

# Missingness & Feature Engineering

#### STRUCTURALLY MISSING VALUES

The missing values in the dataset (-999) resulted from two sources:

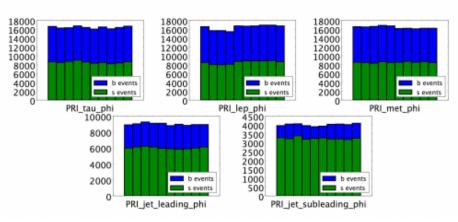
- 1. Bad estimates of the mass of Higgs boson; and Rotated the angle of the remaining 4 phi columns.
- 2. Jets: particles that can appear 0, 1, 2, or 3 times in an event.

To deal with this structural missingness, we:

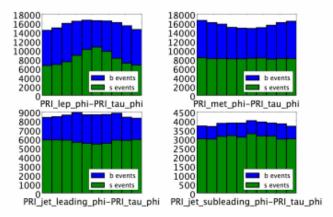
- Converted the -999s into NAs.
- Created a Boolean column to reflect missing(T)/present(F) values in the estimated mass of the Higgs boson (DER\_mass\_MMC).
- Created 8 binary columns reflecting each combination of presence(0)/absence(1) in the estimated mass of the Higgs boson and the number of jets (0,1,2,3).
- o J0 +M1, J0+M0, J1+M1, J1+M0...
- Imputed the column mean for all the NAs.

For more on the structural nature of the missing values in the Higgs boson dataset, see http://www.jmlr.org/proceedings/papers/v42/cowa14.pdf.

Figures 2(a) and 2(b) show the histograms of the original and rotated features respectively. We can see that features that didn't look informative because they had a uniform distribution for signal and background events are now apparently important with this transformation (see figure, showing a distribution with different parameters in the case of the signal and background events.



(a) The histogram of the features related with the  $\phi$  angle in the reference frame (see Apendix A), abscissa axis is in the  $[-\pi, \pi)$  range



(b) Histogram of the new features after a rotation of every event to make PRI\_tau\_phi equal to zero (see section 4.1), abscissa axis is in the  $[0, 2\pi)$  range

Figure 2: Change of variables to create a feature space robust to rotations around the z axis

http://www.jmlr.org/proceedings/papers/v42/diaz14.pdf

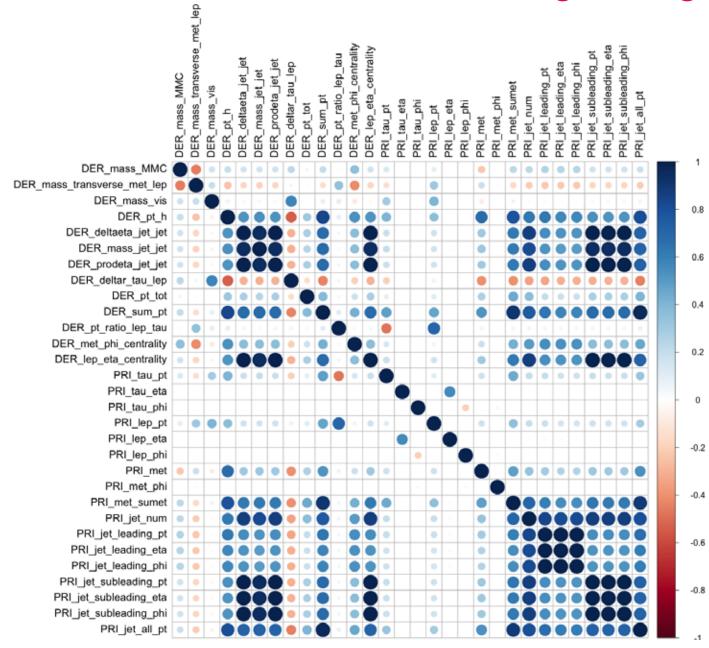
#### **FEATURE SELECTION**

To deal with the risk of overfitting, we:

