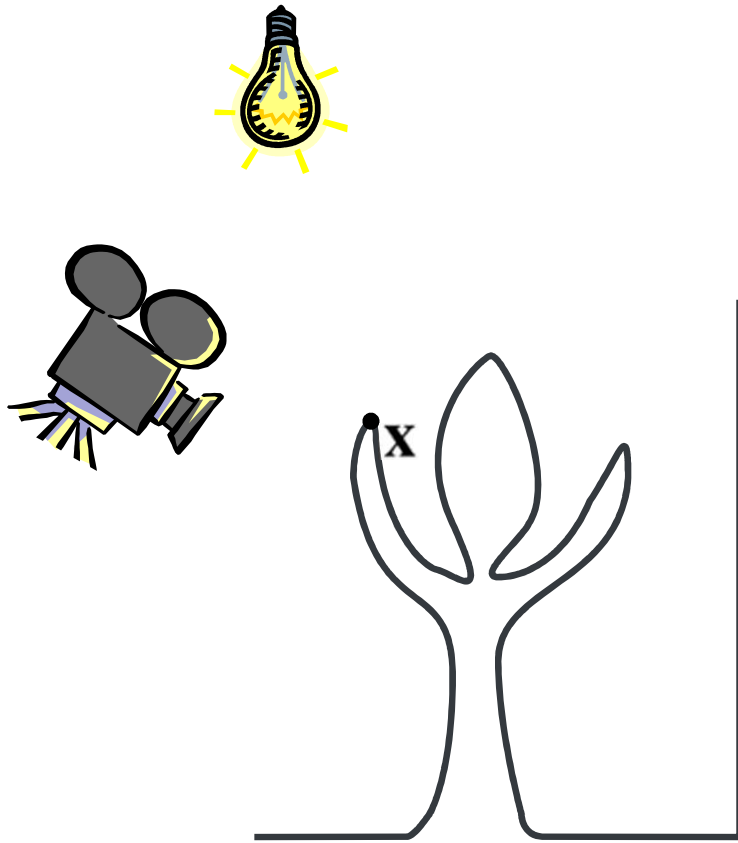


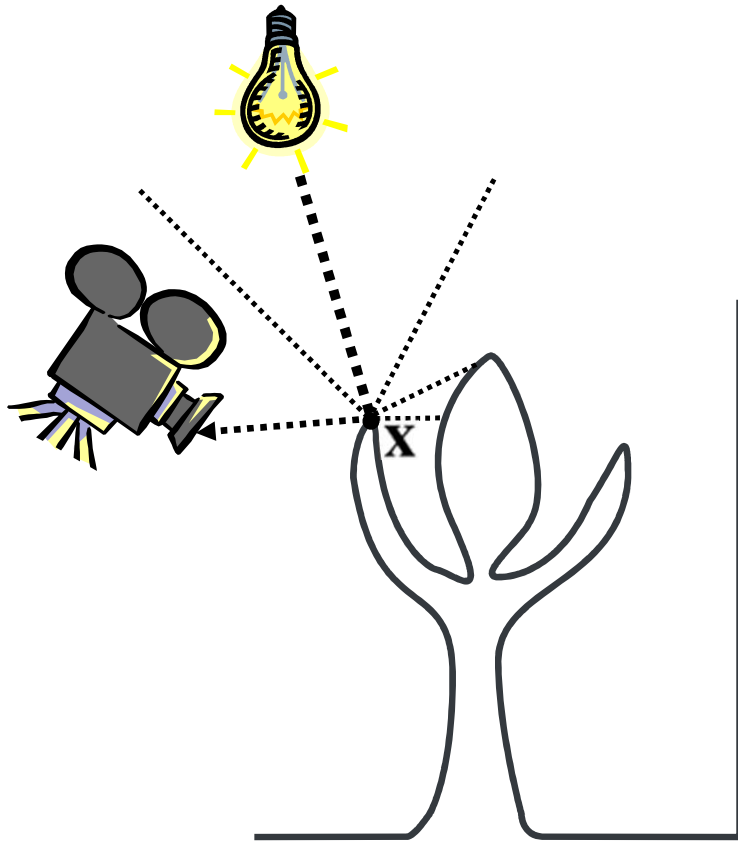
Global Illumination

Light Transport

Light Transport

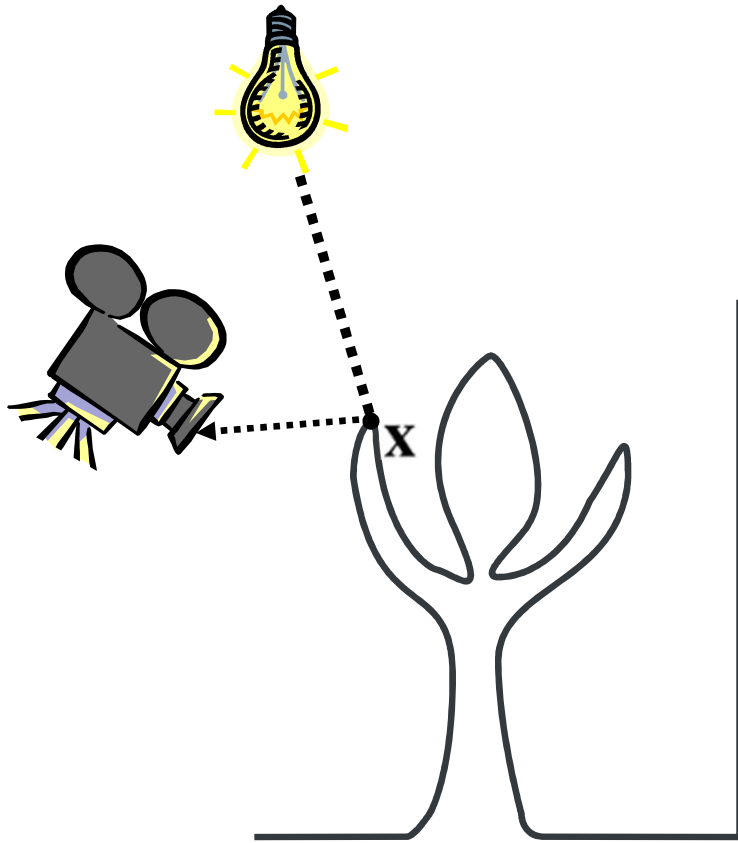


