; i<=r; i++){
                //...do it manually
            }
        }

        void fullupdate(ll val){
            if(islazy){
                //...only update lazyval
            }
            else{
                for(int i=L; i<=R; i++){
                    //...everyone are not equal, make them
                    equal
                }
                islazy = 1;
                //update lazyval
            }
        }

        void update(int l, int r, ll val){
            if(l<=L && r>=R) fullupdate(val);
            else semiupdate(max(l, L), min(r, R), val);
        }

        ll semiquery(int l, int r){
            if(l>r) return 0;
            if(islazy){
                for(int i=L; i<=R; i++){
                    //...distribute lazy to everyone
                }
                islazy = 0;
                lazyval = 0;
            }
        }
    }
}

```

```

}
ll ret = 0;
for(int i=l; i<=r; i++){
    //...take one by one
}
return ret;
}

ll fullquery(){
    //return stored value;

}

ll query(int l, int r){
    if(l<=L && r>=R) return fullquery();
    else return semiquery(max(l, L), min(r, R));
}

};

vector<node> blocks;

void init(int n){
    numberofblocks = (n+sz-1)/sz;
    int curL = 1, curR = sz;
    blocks.resize(numberofblocks+5);
    for(int i=1; i<=numberofblocks; i++){
        curR = min(n, curR);
        blocks[i].ini(curL, curR);
        curL += sz;
        curR += sz;
    }
}

void update(int l, int r, ll val){
    int left = (l-1)/sz+1;
    int right = (r-1)/sz+1;
    for(int i=left; i<=right; i++){
        blocks[i].update(l, r, val);
    }
}

ll query(int l, int r){
    int left = (l-1)/sz+1;
    int right = (r-1)/sz+1;
    ll ret = 0;
    for(int i=left; i<=right; i++){
        ret += blocks[i].query(l, r);
    }
    return ret;
}

};

```

1.5 Segment Tree [73 lines]

```

/*edit:data,combine,build check datatype*/
template<typename T>
struct SegmentTree {
    #define lc (C << 1)
    #define rc (C << 1 | 1)

```

```
#define M ((L+R)>>1)
struct data {
    T sum;
    data() :sum(0) {};
};
vector<data>st;
vector<bool>isLazy;
vector<T>lazy;
int N;
SegmentTree(int _N) :N(_N) {
    st.resize(4 * N);
    isLazy.resize(4 * N);
    lazy.resize(4 * N);
}
void combine(data& cur, data& l, data& r) {
    cur.sum = l.sum + r.sum;
}
void push(int C, int L, int R) {
    if (!isLazy[C]) return;
    if (L != R) {
        isLazy[lc] = 1;
        isLazy[rc] = 1;
        lazy[lc] += lazy[C];
        lazy[rc] += lazy[C];
    }
    st[C].sum = (R - L + 1) * lazy[C];
    lazy[C] = 0;
    isLazy[C] = false;
}
void build(int C, int L, int R) {
    if (L == R) {
        st[C].sum = 0;
        return;
    }
    build(lc, L, M);
    build(rc, M + 1, R);
    combine(st[C], st[lc], st[rc]);
}
data Query(int i, int j, int C, int L, int R) {
    push(C, L, R);
    if (j < L || i > R || L > R) return data();
    // default val 0/INF
    if (i <= L && R <= j) return st[C];
    data ret;
    data d1 = Query(i, j, lc, L, M);
    data d2 = Query(i, j, rc, M + 1, R);
    combine(ret, d1, d2);
    return ret;
}
void Update(int i, int j, T val, int C, int L,
    int R) {
    push(C, L, R);
    if (j < L || i > R || L > R) return;
    if (i <= L && R <= j) {
        isLazy[C] = 1;
        lazy[C] = val;
        push(C, L, R);
        return;
    }
    Update(i, j, val, lc, L, M);
    Update(i, j, val, rc, M + 1, R);
    combine(st[C], st[lc], st[rc]);
}
T Query(int i, int j) {
    return Query(i, j, 1, 1, N).sum;
}
};
```

1.6 Trie Bit [61 lines]

```
struct Trie {
    struct node {
        int next[2];
        int cnt, fin;
        node() :cnt(0), fin(0) {
            for (int i = 0; i < 2; i++) next[i] = -1;
        }
    };
    vector<node>data;
    Trie() {
        data.push_back(node());
    }
    void key_add(int val) {
        int cur = 0;
        for (int i = 30; i >= 0; i--) {
            int id = (val >> i) & 1;
            if (data[cur].next[id] == -1) {
                data[cur].next[id] = data.size();
                data.push_back(node());
            }
            cur = data[cur].next[id];
            data[cur].cnt++;
        }
        data[cur].fin++;
    }
    int key_search(int val) {
        int cur = 0;
        for (int i = 30; ~i; i--) {
            int id = (val >> i) & 1;
            if (data[cur].next[id] == -1) return 0;
            cur = data[cur].next[id];
        }
        return data[cur].fin;
    }
    void key_delete(int val) {
        int cur = 0;
        for (int i = 30; ~i; i--) {
            int id = (val >> i) & 1;
            cur = data[cur].next[id];
            data[cur].cnt--;
        }
        data[cur].fin--;
    }
    bool key_remove(int val) {

```

```
        if (key_search(val)) return key_delete(val),
            1;
        return 0;
    }
    int maxXor(int x) {
        int cur = 0;
        int ans = 0;
        for (int i = 30; ~i; i--) {
            int b = (x >> i) & 1;
            if (data[cur].next[!b] + 1 &&
                data[data[cur].next[!b]].cnt > 0) {
                ans += (1LL << i);
                cur = data[cur].next[!b];
            }
            else cur = data[cur].next[b];
        }
        return ans;
    }
};
```

2 Dynamic Programming

2.1 Convex Hull Trick [91 lines]

```
struct Hull_Static{
    /*all m need to be decreasing order
    if m is in increasing order then negate the
    m(like,add_line(-m,c)),
    remember in query you have to negate the x also*/
    const ll inf=1000000000000000000;
    int min_or_max; //if min then 0 otherwise 1
    int pointer; /*keep track for the best line for
    previous query,requires all insert first*/
    vector<ll>M,C; //y=m*x+c;
    inline void clear(){
        min_or_max=0; //initially with minimum trick
        pointer=0;
        M.clear();
        C.clear();
    }
    Hull_Static(){clear();}
    Hull_Static(int _min_or_max){
        clear();
        this->min_or_max=_min_or_max;
    }
    bool bad_min(int idx1,int idx2,int idx3){
        return (C[idx3]-C[idx1])*(M[idx1]-M[idx2]) <
            (C[idx2]-C[idx1])*(M[idx1]-M[idx3]);
        return 1.0*(C[idx3]-C[idx1])*(M[idx1]-M[idx2])
            <
            1.0*(C[idx2]-C[idx1])*(M[idx1]-M[idx3]); //for
            overflow
    }
    bool bad_max(int idx1,int idx2,int idx3){
        return (C[idx3]-C[idx1])*(M[idx1]-M[idx2]) >
            (C[idx2]-C[idx1])*(M[idx1]-M[idx3]);
        return 1.0*(C[idx3]-C[idx1])*(M[idx1]-M[idx2])
            >
            1.0*(C[idx2]-C[idx1])*(M[idx1]-M[idx3]); //for
            overflow
    }
};
```

```

}
bool bad(int idx1,int idx2,int idx3){
    if(!min_or_max)return bad_min(idx1,idx2,idx3);
    else return bad_max(idx1,idx2,idx3);
}
void add_line(ll m,ll c){/*add line where m is
    given in decreasing order
//if(M.size())>0 and M.back()==m)return; //same
    gradient,no need to add
above line added from tarango khan,this line cost
    me several wa,but some code got ac with this*/
    M.push_back(m);
    C.push_back(c);
    while(M.size()>=3 and bad((int)M.size()-3,
        (int)M.size()-2,(int)M.size()-1)){
        M.erase(M.end()-2);
        C.erase(C.end()-2);
    }
}
ll getval(ll idx,ll x){
    return M[idx]*x+C[idx];
}
ll getminval(ll x){/*if queries are
    non-decreasing order*/
    while(pointer<(int)M.size()-1 and
        getval(pointer+
            1,x)<getval(pointer,x))pointer++;
    return M[pointer]*x+C[pointer];
}
ll getmaxval(ll x){
    while(pointer<(int)M.size()-1 and
        getval(pointer+
            1,x)>getval(pointer,x))pointer++;
    return M[pointer]*x+C[pointer];
}
ll getminvalternary(ll x){
    ll lo=0,hi=(ll)M.size()-1;
    ll ans=inf; /*change with problem*/
    while(lo<=hi){
        ll mid1=lo+(hi-lo)/3;
        ll mid2=hi-(hi-lo)/3;
        ll val1=getval(mid1,x);
        ll val2=getval(mid2,x);
        if(val1<val2){
            ans=min(ans,val2);
            hi=mid2-1;
        }
        else{
            ans=min(ans,val1);
            lo=mid1+1;
        }
    }
    return ans;
}
ll getmaxvalternary(ll x){
    ll lo=0,hi=(ll)M.size()-1;
    ll ans=-inf; /*change with problem*/
    while(lo<=hi){

```

```

        ll mid1=lo+(hi-lo)/3;
        ll mid2=hi-(hi-lo)/3;
        ll val1=getval(mid1,x);
        ll val2=getval(mid2,x);
        if(val1<val2){
            ans=max(ans,val2);
            lo=mid1+1;
        }
        else{
            ans=max(ans,val1);
            hi=mid2-1;
        }
    }
    return ans;
}
}
2.2 Divide and Conquer DP [26 lines]
ll G,L; ///total group, cell size
ll dp[8001][801],cum[8001];
ll C[8001]; ///value of each cell
inline ll cost(ll l,ll r){
    return(cum[r]-cum[l-1])*(r-l+1);
}
void fn(ll g,ll st,ll ed,ll r1,ll r2){
    if(st>ed)return;
    ll mid=(st+ed)/2,pos=-1;
    dp[mid][g]=inf;
    for(int i=r1;i<=r2;i++){
        ll tcost=cost(i,mid)+dp[i-1][g-1];
        if(tcost<dp[mid][g]){
            dp[mid][g]=tcost,pos=i;
        }
    }
    fn(g,st,mid-1,r1,pos);
    fn(g,mid+1,ed,pos,r2);
}
int main(){
    for(int i=1;i<=L;i++){
        cum[i]=cum[i-1]+C[i];
    }
    for(int i=1;i<=L;i++){
        dp[i][1]=cost(1,i);
    }
    for(int i=2;i<=G;i++)fn(i,1,L,1,L);
}

```

2.3 Knuth Optimization [32 lines]

*/*It is applicable where recurrence is in the form*

$$dp[i][j] = \min_{1 \leq k < j} \{ dp[i][k] + dp[k][j] \} + C[i][j]$$

condition for applicability is:

$$A[i, j-1] \leq A[i, j] \leq A[i+1, j]$$

Where,

$A[i][j]$ - the smallest k that gives optimal answer, like-

$$dp[i][j] = dp[i-1][k] + C[k][j]$$

$C[i][j]$ - given cost function

also applicable if: $C[i][j]$ satisfies the following 2 conditions:

$$C[a][c] + C[b][d] \leq C[a][d] + C[b][c], a \leq b < c \leq d$$

$C[b][c] \leq C[a][d], a \leq b < c \leq d$

*reduces time complexity from $O(n^3)$ to $O(n^2)$ */*

