

# Integration of 75MW Solar PV Plant: Transmission System Design Analysis

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**Abstract**—This report presents the design and analysis of transmission system modifications required to integrate a new 75MW solar PV plant while addressing existing system reliability concerns. The study evaluates various transmission line and transformer options to determine the most cost-effective solution that maintains system stability under both normal and N-1 contingency conditions.

## I. INTRODUCTION

The integration of renewable energy sources into existing power grids presents technical challenges. We analyze the design requirements and potential solutions for integrating a new 75 MW utility-scale solar photo-voltaic (PV) facility into an existing 37-bus power system while also solving current reliability issues.

We aim to find the most cost-effective transmission system additions required to integrate 75 MW of solar generation at the NEWSOLAR substation. That goal is subordinate to the constraints of ensuring system reliability through dual transmission paths to the facility and resolving existing system violations identified using PowerWorld's contingency analysis.

The design must satisfy the following constraints. Bus voltages must be maintained between 0.95 and 1.10 per unit, while keeping all line flows below 100% of their thermal limits. The system must maintain stability under both normal operation and N-1 contingency conditions. Additionally, redundant transmission paths to the NEWSOLAR substation are required. The system must accommodate the solar plant operating at both full capacity (75 MW) and offline conditions.

Our approach incorporates contingency analysis, evaluation of available transmission corridors and voltage levels, and assessment of various conductor types and their associated costs. We consider transformer options and substation modifications. We conduct an economic analysis incorporating both capital costs and five-year loss reduction benefits.

Initial contingency analysis reveals specific reliability concerns in the OAK69-BUCKEYE69-APPLE69 corridor, which must be addressed alongside the integration of the new solar facility. The following sections detail the technical analysis, proposed solutions, and economic justification for the recommended design.

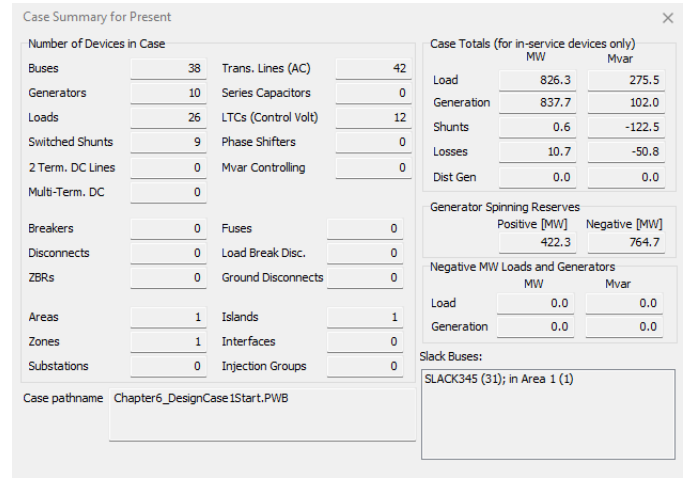
## II. INITIAL SYSTEM ANALYSIS

### A. Base Case Evaluation

The existing 37-bus system operates with a total load of 826.3 MW and 275.5 Mvar, served by ten generators producing 837.7 MW. System losses are approximately 10.7

MW, representing 1.3% of total generation, which indicates reasonably efficient power delivery under normal conditions. The system maintains adequate reactive power compensation through nine switched shunts, collectively providing -122.5 Mvar of reactive support.

PowerWorld's case summary for the existing system is shown in Figure 1



Case Summary for Present			
Number of Devices in Case			
Buses	38	Trans. Lines (AC)	42
Generators	10	Series Capacitors	0
Loads	26	LTCs (Control Volt)	12
Switched Shunts	9	Phase Shifters	0
2 Term. DC Lines	0	Mvar Controlling	0
Multi-Term. DC	0		
Breakers	0	Fuses	0
Disconnects	0	Load Break Disc.	0
ZBRs	0	Ground Disconnects	0
Areas	1	Islands	1
Zones	1	Interfaces	0
Substations	0	Injection Groups	0
Case pathname: Chapter6_DesignCase1Start.PWB			
Case Totals (for in-service devices only)			
	MW		Mvar
Load	826.3		275.5
Generation	837.7		102.0
Shunts	0.6		-122.5
Losses	10.7		-50.8
Dist Gen	0.0		0.0
Generator Spinning Reserves			
	Positive [MW]		Negative [MW]
	422.3		764.7
Negative MW Loads and Generators			
	MW		Mvar
Load	0.0		0.0
Generation	0.0		0.0
Slack Buses:			
SLACK345 (31); in Area 1 (1)			

Fig. 1. Case summary for existing system

### B. Contingency Analysis

PowerWorld's contingency analysis examines conditions when each element of the power system is taken offline. It reveals vulnerability in the 69 kV network in three contingency violations. Specifically, loss of either the PINE138 transformer or the PINE69-APPLE69 line results in overload, with the OAK69-BUCKEYE69 line experiencing loading up to 110.8% of its thermal limit. These violations suggest that the existing infrastructure is approaching its capacity limits.

