

Computer Animation and Simulation

Plants

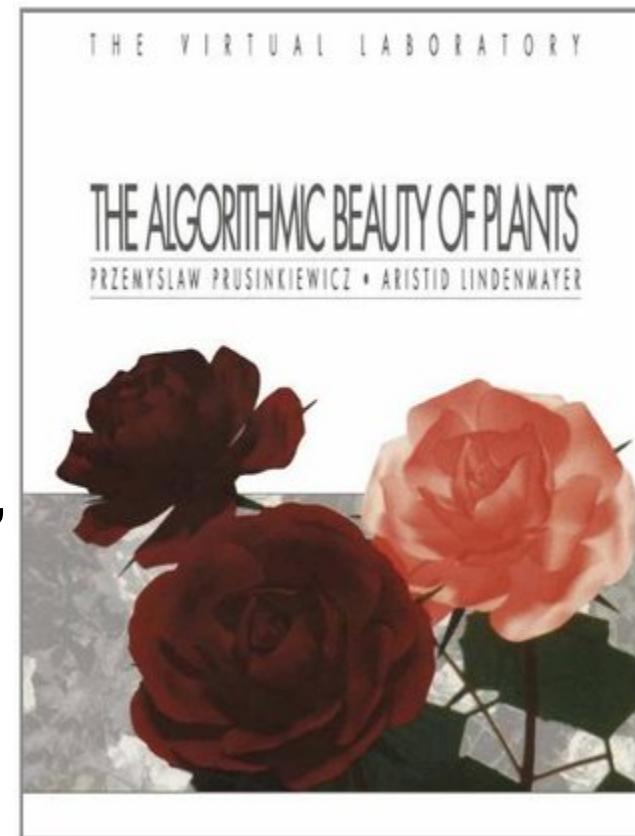
Context

▶ Natural Phenomena

- Plants
- Gaseous phenomena
 - Fire
 - Smoke
 - Clouds
- Water
- ...

Plants

- ▶ Particle systems
- ▶ Fractals
- ▶ 3D Modelling
- ▶ L-systems
 - Lindenmayer Systems
 - “*The Algorithmic Beauty of Plants*” (Prusinkiewicz + Lindenmayer)

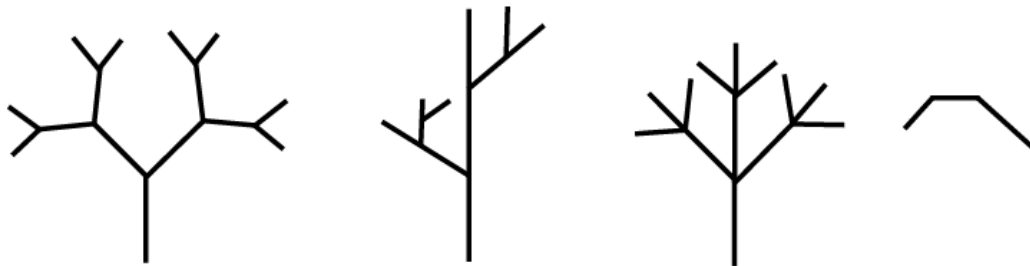


Topology

- ▶ growth from a single source point
- ▶ branching structure over time
 - individual structural elements elongate
 - self-similarity under scale (cf. fractals)



Basic branching schemes



Structures resulting from repeated application of a single branching scheme

Structural Components

Simplifications for graphics modelling vs botany

- ▶ roots
 - not visual, so not important
- ▶ stems and branches
 - above ground, grow upward and bear leaves
- ▶ buds
 - embryonic state of stems, leaves and flowers
 - terminal vs lateral bud
 - vegetative, flower or dormant buds
- ▶ leaves
 - alternate, opposite, whorled pattern
- ▶ flowers

Growth of a Cell Influenced by...

- ▶ lineage
 - growth controlled by age
 - older cells always larger than younger cells
- ▶ cellular descent
 - growth by passing of nutrients and hormones from adjacent cells
 - ends of plants growing more than interior sections
- ▶ tropisms
 - external influences changing the direction of growth
 - phototropism (bending toward light), geotropism (responding to gravity)
- ▶ physical obstacles
 - affect shape and growth

Modelling

L-systems

- ▶ mathematical model (< Astrid Lindenmayer)
 - set of production rules of the form $\alpha_i \rightarrow \beta_i$
 - α_i predecessor, single symbol
 - β_i successor, sequence of symbols
- ▶ parallel rewriting system
 - sequence of symbols given as initial string (i.e. axiom)
 - apply production rules to string, in parallel
 - rewrite each occurrence of α_i as β_i
 - identity rule for symbols without production rule
 - result of productions is a new string
 - repeat iteratively until no production rules can be applied

Parallel Rewriting System

- ▶ assume following production rules
 - $S \rightarrow ABA$
 - $A \rightarrow XX$
 - $B \rightarrow TT$
- ▶ generated string sequence
 1. S (= axiom)
 2. ABA
 3. $XXTTXX$
- ▶ interpret strings to generate images