Light Transport

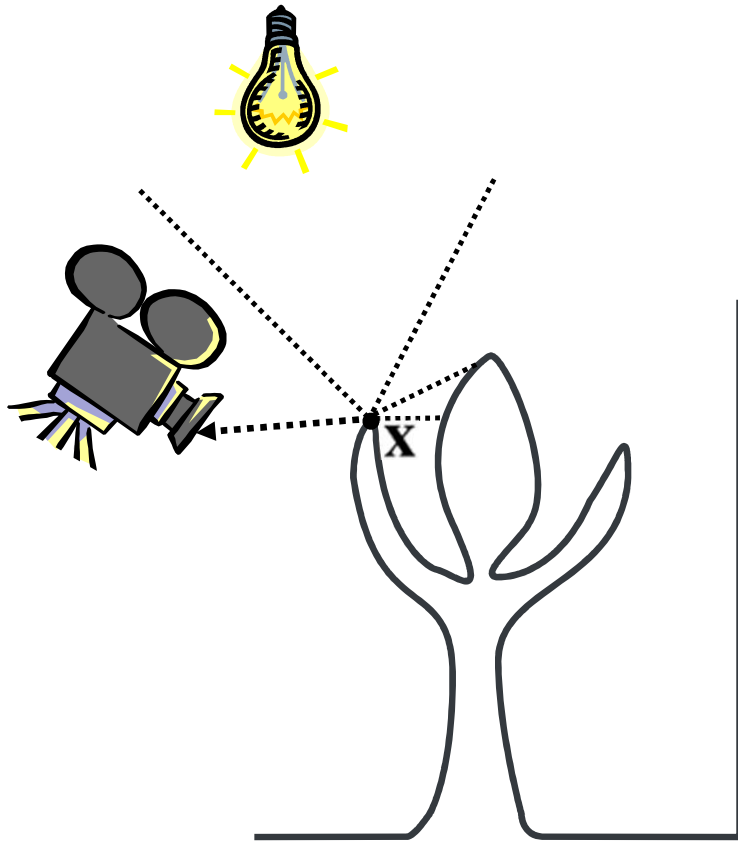


- Incident light arrives at **x**
- Calc outgoing radiance that arrives at the camera