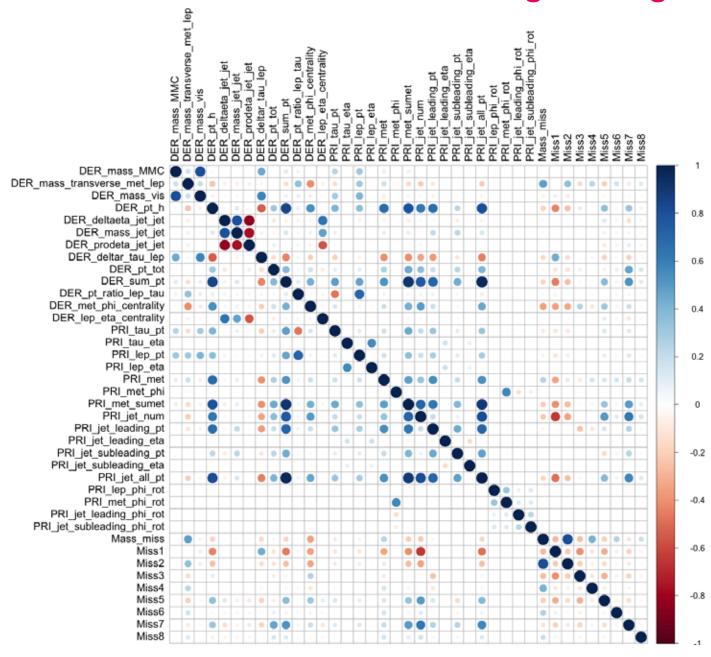
- 1. Subtracted the PRI\_tau\_phi column from the other 4 'phi' columns.
- 2. Rotated the angle of the remaining 4 phi columns.
- 3. Deleted all 5 of the non-rotated phi columns, leaving us with 4 phi columns instead of 5.

This subtraction + rotation process makes the specific pattern of the phi variables more unique, so that, once the model is trained, it is better able to discriminate between signal and background in the test set. For more on the logic of this process, see http://www.jmlr.org/proceedings/papers/v42/diaz14.pdf

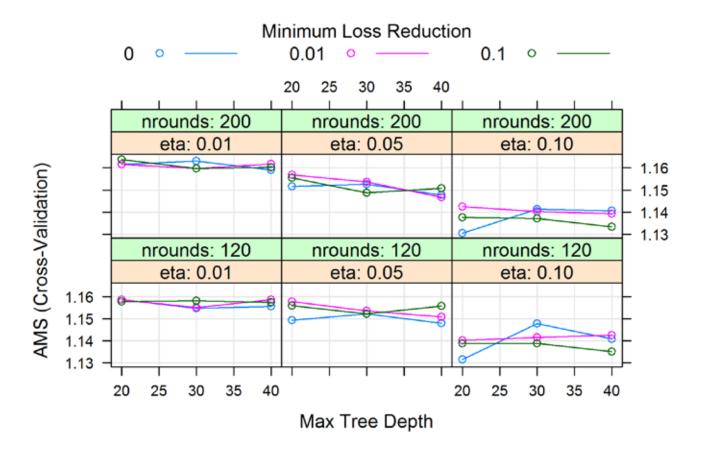
#### **Correlation Plot before Feature Engineering**



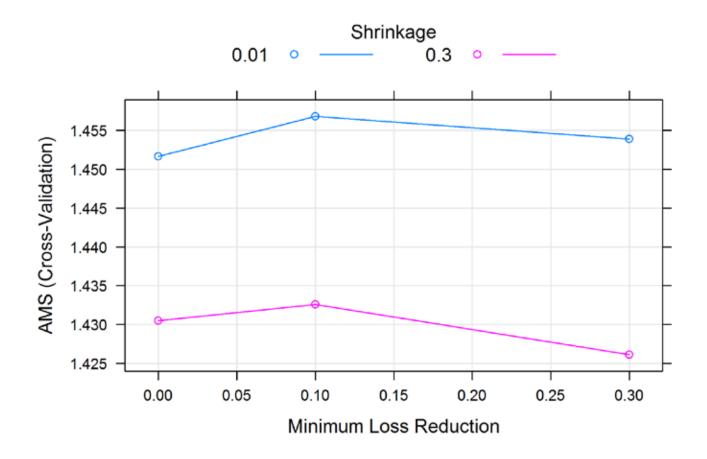
#### **Correlation Plot after Feature Engineering**