```

for(int s=0;s<=k;s++){//s-length(size) of substring
    for(int l=0;l+s<=k;l++){//l-left point
        int r=l+s;//r-right point
        if(s<2){
            res[l][r]=0; //DP base-nothing to break
            mid[l][r]=1; /*mid is equal to left border*/
            continue;
        }
        int mleft=mid[l][r-1]; /*Knuth's trick: getting
            bounds on m*/
        int mright=mid[l+1][r];
        res[l][r]=inf;
        for(int m=mleft;m<=mright;m++){/*iterating for
            m in the bounds only*/
            int64 tres=res[l][m]+res[m][r]+(x[r]-x[l]);
            if(res[l][r]>tres){//relax current solution
                res[l][r]=tres;
                mid[l][r]=m;
            }
        }
    }
}
int64 answer=res[0][k];

```

2.4 LIS $O(n \log n)$ with full path [17 lines]

```

int num[MX],mem[MX],prev[MX],array[MX],res[MX],
maxlen;
void LIS(int SZ,int num[]){
    CLR(mem),CLR(prev),CLR(array),CLR(res);
    int i,k;
    maxlen=1;
    array[0]=-inf;
    RFOR(i,1,SZ+1) array[i]=inf;
    prev[0]=-1,mem[0]=num[0];
    FOR(i,SZ){
        k=lower_bound(array,array+maxlen+1,num[i])-
            array;
        if(k==1) array[k]=num[i],mem[k]=i,prev[i]=-1;
        else
            array[k]=num[i],mem[k]=i,prev[i]=mem[k-1];
        if(k>maxlen) maxlen=k;
    }
    k=0;
    for(i=mem[maxlen];i!=-1;i=prev[i])res[k++]=
        num[i];
}

```

2.5 SOS DP [18 lines]

//iterative version

```

for(int mask = 0; mask < (1<<N); ++mask){
    dp[mask][-1] = A[mask]; //handle base case
    separately (leaf states)
    for(int i = 0; i < N; ++i){
        if(mask & (1<<i))
            dp[mask][i] = dp[mask][i-1] +
                dp[mask^(1<<i)][i-1];
    }
}

```



```

else
    dp[mask][i] = dp[mask][i-1];
}
F[mask] = dp[mask][N-1];
}
//memory optimized, super easy to code.
for(int i = 0; i < (1<<N); ++i)
    F[i] = A[i];
for(int i = 0; i < N; ++i) for(int mask = 0; mask <
    (1<<N); ++mask){
    if(mask & (1<<i))
        F[mask] += F[mask^(1<<i)];
}

```

3 Flow

3.1 Blossom [58 lines]

```

// Finds Maximum matching in General Graph
// Complexity O(NM)
// mate[i] = j means i is paired with j
// source: https://codeforces.com/blog/entry_
// 92339?#comment-810242
vector<int> Blossom(vector<vector<int>>& graph) {
    //mate contains matched edge.
    int n = graph.size(), timer = -1;
    vector<int> mate(n, -1), label(n), parent(n),
        orig(n), aux(n, -1), q;
    auto lca = [&](int x, int y) {
        for (timer++; ; swap(x, y)) {
            if (x == -1) continue;
            if (aux[x] == timer) return x;
            aux[x] = timer;
            x = (mate[x] == -1 ? -1 :
                orig[parent[mate[x]]]);
        }
    };
    auto blossom = [&](int v, int w, int a) {
        while (orig[v] != a) {
            parent[v] = w; w = mate[v];
            if (label[w] == 1) label[w] = 0,
                q.push_back(w);
            orig[v] = orig[w] = a; v = parent[w];
        }
    };
    auto augment = [&](int v) {
        while (v != -1) {
            int pv = parent[v], nv = mate[pv];
            mate[v] = pv; mate[pv] = v; v = nv;
        }
    };
    auto bfs = [&](int root) {
        fill(label.begin(), label.end(), -1);
        iota(orig.begin(), orig.end(), 0);
        q.clear();
        label[root] = 0; q.push_back(root);
        for (int i = 0; i < (int)q.size(); ++i) {
            int v = q[i];
            for (auto x : graph[v]) {
                if (label[x] == -1) {

```

```

                    label[x] = 1; parent[x] = v;
                    if (mate[x] == -1)
                        return augment(x), 1;
                    label[mate[x]] = 0;
                    q.push_back(mate[x]);
                }
            } else if (label[x] == 0 && orig[v] !=
                orig[x]) {
                int a = lca(orig[v], orig[x]);
                blossom(x, v, a); blossom(v, x, a);
            }
        }
    }
    return 0;
};
// Time halves if you start with (any) maximal
// matching.
for (int i = 0; i < n; i++)
    if (mate[i] == -1)
        bfs(i);
return mate;
}

```

3.2 Dinic [72 lines]

```

/* Complexity: O(V^2 E)
   .Call Dinic with total number of nodes.
   .Nodes start from 0.
   .Capacity is long long data.
   .make graph with create edge(u,v,capacity).
   .Get max flow with maxFlow(src,des).*/
#define eb emplace_back
struct Dinic {
    struct Edge {
        int u, v;
        ll cap, flow = 0;
        Edge() {}
        Edge(int u, int v, ll cap) : u(u), v(v),
            cap(cap) {}
    };
    int N;
    vector<Edge> edge;
    vector<vector<int>> adj;
    vector<int> d, pt;
    Dinic(int N) : N(N), edge(0), adj(N), d(N), pt(N)
        {}
    void addEdge(int u, int v, ll cap) {
        if (u == v) return;
        edge.eb(u, v, cap);
        adj[u].eb(edge.size() - 1);
        edge.eb(v, u, 0);
        adj[v].eb(edge.size() - 1);
    }
    bool bfs(int s, int t) {
        queue<int> q({ s });
        fill(d.begin(), d.end(), N + 1);
        d[s] = 0;
        while (!q.empty()) {
            int u = q.front(); q.pop();
            if (u == t) break;

```

```

            for (int k : adj[u]) {
                Edge& e = edge[k];
                if (e.flow < e.cap && d[e.v] > d[e.u] + 1) {
                    d[e.v] = d[e.u] + 1;
                    q.emplace(e.v);
                }
            }
        }
        return d[t] != N + 1;
    }
    ll dfs(int u, int T, ll flow = -1) {
        if (u == T || flow == 0) return flow;
        for (int& i = pt[u]; i < adj[u].size(); i++) {
            Edge& e = edge[adj[u][i]];
            Edge& oe = edge[adj[u][i] ^ 1];
            if (d[e.v] == d[e.u] + 1) {
                ll amt = e.cap - e.flow;
                if (flow != -1 && amt > flow) amt = flow;
                if (ll pushed = dfs(e.v, T, amt)) {
                    e.flow += pushed;
                    oe.flow -= pushed;
                    return pushed;
                }
            }
        }
        return 0;
    }
    ll maxFlow(int s, int t) {
        ll total = 0;
        while (bfs(s, t)) {
            fill(pt.begin(), pt.end(), 0);
            while (ll flow = dfs(s, t)) {
                total += flow;
            }
        }
        return total;
    }
};

```

3.3 Flow [6 lines]

Covering Problems:

- > Maximum Independent Set(Bipartite): Largest set of nodes which do not have any edge between them. sol: $V - (\text{MaxMatching})$
- > Minimum Vertex Cover(Bipartite): -Smallest set of nodes to cover all the edges -sol: MaxMatching
- > Minimum Edge Cover(General graph): -Smallest set of edges to cover all the nodes -sol: $V - (\text{MaxMatching})$ (if edge cover exists, does not exit for isolated nodes)
- > Minimum Path Cover(Vertex disjoint) DAG:
 - Minimum number of vertex disjoint paths that visit all the nodes -sol: make a bipartite graph using same nodes in two sides, one side is "from" other is "to", add edges from "from" to "to", then ans is $V - (\text{MaxMatching})$

> Minimum Path Cover(Vertex Not Disjoint) General graph: -Minimum number of paths that visit all the nodes -sol: consider cycles as nodes then it will become a path cover problem with vertex disjoint on DAG

3.4 HopcroftKarp [67 lines]

```
/* Finds Maximum Matching In a bipartite graph
.Complexity  $O(E\sqrt{V})$ 
.1-indexed
.No default constructor
.add single edge for (u, v)*/
struct HK {
    static const int inf = 1e9;
    int n;
    vector<int> matchL, matchR, dist;
    // matchL contains value of matched node for L part.
    vector<vector<int>> adj;
    HK(int n) : n(n), matchL(n + 1), matchR(n + 1), dist(n + 1) {}

    void addEdge(int u, int v) {
        adj[u].push_back(v);
    }

    bool bfs() {
        queue<int> q;
        for (int u = 1; u <= n; u++) {
            if (!matchL[u]) {
                dist[u] = 0;
                q.push(u);
            }
            else dist[u] = inf;
        }
        dist[0] = inf; // unmatched node matches with 0.
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (auto v : adj[u]) {
                if (dist[matchR[v]] == inf) {
                    dist[matchR[v]] = dist[u] + 1;
                    q.push(matchR[v]);
                }
            }
        }
        return dist[0] != inf;
    }

    bool dfs(int u) {
        if (!u) return true;
        for (auto v : adj[u]) {
            if (dist[matchR[v]] == dist[u] + 1 && dfs(matchR[v])) {
                matchL[u] = v;
                matchR[v] = u;
                return true;
            }
        }
    }
};
```

```
    }
}
dist[u] = inf;
return false;
}
int max_match() {
    int matching = 0;
    while (bfs()) {
        for (int u = 1; u <= n; u++) {
            if (!matchL[u])
                if (dfs(u))
                    matching++;
        }
    }
    return matching;
}
};
```

3.5 Hungarian [116 lines]

```
/* Complexity:  $O(n^3)$  but optimized
It finds minimum cost maximum matching.
For finding maximum cost maximum matching
add -cost and return -matching()
1-indexed */
struct Hungarian {
    long long c[N][N], fx[N], fy[N], d[N];
    int l[N], r[N], arg[N], trace[N];
    queue<int> q;
    int start, finish, n;
    const long long inf = 1e18;
    Hungarian() {}
    Hungarian(int n1, int n2) : n(max(n1, n2)) {}
    for (int i = 1; i <= n; ++i) {
        fy[i] = l[i] = r[i] = 0;
        for (int j = 1; j <= n; ++j) c[i][j] = inf;
    }
    void add_edge(int u, int v, long long cost) {
        c[u][v] = min(c[u][v], cost);
    }
    inline long long getC(int u, int v) {
        return c[u][v] - fx[u] - fy[v];
    }
    void initBFS() {
        while (!q.empty()) q.pop();
        q.push(start);
        for (int i = 0; i <= n; ++i) trace[i] = 0;
        for (int v = 1; v <= n; ++v) {
            d[v] = getC(start, v);
            arg[v] = start;
        }
        finish = 0;
    }
    void findAugPath() {
        while (!q.empty()) {
            int u = q.front();
            q.pop();
        }
    }
};
```

```
for (int v = 1; v <= n; ++v) if (!trace[v]) {
    long long w = getC(u, v);
    if (!w) {
        trace[v] = u;
        if (!r[v]) {
            finish = v;
            return;
        }
        q.push(r[v]);
    }
    if (d[v] > w) {
        d[v] = w;
        arg[v] = u;
    }
}
}
}
void subX_addY() {
    long long delta = inf;
    for (int v = 1; v <= n; ++v) if (trace[v] == 0 && d[v] < delta) {
        delta = d[v];
    }
    // Rotate
    fx[start] += delta;
    for (int v = 1; v <= n; ++v) if (trace[v]) {
        int u = r[v];
        fy[v] -= delta;
        fx[u] += delta;
    }
    else d[v] -= delta;
    for (int v = 1; v <= n; ++v) if (!trace[v] && !d[v]) {
        trace[v] = arg[v];
        if (!r[v]) {
            finish = v;
            return;
        }
        q.push(r[v]);
    }
}
void Enlarge() {
    do {
        int u = trace[finish];
        int nxt = l[u];
        l[u] = finish;
        r[finish] = u;
        finish = nxt;
    } while (finish);
}
long long maximum_matching() {
    for (int u = 1; u <= n; ++u) {
        fx[u] = c[u][1];
        for (int v = 1; v <= n; ++v) {
            fx[u] = min(fx[u], c[u][v]);
        }
    }
}
```

