

Midterm 2017-2018 Sem 2

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1 Question 01 Worst Case Time Complexity

- (1) No 1
[O(1), only need to shift 1 element]
- (2) No 2
[O(N), still need to shift all the elements]
- (3) No 3
[O(N)]
- (4) No 4
[O(N log(N))]
- (5) No 5 (NOTE!!!)
[O(log(N)), binary search is log N]
- (6) No 6
[O(N), you have to index every element thus you can't go any faster than O(N)]
- (7) No 7
[O(1), double linked list can go backwards so only 3 elements]
- (8) No 8
[O(1), just pop and pop from the stack]
- (9) No 9
[O(N), you can only remove from the head in queue]
- (10) No 10
[O(1), for deque, you can remove both head and tail, thus its O(1)]

2 Question 02 Analysis

- (1) No 1
[False, C libraries scanf and printf are compatible with C++, C++ is just a superset of the C programming language]

(2) No 2

[False, *stable_sort* uses merge sort, Randomized quick sort is not the fastest sort as it has the worst case scenario of $O(N^2)$. Furthermore, Randomized quick sort is not stable]

(3) No 3

[True, each vertex in a DLL has a prev vertex and a next vertex, double that of a SLL, thus double the memory per vertex]

(4) No 4

[True, getting any element is $O(1)$ just like the stack's ability to get the first element or rather the head. Note: if this was remove first element, vector is $O(N)$ while stack is $O(1)$, as vectors have to shift all the elements to the right]

(5) No 5

[True, it can compile and has more or less the same methods and operations as a vector]

3 Question 03 Alternative Implications

(1) No 2

[the time complexity of *push_back* for the List ADT is $O(1)$ for this vector implementation, which is the same as the normal STL list]

(2) No 3

[Removing an element in the list takes $O(N)$ time as we need shift the rest of elements to the right starting from the last element.]

(3) No 4

[Inserting an element in the middle and the front is $O(N)$, as we would need to shift the index of all the elements to the right starting from the element at the back.]

(4) No 5

[Removing an element from the back is $O(1)$]

(5) No 6

[Inserting an element from the back is $O(1)$]

(6) No 7

[Sorting the array is takes an extra $O(N)$ time because finding the specific elements of the array based on the index will require iterating from the start of the array at index 0 to the end. This makes the worst-time complexity with a comparison sort like bubble sort at $O(N^3)$ time]

4 Question 04 Singly/e Linked List without Tail Pointer

(1) No 2

[Removing the tail element will still be $O(N)$ as we need to now the prev vertex by iterating through the list]

(2) No 3

[Removing the middle element is still $O(N)$]

(3) No 4

[Inserting at the front would be $O(1)$ as we still know the head vertex]

(4) No 5

[Removing at the front would be $O(1)$ as we still know the head vertex and only need to attach a new vertex to the head of the linked list]

(5) No 6

[Inserting a new tail element will take $O(N)$ time instead of $O(1)$, as we would have to iterate $N - 1$ times starting from the head vertex to the $N-1$ vertex to attach a new vertex, as we do not know the tail vertex]

5 Question 05 Special Sorting Criteria

```
#include <bits/stdc++.h> // you have to complete this question using C/C++ code
using namespace std;
```

```
int main() {
    string name;
    vector<string> listOfNames;
    while (cin >> name, !cin.eof()) { // if can read name in one line (not EOF yet)
        string reversed = reverse(name.begin(), name.end()); //  $O(M)$ ,  $M$  being length of string
        listOfNames.push_back(reversed); //  $O(N)$ 
    }

    stable_sort(listOfNames.begin(), listOfNames.end()); //  $O(N \log N)$ 

    for (auto& name : listOfNames) { //  $O(N)$ 
        cout << name << '\n';
    }

    return 0;
} // the overall time complexity of my C++ code above is  $O(MN + N \log N)$ 
```

6 Question 06 Continuous Median (version IV)

```
#include <bits/stdc++.h> // you have to complete this question using C++ code
using namespace std;
```

```
int main() {
    ios::sync_with_stdio(false);
    cout.tie(NULL);
    cin.tie(NULL); //  $N$  is gigantic, we need fast I/O

    int TC, N, Ai;
    cin >> TC; // always 1 test case for this version IV
    cin >> N;
    long long ans = 0;
    vector<int> arr;
```

```

for (int i = 0; i < N; i++) {
    cin >> Ai; // this time, 1 <= Ai <= 3
    arr.push_back(Ai) // O(1)

    long long sizeOfArr = arr.size(); // O(1)

    if (sizeOfArr % 2 != 0) {
        ans += arr[sizeOfArr / 2];
    } else {
        int first = arr[(sizeOfArr / 2) - 1];
        int second = arr[sizeOfArr / 2];
        ans += (first + second) / 2;
    }
}

cout << ans << endl;
return 0;
} // the overall time complexity of my C++ code above is O(N)

```