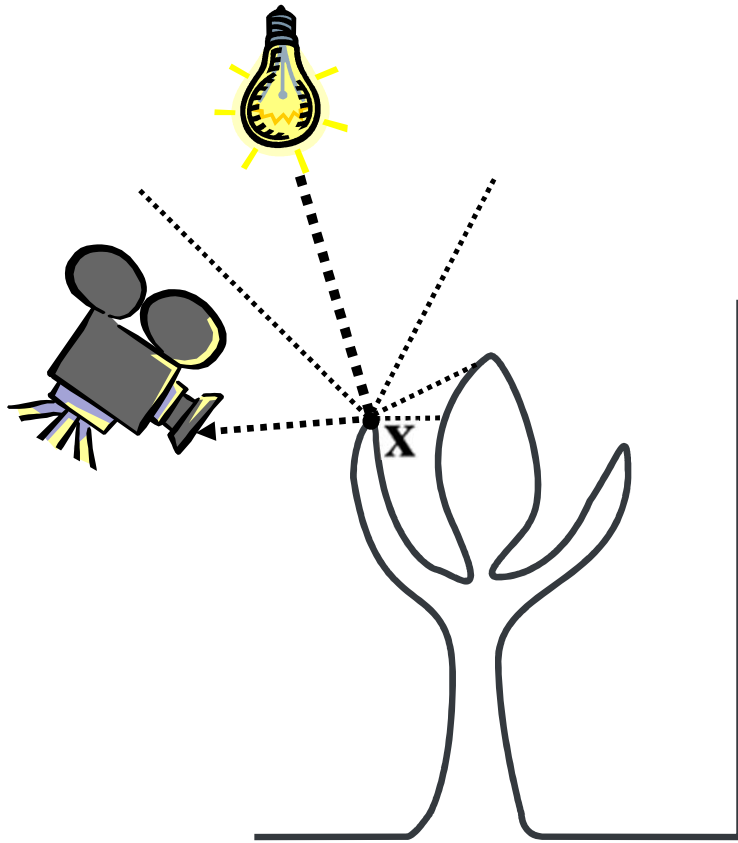
Light Transport – Direct



Light Transport – Indirect

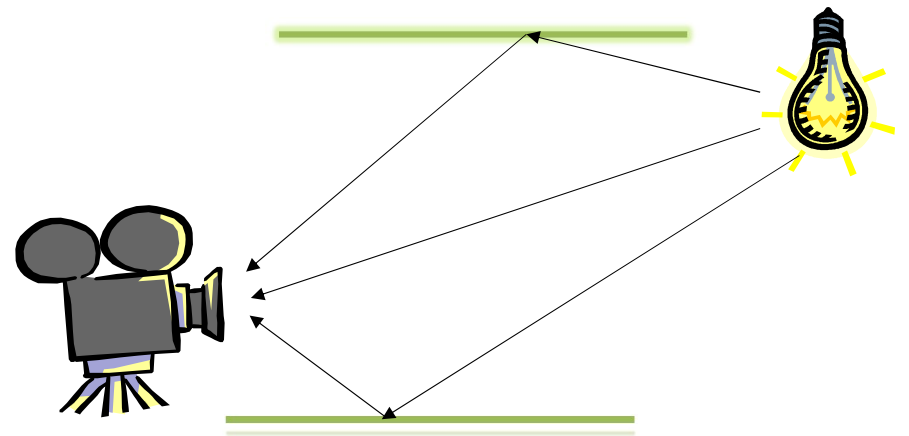


Light Transport



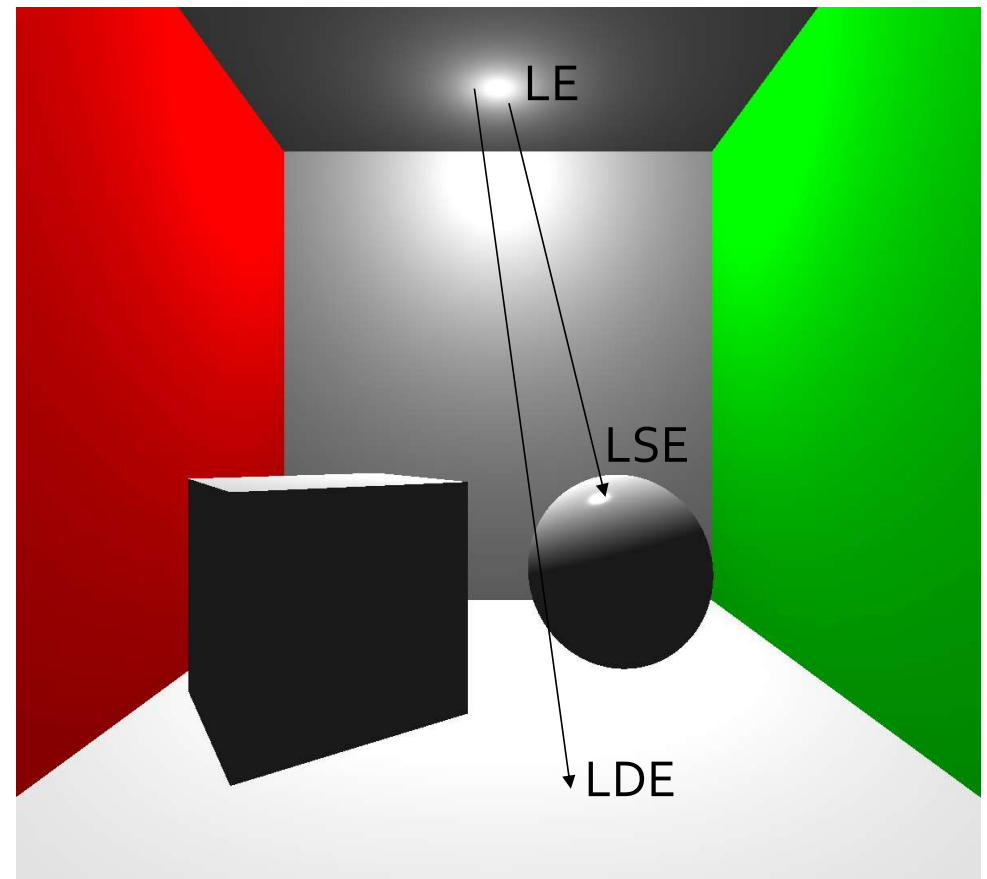
Classify Rendering Algorithms by Light Paths

- Paths
 - Start at a light source, L
 - End at the eye, E
- Two types of surface interactions
 - Pure diffuse, D
 - Pure specular, S
- Regular expressions $L(D|S)^*E$ describes all valid light paths