### XGBoost



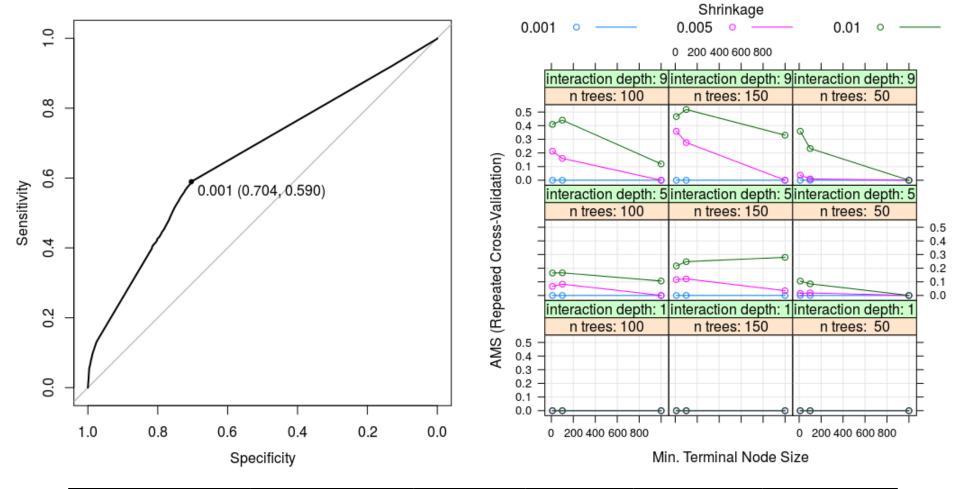
| XGBoost: 1        |          |          |              |  |  |
|-------------------|----------|----------|--------------|--|--|
| Model Pa          | rameters | Accuracy | Kaggle score |  |  |
| n.trees           | 200      | 0.8214   | 1.1637       |  |  |
| interaction depth | 20       |          |              |  |  |
| shrinkage         | 0.01     |          |              |  |  |
| gamma             | 0.1      |          |              |  |  |
| K-folds           | 5        |          |              |  |  |



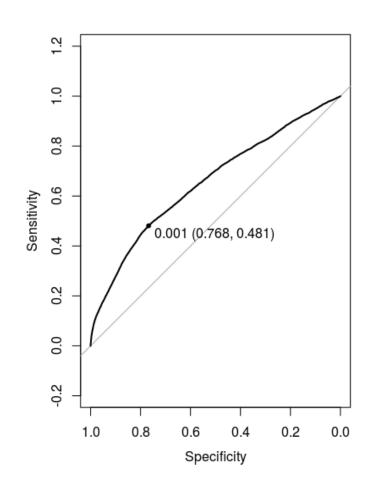
| XGBoost: 2        |          |          |              |  |  |
|-------------------|----------|----------|--------------|--|--|
| Model Par         | rameters | Accuracy | Kaggle score |  |  |
| n.trees           | 300      | 0.8309   | 1.474        |  |  |
| interaction depth | 10       |          |              |  |  |
| shrinkage         | 0.1      |          |              |  |  |
| gamma             | 0.1      |          |              |  |  |
| K-folds           | 3        |          |              |  |  |

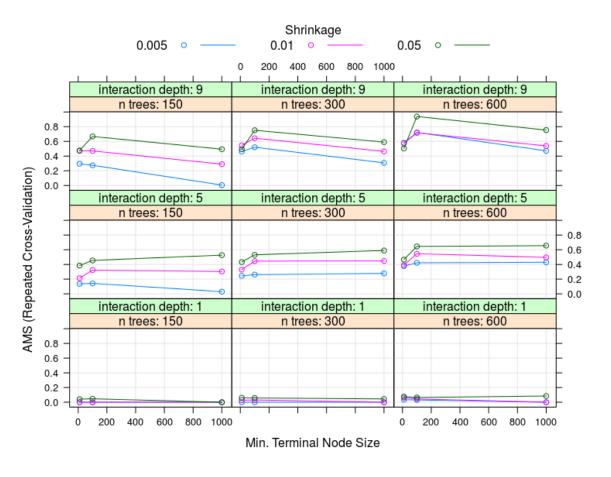
- Number of cv folds: 2 5
- Number of rounds: 50 400
- Eta (shrinkage): 0.001 0.6
- Gamma: 0.01 0.6
- Max tree depth: 6 -10
- Insights and Conclusion:
  - AMS scores on 80% train split: 1.2 1.8+
  - Accuracy rate of 80+ when applied to 20% test
  - Most likely due to overfitting because the AMS scores on the Kaggle full test data site were much lower, with the highest being about .5.

