

## 1.3 DIJKSTRA'S 2-STACK DEMO

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▸ *With correction*



<http://algs4.cs.princeton.edu>

# Dijkstra's two-stack algorithm

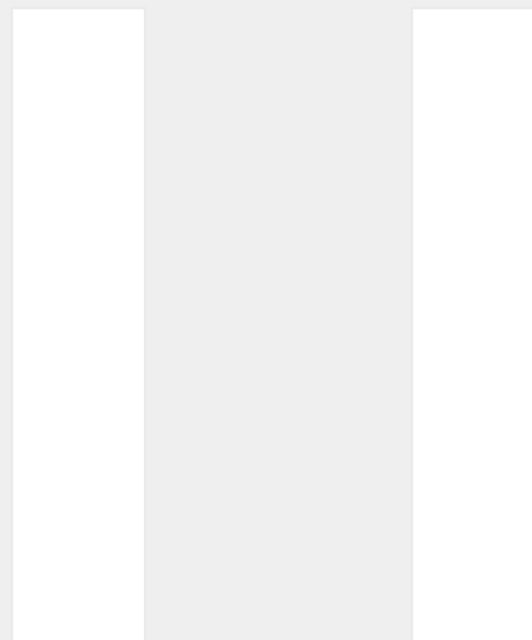
---

**Value:** push onto the value stack.

**Operator:** push onto the operator stack.

**Left parenthesis:** ignore (but see how we use them in the repo).

**Right parenthesis:** pop operator and two values; push the result of applying that operator to those values onto the value stack.

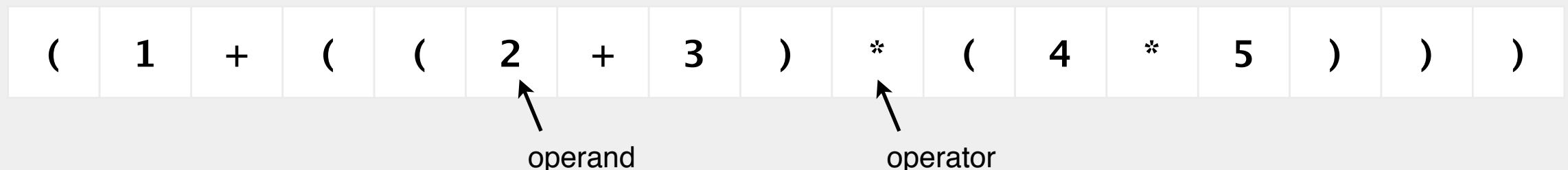


value stack

operator stack

**infix expression**

**(fully parenthesized)**



# Dijkstra's two-stack algorithm

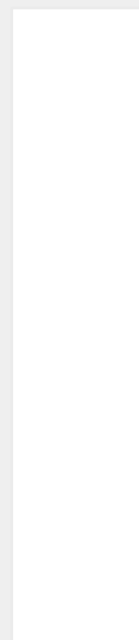
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value stack



operator stack

(	1	+	(	(	2	+	3	)	*	(	4	*	5	)	)	)
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# Dijkstra's two-stack algorithm

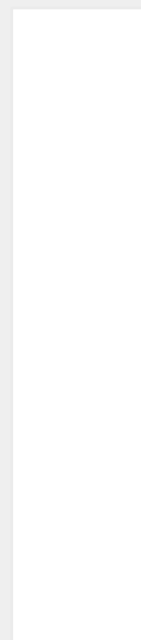
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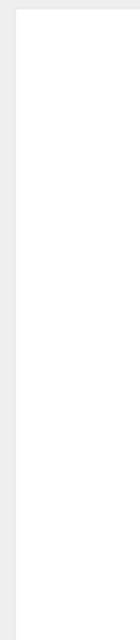
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value stack



