CSC 212: Data Structures and Abstractions Ouick Sort

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Quick Sort

- Divide the array into **two** partitions (subarrays)
 - ' need to pick a *pivot* and rearrange the elements into two partitions
- · Conquer **Recursively** each half
 - ✓ call Quick Sort on each partition (i.e. solve 2 smaller problems)
- Combine Solutions
 - ' there is no need to combine the solutions

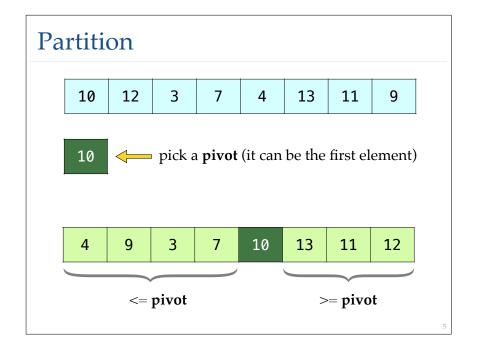
Quick Notes

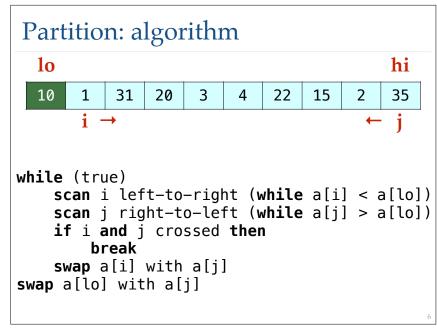
- Assignment 4 is out (recursion/stacks)
 - ✓ 1-2 students
 - √ time-consuming, start early
- · Problem Set
 - √ grading 60% completed
 - √ 2 submissions can't be graded properly
- Midterm Exam (timed)
 - √ past exams available
 - ✓ perhaps a Saturday/Monday review session?

Quick Sort: pseudocode

```
if (hi <= lo) return;
int p = partition(A, lo, hi);
quicksort(A, lo, p-1);
quicksort(A, p+1, hi);</pre>
```

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Partition: do it yourself 12 1 31 20 10 11 8 2 23 1 while (true) scan i left-to-right (while a[i] < a[lo]) scan j right-to-left (while a[j] > a[lo]) if i and j crossed then break swap a[i] with a[j]

swap a[lo] with a[j]

```
Partition: implementation
 int partition(int *A, int lo, int hi) {
     int i = lo;
     int j = hi + 1;
     while (1) {
         // while A[i] < pivot, increase i</pre>
         while (A[++i] < A[lo]) if (i == hi) break;
         // while A[i] > pivot, decrease j
         while (A[lo] < A[--j]) if (j == lo) break;
         // if i and j cross exit the loop
         if (i >= j) break;
         // swap A[i] and A[i]
         std::swap(A[i], A[i]);
     // swap the pivot with A[j]
     std::swap(A[lo], A[i]);
     // return pivot's position
     return i:
 }
```

Quick Sort: implementation

```
void r_quicksort(int *A, int lo, int hi) {
    if (hi <= lo) return;
    int p = partition(A, lo, hi);
    r_quicksort(A, lo, p-1);
    r_quicksort(A, p+1, hi);
}

void quicksort(int *A, int n, int m) {
    // shuffle the array
    std::random_shuffle(A, A+n);
    // call recursive quicksort
    r_quicksort(A, 0, n-1);
}</pre>
```

Animation

https://www.toptal.com/developers/ sorting-algorithms/quick-sort











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Analysis of Quick Sort

• Best-case

√ pivot partitions array evenly (almost never happens)

$$T(n) = 2T(n/2) + \Theta(n)$$

$$= \dots$$

$$= \Theta(n \log n)$$

Analysis of Quick Sort

→ Worst-case

√ input sorted, reverse order, equal elements

$$T(n) = T(n-1) + T(0) + \Theta(n)$$

$$= T(n-1) + \Theta(1) + \Theta(n)$$

$$= T(n-1) + \Theta(n)$$

$$= \dots$$

$$= \Theta(n^2)$$

can shuffle the array (to avoid the worst-case)

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Analysis of Quick Sort

- Average-case
 - √ analysis is more complex (assumes distinct elements)
 - Consider a 9-to-1 proportional split
 - Even a 99-to-1 split yields same running time
 - Faster than merge sort in practice (less data movement)

$$T(n) = T(9n/10) + T(n/10) + \Theta(n)$$

$$= \dots$$

$$= \Theta(n \log n)$$

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Comments on Quick Sort

- Properties
 - √ it is **in-place** but **not stable**
 - ✓ benefits substantially from code tuning
- Improvements
 - √ use insertion sort for small arrays
 - avoid overhead on small instances (~10 elements)
 - √ median of 3 elements
 - estimate true median by inspecting 3 random elements
 - √ three-way partitioning
 - create three partitions < pivot, == pivot, > pivot

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Sorting Algorithms

	Best-Case	Average- Case	Worst-Case	Stable?	In-place?
Selection Sort	θ(n²)	θ(n²)	θ(n²)	No	Yes
Insertion Sort	θ(n)	θ(n²)	θ(n²)	Yes	Yes
Merge Sort	θ(nlogn)	θ(nlogn)	θ(nlogn)	Yes	No
Quick Sort	θ(nlogn)	θ(nlogn)	θ(n²)	No	Yes

Empirical Analysis

Running time estimates:

- Home PC executes 108 compares/second.
- Supercomputer executes 1012 compares/second.

	insertion sort (N²)			mergesort (N log N)			quicksort (N log N)		
computer	thousand	million	billion	thousand	million	billion	thousand	million	billion
home	instant	2.8 hours	317 years	instant	1 second	18 min	instant	0.6 sec	12 min
super	instant	1 second	1 week	instant	instant	instant	instant	instant	instant

Lesson 1. Good algorithms are better than supercomputers.

Lesson 2. Great algorithms are better than good ones.

http://www.cs.princeton.edu/courses/archive/spring18/cos226/lectures/23Quicksort.pdf