

## Project Assignment: GMRES

## 1 Description

- Write tools (library of functions) for operating on sparse matrices, using CSR (compressed sparse row) format. More specifically:
  - It should be able to read matrix data from a file (the  $i, j$  and data entries  $a_{ij}$  for all non-zero entries of the matrix.)
  - It should be able to perform  $A$  times a vector, and  $A^T$  times a vector.
  - Optionally, given  $A$  in CSR format generate  $A^T$  in the same format. This function should use minimal operations (as little as you can think of).
  - Optionally, given two matrices  $A$  and  $B$  in CSR format, compute  $C = AB$  and store it also in CSR format.

**Task 1:** There should be a test driver that you write, which can:

1. Read a matrix  $A$  (could be simply the adjacency matrix of a directed or undirected graph). (Matrices  $A$  will be provided separately or use link <https://sparse.tamu.edu/>.)
2. Optionally: Produce  $B = A^T$  in CSR format.
3. Optionally: Compute  $C = AB$ . Check if  $C$  is symmetric.

**Task 2:** Use some of the functions from your library, for an appropriately given input matrix  $A$  (provided separately, e.g., read from the link above), and

- Implement the GMRES algorithm with restart (provided in a separate .pdf file).
- Perform study when you vary  $m_{\max} = 5, 10, 15, \dots$  the maximal number of steps allowed in the algorithm, and document the total number of iterations and total time to convergence for a given tolerance  $\epsilon$  (and a given matrix). Write your conclusions from the study.

**Grading:**

You will have to document (describe) the implementation of the library and the GMRES algorithm in a project report. The project report is due no later than December 9 (earlier the better).

You need to demonstrate that the code runs (i.e., can generate approximate solution  $\mathbf{x}$  for various r.h.s. vectors  $\mathbf{b}$ , sizes of  $m_{\max}$ , and tolerance  $\epsilon$ .)

The project will be graded after a discussion and looking at your project report on how the library and the GMRES algorithm were implemented.