Geometric Interpretation

Geometric replacement

▶ symbol \rightarrow geometric element

▶ Example

S \rightarrow ABA

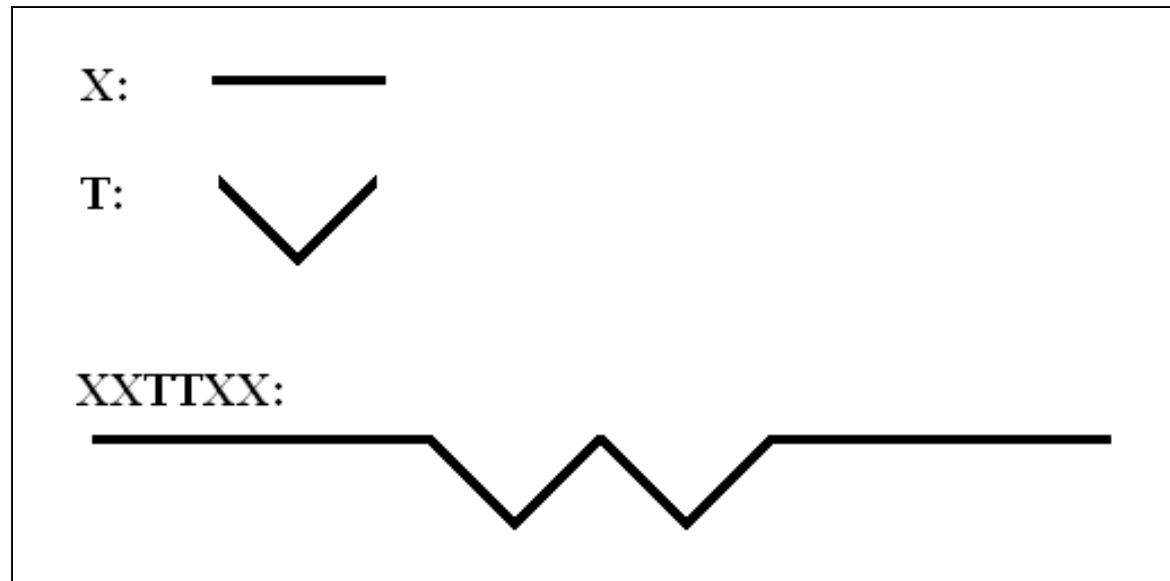
A \rightarrow XX

B \rightarrow TT

1. S

2. ABA

3. XXTTXX



Geometric Interpretation

Turtle graphics

- ▶ symbols are interpreted as drawing commands

The turtle obeys to the following commands:

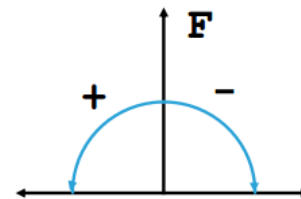
- F** draw a line of length d , the state changes to $(x+d \cos\alpha, y+d \sin\alpha, \alpha)$
- f** move forward a step of length d without drawing
- +** turn left by angle δ , the state changes to $(x, y, \alpha+\delta)$
- turn right by angle δ , the state changes to $(x, y, \alpha-\delta)$

Starting conditions for the turtle:

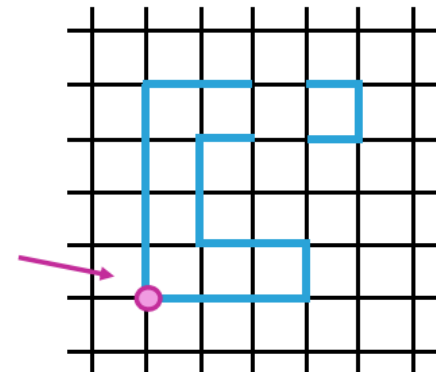
Initial state, d and δ

Example: **FFFF-FFfF-F-FfF+FF+FF-F-FFF**

$d=1, \delta=90^\circ$



start



Geometric Interpretation


Turtle graphics

$S \rightarrow ABA$
 $A \rightarrow FF$
 $B \rightarrow TT$
 $T \rightarrow -F++F-$


Production rules

S ← axiom
 ABA
 $FFTTF$
 $FF-F++F--F++F-FF$

Sequence of strings produced from the axiom

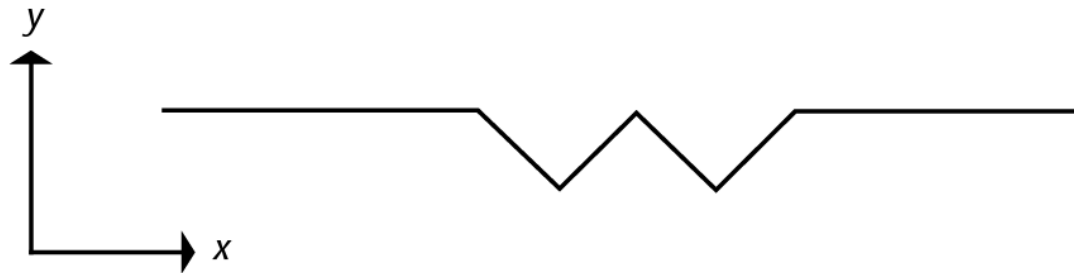
$d =$ 

$\delta = 45^\circ$

reference direction: 

initial state: (10, 10, 0)

Initial conditions



Geometric Interpretation

Turtle graphics

- ▶ using the turtle commands as alphabet
- ▶ construction of Koch's island

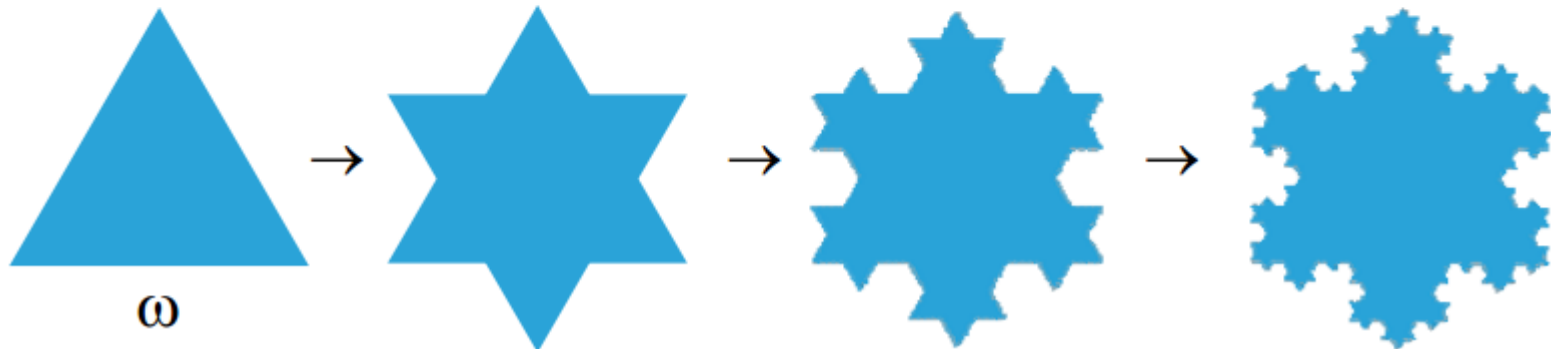
$\delta = 60^\circ$, d depends on derivation length

