3. DESCRIPTIVE STATISTICS [IT2110]

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This will give you an idea about the behavior of data.



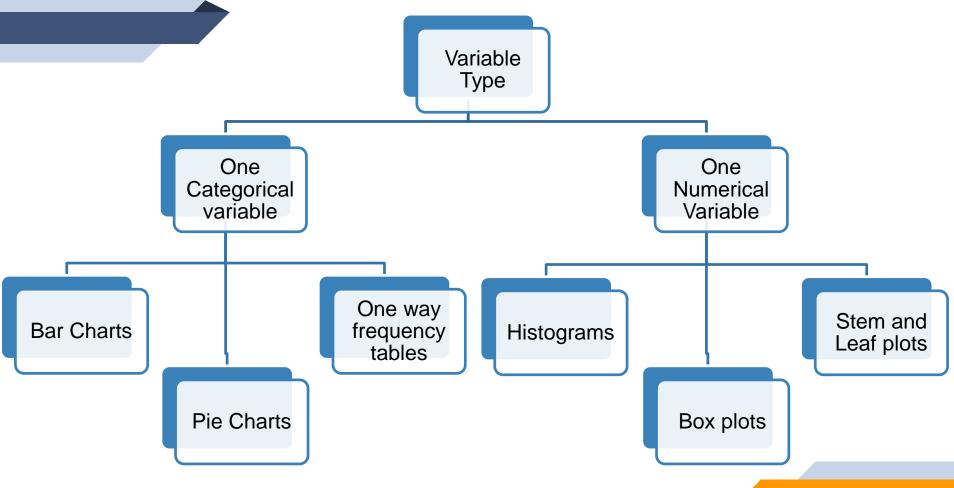
- This is also known as preliminary analysis.
- It describes how the each of the variables in your analysis behave.
- There are two methods that you can use under exploratory analysis. They are,
 - Graphical Methods &
 - Numerical Methods
- Each method depends on the type of the data available

Graphical Methods

 You can use graphical methods to analyze both categorical and numerical variables.

 Type of graph you use depends on the type of the data available







One-way Frequency Tables

Categorical Variable

Gender	Frequency
Male	48
Female	52

Numerical Variable

Marks		Frequency
0-20		12
21-40		8
41-60		42
61-80		56
81-100	Coi Landa la siisas af lafa masi a Tasha al	10

Bar Charts

- In bar charts, each bar will represent each category level. These bars can be drawn in vertically or horizontally.
- Frequency, cumulative frequency or percentages can be used for the y axis while x axis will represent the categorical variable.
- Length of the bar will proportional to the value it represent.

Bar Charts Cont...

There are several type of bar charts. For example,

Simple Bar Charts

Component bar charts / Stacked bar charts

Percentage component bar charts

Multiple bar charts / Clustered bar charts

Pie Charts

- Pie charts are used to analyze one categorical variable.
- In pie charts, area of each sector will proportional to the value of category it represent.
- This is appropriate, when there are few number of categories for the variable or when value of each category is varying widely.

Histograms

- First, divide the given data set into suitable number of classes (intervals/categories) which have the same width.
- Classes with their frequencies (counts) is called a frequency distribution.
- Frequency, relative frequency or percentages can be used for the y axis while x axis will represent the classes of the variable.
- In histograms, each bar will represent each class and length of the bar will proportional to the frequency of respective class.
- In histograms, bars are drawn adjacent with each other (No gaps between two bars).

Example:-

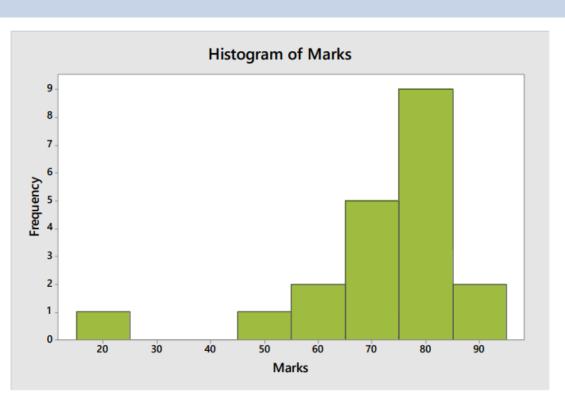
78	74	82	66	91	71	64	88	55	80
51	74	82	75	16	78	84	79	71	83