operator stack



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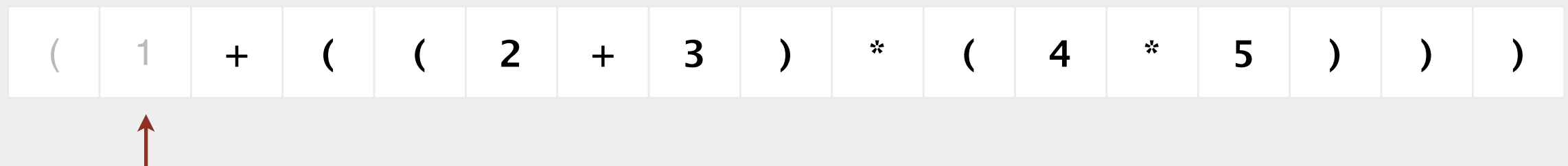
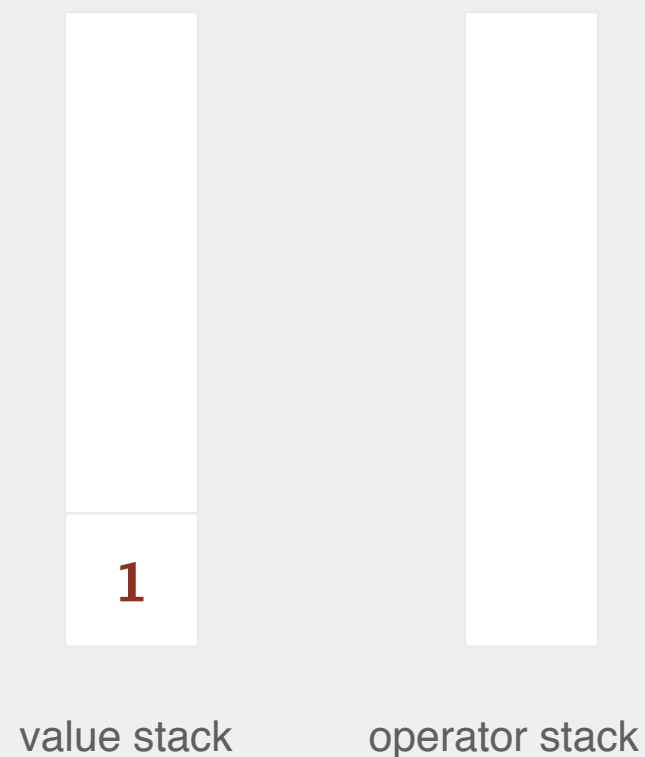
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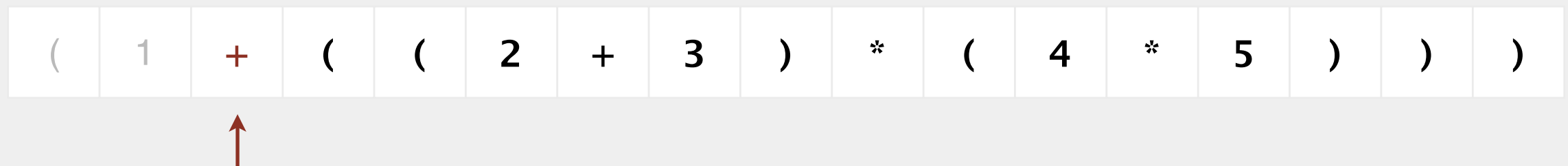