```

}
for (int v = 1; v <= n; ++v) {
    fy[v] = c[1][v] - fx[1];
    for (int u = 1; u <= n; ++u) {
        fy[v] = min(fy[v], c[u][v] - fx[u]);
    }
}
for (int u = 1; u <= n; ++u) {
    start = u;
    initBFS();
    while (!finish) {
        findAugPath();
        if (!finish) subX_addY();
    }
    Enlarge();
}
long long ans = 0;
for (int i = 1; i <= n; ++i) {
    if (c[i][1][i] != inf) ans += c[i][1][i];
    else l[i] = 0;
}
return ans;
}
};

```

3.6 MCMF [116 lines]

*/*Credit: ShahjalalShohag*

.Works for both directed, undirected and with negative cost too

.doesn't work for negative cycles

.for undirected edges just make the directed flag false

*.Complexity: $O(\min(E^2 * V \log V, E \log V * flow))$ */*

```

using T = long long;
const T inf = 1LL << 61;
struct MCMF {
    struct edge {
        int u, v;
        T cap, cost;
        int id;
        edge(int _u, int _v, T _cap, T _cost, int _id) {
            u = _u;
            v = _v;
            cap = _cap;
            cost = _cost;
            id = _id;
        }
    };
    int n, s, t, mxid;
    T flow, cost;
    vector<vector<int>> g;
    vector<edge> e;
    vector<T> d, potential, flow_through;
    vector<int> par;
    bool neg;
    MCMF() {}
    MCMF(int _n) { // 0-based indexing

```

```

        n = _n + 10;
        g.assign(n, vector<int>());
        neg = false;
        mxid = 0;
    }
    void add_edge(int u, int v, T cap, T cost, int id = -1, bool directed = true) {
        if (cost < 0) neg = true;
        g[u].push_back(e.size());
        e.push_back(edge(u, v, cap, cost, id));
        g[v].push_back(e.size());
        e.push_back(edge(v, u, 0, -cost, -1));
        mxid = max(mxid, id);
        if (!directed) add_edge(v, u, cap, cost, -1, true);
    }
    bool dijkstra() {
        par.assign(n, -1);
        d.assign(n, inf);
        priority_queue<pair<T, T>, vector<pair<T, T>>, greater<pair<T, T>>> q;
        d[s] = 0;
        q.push(pair<T, T>(0, s));
        while (!q.empty()) {
            int u = q.top().second;
            T nw = q.top().first;
            q.pop();
            if (nw != d[u]) continue;
            for (int i = 0; i < (int)g[u].size(); i++) {
                int id = g[u][i];
                int v = e[id].v;
                T cap = e[id].cap;
                T w = e[id].cost + potential[u] - potential[v];
                if (d[u] + w < d[v] && cap > 0) {
                    d[v] = d[u] + w;
                    par[v] = id;
                    q.push(pair<T, T>(d[v], v));
                }
            }
        }
        for (int i = 0; i < n; i++) { // update potential
            if (d[i] < inf) potential[i] += d[i];
        }
        return d[t] != inf;
    }
    T send_flow(int v, T cur) {
        if (par[v] == -1) return cur;
        int id = par[v];
        int u = e[id].u;
        T w = e[id].cost;
        T f = send_flow(u, min(cur, e[id].cap));
        cost += f * w;
        e[id].cap -= f;
        e[id ^ 1].cap += f;
        return f;
    }
}

```

```

//returns {maxflow, mincost}
pair<T, T> solve(int _s, int _t, T goal = inf) {
    s = _s;
    t = _t;
    flow = 0, cost = 0;
    potential.assign(n, 0);
    if (neg) {
        // run Bellman-Ford to find starting potential
        d.assign(n, inf);
        for (int i = 0, relax = true; i < n && relax; i++) {
            for (int u = 0; u < n; u++) {
                for (int k = 0; k < (int)g[u].size(); k++) {
                    int id = g[u][k];
                    int v = e[id].v;
                    T cap = e[id].cap, w = e[id].cost;
                    if (d[v] > d[u] + w && cap > 0) {
                        d[v] = d[u] + w;
                        relax = true;
                    }
                }
            }
        }
        for (int i = 0; i < n; i++) if (d[i] < inf) potential[i] = d[i];
    }
    while (flow < goal && dijkstra()) flow += send_flow(t, goal - flow);
    flow_through.assign(mxid + 10, 0);
    for (int u = 0; u < n; u++) {
        for (auto v : g[u]) {
            if (e[v].id >= 0) flow_through[e[v].id] = e[v ^ 1].cap;
        }
    }
    return make_pair(flow, cost);
}
};

```

4 Game Theory

4.1 Points to be noted [14 lines]

```

>[First Write a Brute Force solution]
>Nim = all xor
>Misere Nim = Nim + corner case: if all piles are 1, reverse(nim)
>Bogus Nim = Nim
>Staircase Nim = Odd indexed pile Nim (Even indexed pile doesn't matter, as one player can give bogus moves to drop all even piles to ground)
>Sprague Grundy: [Every impartial game under the normal play convention is equivalent to a one-heap game of nim]

```

Every tree = one nim pile = tree root value; tree leaf value = 0; tree node value = mex of all child nodes.

[Careful: one tree node can become multiple new tree roots (multiple elements in one node), then the value of that node = xor of all those root values]

>Hackenbush (Given a rooted tree; cut an edge in one move; subtree under that edge gets removed; last player to cut wins):

Colon: $//G(u) = (G(v_1) + 1) \oplus (G(v_2) + 1) \oplus \dots [v_1, v_2, \dots \text{ are childs of } u]$

For multiple trees ans is their xor

>Hackenbush on graph (instead of tree given an rooted graph):

fusion: All edges in a cycle can be fused to get a tree structure; build a super node, connect some single nodes with that super node, number of single nodes is the number of edges in the cycle.

Sol: [Bridge component tree] mark all bridges, a group of edges that are not bridges, becomes one component and contributes number of edges to the hackenbush. (even number of edges contributes 0, odd number of edges contributes 1)

5 Geometry

5.1 Rotation Matrix [39 lines]

```
struct { double x; double y; double z; } Point;
double rMat[4][4];
double inMat[4][1] = {0.0, 0.0, 0.0, 0.0};
double outMat[4][1] = {0.0, 0.0, 0.0, 0.0};
void mulMat() {
    for(int i = 0; i < 4; i++) {
        for(int j = 0; j < 1; j++) {
            outMat[i][j] = 0;
            for(int k = 0; k < 4; k++)
                outMat[i][j] += rMat[i][k] * inMat[k][j];
        }
    }
}
void setMat(double ang, double u, double v, double w) {
    double L = (u * u + v * v + w * w);
    ang = ang * PI / 180.0; /*converting to radian value*/
    double u2 = u*u; double v2 = v*v; double w2 = w*w;
    rMat[0][0] = (u2 + (v2 + w2) * cos(ang)) / L;
    rMat[0][1] = (u*v*(1-cos(ang)) - w*sqrt(L)*sin(ang)) / L;
    rMat[0][2] = (u*w*(1-cos(ang)) + v*sqrt(L)*sin(ang)) / L;
    rMat[0][3] = 0.0;
    rMat[1][0] = (u*v*(1-cos(ang)) + w*sqrt(L)*sin(ang)) / L;
    rMat[1][1] = (v2 + (u2 + w2) * cos(ang)) / L;
```

```
rMat[1][2] = (v*w*(1-cos(ang)) - u*sqrt(L)*sin(ang)) / L;
rMat[1][3] = 0.0;
rMat[2][0] = (u*w*(1-cos(ang)) - v*sqrt(L)*sin(ang)) / L;
rMat[2][1] = (v*w*(1-cos(ang)) + u*sqrt(L)*sin(ang)) / L;
rMat[2][2] = (w2 + (u2 + v2) * cos(ang)) / L;
rMat[2][3] = 0.0; rMat[3][0] = 0.0; rMat[3][1] = 0.0;
rMat[3][2] = 0.0; rMat[3][3] = 1.0;
}
/*double ang;
double u, v, w; //points = the point to be rotated
Point point, rotated; //u,v,w=unit vector of line
inMat[0][0] = points.x; inMat[1][0] = points.y;
inMat[2][0] = points.z; inMat[3][0] = 1.0;
setMat(ang, u, v, w); mulMat();
rotated.x = outMat[0][0]; rotated.y = outMat[1][0];
rotated.z = outMat[2][0];*/
```

6 Graph

6.1 2SAT [92 lines]

```
struct TwoSat {
    vector<bool> vis;
    vector<vector<int>> adj, radj;
    vector<int> dfs_t, ord, par;
    int n, intime; //For n node there will be 2*n node in SAT.
    void init(int N) {
        n = N;
        intime = 0;
        vis.assign(N * 2 + 1, false);
        adj.assign(N * 2 + 1, vector<int>());
        radj.assign(N * 2 + 1, vector<int>());
        dfs_t.resize(N * 2 + 1);
        ord.resize(N * 2 + 1);
        par.resize(N * 2 + 1);
    }
    inline int neg(int x) {
        return x <= n ? x + n : x - n;
    }
    inline void add_implication(int a, int b) {
        if (a < 0) a = n - a;
        if (b < 0) b = n - b;
        adj[a].push_back(b);
        radj[b].push_back(a);
    }
    inline void add_or(int a, int b) {
        add_implication(-a, b);
        add_implication(-b, a);
    }
    inline void add_xor(int a, int b) {
        add_or(a, b);
        add_or(-a, -b);
    }
}
```

```
inline void add_and(int a, int b) {
    add_or(a, b);
    add_or(a, -b);
    add_or(-a, b);
}
inline void force_true(int x) {
    if (x < 0) x = n - x;
    add_implication(neg(x), x);
}
inline void add_xnor(int a, int b) {
    add_or(a, -b);
    add_or(-a, b);
}
inline void add_nand(int a, int b) {
    add_or(-a, -b);
}
inline void add_nor(int a, int b) {
    add_and(-a, -b);
}
inline void force_false(int x) {
    if (x < 0) x = n - x;
    add_implication(x, neg(x));
}
inline void topsort(int u) {
    vis[u] = 1;
    for (int v : radj[u]) if (!vis[v]) topsort(v);
    dfs_t[u] = ++intime;
}
inline void dfs(int u, int p) {
    par[u] = p, vis[u] = 1;
    for (int v : adj[u]) if (!vis[v]) dfs(v, p);
}
void build() {
    int i, x;
    for (i = n * 2, intime = 0; i >= 1; i--) {
        if (!vis[i]) topsort(i);
        ord[dfs_t[i]] = i;
    }
    vis.assign(n * 2 + 1, 0);
    for (i = n * 2; i > 0; i--) {
        x = ord[i];
        if (!vis[x]) dfs(x, x);
    }
}
bool satisfy(vector<int> &ret) //ret contains the value that are true if the graph is satisfiable.
{
    build();
    vis.assign(n * 2 + 1, 0);
    for (int i = 1; i <= n * 2; i++) {
        int x = ord[i];
        if (par[x] == par[neg(x)]) return 0;
        if (!vis[par[x]]) {
            vis[par[x]] = 1;
            vis[par[neg(x)]] = 0;
        }
    }
}
```



```

    }
}
for (int i = 1; i <= n; i++) if (vis[par[i]])
ret.push_back(i);
return 1;
}
};