These results are summarized in Table I. A zoomed-in view of the affected areas of the power system is shown in Figure 2.

## III. DESIGN

The design solution must incorporate new transmission infrastructure to connect the 75 MW solar facility at NEWSOLAR while simultaneously addressing existing problems. There must be redundant transmission paths to NEWSOLAR for reliability, meaning at least two separate transmission lines must be constructed. These lines can be either 69 kV or 138

TABLE I  
LINE VIOLATIONS IN CONTINGENCY ANALYSIS

Contingency	Flow(A)	Limit(A)	%
PINE138-PINE69 Xfmr:			
OAK69-BUCKEYE69	760.3	686.1	110.8
BUCKEYE69-APPLE69	454.2	418.4	108.6
PINE69-APPLE69 Line:			
OAK69-BUCKEYE69	699.2	686.1	101.9

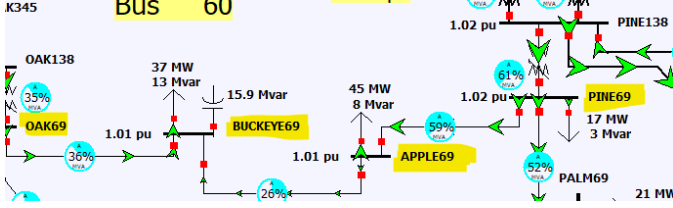


Fig. 2. Existing contingency violations - problem area

kV, with NEWSOLAR and all existing substations capable of accommodating either voltage level through installation of transformers. The system must maintain all bus voltages between 0.95 and 1.10 per unit and keep all line flows below their thermal limits under both normal operation and any single-contingency (N-1) scenario.

The optimal solution will minimize total cost, calculated as the construction costs minus any savings from reduced system losses over a 5-year period at \$60/MWh. Construction costs include both fixed components (\$1.25M for 138 kV or \$750k for 69 kV lines) and variable costs based on distance and conductor type. If 138 kV is utilized, additional costs include substation upgrades (\$900k per substation) and necessary transformers (\$1.5M for 101 MVA or \$1.8M for 168 MVA). The solution must resolve existing contingency violations, particularly the overloads observed in the OAK69-BUCKEYE69-APPLE69 corridor, while ensuring reliable operation both when the solar plant is at full output and when it is offline.

#### A. Transmission Line Parameters

A note on how to input transmission line parameters into PowerWorld is in order. Table A.4 in the text gives resistance in ohms per conductor per mile for 50°C at 60Hz as well as series inductance (ohms/mile/conductor for 1 foot spacing) and shunt capacitance (S/mile/conductor for 1 foot spacing). Resistance pulled from Table A.4 can be used directly in the "Calculate Impedances" dialog box in PowerWorld. But for 69kV lines, the three phases are spaced 2m apart and 4m apart for 138kV lines. We need a way to convert the 1-foot spacing parameters appropriately. Assuming equilateral spacing of lines, Equation 4.5.9 [1] in the text suggests a simple way to adjust series per-mile impedance from the table:

$$X_{2m} = X_{1ft} \cdot \frac{\ln\left(\frac{2 \times 3.28}{GMR}\right)}{\ln\left(\frac{1}{GMR}\right)} \quad (1)$$

where GMR comes from the same table for the conductor of interest.

Parameter	Rook	Crow	Condor
R ( $\Omega$ /mile)	0.1688	0.1482	0.1378
X ( $\Omega$ /mile)	0.6421	0.6352	0.6326
B (S/mile)	$6.63 \times 10^{-6}$	$6.71 \times 10^{-6}$	$6.78 \times 10^{-6}$

TABLE II  
TRANSMISSION LINE PARAMETERS AT 60 HZ, 2M SPACING

We calculate shunt susceptance similarly given the 1-foot spacing shunt reactance and outer diameter given in the table:

$$B_{2m} = \frac{\ln(1/r)}{X_{c1ft} \cdot \ln(2 \times 3.28/r)} \quad (2)$$

where  $r$  is the conductor's outer radius. Though these are stranded conductors, we treat them as solid since the associated error is small. Note that we multiply this value by 3 for 3 phases.