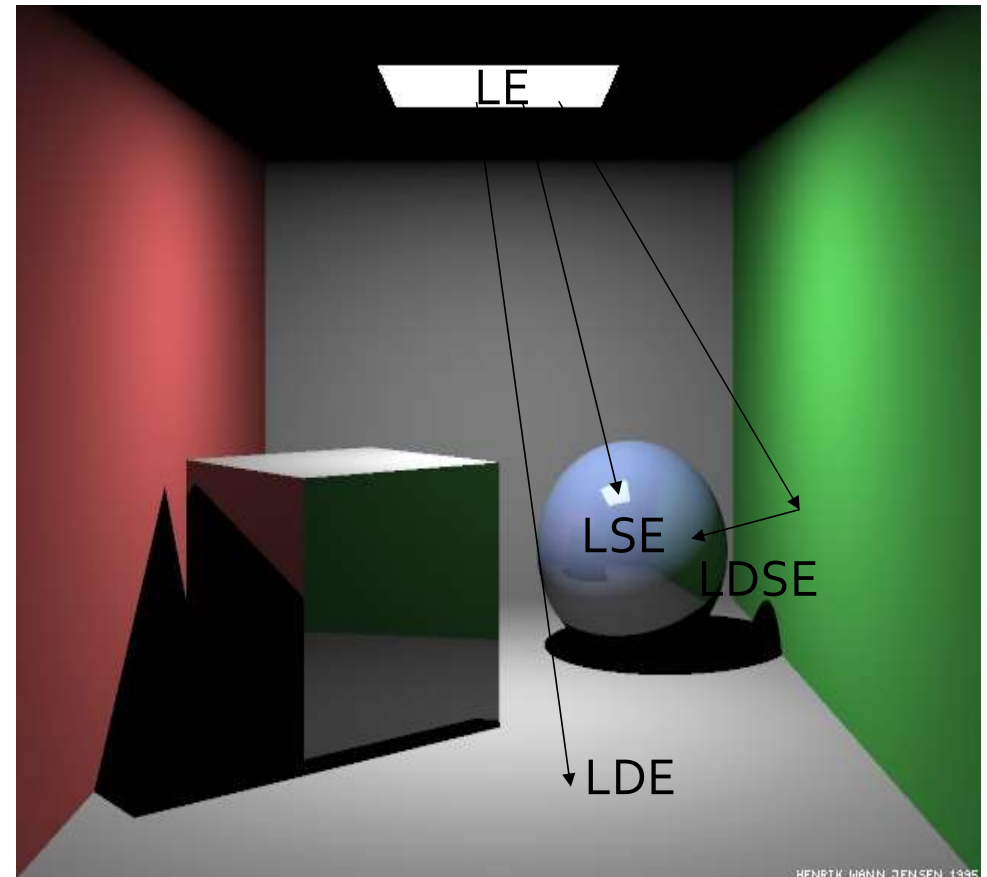
Light Path Examples – Local Illumination

- LE - from light to viewer
- LDE - from light to diffuse surface to viewer
- LSE - light is reflected off a specular surface into the viewer's eyes (only point lights)
- L(D|S)?E - light is reflected off either a diffuse surface or a specular surface or directly to the viewer



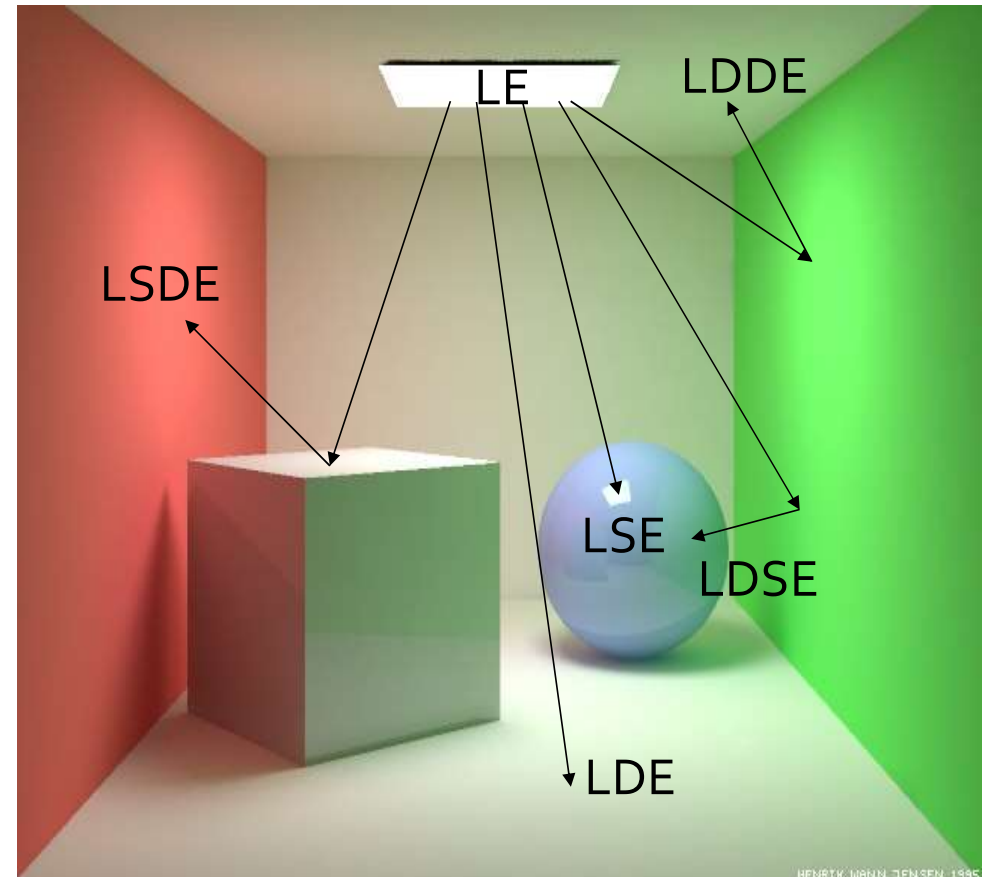
Light Path Examples – Classic Ray Tracing

- LDSE - light is reflected off a diffuse surface onto a specular surface toward the viewer
- LD?S*E - recursion of specular reflections optionally starting with a diffuse surface
- Simple light occlusion (hard shadows)



Light Path Examples – Path Tracer

- LSDE - light is reflected off a specular surface onto a diffuse surface toward the viewer (caustics)
- LDDE - light is reflected off a diffuse surface onto a diffuse surface toward the viewer (color bleeding)
- Complex light occlusion (soft shadows, ambient occlusion)