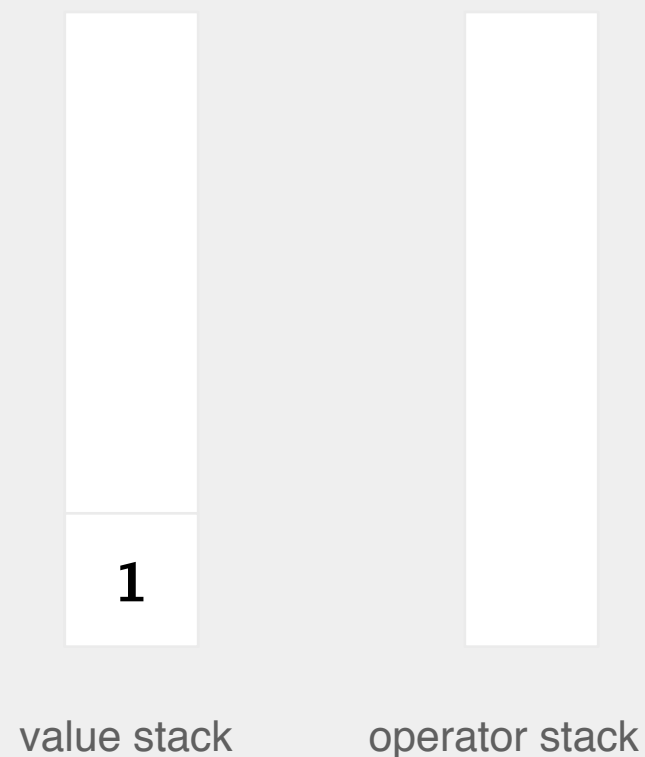
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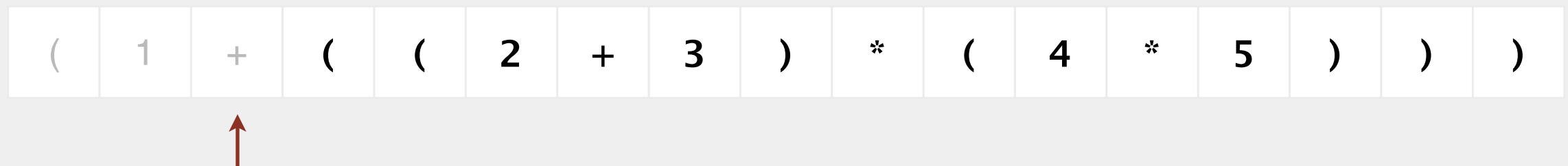
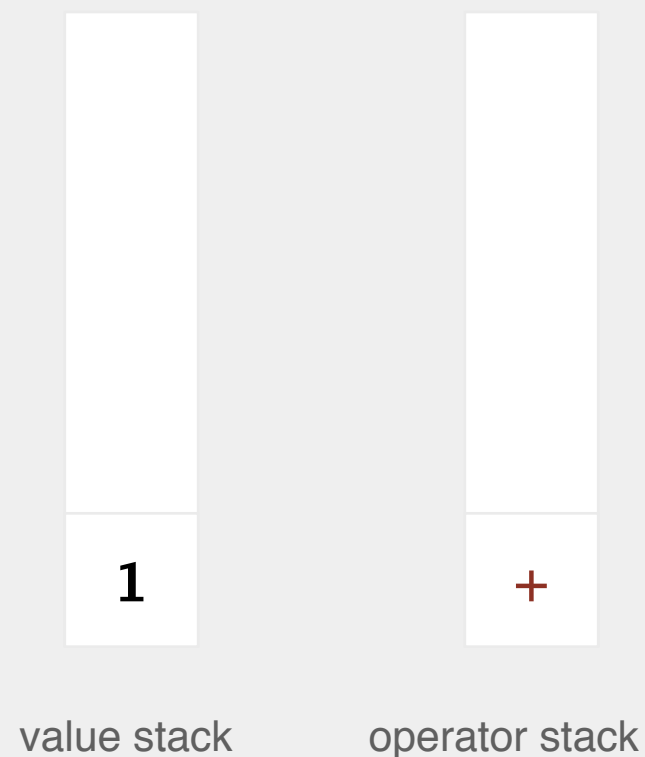
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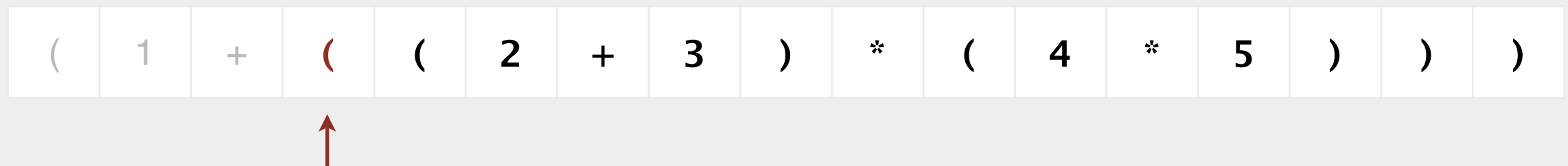
