

29 题用到 n 个知识:

无符号加减法:

$$\text{result} = \begin{cases} x+y & (x+y < 2^n) \text{ 正常} \\ x+y & (2^n \leq x+y < 2^{n+1}) \text{ 溢出} \end{cases}$$

$$\text{result} = \begin{cases} x-y & (x-y > 0) \text{ 正常} \\ x-y+2^n & (x-y < 0) \text{ 溢出} \end{cases}$$

带符号加减法:

$$\text{result} = \begin{cases} x+y-2^n & (2^{n-1} \leq x+y) \text{ 正溢出} \\ x+y & (-2^{n-1} \leq x+y < 2^{n-1}) \text{ 正常} \\ x+y+2^n & (x+y < -2^{n-1}) \text{ 负溢出} \end{cases}$$

$$\text{result} = \begin{cases} x-y-2^n & (2^{n-1} \leq x-y) \text{ 正溢出} \\ x-y & (-2^{n-1} \leq x-y < 2^{n-1}) \text{ 正常} \\ x-y+2^n & (x-y < -2^{n-1}) \text{ 负溢出} \end{cases}$$

做该题时同学们可参考例题 2.32

答案及过程:

① unsigned $X = 0x80 \Rightarrow$ 二进制: $10110000 \Rightarrow$ 十进制: $x = 176$
 $Y = 0x8C \Rightarrow$ 二进制: $10001100 \Rightarrow$ 十进制: $y = 140$.

$$X+Y = 10110000 + 10001100 = (1)00111100 = 0x3C$$

$$\text{sub} = \begin{cases} 0 & \text{加法运算} \\ 1 & \text{减法运算} \end{cases}$$

$$176 + 140 = 316 > 2^8 \Rightarrow x+y = 316 - 256 = 60.$$

$$\text{进位符: } CF = \text{sub} \oplus C = 0 \oplus 1 = 1, SF = 0$$

进行的是两个异号数相加, 则结果一定不会出现溢出

$OF = 1$ (加法器中两个同号数相加, 结果的符号数不同于加数的, 则发生溢出)

带符号:

$$X-Y = 10110000 + 01110100 = (1)00100100 = 36 = 0x24; CF = \text{sub} \oplus C = 1 \oplus 1 = 0, SF = 0$$

$$X = 0x80 \Rightarrow$$
 二进制: $10110000 \Rightarrow$ ~~非进位~~ 真值 $x = -80 = -01010000$

$$Y = 0x8C \Rightarrow$$
 真值 $y = -116 = -01110100$

\downarrow
10110000 的补码.

$$x+y = -80 + (-116) = -196 < 0 \text{ 溢出 } x+y = -196 + 256 = 60$$

$$X+Y = +00111100 = 60 = 0x3C$$

$$X-Y = +00100100 = 36 = 0x24$$

$$-80 - (-116) = 36 > 0. \text{ 正常.}$$

$$CF = \text{sub} \oplus C = 1 \oplus 1 = 0$$

② 无符号: $X = 0x7E = (0111\ 1110)_2 \Rightarrow$ 真值 $x = 126$

$$Y = 0x5D = (0101\ 1101)_2 \Rightarrow \text{真值 } y = 93.$$

$$x+y = 126+93 = 219 < 256 \text{ 正常}$$

$$X+Y = 0111\ 1110 + 0101\ 1101 = (0)1101\ 1011$$

$$CF = \text{sub} \oplus C = 0 \oplus 0 = 0, \quad SF = 1$$

$$OF = 1$$

$$x-y = 126-93 = 33 > 0.$$

$$X-Y = 0111\ 1110 + \underbrace{(-0101\ 1101)}_{= 1010\ 0011} = (1)0010\ 0001$$

$$CF = \text{sub} \oplus C = 1 \oplus 1 = 0 \quad SF = 0 \quad OF = 0 \text{ (加法器中)}$$

进行的是两个异号数相加. 那么结果一定不会发生溢出)

带符号:

~~带符号:~~

$$X = 0x7E = (0111\ 1110)_2 \Rightarrow x = 126. \quad Y = 0x5D = (0101\ 1101)_2 \Rightarrow y = 93$$

$$126+93 = 219 > 2^{8-1} = 128 \text{ 正溢出 } x+y = 129-256 = -127$$

$$X+Y = 1101\ 1011 = -101\ 1011$$

$$CF = \text{sub} \oplus C = 0 \oplus 0 = 0 \quad SF = 1 \quad OF = 1$$

$$\cancel{126-93}: x-y = 126-93 = 33.$$

$$X-Y = 0111\ 1110 + (-0101\ 1101) = (1)0010\ 0001$$

$$CF = \text{sub} \oplus C = 1 \oplus 1 = 0 \quad SF = 0 \quad OF = 0.$$