$\omega = \mathbf{F--F--F}$

//Initiator

$\mathbf{F} \rightarrow \mathbf{F+F--F+F}$

//Generator



D0L-systems

- ▶ simplest class of L-system
 - see previous examples
- ▶ deterministic
 - predecessor α_i appears only once on the left-hand side of a production rule
- ▶ context free
 - no context-sensitive production rules

$S \rightarrow ABA$

$A \rightarrow XX$

$B \rightarrow TT$

Production rules

S

ABA

XXTTXX

String sequence

← axiom

Bracketed L-systems

- ▶ L-systems up till now only linear
- ▶ brackets [and] used to mark the beginning and end of additional offshoots from the main lineage
- ▶ stack of turtle graphics is used, brackets push and pop states onto the stack
 - [= push state
 -] = pop state

Bracketed L-systems

$S \rightarrow FAF$

$A \rightarrow [+FBF]$

$A \rightarrow F$

$B \rightarrow [-FBF]$

$B \rightarrow F$

(non-deterministic in this case:
so, random choice of production
rule)

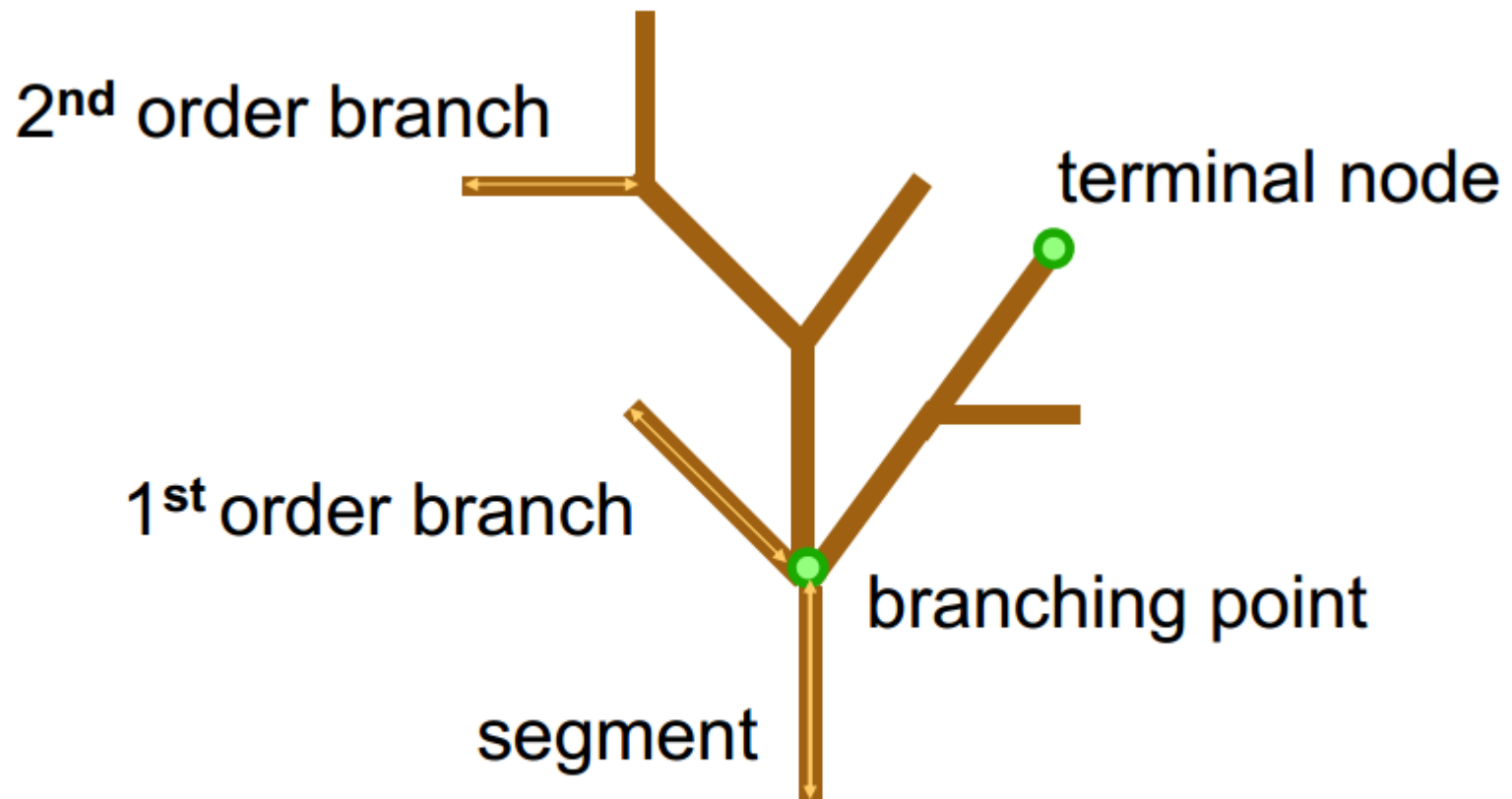
FAF

$F[+FBF]F$

$F[+F[-FFF]F]F$



Bracketed L-systems



$F [+F] [-F [-F] F] F [+F [+F] [-F]] [-F]$

Bracketed L-systems



$$n=5, \delta=25.7^\circ$$

$$\omega:F$$

$$F \rightarrow F [+F] F [-F] F$$



$$n=5, \delta=20^\circ$$

$$\omega:F$$

$$F \rightarrow F [+F] F [-F] [F]$$

Bracketed L-systems

Node replacement

$n=7, \delta=20^\circ$

$\omega: \mathbf{X}$

$\mathbf{X} \rightarrow \mathbf{F}[+\mathbf{X}]\mathbf{F}[-\mathbf{X}]+\mathbf{X}$

