

Intro to Rotation Matrices

Rotation and Transformation Matrices, 1/3

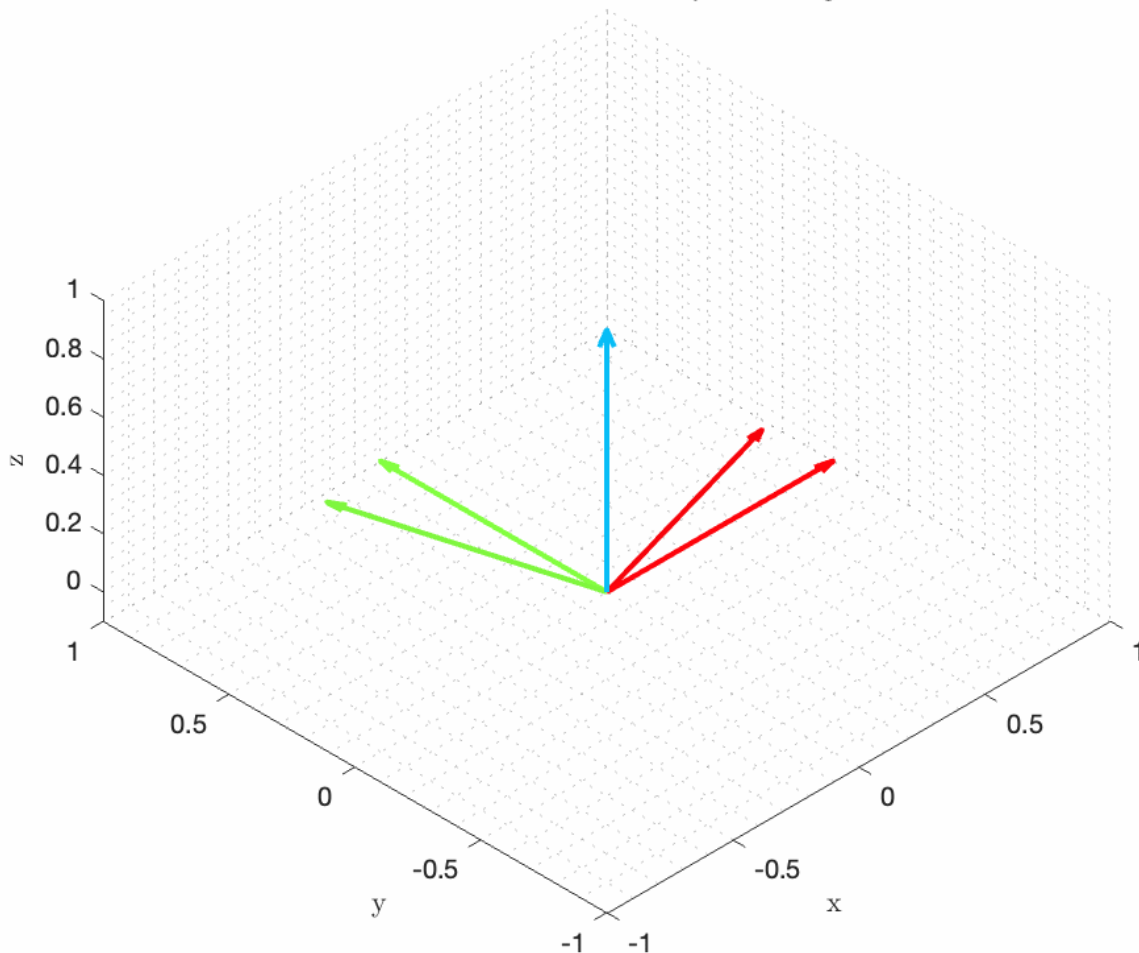
demonstrated

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For tutoring purposes | Entry level Robotics | 11/23/2022

A rotation matrix is an implicit representation of orientation. With three unit vectors defining new axis in the frame of another axis, rotation matrices avoid singularities of explicit representations. The way longitude and latitude change with respect to position near a pole is an example of a singularity. Rotation matrices can also be used to rotate a vector in space.

Rotation about the Z Axis by 16.00 degrees



The rotation matrix around an axis in terms of the angle can be represented:

```
syms theta
rot_Z = rotZ(theta)
```

Functions for each axis. Note that Rodrigues formula can be used to rotate about any axis

```
function rot = rotX(a)
% useful for rigid-body motions
% takes an angle of rotation (radians)
% returns the corresponding rotation matrix, about the Z axis
rot = [1,0,0;0,cos(a),-sin(a);0,sin(a),cos(a)];
end
```

```
function rot = rotY(b)
% useful for rigid-body motions
% takes an angle of rotation (radians)
% returns the corresponding rotation matrix, about the Y axis
    rot = [cos(b),0,sin(b);0,1,0;-sin(b),0,cos(b)];
end

function rot = rotZ(g)
% useful for rigid-body motions
% takes an angle of rotation (radians)
% returns the corresponding rotation matrix, about the Z axis
    rot= [cos(g),-sin(g),0;sin(g),cos(g),0;0,0,1];
end
```