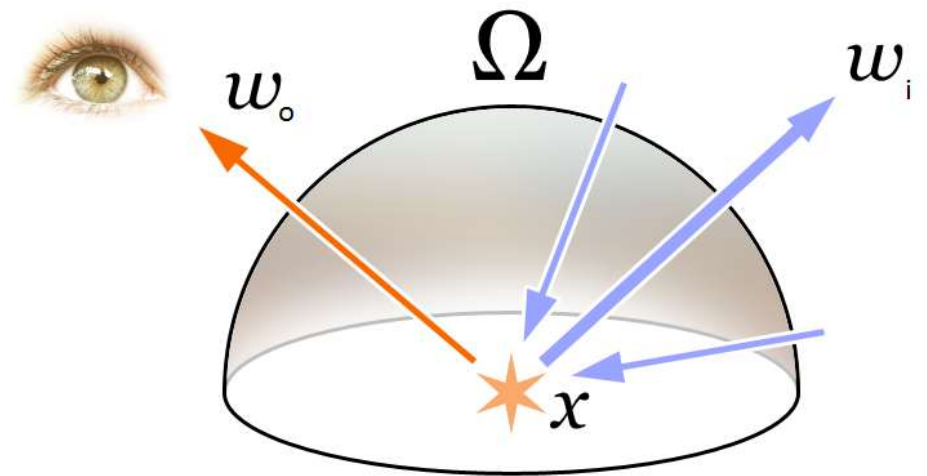


Global Illumination

The Rendering Equation

Rendering Equation [Kajiya86]

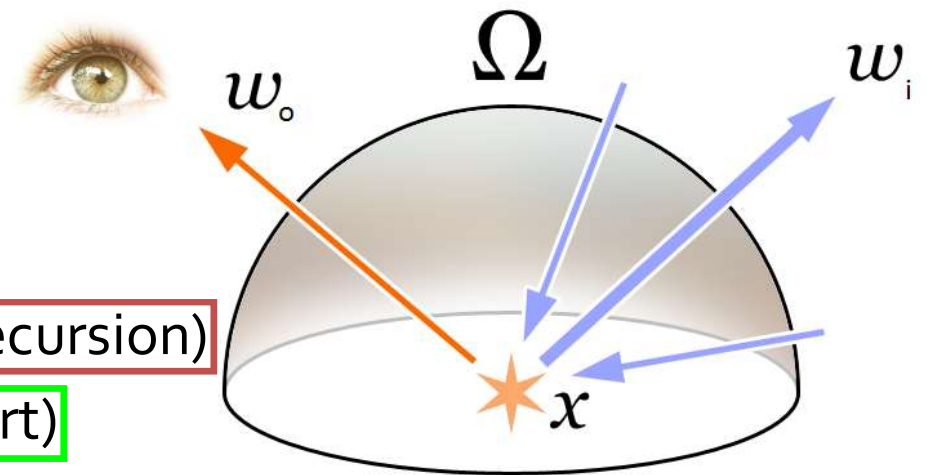
- Total amount of light emitted from a point \mathbf{x} along a particular viewing direction $\boldsymbol{\omega}_o$ at wavelength λ and time t



$$L_o(\mathbf{x}, \omega_o, \lambda, t) = L_e(\mathbf{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\mathbf{x}, \omega_i, \omega_o, \lambda, t) L_i(\mathbf{x}, \omega_i, \lambda, t) (\omega_i \cdot \mathbf{n}) d\omega_i$$

Rendering Equation [Kajiya86]

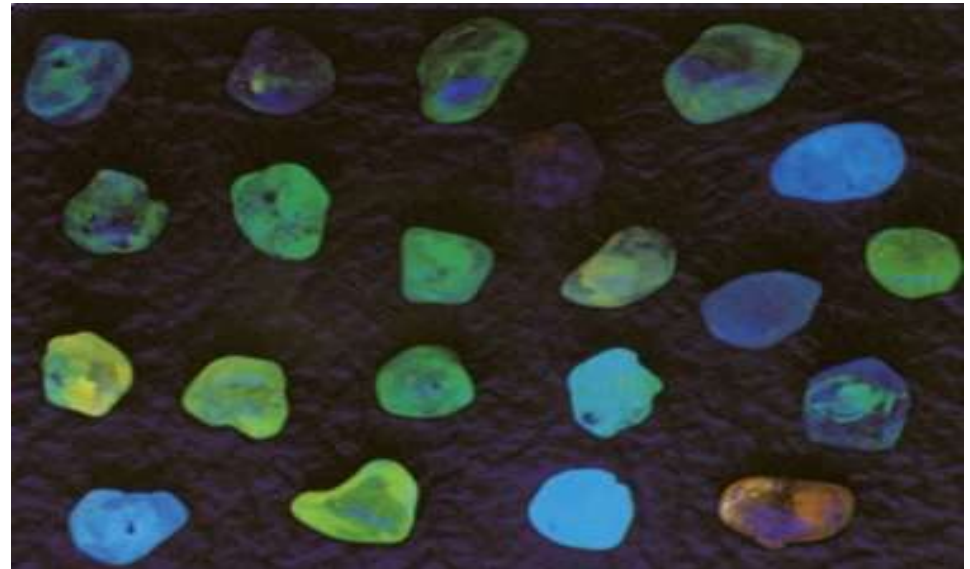
- Emitted energy
 - Outgoing light
 - Locally emitted light
 - Reflected incoming light
 - Surface reflection (BRDF)
 - Incoming light from direction ω_i (recursion)
 - Attenuation of inward light (Lambert)



$$L_o(\mathbf{x}, \omega_o, \lambda, t) = L_e(\mathbf{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\mathbf{x}, \omega_i, \omega_o, \lambda, t) L_i(\mathbf{x}, \omega_i, \lambda, t) (\omega_i \cdot \mathbf{n}) d\omega_i$$