- Range = Max Min = 91-16 = 75
- Divide the range into required number of classes to find class width (Eg:- 8):-

$$75 / 8 = 9.375 \approx 10$$

Classes can be selected by fixing the class width also

Example:-



Class	Frequency
14.5 – 24.5	1
24.5 – 34.5	0
34.5 – 44.5	0
44.5 – 54.5	1
54.5 – 64.5	2
64.5 – 74.5	5
74.5 - 84.5	9
84.5 – 94.5	2

Box Plots

- To draw a box plot, it is need to identify the five number summary & outliers for the variable.
- Five Number Summary:
 - **Minimum**
 - Maximum
 - > Q1
 - Q2 (Median)
 - \triangleright Q3

Outliers

- Before drawing the box-plot we should identify the potential outliers.
- A limit should be defined for the accepted range of values.

$$Upper\ Bound = Q_3 + 1.5 * IQR$$

 $Lower\ Bound = Q_1 - 1.5 * IQR$

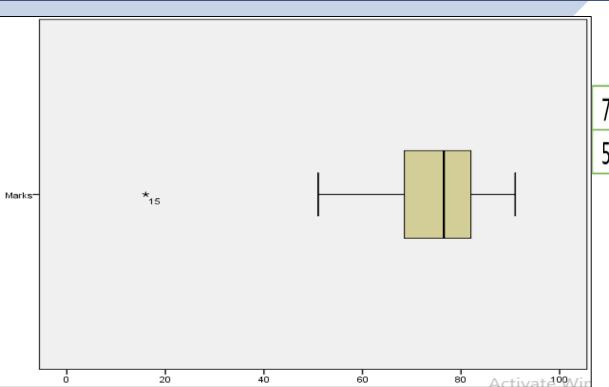
 Values outside the range are considered as outliers and marked with asterisks (*).

Outliers

Q1, Median, Q3 are marked as a box.

Minimum & maximum values which are not outliers, will be end point for whiskers of the box plot.

Example:-





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Stem-and-Leaf Plots

- These plots are useful when the data set is very small.
- Before drawing this plot, it is need to arrange the data in ascending order.
- Then, each data value will split into two parts known as stem and leaf.
- The "leaf" is usually the last digit of the number.
- The other digits to the left of the "leaf" form the "stem".
- These plots are not much use in preliminary analysis.

Example:-

Stem	Leaves					
1	6					
2						
3						
4						
5	1 5					
6	4 6					
7	11445889					
8	022348					
9	1					
Key: 1 6 → 16						

78									
51	74	82	75	16	78	84	79	71	83

Describing Two Variables

Two categorical variables:

- Two-way frequency table
- Clustered bar chart
- Stacked bar chart

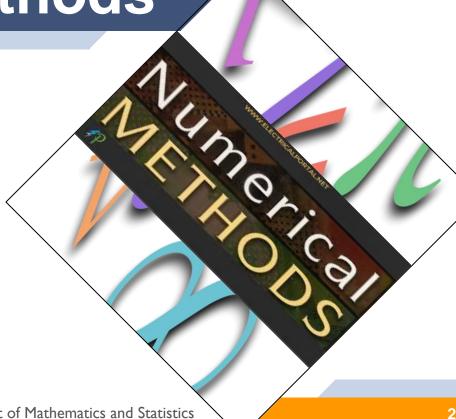
One categorical & one numerical variable:

- Parallel box plots
- Comparison of location measurements for each category.
- Two numerical variables:

Numerical Methods

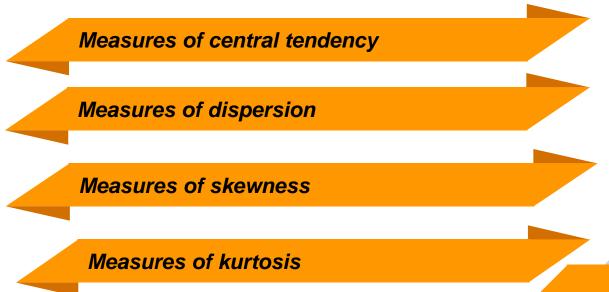
Numerical methods are applied only for numerical variables.