Table II shows parameters for the 69kV lines which go into PowerWorld's Impedance Calculator. We do not include the 138kV lines for reasons explained in the next section.

#### B. Candidate Solutions

Table III shows all possible NEWSOLAR connections to the network, given the provided set of right-of-way paths available to us. We include cost of installing the least expensive conductors (Rook for 69kV, Crow for 138kV) in the last column. Note that for any 138kV connections, we need to install a 138kV bus with 69-138 transformer at NEWSOLAR. This cost is included in Table III and suggests we can eliminate any solution involving those lines; we will connect NEWSOLAR exclusively with 69kV lines unless we are unable to meet the requirements.

The approach here is to start with the solution involving least total line distance (case 1). We move to solutions involving longer connections only if we run into contingency violations. Further, we use the least expensive conductors to start and upgrade only if needed.

Case number	Destination buses	Total distance (km)	Total Cost (M\$)
1	BK69, AP69	12	5.94
2	BK69, OAK69	19	8.53
3	BK69, OAK138	19	14.37
4	AP69, OAK69	19	8.53
5	AP69, OAK138	19	14.37
6	BK69, PINE69	20	8.90
7	BK69, PINE138	20	14.90
8	AP69, PINE69	20	8.90
9	AP69, PINE138	20	14.90
10	BK69, MP69	21	9.27
11	AP69, MP69	21	9.27
12	OAK69, PINE69	27	11.49
13	OAK69, PINE138	27	18.36
14	OAK138, PINE69	27	18.36
15	OAK138, PINE138	27	18.36
16	OAK69, MP69	28	11.86
17	OAK138, MP69	28	18.89
18	PINE69, MP69	29	12.23
19	PINE138, MP69	29	19.42

TABLE III  
POSSIBLE NEWSOLAR CONNECTIONS WITH LINE COSTS (M\$)

We found that simply installing connections to BUCKEYE and APPLE results in several contingency violations. These violations came from over-currents on the OAK-BUCKEYE line so we replaced that line with Crow conductors to ensure ample allowance for current. With the replaced line we saw no violations. We also saw no violations when we turned off the NEWSOLAR plant in this configuration.

We see significant power loss savings with this configuration. The screenshot in Figure 3 demonstrates new losses of 9.8MW, a savings of 0.9MW from the base case. To calculate the economic value of this improvement over the five-year period:

$$\text{Annual hours} = 365 \text{ days} \times 24 \text{ hours} = 8760 \text{ hours} \quad (3)$$

$$\begin{aligned} \text{Energy saved} &= 0.9 \text{ MW} \times 8760 \text{ hours/year} \times 5 \text{ years} \\ &= 39,420 \text{ MWh} \end{aligned} \quad (4)$$

$$\begin{aligned} \text{Cost savings} &= 39,420 \text{ MWh} \times \$60/\text{MWh} \\ &= \$2.37\text{M} \end{aligned} \quad (5)$$

The total cost for case 1 with this upgrade (and including the power loss savings) is shown in Table IV.

Case Summary for Present			
Number of Devices in Case			
Buses	38	Trans. Lines (AC)	44
Generators	10	Series Capacitors	0
Loads	26	LTCs (Control Volt)	12
Switched Shunts	9	Phase Shifters	0
2 Term. DC Lines	0	Mvar Controlling	0
Multi-Term. DC	0		
Breakers	0	Fuses	0
Disconnects	0	Load Break Disc.	0
ZBRs	0	Ground Disconnects	0
Areas	1	Islands	1
Zones	1	Interfaces	0
Substations	0	Injection Groups	0
Case path name: C:\Users\p\rent\OneDrive\Documents\U\Mass ECE\ECE590\termProject\ECE590\PowerWorld_files\case1_finalcheck.PWB			
Case Totals (for in-service devices only)			
Load	826.3	MW	275.5
Generation	836.9	MW	87.5
Shunts	0.6	Mvar	-122.2
Losses	9.8	MW	-65.7
Dist Gen	0.0	MW	0.0
Generator Spinning Reserves			
Positive [MW]	498.1	Negative [MW]	763.9
Negative MW Loads and Generators			
Load	0.0	MW	0.0
Generation	0.0	MW	0.0
Slack Buses:			
SLACK345 (31); in Area 1 (1)			

