Regression Analysis Project 1

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Fit a multiple regression model using Earnings as the dependent variable, and Events and Score as the independent variable

First lets load in the packages and data.

```
# Core packages
suppressPackageStartupMessages(library(tidyverse))
suppressPackageStartupMessages(library(tidymodels))
golf = read_csv("Golf.csv", show_col_types = FALSE)

# Peek
summary(golf)
```

Earnings		Events	Score	
Min.	: 21250	Min. :16.00	Min. :68.98	
1st Qu	.: 402589	1st Qu.:23.00	1st Qu.:70.31	
Median	:1156517	Median :26.00	Median :70.92	
Mean	:1726394	Mean :25.76	Mean :71.14	
3rd Qu	.:2359507	3rd Qu.:30.00	3rd Qu.:71.75	
Max.	:5787225	Max. :36.00	Max. :75.01	

Now we can fit the multiple regression model.

```
golf_recipe = recipe(Earnings ~ Events + Score, data = golf)

lm_model = linear_reg() |>
    set_engine("lm")

lm_workflow = workflow() |>
    add_recipe(golf_recipe) |>
```

```
add_model(lm_model)
lm fit = lm workflow |>
  fit(data = golf)
#coeffecients
lm_fit |> tidy()
# A tibble: 3 x 5
  term
               estimate std.error statistic
                                               p.value
                                     <dbl>
                            <dbl>
                                                 <dbl>
  <chr>
                  <dbl>
                                       6.55 0.00000369
1 (Intercept) 73365196. 11192809.
              -116049.
2 Events
                           43500.
                                     -2.67 0.0157
3 Score
              -965038.
                          162452.
                                     -5.94 0.0000127
#F-test p-value & r squared
lm_fit |> glance()
# A tibble: 1 x 12
  r.squared adj.r.squared
                            sigma statistic
                                               p.value
                                                          df logLik
                                                                      AIC
                                                                            BIC
      <dbl>
                    <dbl>
                            <dbl>
                                      <dbl>
                                                 <dbl> <dbl> <dbl> <dbl> <dbl> <
      0.777
                    0.752 926971.
                                       31.3 0.00000137
                                                           2 -317.
                                                                     641.
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
# analysis of variance table
lm_fit |> extract_fit_engine() |> anova()
Analysis of Variance Table
Response: ..y
         Df
                           Mean Sq F value
                                              Pr(>F)
                 Sum Sq
           1 2.3514e+13 2.3514e+13 27.365 5.645e-05 ***
Events
           1 3.0323e+13 3.0323e+13 35.289 1.273e-05 ***
Residuals 18 1.5467e+13 8.5927e+11
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Comments

Individual Slope Tests

```
#coeffecients
lm_fit |> tidy()
```

2 Events -116049. 43500. -2.67 0.0157 3 Score -965038. 162452. -5.94 0.0000127

For each predictor, we test $(H_0: \beta_i = 0)$ versus $(H_a: \beta_i \neq 0)$.

Predictor	Estimate	t-value	p-value	Decision
Events	-116,049	-2.668	0.0157	Significant
Score	-965,039	-5.940	$1.27{\times}10$	Significant

- For Events: (t = -2.67, p = 0.0157 < 0.05). We reject (H_0) and conclude that Events has a significant linear relationship with Earnings when Score is held constant.
- For Score: (t = -5.94, p < 0.001). We reject (H_0) and conclude that Score is also a significant linear predictor of Earnings when Events is held constant.

Thus, both predictors make significant contributions to explaining variation in Earnings.

F-Test

Hypotheses:

$$H_0: \beta_1 = \beta_2 = 0 H_a:$$
 At least one $\beta_j \neq 0$

$$F(2,18)=31.33, \quad p=1.374\times 10^{-6}$$

Because the p-value is less than 0.05, we reject H_0 . There is sufficient evidence that at least one of the slope coefficients differs from zero. Therefore, the regression model provides useful linear predictive information for Earnings.

Coefficient of Determination

The coefficient of determination is $(R^2 = 0.7768)$. This indicates that approximately 77.68% of the variability in Earnings is explained by the linear relationship with Events and Score.

Give the equation of the model and the equation of the fitted model

The regression model is given by:

Earnings =
$$73,365,196 - 116,049$$
(Events) $-965,039$ (Score)

Where:

- $\beta_0 = \text{Intercept} = 73,365,196$
- β_1 = Coefficient for Events = -116,049
- β_2 = Coefficient for Score = -965,039

The fitted model is given by:

```
E(Earnings \mid Events, Score) = 73,365,196 - 116,049(Events) - 965,039(Score)
```

Which of the independent variables, Events or Score, would you choose if you want only one predictor?

We think score makes more sense to use because a higher score in golf just means you played worse. That should impact the earnings as a lower score means one is golfing better, and in turn probably earned more.

Fit a model with the independent variable chosen (Score) from the previous step

```
fit_score = lm(Earnings ~ Score, data = golf)
summary(fit_score)
```

Call:

lm(formula = Earnings ~ Score, data = golf)

Residuals:

Min 1Q Median 3Q Max -1089495 -657702 -507083 282169 2653186

Coefficients:

Estimate Std. Error t value Pr(>|t|)

(Intercept) 81760015 12350070 6.620 2.47e-06 ***

Score -1125076 173581 -6.482 3.28e-06 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1066000 on 19 degrees of freedom Multiple R-squared: 0.6886, Adjusted R-squared: 0.6722 F-statistic: 42.01 on 1 and 19 DF, p-value: 3.279e-06

Comments

F-test

Hypotheses:

$$H_0: \beta_1 = 0$$
 vs $H_a: \beta_1 \neq 0$.

From the summary output:

$$F(1,19) = 42.01, \quad p = 3.279 \times 10^{-6}.$$

Because the p-value is less than 0.05, we reject (H_0) . There is sufficient evidence that the model provides useful linear predictive information for Earnings.

t-test

For the slope of Score:

$$t = -6.482, \quad p = 3.28 \times 10^{-6}.$$

Since (p < 0.05), we reject (H_0) and conclude that Score is a significant linear predictor of Earnings.

Coefficient of Determination

$$R^2 = 0.6886$$

Thus, approximately 68.86% of the variation in Earnings is explained by its linear relationship with Score.

Give the equation of the model and the equation of the fitted model.

Model Form: $E(\text{Earnings} \mid \text{Score}) = \beta_0 + \beta_1(\text{Score})$

Fitted Model: $\widehat{Earnings} = 81,760,015 - 1,125,076(Score)$

Where: - β_0 = Intercept = 81,760,015 - β_1 = Coefficient for Score = -1,125,076

Compare the model that uses both predictors and the model that just uses one predictor.

Model	Predictors	Adjusted (R^2)
Multiple Regression Simple Regression	Events and Score Score only	0.752 0.672

The multiple regression model with Events and Score explains a larger proportion of the variation in Earnings (adjusted $(R^2 = 0.752)$) than the simple regression model using only Score (adjusted $(R^2 = 0.672)$).

Because the increase in explained variability is meaningful and both predictors are significant in the multiple model, we prefer the multiple regression model. This model provides greater explanatory power while still maintaining a relatively simple structure with only two predictors.