6.2 BellmanFord [57 lines]
#include <bits/stdc++.h>
using namespace std;
const int mx = 1e5+6;
const int INF = 0x3f3f3f3f;
struct edge{
    int u,v;
    int cost;
};
vector<edge>e;
vector<int>path(mx);
int dist[mx];
/*
    Time-complexity:  $O(|V|*|E|)$ 
    Space-complexity:  $O(|V|)$ 
    To find any negative cycle assign  $dist[i] = 0$ 
    for all.
    We can use floyd-warshall algorithm to find
    negative cycle too.
    *Handle LL carefully.
    */
void bellmanford(int s,int n){
    int m = e.size();
    memset(dist,0x3f3f3f3f,sizeof dist);
    dist[s] = 0;
    int x;
    for (int i = 0; i < n; ++i) {
        x = -1;
        for (int j = 0; j < m; ++j)
            if (dist[e[j].u] < INF)
                if (dist[e[j].v] > dist[e[j].u] +
                    e[j].cost) {
                    dist[e[j].v] = max(-INF, dist[e[j].u] +
                        e[j].cost);
                    path[e[j].v] = e[j].u;
                    x = e[j].v;
                }
    }

    if (x == -1)
        cout << "No negative cycle from " << s;
    else {
        int y = x;
        for (int i = 0; i < n; ++i)
            y = path[y];

        vector<int> path;
        for (int cur = y; ; cur = path[cur]) {
            path.push_back(cur);
            if (cur == y && path.size() > 1)
                break;
        }
    }
}

```

```

    }
reverse(path.begin(), path.end());

    cout << "Negative cycle: ";
    for (size_t i = 0; i < path.size(); ++i)
        cout << path[i] << ' ';
    }
}

int main(){
}

6.3 BridgeTree [66 lines]
int N, M, timer, compid;
vector<pair<int, int>> g[mx];
bool used[mx], isBridge[mx];
int comp[mx], tin[mx], minAncestor[mx];
vector<int> Tree[mx]; // Store 2-edge-connected
                        component tree. (Bridge tree).
void markBridge(int v, int p) {
    tin[v] = minAncestor[v] = ++timer;
    used[v] = 1;
    for (auto& e : g[v]) {
        int to, id;
        tie(to, id) = e;
        if (to == p) continue;
        if (used[to]) minAncestor[v] =
            min(minAncestor[v], tin[to]);
        else {
            markBridge(to, v);
            minAncestor[v] = min(minAncestor[v],
                minAncestor[to]);
            if (minAncestor[to] > tin[v]) isBridge[id]
                = true;
            // if (tin[u] <= minAncestor[v]) ap[u] = 1;
        }
    }
}

void markComp(int v, int p) {
    used[v] = 1;
    comp[v] = compid;
    for (auto& e : g[v]) {
        int to, id;
        tie(to, id) = e;
        if (isBridge[id]) continue;
        if (used[to]) continue;
        markComp(to, v);
    }
}

vector<pair<int, int>> edges;
void addEdge(int from, int to, int id) {
    g[from].push_back({ to, id });
    g[to].push_back({ from, id });
    edges[id] = { from, to };
}

void initB() {
    for (int i = 0; i <= compid; ++i)
        Tree[i].clear();
    for (int i = 1; i <= N; ++i) used[i] = false;
}

```

```

    for (int i = 1; i <= M; ++i) isBridge[i] =
        false;
    timer = compid = 0;
}

void bridge_tree() {
    initB();
    markBridge(1, -1); //Assuming graph is
                        connected.
    for (int i = 1; i <= N; ++i) used[i] = 0;
    for (int i = 1; i <= N; ++i) {
        if (!used[i]) {
            markComp(i, -1);
            ++compid;
        }
    }

    for (int i = 1; i <= M; ++i) {
        if (isBridge[i]) {
            int u, v;
            tie(u, v) = edges[i];
            // connect two componets using edge.
            Tree[comp[u]].push_back(comp[v]);
            Tree[comp[v]].push_back(comp[u]);
            int x = comp[u];
            int y = comp[v];
        }
    }
}
}

```

6.4 Centroid Decomposition [49 lines]

```

ll n,subsize[mx];
vector<ll>adj[mx];
char ans[mx];
bool brk[mx];
void calculatesize(ll u,ll par){
    subsize[u]=1;
    for(ll i=0;i<(ll)adj[u].size();i++){
        ll v=adj[u][i];
        if(v==par or brk[v]==true)continue;
        calculatesize(v,u);
        subsize[u]+=subsize[v];
    }
}

ll getcentroid(ll u,ll par,ll n){
    ll ret=u;
    for(ll i=0;i<(ll)adj[u].size();i++){
        ll v=adj[u][i];
        if(v==par or brk[v]==true)continue;
        if(subsize[v]>(n/2)){
            ret=getcentroid(v,u,n);
            break;
        }
    }
    return ret;
}

void decompose(ll u,char rank){
    calculatesize(u,-1);
}

```

```

11 c=getcentroid(u,-1,subsize[u]);
brk[c]=true;
ans[c]=rank;
for(11 i=0;i<(11)adj[c].size();i++){
    11 v=adj[c][i];
    if(brk[v]==true)continue;
    decompose(v,rank+1);
}
}
int main(){
    scanf("%lld",&n);
    for(11 i=0;i<n-1;i++){
        11 a,b;
        scanf("%lld %lld",&a,&b);
        adj[a].push_back(b);
        adj[b].push_back(a);
    }
    decompose(1,'A');
    for(11 i=1;i<=n;i++){
        printf("%c",ans[i]);
    }
}

```

6.5 DSU on Tree [69 lines]

```

int n;
//extra data you need
vector<int> adj[mxn];
vector<int> *dsu[mxn];
void call(int u, int p=-1){
    sz[u] = 1;
    for(auto v: adj[u]){
        if(v != p){
            dep[v] = dep[u]+1;
            call(v, u);
            sz[u] += sz[v];
        }
    }
}
void dfs(int u, int p = -1, int isb = 1){
    int mx=-1, big=-1;
    for(auto v: adj[u]){
        if(v != p && sz[v]>mx){
            mx = sz[v];
            big = v;
        }
    }
    for(auto v: adj[u]){
        if(v != p && v != big){
            dfs(v, u, 0);
        }
    }
    if(big != -1){
        dfs(big, u, 1);
        dsu[u] = dsu[big];
    }
    else{
        dsu[u] = new vector<int>();
    }
    dsu[u]->push_back(u);
}

```

//calculation

```

for(auto v: adj[u]){
    if(v == p || v == big) continue;
    for(auto x: *dsu[v]){
        dsu[u]->push_back(x);
    }
}

```

//calculate ans for node u

```

if(isb == 0){
    for(auto x: *dsu[u]){
        //reverse calculation
    }
}

```

```

int main()
{
    scanf("%d", &n);
    for(int i=1; i<n; i++){
        int u, v;
        scanf("%d %d", &u, &v);
        adj[u].pb(v);
        adj[v].pb(u);
    }

    dep[1] = 1;
    call(1);
    dfs(1);
}

```

6.6 Dijkstra [33 lines]

```

#include<bits/stdc++.h>
#define ff first
#define ss second
using namespace std;
const int mx = 1e5 + 5;
using ll = long long;
using pll = pair<ll, ll>;
vector<pll>adj[mx];
int dis[mx];
bool vis[mx];
//Complexity O(V+ElogV)
void Dijkstra(int src) {
    priority_queue<pll, vector<pll>, greater<pll>>
    >pq;
    pq.push({ 0,src });
    memset(dis, 0x3f3f3f3f, sizeof dis);
    memset(vis, 0, sizeof vis);
    dis[src] = 0;
    while (!pq.empty()) {
        int u = pq.top().ss;
        pq.pop();
        if (vis[u]) continue;
        vis[u] = true;
    }
}

```

```

for (auto v : adj[u]) {
    if (dis[v.ss] > dis[u] + v.ff) {
        dis[v.ss] = dis[u] + v.ff;
        pq.push({ dis[v.ss],v.ss });
    }
}
}
int main() {
}

```

6.7 Heavy Light Decomposition [73 lines]

```

/*Heavy Light Decomposition
Build Complexity O(n)
Query Complexity O(lg^2 n)
Call init()with number of nodes
It's probably for the best to not do"using
namespace hld"*/
namespace hld {
    //N is the maximum number of nodes
    //par,lev,size corresponds to
    //parent,depth,subtree-size*/
    //head[u]is the starting node of the chain u is
    //in
    //in[u]to out[u]keeps the subtree indices
    const int N=100000+7;
    vector<int>g[N];
    int par[N],lev[N],head[N],size[N],in[N],out[N];
    int cur_pos,n;
    //returns the size of subtree rooted at u
    //maintains the child with the largest subtree
    //at the front of g[u]*/
    //WARNING: Don't change anything here specially
    //with size[]if Jon Snow
    int dfs(int u,int p){
        size[u]=1,par[u]=p;
        lev[u]=lev[p]+1;
        for(auto &v : g[u]){
            if(v==p)continue;
            size[u]+=dfs(v,u);
            if(size[v]>size[g[u].front()]){
                swap(v,g[u].front());
            }
        }
        return size[u];
    }
}
//decomposed the tree in an array
//note that there is no physical array here
void decompose(int u,int p){
    in[u]++;cur_pos;
    for(auto &v : g[u]){
        if(v==p)continue;
        head[v]=(v==g[u].front()? head[u]: v);
        decompose(v,u);
    }
}

```

```

    out[u]=cur_pos;
}
//initializes the structure with _n nodes
void init(int _n,int root=1){
    n=_n;
    cur_pos=0;
    dfs(root,0);
    head[root]=root;
    decompose(root,0);
}
//checks whether p is an ancestor of u
bool isances(int p,int u){
    return in[p]<=in[u] and out[u]<=out[p];
}
//Returns the maximum node value in the path u-v
ll query(int u,int v){
    ll ret=-INF;
    while(!isances(head[u],v)){
        ret=max(ret,seg.query(1,1,n,in[head[u]],in[u]));
        u=par[head[u]];
    }
    swap(u,v);
    while(!isances(head[u],v)){
        ret=max(ret,seg.query(1,1,n,in[head[u]],in[u]));
        u=par[head[u]];
    }
    if(in[v]<in[u])swap(u,v);
    ret=max(ret,seg.query(1,1,n,in[u],in[v]));
    return ret;
}
//Adds val to subtree of u
void update(int u,ll val){
    seg.update(1,1,n,in[u],out[u],val);
}
};

```

6.8 K'th Shortest path [40 lines]

```

int m,n,deg[MM],source,sink,K,val[MM][12];
struct edge{
    int v,w;
}adj[MM][500];
struct info{
    int v,w,k;
    bool operator<(const info &b)const{
        return w>b.w;
    }
};
priority_queue<info,vector<info>>Q;
void kthBestShortestPath(){
    int i,j;
    info u,v;
    for(i=0;i<n;i++){
        for(j=0;j<K;j++)val[i][j]=inf;
        u.v=source,u.k=0,u.w=0;
        Q.push(u);
        while(!Q.empty()){

```

```

            u=Q.top();
            Q.pop();
            for(i=0;i<deg[u.v];i++){
                v.v=adj[u.v][i].v;
                int cost=adj[u.v][i].w+u.w;
                for(v.k=u.k;v.k<K;v.k++){
                    if(cost==inf)break;
                    if(val[v.v][v.k]>cost){
                        swap(cost,val[v.v][v.k]);
                        v.w=val[v.v][v.k];
                        Q.push(v);
                        break;
                    }
                }
                for(v.k++;v.k<K;v.k++){
                    if(cost==inf)break;
                    if(val[v.v][v.k]>cost)swap(cost,
                        val[v.v][v.k]);
                }
            }
        }
    }
}

```

6.9 LCA [46 lines]