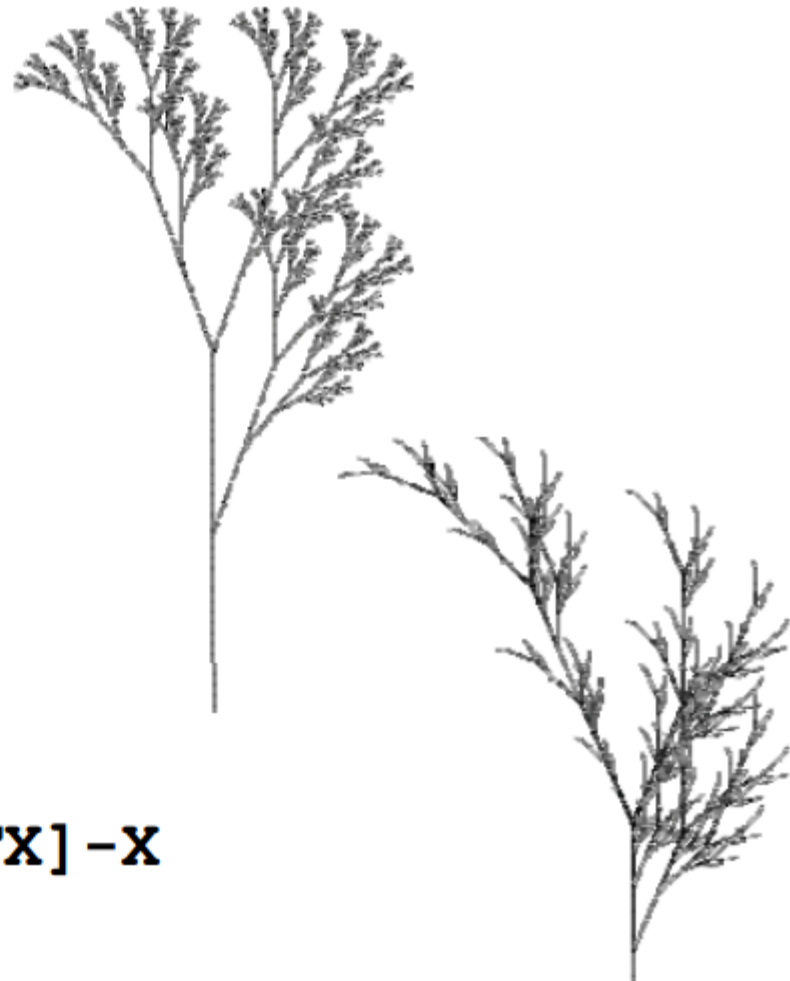
$\mathbf{F} \rightarrow \mathbf{FF}$

$n=5, \delta=22.5^\circ$

$\omega: \mathbf{X}$

$\mathbf{X} \rightarrow \mathbf{F}-[[\mathbf{X}]+\mathbf{X}]+\mathbf{F}[+\mathbf{FX}]-\mathbf{X}$

$\mathbf{F} \rightarrow \mathbf{FF}$



Stochastic L-systems

- ▶ assign probabilities to nondeterministic L-systems
 - probabilities of production rules with same predecessor sum up to 1
 - id: pred \rightarrow succ : probability
- ▶ example

$S_{1.0}$	\rightarrow	FAF	
$A_{0.8}$	\rightarrow	[+FBF]	// $A_{0.8}$ [+FBF] : 0.8
$A_{0.2}$	\rightarrow	F	
$B_{0.4}$	\rightarrow	[-FBF]	
$B_{0.6}$	\rightarrow	F	

Stochastic L-systems

ω : **F**

P_1 : **F** $^{0.33} \rightarrow$ **F** **[+F]** **F** **[-F]** **F**

P_2 : **F** $^{0.33} \rightarrow$ **F** **[+F]** **F**

P_3 : **F** $^{0.33} \rightarrow$ **F** **[-F]** **F**



Context Sensitive L-systems

- ▶ specify a context, in which the predecessor must appear in order for the production rule to be applicable

id: `left-side_context` < pred > `right-side_context` \longrightarrow succ : prob

- ▶ n left-side and m right-side context symbols
 - (n, m) L-systems

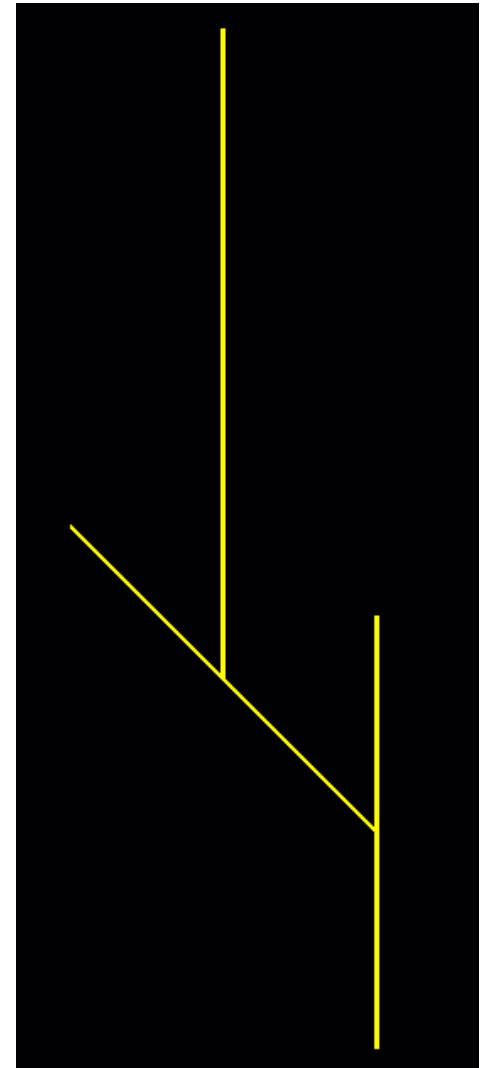
Context Sensitive L-systems

- ▶ production rules

$$\begin{array}{lll} S & \longrightarrow & FAT \\ A > T & \longrightarrow & [+FBF] \\ A > F & \longrightarrow & F \\ B & \longrightarrow & [-FAF] \\ T & \longrightarrow & F \end{array}$$