# Gradient Boosting Model



| GBM: 1            |      |           |        |          |              |
|-------------------|------|-----------|--------|----------|--------------|
| Model Parameters  |      | AUC       |        | Accuracy | Kaggle score |
| n.trees           | 50   | AUC       | 0.6583 | 0.67282  | 1.03128      |
| interaction depth | 9    |           |        |          |              |
| shrinkage         | 0.01 | threshold | 0.001  |          |              |
| min obs in bin    | 10   |           |        |          |              |
| K-folds           | 5    |           |        |          |              |



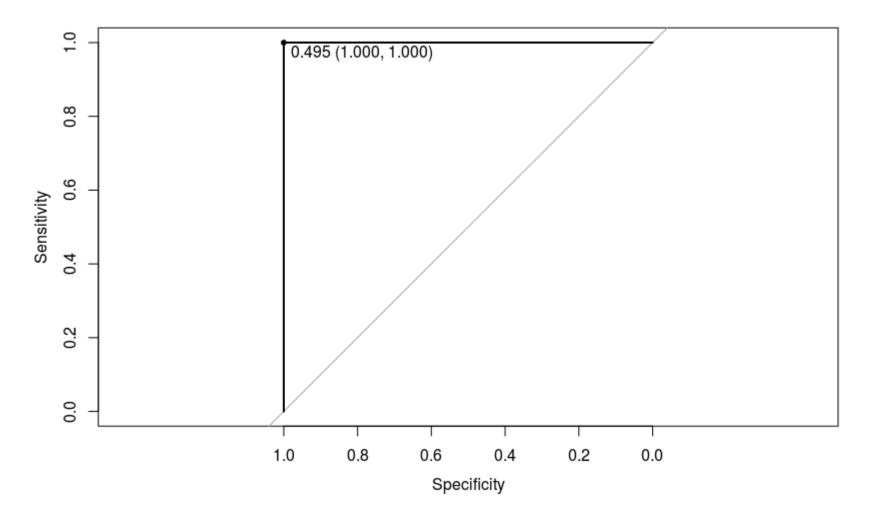


| GBM: 2            |      |           |       |          |              |
|-------------------|------|-----------|-------|----------|--------------|
| Model Parameters  |      | AUC       |       | Accuracy | Kaggle score |
| n.trees           | 600  | AUC       | 0.656 | 0.644    | 1.06846      |
| interaction depth | 9    |           |       |          |              |
| shrinkage         | 0.05 | threshold | 0.001 |          |              |
| min obs in bin    | 100  |           |       |          |              |
| K-folds           | 3    |           |       |          |              |

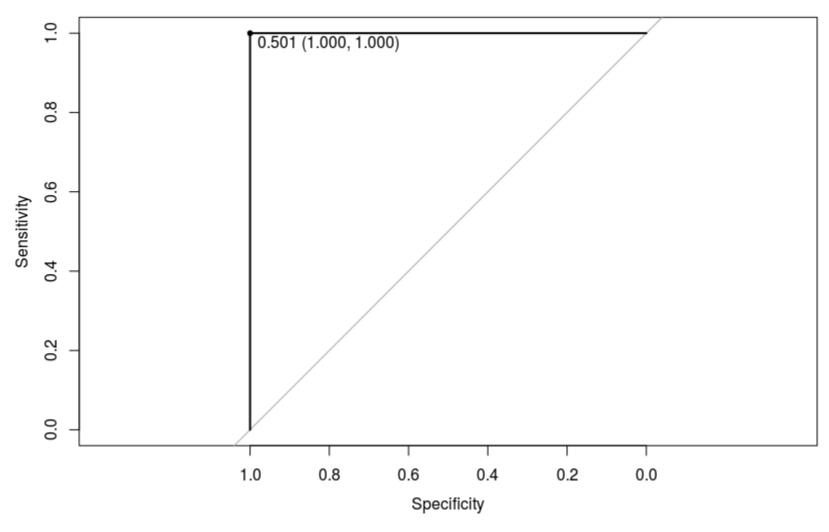
#### Insights and conclusions:

- Should have increased the number of trees and held the shrinkage parameters constant to compare.
- In the future, I would grow the model slower by increasing the number of trees and starting with a much smaller shinkage parameter.
- For future Kaggle competitions, look at benchmark documents first to get a sense of optimal number of trees.
- In general our boosted models underperformed because of the small number of trees.

## Random Forest



| Random Forest: 1 |         |           |       |              |  |
|------------------|---------|-----------|-------|--------------|--|
| Model Par        | ameters | AL        | JC    | Kaggle score |  |
| m.try            | 38      | AUC       | 1     | 2.8554       |  |
|                  |         | threshold | 0.495 |              |  |