```

const int Lg = 22;
vector<int>adj[mx];
int level[mx];
int dp[Lg][mx];
void dfs(int u) {
    for (int i = 1; i < Lg; i++)
        dp[i][u] = dp[i - 1][dp[i - 1][u]];
    for (int v : adj[u]) {
        if (dp[0][u] == v)continue;
        level[v] = level[u] + 1;
        dp[0][v] = u;
        dfs(v);
    }
}
int lca(int u, int v) {
    if (level[v] < level[u])swap(u, v);
    int diff = level[v] - level[u];
    for (int i = 0; i < Lg; i++)
        if (diff & (1 << i))
            v = dp[i][v];
    for (int i = Lg - 1; i >= 0; i--)
        if (dp[i][u] != dp[i][v])
            u = dp[i][u], v = dp[i][v];
    return u == v ? u : dp[0][u];
}
int kth(int u, int k) {
    for (int i = Lg - 1; i >= 0; i--)
        if (k & (1 << i))
            u = dp[i][u];
    return u;
}
//kth node from u to v. 0th is u.
int go(int u, int v, int k) {
    int l = lca(u, v);
    int d = level[u] + level[v] - (level[l] << 1);

```

```

    assert(k <= d);
    if (level[l] + k <= level[u]) return kth(u, k);
    k -= level[u] - level[l];
    return kth(v, level[v] - level[l] - k);
}
/*
    LCA(u,v) with root r:
    lca(u,v)^lca(u,r)^lca(v,r)
    Distance between u,v:
    level(u) + level(v) - 2*level(lca(u,v))
*/

```

6.10 SACK [50 lines]

```

int sz[maxn];
void getsz(int v,int p){
    sz[v]=1;
    for(auto u : g[v])
        if(u!=p){
            getsz(u,v);
            sz[v]+=sz[u];
        }
}
//SACK O(nlog^2n)
map<int,int>*cnt[maxn];
void dfs(int v,int p){
    int mx=-1,bigChild=-1;
    for(auto u : g[v])
        if(u!=p){
            dfs(u,v);
            if(sz[u]>mx)mx=sz[u],bigChild=u;
        }
    if(bigChild!=-1)cnt[v]=cnt[bigChild];
    else cnt[v]=new map<int,int>();
    (*cnt[v])[col[v]]++;
    for(auto u : g[v])
        if(u!=p && u!=bigChild){
            for(auto x : *cnt[u])
                (*cnt[v])[x.first]+=x.second;
        }
}
//SACK-O(nlogn)
vector<int>*vec[maxn];
int cnt[maxn];
void dfs(int v,int p,bool keep){
    int mx=-1,bigChild=-1;
    for(auto u : g[v])
        if(u!=p&&sz[u]>mx)mx=sz[u],bigChild=u;
    for(auto u : g[v])
        if(u!=p && u!=bigChild)dfs(u,v,0);
    if(bigChild!=-1)
        dfs(bigChild,v,1),vec[v]=vec[bigChild];
    else vec[v]=new vector<int>();
    vec[v]->push_back(v);cnt[col[v]]++;
    for(auto u : g[v])
        if(u!=p && u!=bigChild)
            for(auto x : *vec[u]){
                cnt[col[x]]++;
            }
}

```

```

    vec[v]->push_back(x);
}
/*in this step*vec[v]contains all of the subtree
of vertex v.*/
if(keep==0)
    for(auto u:*vec[v])cnt[col[u]]--;
}

```

6.11 SCC [43 lines]

*/*components: number of SCC.
sz: size of each SCC.
comp: component number of each node.
Create reverse graph.
Run find_scc() to find SCC.
Might need to create condensation graph by
create_condensed().
Think about indeg/outdeg
for multiple test cases- clear
adj/radj/comp/vis/sz/topo/condensed.*/*

vector<int>adj[mx], radj[mx];

```

int comp[mx], vis[mx], sz[mx], components;
vector<int>topo;
void dfs(int u) {
    vis[u] = 1;
    for (int v : adj[u])
        if (!vis[v]) dfs(v);
    topo.push_back(u);
}

```

```

void dfs2(int u, int val) {
    comp[u] = val;
    sz[val]++;
    for (int v : radj[u])
        if (comp[v] == -1)
            dfs2(v, val);
}

```

```

void find_scc(int n) {
    memset(vis, 0, sizeof vis);
    memset(comp, -1, sizeof comp);
    for (int i = 1; i <= n; i++)
        if (!vis[i])
            dfs(i);
    reverse(topo.begin(), topo.end());
    for (int u : topo)
        if (comp[u] == -1)
            dfs2(u, ++components);
}

```

```

vector<int>condensed[mx];
void create_condensed(int n) {
    for (int i = 1; i <= n; i++)
        for (int v : adj[i])
            if (comp[i] != comp[v])
                condensed[comp[i]].push_back(comp[v]);
}

```

7 Math

7.1 Big Sum [13 lines]

```

ll bigsum(ll a, ll b, ll m) {
    if (b == 0) return 0;

```

```

    ll sum; a %= m;
    if (b & 1) {
        sum = bigsum((a * a) % m, (b - 1) / 2, m);
        sum = (sum + (a * sum) % m) % m;
        sum = (1 + (a * sum) % m) % m;
    } else {
        sum = bigsum((a * a) % m, b / 2, m);
        sum = (sum + (a * sum) % m) % m;
    }
    return sum;
}

```

7.2 CRT [52 lines]

```

ll ext_gcd(ll A, ll B, ll* X, ll* Y) {
    ll x2, y2, x1, y1, x, y, r2, r1, q, r;
    x2 = 1; y2 = 0;
    x1 = 0; y1 = 1;
    for (r2 = A, r1 = B; r1 != 0; r2 = r1, r1 = r,
        x2 = x1, y2 = y1, x1 = x, y1 = y) {
        q = r2 / r1;
        r = r2 % r1;
        x = x2 - (q * x1);
        y = y2 - (q * y1);
    }
    *X = x2; *Y = y2;
    return r2;
}

```

```

/*-----BlackBox-----*/
class ChineseRemainderTheorem {
    typedef long long vlong;
    typedef pair<vlong, vlong> pll;
    /** CRT Equations stored as pairs of vector. See
        addEquation()*/
    vector<pll> equations;
    public:
    void clear() {
        equations.clear();
    }
    /** Add equation of the form  $x = r \pmod m$ */
    void addEquation(vlong r, vlong m) {
        equations.push_back({ r, m });
    }
    pll solve() {
        if (equations.size() == 0) return { -1, -1 };
        /// No equations to solve
        vlong a1 = equations[0].first;
        vlong m1 = equations[0].second;
        a1 %= m1;
        /** Initially  $x = a_0 \pmod{m_0}$ */
        /** Merge the solution with remaining
            equations */
        for (int i = 1; i < equations.size(); i++) {
            vlong a2 = equations[i].first;
            vlong m2 = equations[i].second;
            vlong g = __gcd(m1, m2);
            if (a1 % g != a2 % g) return { -1, -1 }; ///
            Conflict in equations
            /** Merge the two equations*/
            vlong p, q;

```

```

            ext_gcd(m1 / g, m2 / g, &p, &q);
            vlong mod = m1 / g * m2;
            vlong x = ((__int128)a1 * (m2 / g) % mod * q
                % mod + (__int128)a2 * (m1 / g) % mod * p %
                mod) % mod;
            /** Merged equation*/
            a1 = x;
            if (a1 < 0) a1 += mod;
            m1 = mod;
        }
        return { a1, m1 };
    }
};

```

7.3 FFT [85 lines]

```

template<typename float_t>
struct mycomplex {
    float_t x, y;
    mycomplex<float_t>(float_t _x = 0, float_t _y =
        0) : x(_x), y(_y) {}
    float_t real() const { return x; }
    float_t imag() const { return y; }
    void real(float_t _x) { x = _x; }
    void imag(float_t _y) { y = _y; }
    mycomplex<float_t>& operator+=(const
        mycomplex<float_t> &other) { x += other.x; y
        += other.y; return *this; }
    mycomplex<float_t>& operator-=(const
        mycomplex<float_t> &other) { x -= other.x; y
        -= other.y; return *this; }
    mycomplex<float_t> operator+(const
        mycomplex<float_t> &other) const { return
        mycomplex<float_t>(*this) += other; }
    mycomplex<float_t> operator-(const
        mycomplex<float_t> &other) const { return
        mycomplex<float_t>(*this) -= other; }
    mycomplex<float_t> operator*(const
        mycomplex<float_t> &other) const {
        return {x * other.x - y * other.y, x * other.y
        + other.x * y};
    }
    mycomplex<float_t> operator*(float_t mult) const
    {
        return {x * mult, y * mult};
    }
    friend mycomplex<float_t> conj(const
        mycomplex<float_t> &c) {
        return {c.x, -c.y};
    }
    friend ostream& operator<<(ostream &stream,
        const mycomplex<float_t> &c) {
        return stream << '(' << c.x << ", " << c.y <<
        ')';
    }
};
using cd = mycomplex<double>;

```



```

void fft(vector<cd> & a, bool invert) {
    int n = a.size();
    for (int i = 1, j = 0; i < n; i++) {
        int bit = n >> 1;
        for (; j & bit; bit >>= 1)
            j ^= bit;
        j ^= bit;
        if (i < j)
            swap(a[i], a[j]);
    }
    for (int len = 2; len <= n; len <= 1) {
        double ang = 2 * PI / len * (invert ? -1 : 1);
        cd wlen(cos(ang), sin(ang));
        for (int i = 0; i < n; i += len) {
            cd w(1);
            for (int j = 0; j < len / 2; j++) {
                cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
                a[i+j+len/2] = u - v;
                w = w*wlen;
            }
        }
    }
    if (invert) {
        for (cd & x : a) {
            double z = n;
            z = 1/z;
            x = x*z;
        }
        // x /= n;
    }
}

void multiply (const vector<bool> & a, const
vector<bool> & b, vector<bool> & res)
{//change all the bool to your type needed
vector<cd> fa (a.begin(), a.end()), fb
(b.begin(), b.end());
size_t n = 1;
while (n < max (a.size(), b.size())) n <= 1;
n <= 1;
fa.resize (n), fb.resize (n);
fft (fa, false), fft (fb, false);
for (size_t i=0; i<n; ++i)
    fa[i] = fa[i] * fb[i];
fft (fa, true);
res.resize (n);
for (size_t i=0; i<n; ++i)
    res[i] = round(fa[i].real());
while(res.back()==0) res.pop_back();
}

void pow(const vector<bool> &a, vector<bool>
&res, long long int k){
vector<bool> po=a;
res.resize(1);
res[0] = 1;
while(k){
    if(k&1){
        multiply(po, res, res);
    }
}

```

```

}
multiply(po, po, po);
k/=2;
}
}

7.4 GaussElimination [39 lines]
template<typename ld>
int gauss(vector<vector<ld>>& a, vector<ld>& ans)
{
    const ld EPS = 1e-9;
    int n = a.size();//number of equations
    int m = a[0].size() - 1;//number of variables
    vector<int> where(m, -1);//indicates which row
contains the solution
    int row, col;
    for (col = 0, row = 0; col < m && row < n; ++col)
    {
        int sel = row;//which row contains the
maximum value/
        for (int i = row + 1; i < n; i++)
            if (abs(a[i][col]) > abs(a[sel][col]))
                sel = i;
        if (abs(a[sel][col]) < EPS) continue;//it's
basically 0.
        a[sel].swap(a[row]);//taking the max row up
        where[col] = row;
        ld t = a[row][col];
        for (int i = col; i <= m; i++) a[row][i] /= t;
        for (int i = 0; i < n; i++) {
            if (i != row) {
                ld c = a[i][col];
                for (int j = col; j <= m; j++)
                    a[i][j] -= a[row][j] * c;
            }
        }
        row++;
    }
    ans.assign(m, 0);
    for (int i = 0; i < m; i++)
        if (where[i] != -1)
            ans[i] = a[where[i]][m] / a[where[i]][i];
    for (int i = 0; i < n; i++) {
        ld sum = 0;
        for (int j = 0; j < m; j++)
            sum += ans[j] * a[i][j];
        if (abs(sum - a[i][m]) > EPS) //L.H.S!=R.H.S
            ans.clear();//No solution
    }
    return row;
}

```

7.5 GaussMod2 [44 lines]