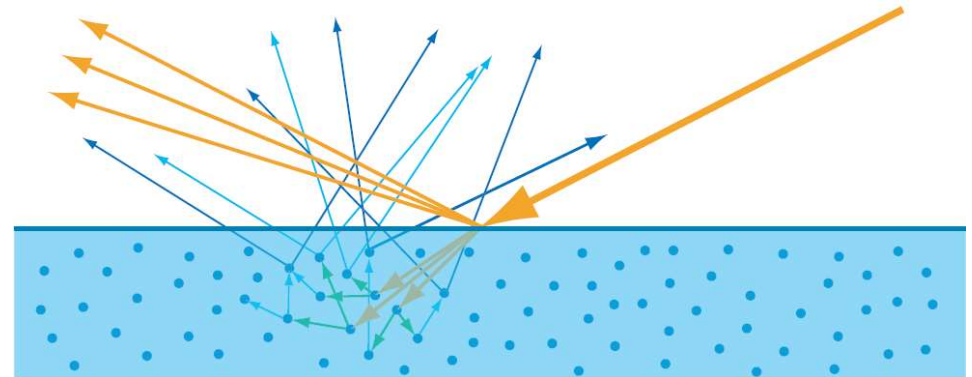
Rendering Equation – Missing Aspects

- **Phosphorescence**, which occurs when light is absorbed at one moment in time and emitted at a different time
- **Fluorescence**, where the absorbed and emitted light have different wavelengths



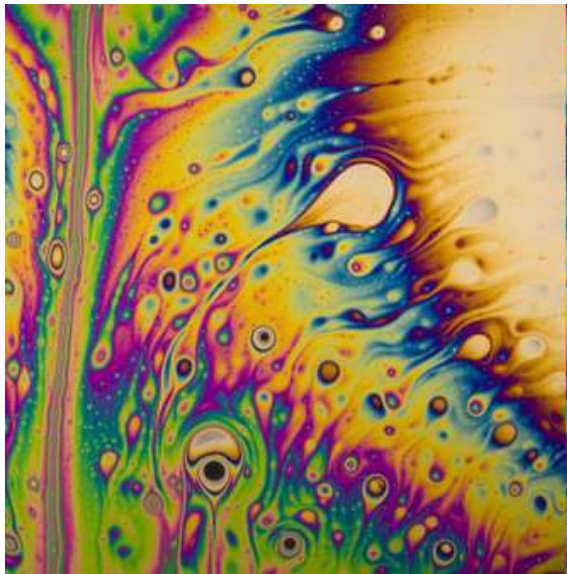
Rendering Equation – Missing Aspects

- **Interference**, where the wave properties of light are exhibited
- **Subsurface scattering**, where the spatial locations for incoming and departing light are different



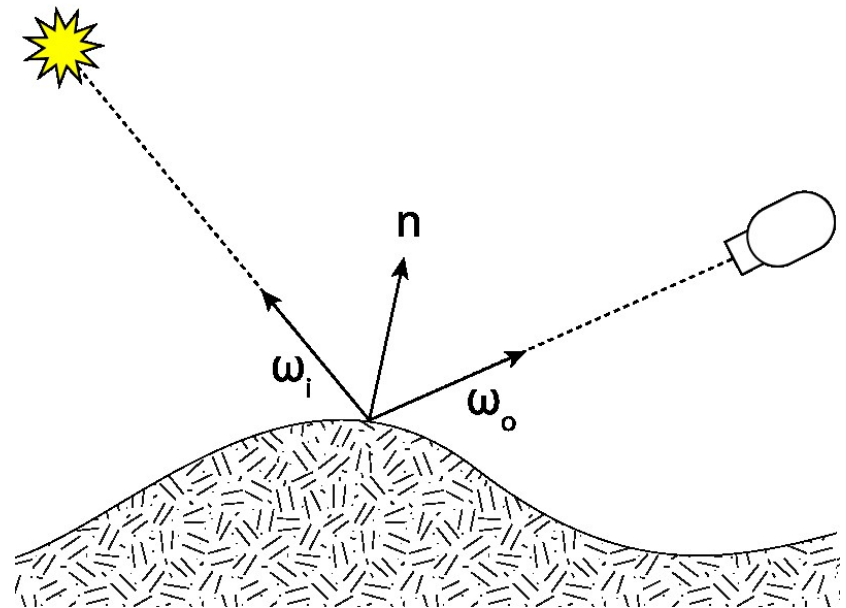
Rendering Equation – Missing Aspects

- **Interference**, where the wave properties of light are exhibited
- **Subsurface scattering**, where the spatial locations for incoming and departing light are different