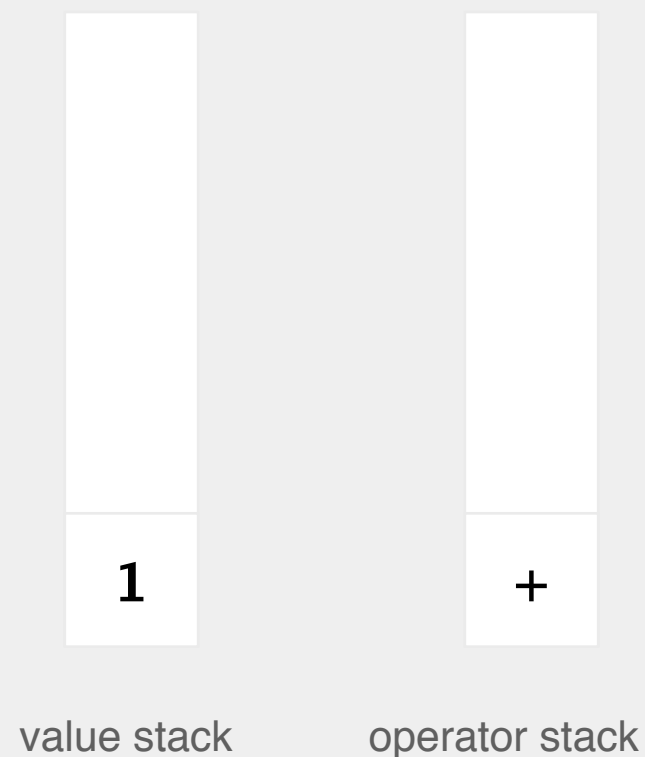
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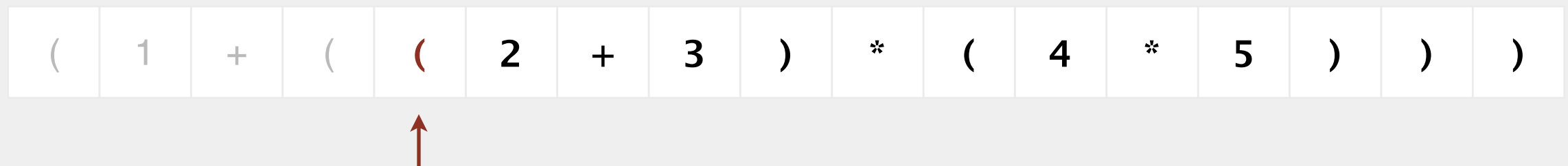
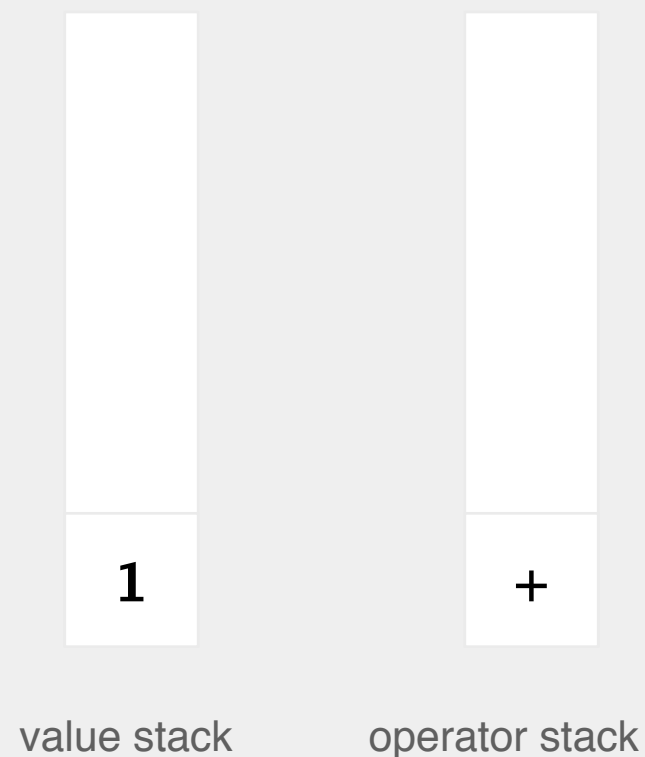
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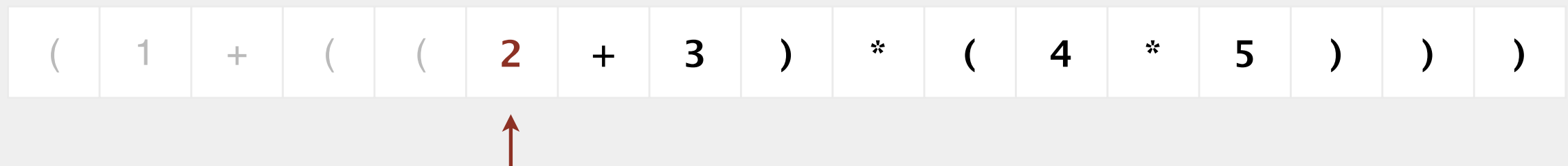