```

template<typename T>
struct Gauss {
    int bits = 60;
    vector<T> table;
    Gauss() {
        table = vector<T>(bits, 0);
    }
}

```

```

}
//call with constructor to define bit size.
Gauss(int _bits) {
    bits = _bits;
    table = vector<T>(bits, 0);
}
int basis()//return rank/size of basis
{
    int ans = 0;
    for (int i = 0; i < bits; i++)
        if (table[i])
            ans++;
    return ans;
}
bool can(T x)//can x be obtained from the basis
{
    for (int i = bits - 1; i >= 0; i--) x = min(x, x
^ table[i]);
    return x == 0;
}
void add(T x) {
    for (int i = bits - 1; i >= 0 && x; i--) {
        if (table[i] == 0) {
            table[i] = x;
            x = 0;
        }
        else x = min(x, x ^ table[i]);
    }
}
T getBest() {
    T x = 0;
    for (int i = bits - 1; i >= 0; i--)
        x = max(x, x ^ table[i]);
    return x;
}
void Merge(Gauss& other) {
    for (int i = bits - 1; i >= 0; i--)
        add(other.table[i]);
}
};

```

7.6 Karatsuba Idea [5 lines]

Three subproblems:

$a = xH \ yH$

$d = xL \ yL$

$e = (xH + xL)(yH + yL) - a - d$

Then $xy = a \cdot rn + e \cdot rn/2 + d$

7.7 Linear Diophantine [12 lines]

```

/*x'=x+(k*B/g), y'=y-(k*A/g); infinite soln
if A=B=0, C must equal 0 and any x,y is solution;
if A|B=0, (x,y)=(C/A,k)|(k,C/B)*/
bool LDE(int A, int B, int C, int*x, int*y){
    int g=gcd(A,B);
    if(C%g!=0) return false;
    int a=A/g, b=B/g, c=C/g;
    extended_gcd(a,b,x,y);//ax+by=1
}

```

```

    if(g<0)a*=-1;b*=-1;c*=-1;//Ensure gcd(a,b)=1
    *x*=c;*y*=c;//ax+by=c
    return true;//Solution Exists
}

```

7.8 Matrix [100 lines]

```

template<typename T>
struct Matrix {
    T MOD = 1e9 + 7; ///change if necessary
    T add(T a, T b) const {
        T res = a + b;
        if (res >= MOD) return res - MOD;
        return res;
    }
    T sub(T a, T b) const {
        T res = a - b;
        if (res < 0) return res + MOD;
        return res;
    }
    T mul(T a, T b) const {
        T res = a * b;
        if (res >= MOD) return res % MOD;
        return res;
    }
    int R, C;
    vector<vector<T>>mat;
    Matrix(int _R = 0, int _C = 0) {
        R = _R, C = _C;
        mat.resize(R);
        for (auto& v : mat) v.assign(C, 0);
    }
    void print() {
        for (int i = 0; i < R; i++)
            for (int j = 0; j < C; j++)
                cout << mat[i][j] << " \n"[j == C - 1];
    }
    void createIdentity() {
        for (int i = 0; i < R; i++)
            for (int j = 0; j < C; j++)
                mat[i][j] = (i == j);
    }
    Matrix operator+(const Matrix& o) const {
        Matrix res(R, C);
        for (int i = 0; i < R; i++)
            for (int j = 0; j < C; j++)
                res[i][j] = add(mat[i][j] + o.mat[i][j]);
    }
    Matrix operator-(const Matrix& o) const {
        Matrix res(R, C);
        for (int i = 0; i < R; i++)
            for (int j = 0; j < C; j++)
                res[i][j] = sub(mat[i][j] + o.mat[i][j]);
    }
    Matrix operator*(const Matrix& o) const {
        Matrix res(R, o.C);
        for (int i = 0; i < R; i++)
            for (int j = 0; j < o.C; j++)
                for (int k = 0; k < C; k++)

```

```

                res.mat[i][j] = add(res.mat[i][j],
mul(mat[i][k], o.mat[k][j]));
                return res;
            }
        }
        Matrix pow(long long x) {
            Matrix res(R, C);
            res.createIdentity();
            Matrix<T> o = *this;
            while (x) {
                if (x & 1) res = res * o;
                o = o * o;
                x >>= 1;
            }
            return res;
        }
        Matrix inverse() ///Only square matrix &&
            non-zero determinant
        {
            Matrix res(R, R + R);
            for (int i = 0; i < R; i++) {
                for (int j = 0; j < R; j++)
                    res.mat[i][j] = mat[i][j];
                res.mat[i][R + i] = 1;
            }
            for (int i = 0; i < R; i++) {
                ///find row 'r' with highest value at [r][i]
                int tr = i;
                for (int j = i + 1; j < R; j++)
                    if (abs(res.mat[j][i]) >
abs(res.mat[tr][i]))
                        tr = j;
                ///swap the row
                res.mat[tr].swap(res.mat[i]);
                ///make 1 at [i][i]
                T val = res.mat[i][i];
                for (int j = 0; j < R + R; j++) res.mat[i][j]
/= val;
                ///eliminate [r][i] from every row except i.
                for (int j = 0; j < R; j++) {
                    if (j == i) continue;
                    for (int k = R + R - 1; k >= i; k--) {
                        res.mat[j][k] -= res.mat[i][k] *
res.mat[j][i] / res.mat[i][i];
                    }
                }
            }
            Matrix ans(R, R);
            for (int i = 0; i < R; i++)
                for (int j = 0; j < R; j++)
                    ans.mat[i][j] = res.mat[i][R + j];
            return ans;
        }
    };
}

```

7.9 Miller-Rabin-Pollard-Rho [68 lines]

```

ll powmod(ll a, ll p, ll m) ///(a^p % m)
ll result = 1;
a %= m;
while (p) {

```

```

    if (p & 1)
        result = (vll)result * a % m;
    a = (vll)a * a % m;
    p >>= 1;
}
return result;
}
bool check_composite(ll n, ll a, ll d, int s) {
    ll x = powmod(a, d, n);
    if (x == 1 || x == n - 1)
        return false;
    for (int r = 1; r < s; r++) {
        x = (vll)x * x % n;
        if (x == n - 1)
            return false;
    }
    return true;
}
bool MillerRabin(ll n) {
    if (n < 2) return false;
    int r = 0;
    ll d = n - 1;
    while ((d & 1) == 0) {
        d >>= 1;
        r++;
    }
    for (int a : {2, 3, 5, 7, 11, 13, 17, 19, 23,
29, 31, 37}) {
        if (n == a) return true;
        if (check_composite(n, a, d, r))
            return false;
    }
    return true;
}
ll mult(ll a, ll b, ll mod) {
    return (vll)a * b % mod;
}
ll f(ll x, ll c, ll mod) {
    return (mult(x, x, mod) + c) % mod;
}
ll rho(ll n) {
    if (n % 2 == 0) return 2;
    ll x = myrand() % n + 1, y = x, c = myrand() % n
+ 1, g = 1;
    while (g == 1) {
        x = f(x, c, n);
        y = f(y, c, n);
        y = f(y, c, n);
        g = __gcd(abs(x - y), n);
    }
    return g;
}
set<ll>prime;
void prime_factorization(ll n) {
    if (n == 1) return;
    if (MillerRabin(n)) {
        prime.insert(n);

```

```

    return;
}
ll x = n;
while (x == n) x = rho(n);
prime_factorization(x);
prime_factorization(n / x);
}
//call prime_factorization(n) for prime factors.
//call MillerRabin(n) to check if prime.

```

7.10 Mod Inverse [5 lines]

```

int modInv(int a, int m) {
    int x, y; //if g==1 Inverse doesn't exist
    int g = gcdExt(a, m, x, y);
    return (x % m + m) % m;
}

```

7.11 NTT [96 lines]

```

ll power(ll a, ll p, ll mod) {
    if (p==0) return 1;
    ll ans = power(a, p/2, mod);
    ans = (ans * ans)%mod;
    if(p%2) ans = (ans * a)%mod;
    return ans;
}
int primitive_root(int p) {
    vector<int> factor;
    int phi = p-1, n = phi;
    for (int i=2; i*i<=n; i++) {
        if (n%i) continue;
        factor.push_back(i);
        while (n%i==0) n/=i;
    }
    if (n>1) factor.push_back(n);
    for (int res =2; res<=p; res++) {
        bool ok = true;
        for (int i=0; i<factor.size() && ok; i++)
            ok &= power(res, phi/factor[i], p) != 1;
        if (ok) return res;
    }
    return -1;
}
int nttdata(int mod, int &root, int &inv, int &pw)
{
    int c = 0, n = mod-1;
    while (n%2==0) c++, n/=2;
    pw = (mod-1)/n;
    int g = primitive_root(mod);
    root = power(g, n, mod);
    inv = power(root, mod-2, mod);
    return c;
}
const int M = 786433;
struct NTT {
    int N;
    vector<int> perm;
    int mod, root, inv, pw;
    NTT(){}
}

```

```

NTT(int mod, int root, int inv, int pw) :
    mod(mod), root(root), inv(inv), pw(pw) {}
void precalculate() {
    perm.resize(N);
    perm[0] = 0;
    for (int k=1; k<N; k<=1) {
        for (int i=0; i<k; i++) {
            perm[i] <= 1;
            perm[i+k] = 1 + perm[i];
        }
    }
}
void fft(vector<ll> &v, bool invert = false) {
    if (v.size() != perm.size()) {
        N = v.size();
        assert(N && (N&(N-1)) == 0);
        precalculate();
    }
    for (int i=0; i<N; i++)
        if (i < perm[i])
            swap(v[i], v[perm[i]]);
    for (int len = 2; len <= N; len <=1) {
        ll factor = invert ? inv : root;
        for (int i=len; i<pw; i<=1)
            factor = (factor * factor) % mod;
        for (int i=0; i<N; i+=len) {
            ll w = 1;
            for (int j=0; j<len/2; j++) {
                ll x = v[i+j], y = (w*v[i+j+len/2])%mod;
                v[i+j] = (x+y)%mod;
                v[i+j+len/2] = (x-y+mod)%mod;
                w = (w*factor)%mod;
            }
        }
    }
    if (invert) {
        ll n1 = power(N, mod-2, mod);
        for (ll &x: v) x = (x*n1)%mod;
    }
}
vector<ll> multiply(vector<ll> a, vector<ll> &b)
{
    while (a.size() && a.back() == 0)
        a.pop_back();
    while (b.size() && b.back() == 0)
        b.pop_back();
    int n = 1;
    while (n < a.size() + b.size()) n<=1;
    a.resize(n);
    b.resize(n);
    fft(a);
    fft(b);
    for (int i=0; i<n; i++) a[i] = (a[i] *
        b[i])%M;
    fft(a, true);
    while (a.size() && a.back() == 0)
        a.pop_back();
    return a;
}

```

```

}
// int mod=786433, root, inv, pw;
// nttdata(mod, root, inv, pw);
// NTT nn = NTT(mod, root, inv, pw);
};

```

7.12 No of Digits in n! in base B [7 lines]