Fig. 3. Case summary for case 1 + upgrade

Modification	Cost (M\$)
<b>Replace OAK-BUCKEYE (69kV Crow)</b>	
Fixed Cost	0.75
Variable Cost (\$390,000/km for 8 km)	3.12
<b>Total</b>	<b>3.87</b>
<b>New Line NEWSOLAR-BUCKEYE (69kV Rook)</b>	
Fixed Cost	0.75
Variable Cost (\$370,000/km for 6 km)	2.22
<b>Total</b>	<b>2.97</b>
<b>New Line NEWSOLAR-APPLE (69kV Rook)</b>	
Fixed Cost	0.75
Variable Cost (\$370,000/km for 6 km)	2.22
<b>Total</b>	<b>2.97</b>
<b>Loss Savings (0.9 MW over 5 years)</b>	<b>-2.37</b>
<b>Grand Total</b>	<b>7.44</b>

TABLE IV  
COST BREAKDOWN FOR CASE 1 IMPLEMENTATION WITH  
OAK-BUCKEYE UPGRADE

We consider cases 2, 4, 6, 8, 10 and 11 as seen in Table III because their base cost is in the same neighborhood. Since it is difficult to predict power loss savings, due diligence requires at least a cursory examination. However, the cheapest 6km installation costs \$3M, so for any of these other cases to be preferred there must be no contingency violations. Any corrective line replacement will almost certainly make that option more expensive than case 1 with upgrade. Our approach to this analysis was to install all considered lines and alternately turn on or off the relevant lines, shown in Figure 4.

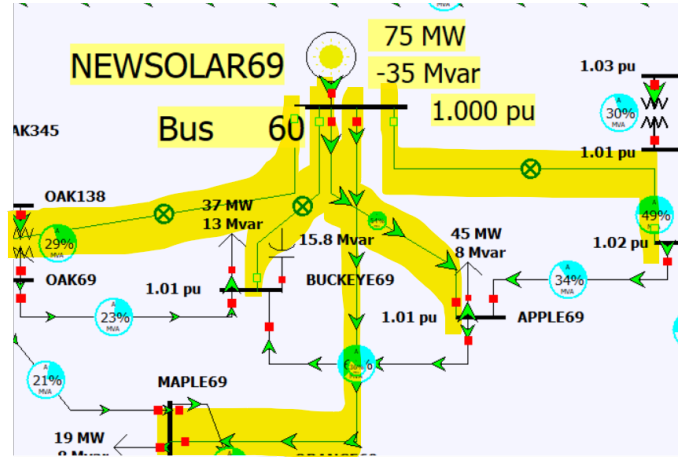


Fig. 4. Approach to multiple connection analysis

Case 2 shows four contingency violations related to undervoltage at the OAK 138 & 345 buses and overcurrent on the BUCKEYE-APPLE line. Case 4 shows the same undervoltage violations as case 2. Case 6 results in the same overcurrent violation observed in the base case (though only when NEWSOLAR is turned off). Cases 8, 10 and 11 all cause overcurrent contingency violations. To correct any of these issues, we would need to install a minimum of 6km of Rook conductors. That makes all these cases more expensive than case 1 plus upgrade.

For due diligence we probed our case 1 + upgrades solution for even more cost effective solutions. We discovered that dropping the OAK-BUCKEYE line upgrade but installing a new Rook 69kV line from APPLE to ORANGE improves power loss while requiring only 1 additional km of line. This configuration throws no contingency violations with NEWSOLAR on or off. Figure 5 shows the lines we installed. There are no upgrades outside of installed lines. Figure 6 shows a new loss of 9.7MW.

Further analysis revealed that this configuration provides several advantages over the previous solution. It eliminates the need to replace the existing OAK-BUCKEYE line, reducing construction complexity and avoiding potential service interruptions during upgrades. The new APPLE-ORANGE connection creates an alternative power flow path that naturally redistributes power flow during contingencies, resulting in slightly better loss reduction (1.0 MW versus 0.9 MW). Table