- ▶ string sequence

1. S
2. FAT
3. F[+FBF]F
4. F[+F[-FAF]F]F
5. F[+F[-FFF]F]F



Context Sensitive L-systems

- ▶ used to simulate the propagation of signals like hormones and nutrients

ω : baaaaaaaa

p_1 : b < a \rightarrow b

p_2 : b \rightarrow a

baaaaaaaa

abaaaaaaaa

aabaaaaaaaa

aaabaaaaa

aaaabaaa

aaaaabaa

aaaaaaba

Animation

Types of Animation

- ▶ flexible movement of static structure
 - e.g., plant being subjected to wind
 - see chapter “*physically-based animation*”
- ▶ changes in topology during growth
 - modeled by L-system as the application of a production that encapsulates a branching of the form $A \rightarrow F[+F]B$
- ▶ elongation of existing structures
 - modeled by productions of the form $F \rightarrow FF$
 - uniform growth
 - no criteria to stop
 - \Rightarrow solution: introduce parameters into L-systems

Parametric L-systems

- ▶ symbols can have one or more parameters
 - parameters can be set and modified by productions
 - conditional terms can be associated with productions
 - production is valid \Leftrightarrow condition is “true”

- ▶ example

S	$-->$	$A(0)$
$A(t)$	$-->$	$A(t+0.01)$
$A(t) : t \geq 1.0$	$-->$	F

- ▶ context-sensitive example

- passing nutrients along stem
- $A(t_0) < A(t_1) > A(t_2) : t_2 > t_1 \ \& \ t_1 > t_0 --> A(t_1 + 0.01)$

Parametric L-systems

ω : $B(2)A(4,4)$

p_1 : $A(x,y) : y \leq 3 \rightarrow A(x*2, x+y)$

p_2 : $A(x,y) : y > 3 \rightarrow B(x)A(x/y, 0)$

p_3 : $B(x) : x < 1 \rightarrow C$

p_4 : $B(x) : x \geq 1 \rightarrow B(x-1)$

Result: $B(2)A(4,4)$

$B(1)B(4)A(1,0)$

$B(0)B(3)A(2,1)$

$C \quad B(2)A(4,3)$

$C \quad B(1)A(8,7)$

$C \quad B(0)B(8)A(1.142,0)$

Timed L-systems

- ▶ 2 new concepts
 - global time variable, accessible to all productions
 - local age value τ_i associated with each letter μ_i
- ▶ a timed L-system production rule
 - $(\mu_0, \beta_0) \dashrightarrow ((\mu_1, \alpha_1), (\mu_2, \alpha_2), \dots, (\mu_n, \alpha_n))$
 - β_0 = terminal age of μ_0
 - α_i = initial age of μ_i
 - applied when symbol's terminal age is reached
- ▶ geometric interpretation of each symbol is potentially based on local age of symbol

Timed L-systems

▶ Axiom

		(A,0)
(A,3)	→	(S,0)[+(B,0)](S,0)
(B,2)	→	(S,0)

▶ Sequence

	global time
(A,0)	0
(A,1)	1
(A,2)	2
(A,3)	3
(S,0)[+(B,0)](S,0)	4
(S,1)[+(B,1)](S,1)	5
(S,2)[+(B,2)](S,2)	6
(S,3)[+(S,0)](S,3)	7

A = plant seed

S = internode stem segment

B = bud turning into stem of a branch
(length ~ age)