```

ll NoOfDigitInNFactInBaseB(ll N, ll B) {
    ll i;
    double ans=0;
    for(i=1; i<=N; i++) ans+=log(i);
    ans=ans/log(B), ans=ans+1;
    return (ll)ans;
}

```

7.13 SOD Upto N [16 lines]

```

ll SOD_Upto_N(ll N) {
    ll i, j, ans=0; //upto N in Sqrt(N)
    for(i=1; i*i<=N; i++) {
        j=N/i;
        ans+=((j*(j+1))/2)-(((i-1)*i)/2);
        ans+=((j-i)*i);
    }
    return ans;
}
ll SODUptoN(ll N) {
    ll res=0, u=sqrt(N);
    for(ll i=1; i<=u; i++)
        res+=(N/i)-i;
    res*=2, res+=u;
    return res;
}

```

7.14 Sieve-Phi-Mobius [26 lines]

```

const int N = 1e7;
vector<int> pr;
int mu[N + 1], phi[N + 1], lp[N + 1];
void sieve() {
    phi[1] = 1, mu[1] = 1;
    for (int i = 2; i <= N; i++) {
        if (lp[i] == 0) {
            lp[i] = i;
            phi[i] = i - 1;
            pr.push_back(i);
        }
        for (int j = 0; j < pr.size() && i * pr[j]
            <= N; j++) {
            lp[i * pr[j]] = pr[j];
            if (i % pr[j] == 0) {
                phi[i * pr[j]] = phi[i] * pr[j];
                break;
            }
            else
                phi[i * pr[j]] = phi[i] *
                phi[pr[j]];
        }
    }
    for (int i = 2; i <= N; i++) {
        if (lp[i / lp[i]] == lp[i]) mu[i] = 0;
    }
}

```

```

    else mu[i] = -1 * mu[i / lp[i]];
}
}

```

8 Misc

8.1 Bit hacks [12 lines]

```

# x & -x is the least bit in x.
# iterate over all the subsets of the mask
for (int s=m; ; s=(s-1)&m) {
    ... you can use s ...
    if (s==0) break;
}
# c = x&-x, r = x+c; (((r^x) >> 2)/c) | r is the
next number after x with the same number of bits
set.
# __builtin_popcount(x) //number of ones in binary
__builtin_popcountll(x) // for long long
# __builtin_clz(x) // number of leading zeros
__builtin_ctz(x) // number of trailing zeros,
they also have long long version

```

8.2 Bitset C++ [13 lines]

```

bitset<17>BS;
BS[1] = BS[7] = 1;
cout<<BS._Find_first()<<endl; // prints 1
bs._Find_next(idx). This function returns first
set bit after index idx. for example:

```

```

bitset<17>BS;
BS[1] = BS[7] = 1;
cout<<BS._Find_next(1)<<' ' <<BS._Find_next(3)
<<endl; // prints
7,7

```

So this code will print all of the set bits of BS:

```

for(int i=BS._Find_first();i< BS.size();i =
BS._Find_next(i))
    cout<<i<<endl;
//Note that there isn't any set bit after idx,
BS._Find_next(idx) will return BS.size(); same
as calling BS._Find_first() when bitset is
clear;

```

8.3 Template [30 lines]

```

// #pragma GCC optimize("O3,unroll-loops")
// #pragma GCC
    target("avx2,bmi,bmi2,lzcnt,popcnt")
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
template <typename A, typename B> ostream&
operator<<(ostream& os, const pair<A, B>& p) {
    return os << '(' << p.first << ", " <<
p.second << ')'; }

```

```

template <typename T_container, typename T =
typename enable_if<!is_same<T_container,
string>::value, typename
T_container::value_type>::type> ostream&
operator<<(ostream& os, const T_container& v)
{ os << '{'; string sep; for (const T& x : v)
os << sep << x, sep = ", "; return os << '}';
}

```

```

void dbg_out() { cerr << endl; }
template <typename Head, typename... Tail> void
dbg_out(Head H, Tail... T) { cerr << " " <<
H; dbg_out(T...); }

```

```

#ifdef SMIE
#define debug(args...) cerr << "(" << #args <<
    "):", dbg_out(args)
#else
#define debug(args...)
#endif

```

```

template <typename T> inline T gcd(T a, T b) { T
c;while (b) { c = b;b = a % b;a = c; }return
a; } // better than __gcd
ll powmod(ll a, ll b, ll MOD) { ll res = 1;a %=
MOD;assert(b >= 0);for (; b >= 1) { if (b
& 1)res = res * a % MOD;a = a * a % MOD;
}return res; }
template <typename T>using orderedSet = tree<T,
null_type, less_equal<T>, rb_tree_tag,
tree_order_statistics_node_update>;
//order_of_key(k) - number of element strictly
less than k
//find_by_order(k) - k'th element in set.(0
indexed)(iterator)
using ll = long long;
mt19937
rng(chrono::steady_clock::now().time_since_epoch()
.count());
//uniform_int_distribution<int>(0, i)(rng)
int main() {
    ios_base::sync_with_stdio(false);//DON'T CC++
cin.tie(NULL);//DON'T use for interactive
}

```

8.4 Vimrc [26 lines]

```

filetype plugin indent on
syntax on
set hls is ar ai cul wrap lbr nu rnu et magic sc
aw sb spr gd so=2 tm=400 mouse=a sw=4 sts=4
ts=4 ls=2 bs=indent,eol,start
au TerminalOpen * setlocal nonu nornu
au BufNewFile *.cpp -r ./template.cpp | 14
set tgc
imap jk <esc>
imap <c-h> <left>

```

```

noremap <c-c> "+y
nnoremap <leader>f :let @+ = expand('%:p')<cr>
noremap <leader>d "_d

```

```

nnoremap <leader>ca :%y+<cr>
nnoremap <leader>cd :cd %:h<cr>
nnoremap <leader>b :ls<cr>b
nnoremap <leader>vim :vs ~/.vimrc<cr>
nnoremap <leader>r %x<c-o>x

```

```

inoremap {<cr> {<cr><esc>O
inoremap ( <c-]>(<left>
inoremap (( (
vnoremap ( <esc>`a<esc>`<i(<esc>

```

```

inorea aLL <esc>yT(f.abegin(), <c-r>".end()
inorea raLL <esc>yT(f.arbegin(), <c-r>".rend()

```

8.5 build [3 lines]

```

#!/bin/bash
>&2 echo -e "Compiling $1.cpp with -std=gnu++17
$2" &&
g++ -std=gnu++17 -Wshadow -Wall -Wextra
-Wno-unused-result -O2 -g -fsanitize=undefined
-fsanitize=address $2 "$1.cpp" -o "$1"

```

8.6 debug [6 lines]

```

#!/bin/bash
bar="-----"
build $1 -DSMIE && >&2 echo -e "\tRunning
$1\n$bar" && ts=$(date +%s%N) &&
\time -f "$bar\nMemory Usage : %M KB" ".$1" &&
>&2 echo -e "Execution Time : $((($date +%s%N) -
$ts)/1000000)) ms"

```

8.7 stress-test [16 lines]

```

#!/bin/bash
build $1 $2 && build $1_gen $2 && build $1_brute
$2 &&
for((i = 1; ; ++i)); do
    echo -e "\nTest Case "$i
    ./$1_gen $i > inp
    echo -e "=====\nINPUT\n-----"
    cat inp
    ./$1 < inp > out1
    echo -e "\nOUTPUT\n-----"
    cat out1
    ./$1_brute < inp > out2
    echo -e "\nEXPECTED\n-----"
    cat out2
    echo ""
    diff -w out1 out2 || break
done

```

9 String

9.1 Aho-Corasick [124 lines]

```

const int NODE=3000500;///Maximum Nodes
const int LGN=30; ///Maximum Number of Tries
const int MXCHR=53; ///Maximum Characters
const int MXP=5005; ///
struct node {
    int val;
    int child[MXCHR];
}

```



```

vector<int> graph;
void clear(){
    CLR(child,0);
    val=0;
    graph.clear();
}
}Trie[NODE+10];
int maxNodeId,fail[NODE+10],par[NODE+10];
int nodeSt[NODE+10],nodeEd[NODE+10];
vlong csum[NODE+10],pLoc[MXP];
void resetTrie(){
    maxNodeId=0;
}
int getNode(){
    int curNodeId=++maxNodeId;
    Trie[curNodeId].clear();
    return curNodeId;
}
inline void upd(vlong pos){
    csum[pos]++;
}
inline vlong qry(vlong pos){
    vlong res=csum[pos];
    return res;
}
struct AhoCorasick {
    int root,size,euler;
    void clear(){
        root=getNode();
        size=euler=0;
    }
    inline int getName(char ch){
        if(ch=='-')return 52;
        else if(ch>='A' && ch<='Z')return 26+(ch-'A');
        else return(ch-'a');
    }
    void addToTrie(string &s,int id){
        //Add string s to the Trie in general way
        int len=SZ(s),cur=root;
        FOR(i,0,len-1){
            int c=getname(s[i]);
            if(Trie[cur].child[c]==0){
                int curNodeId=getNode();
                Trie[curNodeId].val=c;
                Trie[cur].child[c]=curNodeId;
            }
            cur=Trie[cur].child[c];
        }
        pLoc[id]=cur;
        size++;
    }
    void calcFailFunction(){
        queue<int> Q;
        Q.push(root);
        while(!Q.empty()){
            int s=Q.front();
            Q.pop();
            //Add all the children to the queue:

```

```

        FOR(i,0,MXCHR-1){
            int t=Trie[s].child[i];
            if(t!=0){
                Q.push(t);
                par[t]=s;
            }
        }
        if(s==root){/*Handle special case when s is root*/
            fail[s]=par[s]=root;
            continue;
        }
        //Find fall back of s:
        int p=par[s],f=fail[p];
        int val=Trie[s].val;
        /*Fall back till you found a node who has got val as a child*/
        while(f!=root && Trie[f].child[val]==0){
            f=fail[f];
        }
        fail[s]=(Trie[f].child[val]==0)? root :
        Trie[f].child[val];
        //Self fall back not allowed
        if(s==fail[s]){
            fail[s]=root;
        }
        Trie[fail[s]].graph.push_back(s);
    }
    void dfs(int pos){
        ++euler;
        nodeSt[pos]=euler;
        for(auto x: Trie[pos].graph){
            dfs(x);
        }
        nodeEd[pos]=euler;
    }
    //Returns the next state
    int goTo(int state,int c){
        if(Trie[state].child[c]!=0){/*No need to fall back*/
            return Trie[state].child[c];
        }
        //Fall back now:
        int f=fail[state];
        while(f!=root && Trie[f].child[c]==0){
            f=fail[f];
        }
        int res=(Trie[f].child[c]==0)?
        root:Trie[f].child[c];
        return res;
    }
}
/*Iterate through the whole text and find all the matchings*/
void findmatching(string &s){
    int cur=root,idx=0;
    int len=SZ(s);
    while(idx<len){

```

```

        int c=getname(s[idx]);
        cur=goTo(cur,c);
        upd(nodeSt[cur]);
        idx++;
    }
}
}acorasick;

```

9.2 Double Hasing [50 lines]