Bidirectional reflectance distribution function

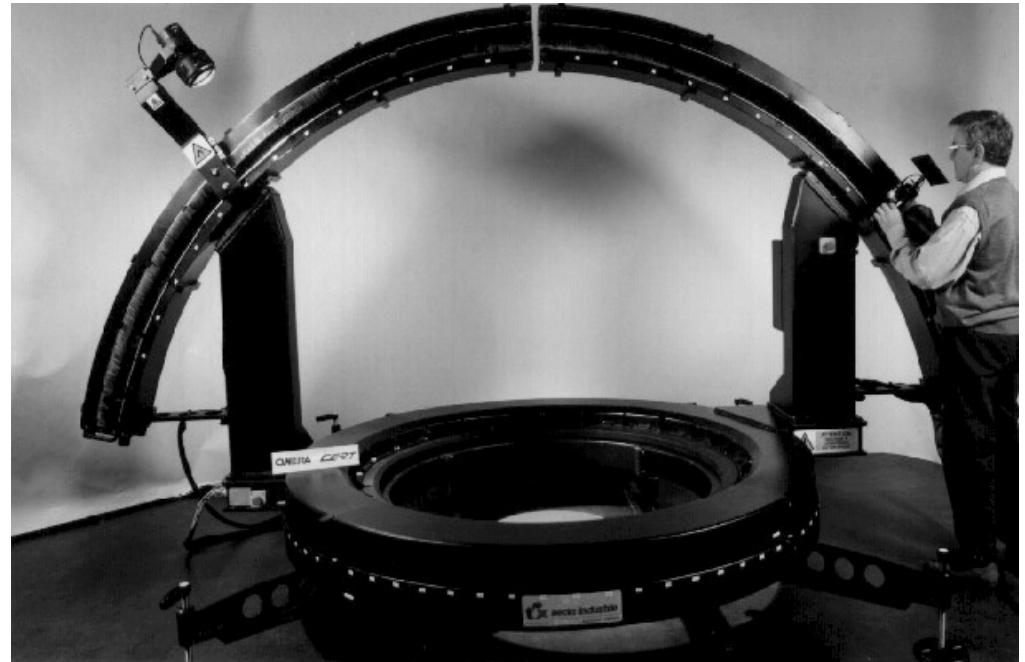
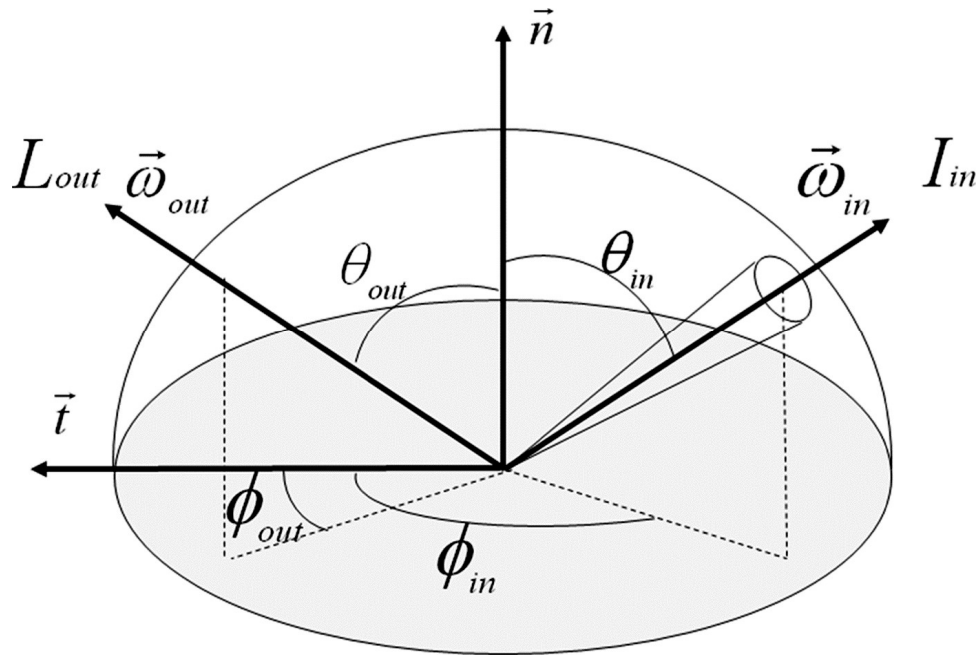
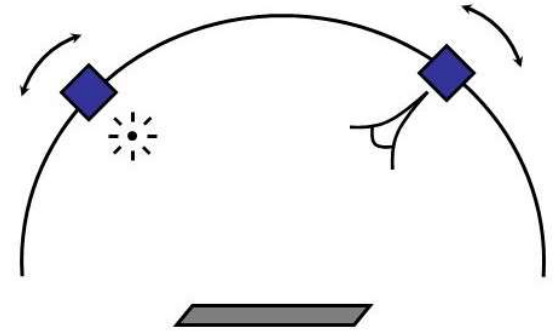
- Describes how light is reflected at an (opaque) surface (physical material)
- Different versions that depend on varying numbers of parameters
 - Incoming light direction ω_i
 - Outgoing light direction ω_o
 - [Surface position \mathbf{x} (spatially varying)]
 - Many more optional parameters for scattering, wavelength change, ...



$$L_o(\mathbf{x}, \omega_o, \lambda, t) = L_e(\mathbf{x}, \omega_o, \lambda, t) + \int_{\Omega} \boxed{f_r(\mathbf{x}, \omega_i, \omega_o, \lambda, t)} L_i(\mathbf{x}, \omega_i, \lambda, t) (\omega_i \cdot \mathbf{n}) d\omega_i$$