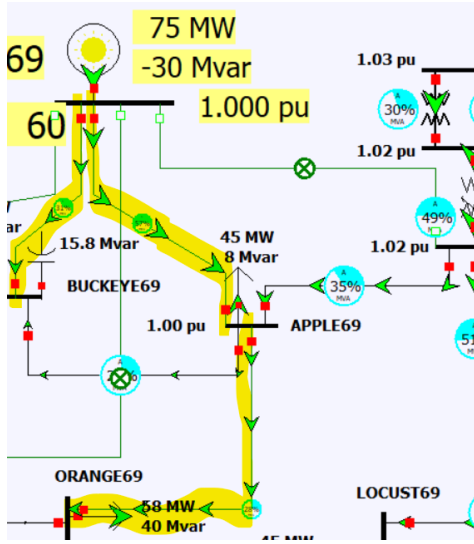


Fig. 5. Schematic of final solution: case 1 + APPLE-ORANGE

Case Summary for Present			
Number of Devices in Case		Case Totals (for in-service devices only)	
Buses	38	Trans. Lines (AC)	48
Generators	10	Series Capacitors	0
Loads	26	LTCs (Control Volt)	12
Switched Shunts	9	Phase Shifters	0
2 Term. DC Lines	0	Mvar Controlling	0
Multi-Term. DC	0		
Breakers	0	Fuses	0
Disconnects	0	Load Break Disc.	0
ZBRs	0	Ground Disconnects	0
Areas	1	Islands	1
Zones	1	Interfaces	0
Substations	0	Injection Groups	0
Case pathname: case2upfinalcheck.PWB			
		Generator Spinning Reserves	
		Positive [MW]	Negative [MW]
		498.3	763.7
		Negative MW Loads and Generators	
		MW	Mvar
		Load	0.0
		Generation	0.0
		Slack Buses:	
		SLACK345 (31); in Area 1 (1)	

Fig. 6. Case summary for final solution: case 1 + APPLE-ORANGE

V demonstrates a modest cost savings over the previous solution, making this our preferred design. Table V demonstrates a slim savings over the previous solution of about \$50k. We choose this as our final solution since it meets all other design criteria.

#### IV. CONCLUSION

Through systematic analysis of 19 possible configurations for the new 75 MW solar facility, we determined that the most cost-effective solution is to connect NEWSOLAR to both BUCKEYE69 and APPLE69 substations using 69 kV lines with Rook conductors, while adding a new 69 kV Rook line between APPLE69 and ORANGE69. This configuration, costing \$7.39M, represents the optimal balance between reliability requirements and economic constraints.

The decision to use exclusively 69 kV connections was driven by the substantial cost premium associated with 138 kV options, which required additional substation infrastruc-

Modification	Cost (M\$)
<b>New Line NEWSOLAR-BUCKEYE (69kV Rook)</b>	
Fixed Cost	0.75
Variable Cost (\$370,000/km for 6 km)	2.22
<b>Total</b>	<b>2.97</b>
<b>New Line NEWSOLAR-APPLE (69kV Rook)</b>	
Fixed Cost	0.75
Variable Cost (\$370,000/km for 6 km)	2.22
<b>Total</b>	<b>2.97</b>
<b>New Line APPLE-ORANGE (69kV Rook)</b>	
Fixed Cost	0.75
Variable Cost (\$370,000/km for 9 km)	3.33
<b>Total</b>	<b>4.08</b>
<b>Loss Savings (1.0 MW over 5 years)</b>	<b>-2.63</b>
<b>Grand Total</b>	<b>7.39</b>

TABLE V  
COST BREAKDOWN FOR FINAL SOLUTION WITH APPLE-ORANGE CONNECTION

ture and more expensive conductors. While several other 69 kV configurations appeared comparable in cost, all required remedial upgrades to address contingency violations that ultimately made them more costly than our chosen solution. The addition of the APPLE69-ORANGE69 line provides an alternative power flow path that effectively resolves the existing contingency violations while avoiding the need to upgrade the OAK69-BUCKEYE69 line. This configuration maintains stability under all N-1 contingency scenarios both with NEWSOLAR at full output and when offline.

This design successfully achieves all project objectives: it provides redundant transmission paths to the solar facility, resolves existing system violations, maintains system stability under N-1 contingency conditions, and does so at minimum cost. The solution's use of standard components and strategic placement of the new APPLE69-ORANGE69 line not only reduces initial capital costs but also provides better loss reduction, saving an additional 0.1 MW compared to alternative solutions. The simplicity of using consistent conductor types (Rook) for all new lines should also facilitate maintenance and reduce implementation complexity.

#### REFERENCES

- [1] J. D. Glover, M. S. Sarma, and T. J. Overbye, *Power Systems Analysis and Design*, 4th ed. Stamford, CT: Cengage Learning, 2007.