```

struct SimpleHash {
    int len;
    long long base, mod;
    vector<int> P, H, R;
    SimpleHash() {}
    SimpleHash(const char* str, long long b, long
    long m) {
        base = b, mod = m, len = strlen(str);
        P.resize(len + 4, 1), H.resize(len + 3, 0),
        R.resize(len + 3, 0);
        for (int i = 1; i <= len + 3; i++)
            P[i] = (P[i - 1] * base) % mod;
        for (int i = 1; i <= len; i++)
            H[i] = (H[i - 1] * base + str[i - 1] + 1007)
            % mod;
        for (int i = len; i >= 1; i--)
            R[i] = (R[i + 1] * base + str[i - 1] + 1007)
            % mod;
    }
    inline int range_hash(int l, int r) {
        int hashval = H[r + 1] - ((long long)P[r - 1
        + 1] * H[1] % mod);
        return (hashval < 0 ? hashval + mod :
        hashval);
    }
    inline int reverse_hash(int l, int r) {
        int hashval = R[l + 1] - ((long long)P[r - 1
        + 1] * R[r + 2] % mod);
        return (hashval < 0 ? hashval + mod :
        hashval);
    }
};
struct DoubleHash {
    SimpleHash sh1, sh2;
    DoubleHash() {}
    DoubleHash(const char* str) {
        sh1 = SimpleHash(str, 1949313259, 2091573227);
        sh2 = SimpleHash(str, 1997293877, 2117566807);
    }
    long long concate(DoubleHash& B, int l1, int
    r1, int l2, int r2) {
        int len1 = r1 - l1 + 1, len2 = r2 - l2 + 1;
        long long x1 = sh1.range_hash(l1, r1),
        x2 = B.sh1.range_hash(l2, r2);
        x1 = (x1 * B.sh1.P[len2]) % 2091573227;
        long long newx1 = (x1 + x2) % 2091573227;
        x1 = sh2.range_hash(l1, r1);
        x2 = B.sh2.range_hash(l2, r2);

```

```

x1 = (x1 * B.sh2.P[len2]) % 2117566807;
long long newx2 = (x1 + x2) % 2117566807;
return (newx1 << 32) ^ newx2;
}
inline long long range_hash(int l, int r) {
    return ((long long)sh1.range_hash(l, r) << 32)
    ^ sh2.range_hash(l, r);
}
inline long long reverse_hash(int l, int r) {
    return ((long long)sh1.reverse_hash(l, r) <<
    32) ^ sh2.reverse_hash(l, r);
}
};

```

9.3 KMP [23 lines]

```

char P[maxn], T[maxn];
int b[maxn], n, m;
void kmpPreprocess(){
    int i=0, j=-1;
    b[0]=-1;
    while(i<m){
        while(j>=0 and P[i]!=P[j])
            j=b[j];
        i++;j++;
        b[i]=j;
    }
}
void kmpSearch(){
    int i=0, j=0;
    while(i<n){
        while(j>=0 and T[i]!=P[j])
            j=b[j];
        i++;j++;
        if(j==m){
            //pattern found at index i-j
        }
    }
}

```

9.4 Palindromic Tree [30 lines]

```

struct PalindromicTree{
    int n,idx,t;
    vector<vector<int>> tree;
    vector<int> len,link;
    string s; // 1-indexed
    PalindromicTree(string str){
        s="$"+str;
        n=s.size();
        len.assign(n+5,0);
        link.assign(n+5,0);
        tree.assign(n+5,vector<int>(26,0));
    }
    void extend(int p){
        while(s[p-len[t]-1]!=s[p]) t=link[t];
        int x=link[t],c=s[p]-'a';
        while(s[p-len[x]-1]!=s[p]) x=link[x];
        if(!tree[t][c]){
            tree[t][c]=++idx;
            len[idx]=len[t]+2;

```

```

            link[idx]=len[idx]==1?2:tree[x][c];
        }
        t=tree[t][c];
    }
    void build(){
        len[1]=-1,link[1]=1;
        len[2]=0,link[2]=1;
        idx=t=2;
        for(int i=1;i<n;i++) extend(i);
    }
};

```

9.5 Suffix Array [78 lines]

```

struct SuffixArray {
    vector<int> p, c, rank, lcp;
    vector<vector<int>> st;
    SuffixArray(string const& s) {
        build_suffix(s + char(1));
        p.erase(p.begin());
        build_rank(p.size());
        build_lcp(s);
        build_sparse_table(lcp.size());
    }
    void build_suffix(string const& s) {
        int n = s.size();
        const int MX_ASCII = 256;
        vector<int> cnt(max(MX_ASCII, n), 0);
        p.resize(n); c.resize(n);
        for (int i = 0; i < n; i++) cnt[s[i]]++;
        for (int i=1; i<MX_ASCII; i++) cnt[i]+=cnt[i-1];
        for (int i = 0; i < n; i++) p[--cnt[s[i]]] = i;
        c[p[0]] = 0;
        int classes = 1;
        for (int i = 1; i < n; i++) {
            if (s[p[i]] != s[p[i-1]]) classes++;
            c[p[i]] = classes - 1;
        }
        vector<int> pn(n), cn(n);
        for (int h = 0; (1 << h) < n; ++h) {
            for (int i = 0; i < n; i++) {
                pn[i] = p[i] - (1 << h);
                if (pn[i] < 0) pn[i] += n;
            }
            fill(cnt.begin(), cnt.begin() + classes, 0);
            for (int i = 0; i < n; i++) cnt[c[pn[i]]]++;
            for (int i=1; i<classes; i++)
                cnt[i]+=cnt[i-1];
            for (int i=n-1;i>=0;i--)
                p[--cnt[c[pn[i]]]]=pn[i];
            cn[p[0]] = 0; classes = 1;
            for (int i = 1; i < n; i++) {
                pair<int, int> cur = {c[p[i]], c[(p[i] + (1
                << h)) % n]};
                pair<int, int> prev = {c[p[i-1]], c[(p[i-1]
                + (1 << h)) % n]};
                if (cur != prev) ++classes;
                cn[p[i]] = classes - 1;
            }
            c.swap(cn);

```

```

        }
    }
    void build_rank(int n) {
        rank.resize(n, 0);
        for (int i = 0; i < n; i++) rank[p[i]] = i;
    }
    void build_lcp(string const& s) {
        int n = s.size(), k = 0;
        lcp.resize(n - 1, 0);
        for (int i = 0; i < n; i++) {
            if (rank[i] == n - 1) {
                k = 0;
                continue;
            }
            int j = p[rank[i] + 1];
            while (i + k < n && j + k < n && s[i+k] ==
            s[j+k])
                k++;
            lcp[rank[i]] = k;
            if (k) k--;
        }
    }
    void build_sparse_table(int n) {
        int lim = __lg(n);
        st.resize(lim + 1, vector<int>(n)); st[0] = lcp;
        for (int k = 1; k <= lim; k++)
            for (int i = 0; i + (1 << k) <= n; i++)
                st[k][i] = min(st[k - 1][i], st[k - 1][i +
                (1 << (k - 1))]);
    }
    int get_lcp(int i) { return lcp[i]; }
    int get_lcp(int i, int j) {
        if (j < i) swap(i, j);
        j--; /*for lcp from i to j we don't need last
        lcp*/
        int K = __lg(j - i + 1);
        return min(st[K][i], st[K][j - (1 << K) + 1]);
    }
};

```

9.6 Suffix Automata [119 lines]

```

const int MXCHR = 26;
/*
take an object of suffixAutomata
call extend(c) for each character c in string
call Process() to initiate the important values
*/
struct suffixAutomata {
    /**
    * len -> largest string length of the
    corresponding endpos-equivalent class
    * link -> longest suffix that is another
    endpos-equivalent class
    * firstpos -> end position of the first
    occurrence of the largest string of
    *that node

```

```

    */
    struct state {
        int link, len;
        int next[MXCHR];
        state() {}
        state(int l) {
            len = l;
            link = -1;
            for (int i = 0; i < MXCHR; i++)
                next[i] = -1;
        }
    };
    vector<state> node;
    int sz, last;
    vector<int> cnt, distinct, firstPos, occur, SA;
    vector<vector<int>> adj; // suffix links tree
    // cnt and SA for counting sort the nodes.
    int L;

    suffixAutomata() {
        node.push_back(state(0));
        firstPos.push_back(-1);
        occur.push_back(0);
        last = 0;
        sz = 0;
        L = 0;
    }
    int getID(char c) {
        return c - 'a'; // change according to
        problem
    }
    void extend(char c) {
        int idx = ++sz, p = last, id = getID(c);
        L++;
        node.push_back(state(node[last].len + 1));
        firstPos.push_back(node[idx].len - 1);
        occur.push_back(1);

        while (p != -1 && node[p].next[id] == -1)
        {
            node[p].next[id] = idx;
            p = node[p].link;
        }
        if (p == -1)
            node[idx].link = 0;
        else {
            int q = node[p].next[id];
            if (node[p].len + 1 == node[q].len)
                node[idx].link = q;
            else {
                int clone = ++sz;
                state x = node[q];
                x.len = node[p].len + 1;
                node.push_back(x);
                firstPos.push_back(firstPos[q]);
                occur.push_back(0);
            }
        }
    }

```

```

        while (p != -1 && node[p].next[id]
        == q) {
            node[p].next[id] = clone;
            p = node[p].link;
        }
        node[idx].link = node[q].link =
        clone;
    }
    last = idx;
}
void Process() {
    cnt.resize(sz + 1);
    distinct.resize(sz + 1);
    SA.resize(sz + 1);
    adj.resize(sz + 1);
    for (int i = 0; i <= sz; i++)
        cnt[node[i].len]++;
    for (int i = 1; i <= L; i++) cnt[i] +=
    cnt[i - 1];
    for (int i = 0; i <= sz; i++)
        SA[--cnt[node[i].len]] = i;
    for (int i = sz; i > 0; i--) {
        int idx = SA[i];
        occur[node[idx].link] += occur[idx];
        adj[node[idx].link].push_back(idx);
        distinct[idx] = 1;
        for (int j = 0; j < MXCHR; j++) {
            if (node[idx].next[j] != -1)
                distinct[idx] +=
                distinct[node[idx].next[j]];
        }
    } // counts distinct substrings and
    occurrence of each state
    for (int i = 0; i < MXCHR; i++)
        if (node[0].next[i] != -1) distinct[0]
        += distinct[node[0].next[i]];
}
pair<int, int> lcs(string &str) {
    int mxlen = 0, bestpos = -1, pos = 0, len
    = 0;
    int u = 0; // LCS of two string. returns
    start position and length
    for (char c : str) {
        int v = getID(c);
        while (u && node[u].next[v] == -1) {
            u = node[u].link;
            len = node[u].len;
        }
        if (node[u].next[v] != -1) {
            len++;
            u = node[u].next[v];
        }
        if (len > mxlen) {
            mxlen = len;
            bestpos = pos;
        }
        pos++;
    }
}

```

```

    }
    return {bestpos - mxlen + 1, mxlen};
}
state &operator[](int index) { return
node[index]; }
};

9.7 Trie [28 lines]
const int maxn=100005;
struct Trie{
    int next[27][maxn];
    int endmark[maxn],sz;
    bool created[maxn];
    void insertTrie(string& s){
        int v=0;
        for(int i=0;i<(int)s.size();i++){
            int c=s[i]-'a';
            if(!created[next[c][v]]){
                next[c][v]=++sz;
                created[sz]=true;
            }
            v=next[c][v];
        }
        endmark[v]++;
    }
    bool searchTrie(string& s){
        int v=0;
        for(int i=0;i<(int)s.size();i++){
            int c=s[i]-'a';
            if(!created[next[c][v]])
                return false;
            v=next[c][v];
        }
        return(endmark[v]>0);
    }
};

9.8 Z-Algorithm [19 lines]
void compute_z_function(const char*S,int N){
    int L=0,R=0;
    for(int i=1;i<N;++i){
        if(i>R){
            L=R=i;
            while(R<N && S[R-L]==S[R])++R;
            Z[i]=R-L,--R;
        }
        else{
            int k=i-L;
            if(Z[k]<R-i+1)Z[i]=Z[k];
            else{
                L=i;
                while(R<N && S[R-k]==S[R])++R;
                Z[i]=R-L,--R;
            }
        }
    }
}
}

```