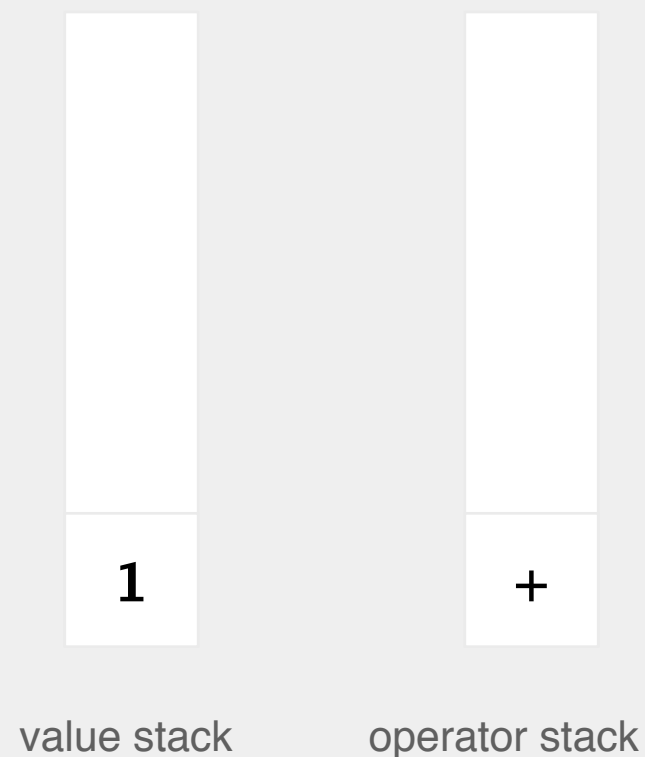
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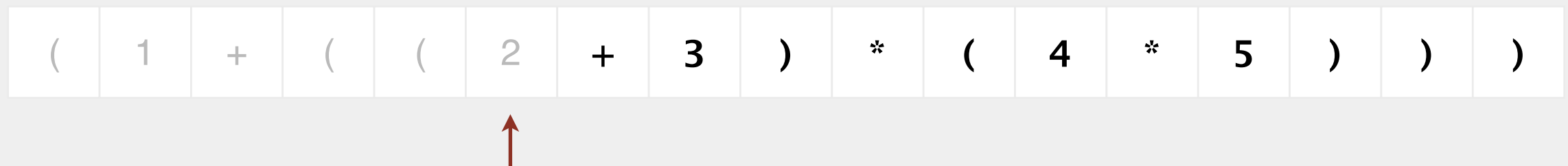
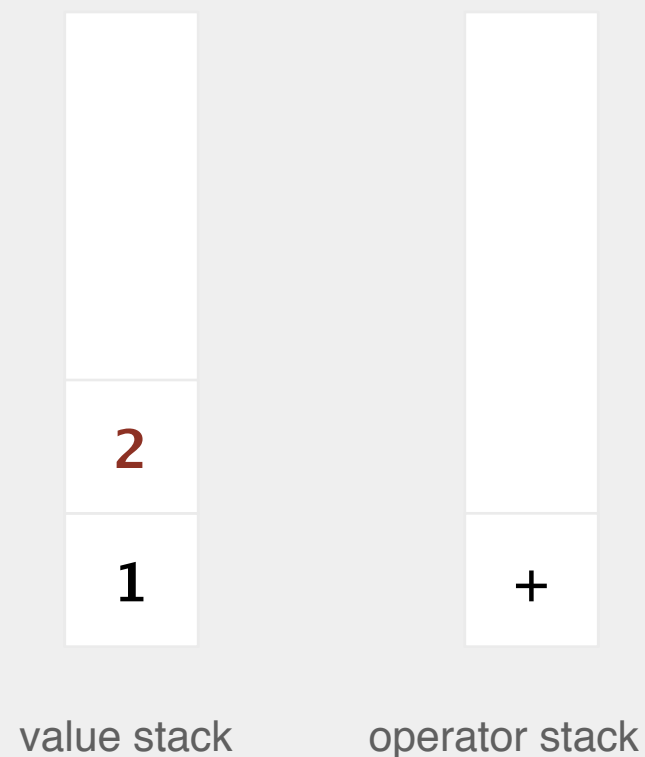
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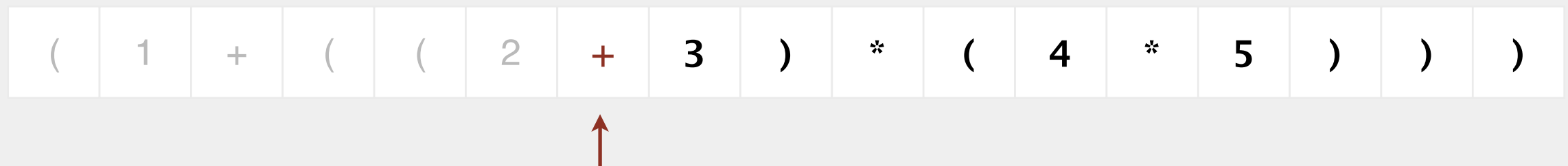