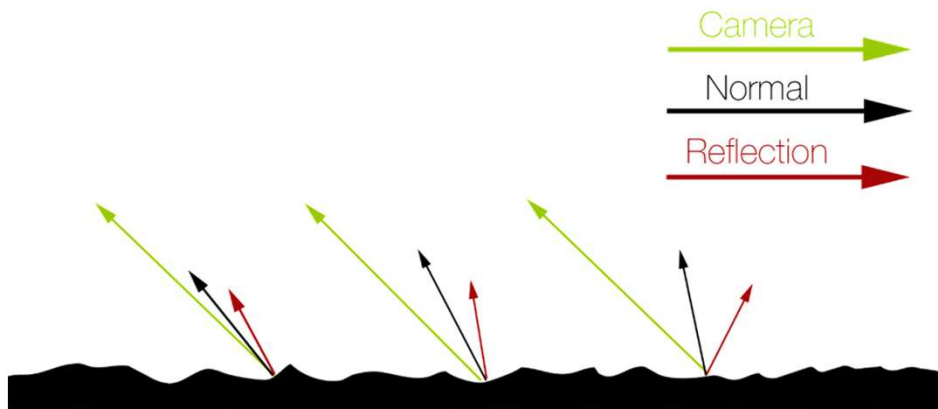
Measuring BRDFs

- Using real materials
- Often only 4D

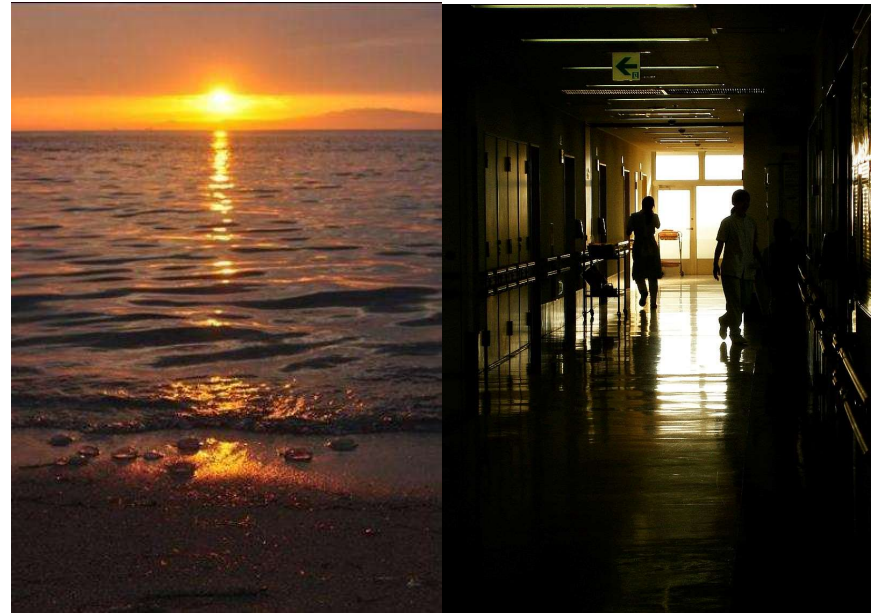


BRDF -Models

- *Lambertian*: perfectly diffuse (matte) surfaces with constant BRDF
- *Phong*: plastic-like specularity
- *Cook–Torrance*: specular-microfacet, Fresnel term, self-shadowing
- *Ward*: specular-microfacet, anisotropic
- *Oren–Nayar*: diffuse microfacet model

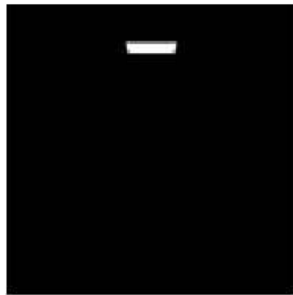
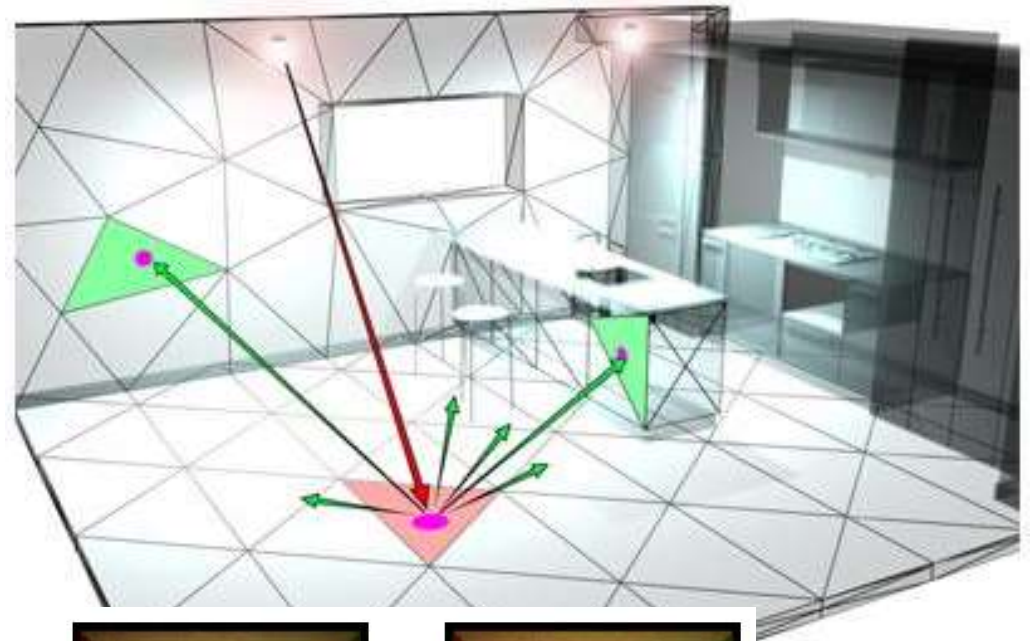


Microfacet BRDF



Solving the Rendering Equation – Radiosity

- Finite elements method
 - Recursive energy propagation between elements
- Soft shadows and indirect lighting
- View independent solution
- Only diffuse





Solving the Rendering Equation – Path Tracing

- Monte Carlo method
 - Numerical integration
 - Repeated random sampling
- Sample = follow one ray per pixel