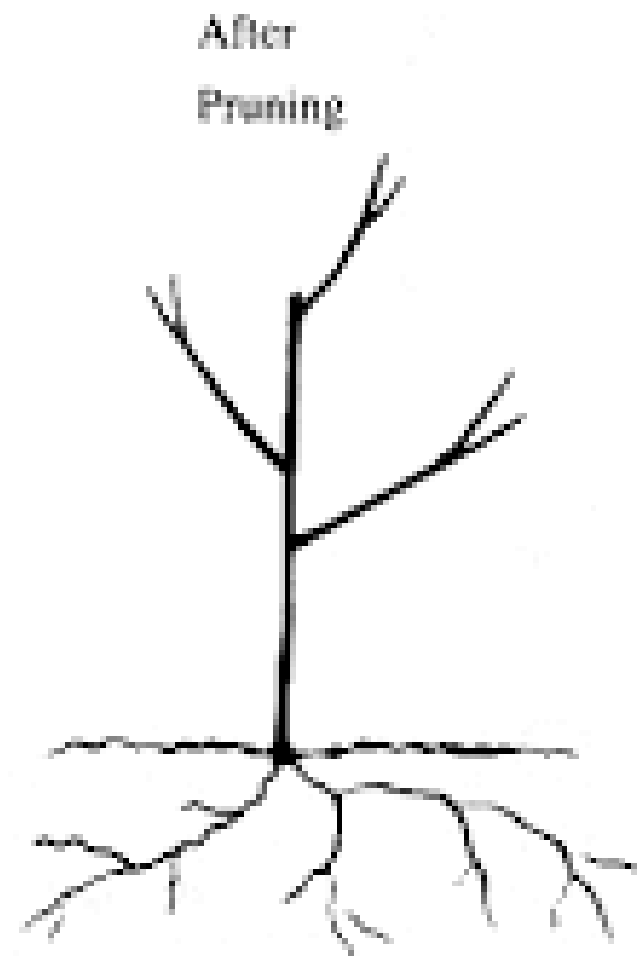
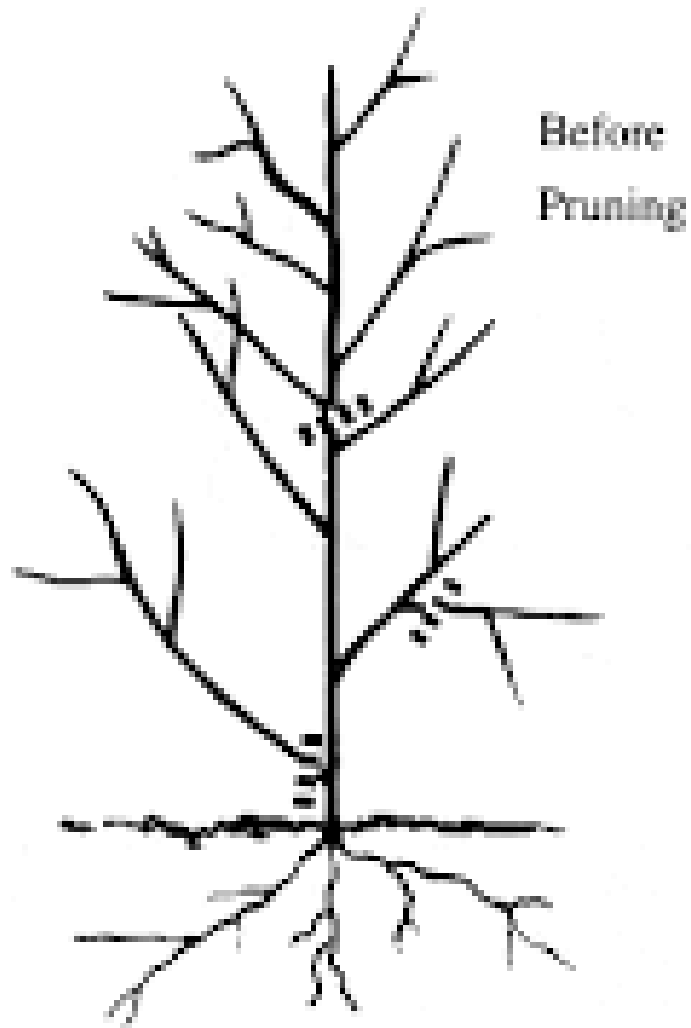
Environment-sensitive L-systems

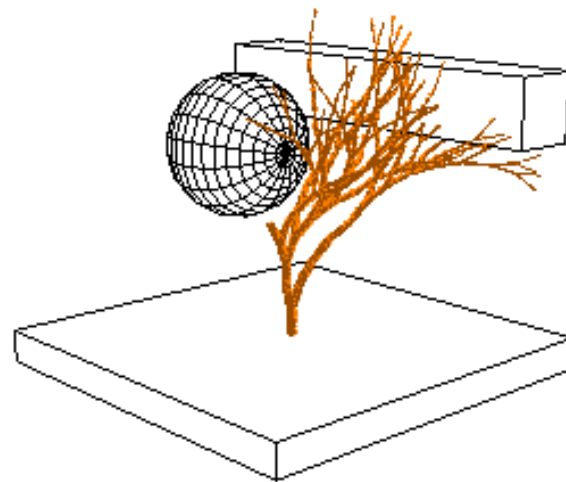
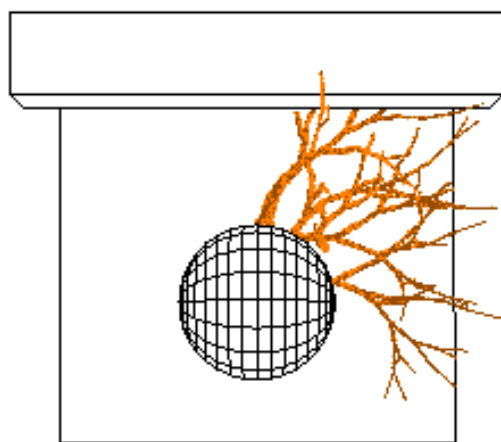
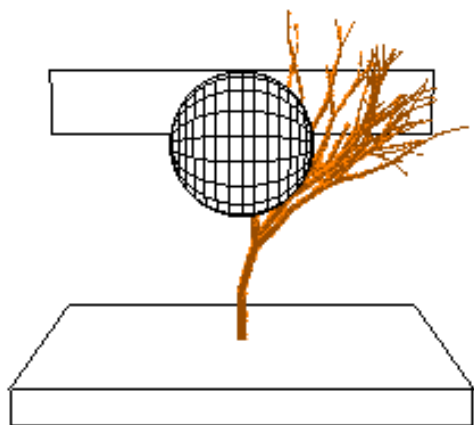
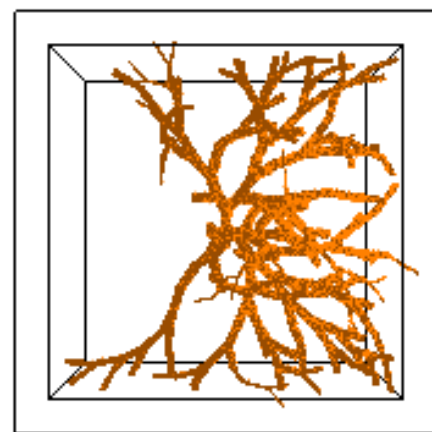
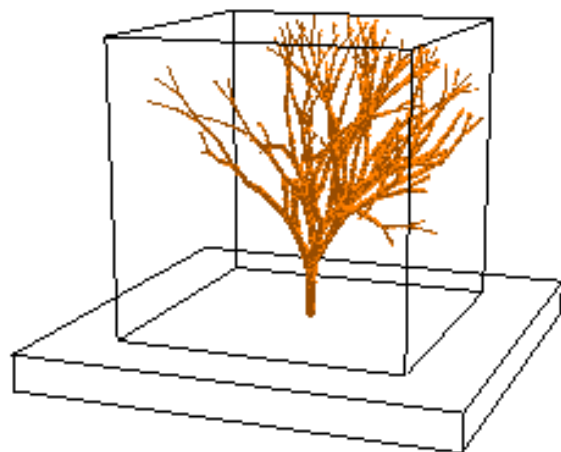
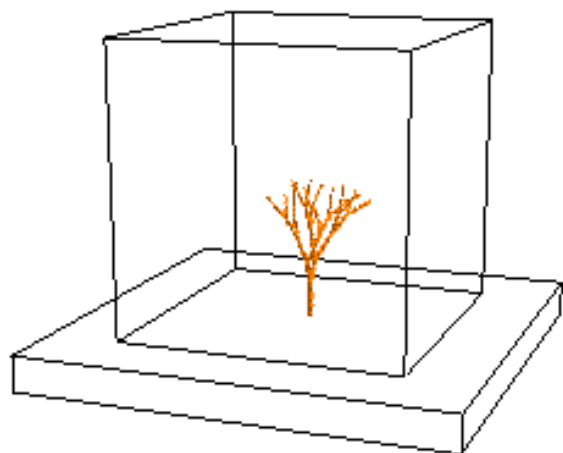
- ▶ interaction with objects, other plants, parts of the plant itself, light, gravity, wind...
 - competition for space between individual plants
 - competition for light between branches of a tree
 - competition between roots for water in the soil
- ▶ open L-systems
 - introduction of communication symbols which can exchange parameter values with the environment
- ▶ pruning
 - “%”: remove all symbols that are still present between the current []-pair
 - example: $T(p):p==0 \rightarrow \%$

