



From calculus, the exponential function is sometimes defined from the power series

$$e^x = 1 + x + \frac{1}{2!} x^2 + \frac{1}{3!} x^3 + \dots$$

In analogy, the matrix exponential of an  $n$ -by- $n$  matrix  $A$  can be defined by

$$e^A = I + A + \frac{1}{2!} A^2 + \frac{1}{3!} A^3 + \dots$$

If  $A$  is diagonalizable, show that

$$e^A = S e^\Lambda S^{-1},$$

where

$$e^\Lambda = \begin{pmatrix} e^{\lambda_1} & 0 & \dots & 0 \\ 0 & e^{\lambda_2} & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & e^{\lambda_n} \end{pmatrix}.$$

Mark as completed