These methods summarize the variable into a single value.



Numerical Methods Cont...

This has measurements under four main sections.
 They are,



Measures of Central Tendency

- This gives an idea about the *location* of the data as a whole.
- Following three measurements can be used for this.
 - Mean
 - Median
 - Mode
- Other location measurements :
 - Percentiles / Deciles / Quartiles

Mean

Different types of means

- Arithmetic mean
- Geometric mean
- Harmonic mean

Only the arithmetic mean is discussed (referred to as the mean).

• Mean of a population (μ) , with N elements (x1, x2, ..., xN),

$$\mu = \frac{\sum_{i=1}^{N} x_i}{N}$$

Mean of a sample (\bar{x}) , with n elements (x1, x2, ..., xn),

$$\overline{x} = \frac{\sum_{i=1}^{n} x_i}{n}$$

If not specified, consider the data are coming from a sample.

Examples:-

Example 1.2 (revisited):

Find the median "marks for FCS" of each student at SLIIT Metro.

78	74	82	66	91	71	64	88	55	80
51	74	82	75	16	78	84	79	71	83

Example 1.3 (revisited):

A load of aluminum sheets were purchased to construct a temporary shed. Twenty such sheets were examined for surface flaws. Find the median number of flaws in a sheet.

Number of flaws	Frequency
0	4
1	3
2	5
3	2
4	4
5	1
_ 6	1

Mode

A value with the highest frequency in a data set.

There can be multiple modes in a data set.

If all the data values are different, the data set has no mode.

Percentiles

- Divides the entire set of values into 100 equal sections.
- The values should be ordered in ascending order.
- Position of the k th percentile. (n number of observations)

Position of
$$P_k = (\frac{n+1}{100}) * k$$

- Find the value that corresponds to the found position from the ordered set of values.
- If the position is not an integer the following methods can be used.
 - Nearest Rank method
 - Linear Interpolation

Deciles & Quartiles

- Deciles divides the entire set of values into 10 equal sections.
- Quartiles divides the entire set of values into 4 equal sections.

Method is the same as what has used for percentiles.

Measures of Dispersion

- This gives an idea about the dispersion / spread of the data as a whole.
- Following three measurements can be used for this.
 - Range (Max Min)
 - IQR (Q3 Q1)
 - Variance & Standard Deviation (√Variance)
- Range is more suitable for small data sets.
- Range and variance are highly sensitive for outliers while, IQR is not sensitive for outliers.

Variance & SD

This is a measurement of dispersion/spread of the data. This describes how the data has dispersed around its mean.

Sensitive to outliers.(Not robust for outliers).

• Variance of a population (σ^2) , with N elements $(x1,x2, \dots, xN)$,

$$\sigma^2 = \frac{\sum_{i=1}^{N} (x_i - \mu)^2}{N}$$

Variance of a sample (s^2) , with n elements (x1, x2, ..., xn),

$$s^2 = \frac{\sum_{i=1}^n (x_i - \overline{x})^2}{n-1}$$

If not specified, consider the data are coming from a sample.

- Standard deviation (SD) is the square-root of the variance.
 - Population SD σ
 - Sample SD s

Measures of Skewness

- This gives an idea about the asymmetry of the data as a whole.
- If the data set is symmetric skewness will be zero.
- A negative skew means that the left tail is longer; the mass of the distribution is concentrated on the right.
- A positive skew means that the right tail is longer; the mass of the distribution is concentrated on the left.

Measures of Kurtosis

This gives an idea about whether the distribution is peaked or flat.

Example

A sample of 25 plastic hinges was subjected to repealed stress cycles until failure. The number of cycles which each survived is given below.

```
72, 35, 63, 67, 87, 71, 64, 47, 60, 81, 39, 52, 57, 74, 43, 55, 37, 83, 48, 91, 53, 44, 94, 65, 75
```

- Find five number summary
- II. Find mode, p_{15} , D_3 , mean, variance & sd.
- III. Draw box plot & stem & leaf plot.
- V. Comment on the distribution of data.



THANKS!

Any questions?