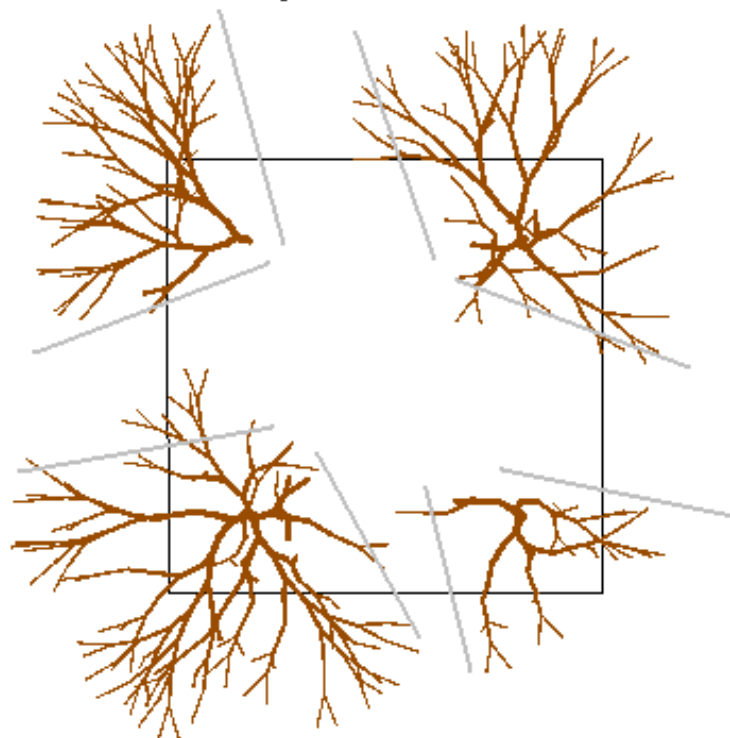
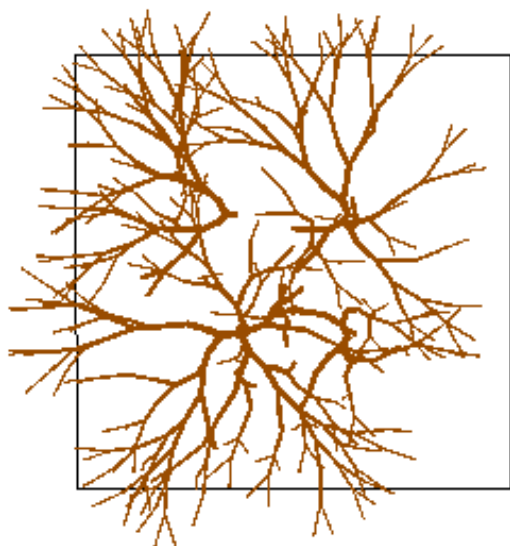
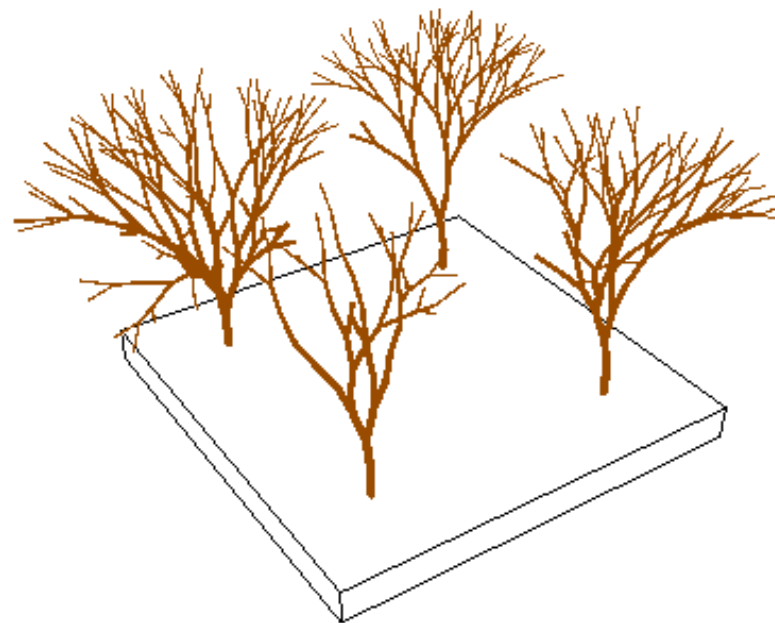
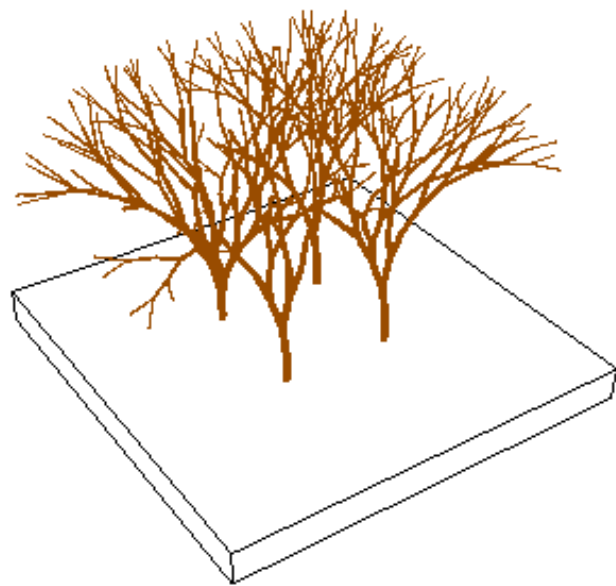
$F[+F[+FF]FT(?)F[-F]F[-FF]$
 $F[+F[+FF]F\%F[-F]F[-FF]$
 $F[+F[+FF]F]F[-FF]$