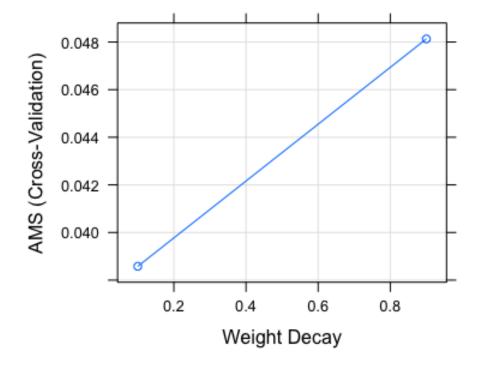


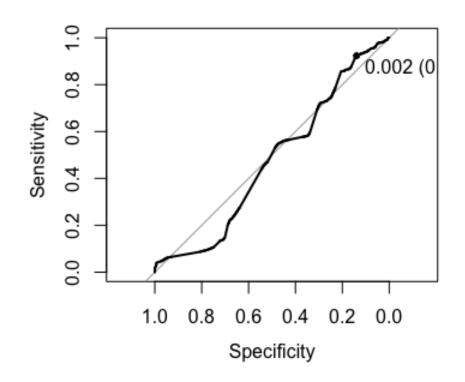
| Random Forest: 2 |         |           |       |              |  |
|------------------|---------|-----------|-------|--------------|--|
| Model Par        | ameters | AL        | JC    | Kaggle score |  |
| m.try            | 7,12,38 | AUC       | 1     | 2.8554       |  |
|                  |         | threshold | 0.501 |              |  |

#### Insights & Conclusions

- Because I was using Random Forests, I trained my model on the entire training dataset, using the out of bag error.
- There was no difference between bagging (mtry=38) and a tuneGrid containing 7, 12, and 38.
- Using parallel processing and a server enabled me to process my models more quickly than on my laptop.
- I should have selected the number of trees myself, as practice for comparing a random forest and boosted trees model trained on the same dataset, which would help enable determining the point at which a boosted model outperforms the random forest model on that dataset.

## Neural Networks





| <b>Neural Net</b> |          |           |        |          |
|-------------------|----------|-----------|--------|----------|
| Model Par         | ameters  | AL        | JC     | Accuracy |
| K-Folds           | 10       | AUC       | 0.4727 | 0.39484  |
| hidden layers     | 20,20,20 | threshold | 0.002  |          |

#### Conclusion:

- Adding more hidden layers does not necessarily mean better threshold
- Implement the dropout technique for future analysis

## Conclusions & next steps

#### What we would like to do next:

- Look into ensembling models
- Exploration of other packages other than Caret.
- With more time, we could have written a function that:
  - Identifies values of PRI\_tau\_eta < 0</li>
  - Converts the signs of all eta values in the same row (- to +, + to -)
  - Imputes the column mean for missing values and randomly assigns a sign (+,-)
  - http://www.jmlr.org/proceedings/papers/v42/diaz14.pdf

|           | PRI_tau_eta <sup>‡</sup>          | PRI_lep_eta <sup>‡</sup> | PRI_jet_leading_eta <sup>‡</sup> | PRI_jet_subleading_eta <sup>‡</sup> |  |  |
|-----------|-----------------------------------|--------------------------|----------------------------------|-------------------------------------|--|--|
| 1         | 1.017                             | 2.273                    | 2.150                            | 1.240                               |  |  |
| 2         | 2.039                             | 0.501                    | 0.725                            | -999.000                            |  |  |
| 3         | -0.705                            | -0.953                   | 2.053                            | -999.000                            |  |  |
| 4         | -1.655                            | -0.522                   | -999.000                         | -999.000                            |  |  |
| 5         | -2.197                            | 0.798                    | -999.000                         | -999.000                            |  |  |
| 6         | 0.371                             | -0.884                   | -2.412                           | 0.224                               |  |  |
| 7         | 1.113                             | 0.675                    | 0.864                            | 0.131                               |  |  |
| 8         | 0.654                             | 0.506                    | -0.715                           | -999.000                            |  |  |
| 9         | 2.433                             | 0.210                    | -999.000                         | -999.000                            |  |  |
| 10        | -1.533                            | -0.317                   | -2.767                           | -999.000                            |  |  |
| 11        | -0.866                            | 0.126                    | -999.000                         | -999.000                            |  |  |
| 12        | -0.669                            | -0.165                   | -0.790                           | 1.773                               |  |  |
| 13        | -0.766                            | 0.722                    | -0.970                           | -999.000                            |  |  |
| 14        | -0.654                            | -1.665                   | -999.000                         | -999.000                            |  |  |
| 15        | 1.389                             | 1.856                    | -999.000                         | -999.000                            |  |  |
| 16        | -1.107                            | -1.944                   | -999.000                         | -999.000                            |  |  |
| 17        | 0.484                             | -0.215                   | -0.766                           | -999.000                            |  |  |
| Showing 1 | nowing 1 to 18 of 250,000 entries |                          |                                  |                                     |  |  |