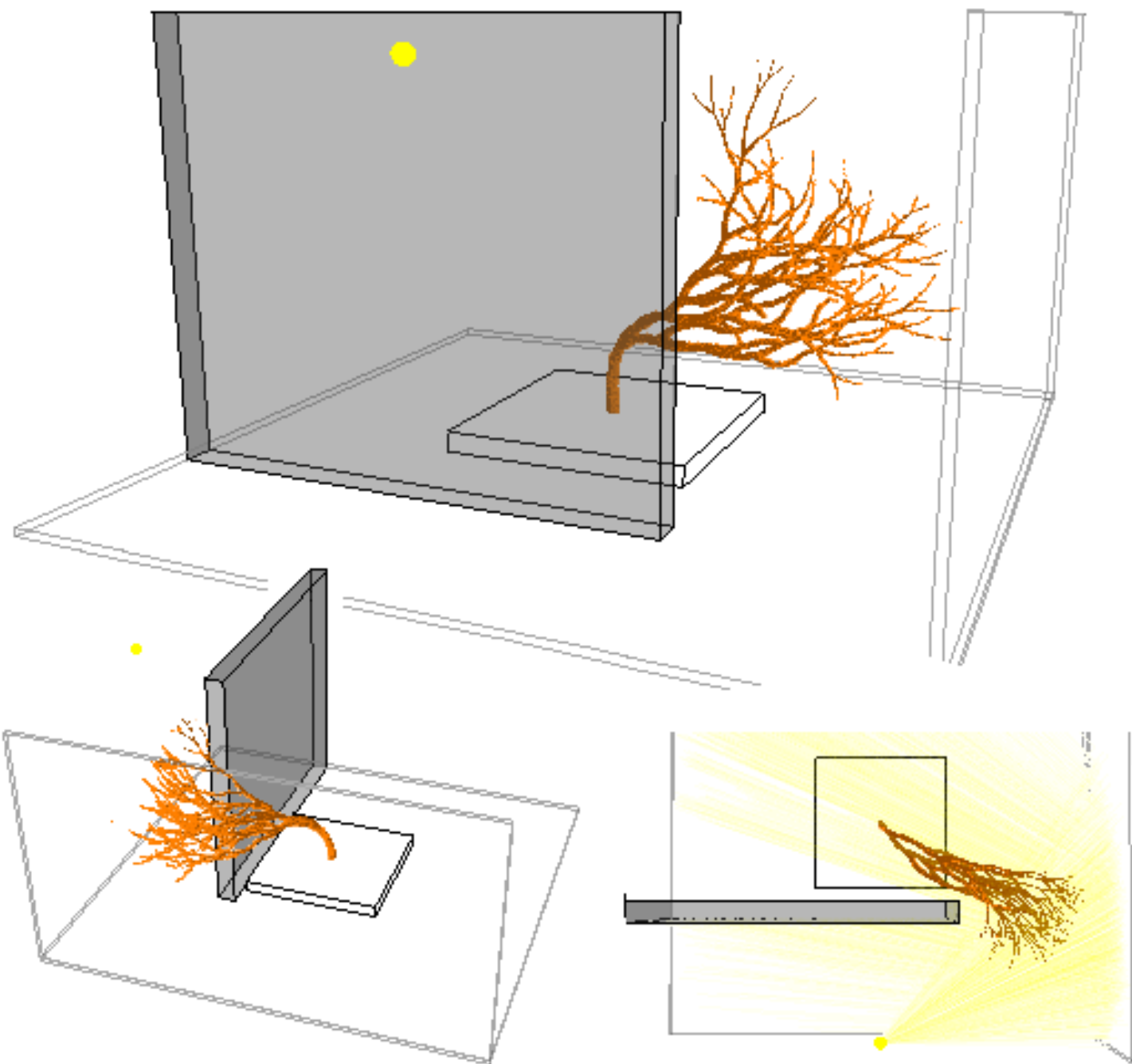
$F[+F[+FF]FT(?)F[-F]F[-FF]$
 $F[+F[+FF]F\%F[-F]F[-FF]$
 $F[+F[+FF]F]F[-FF]$

Pruning









Growth under a table



References

- ▶ <http://algorithmicbotany.org>
- ▶ <http://xfrog.com/>