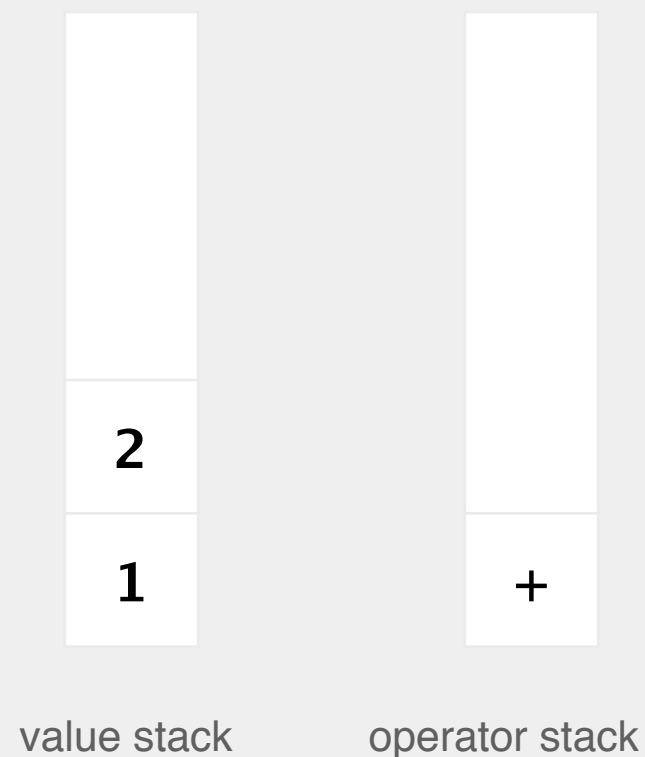
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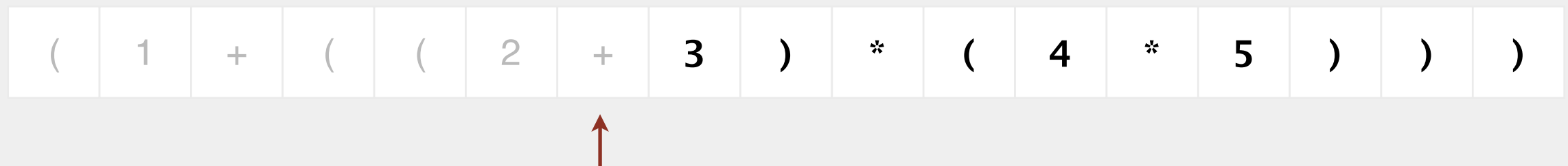
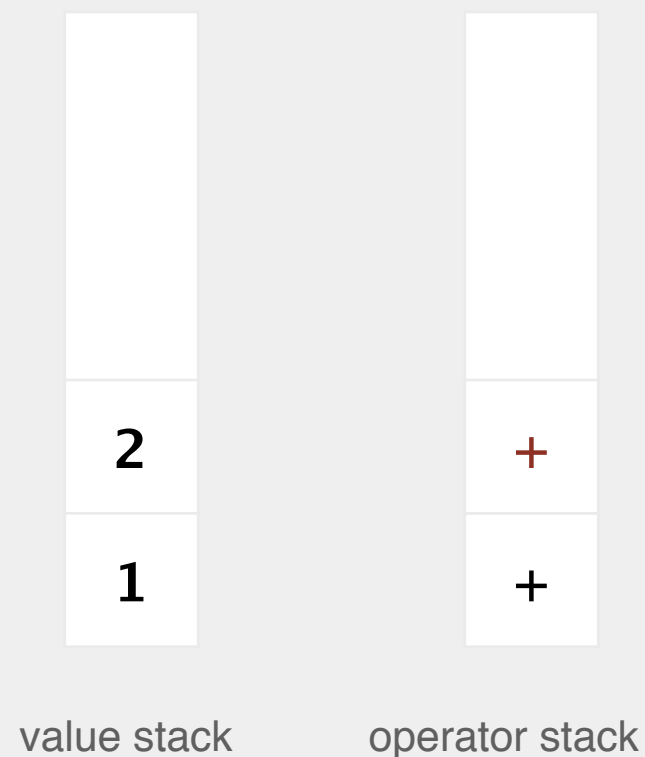
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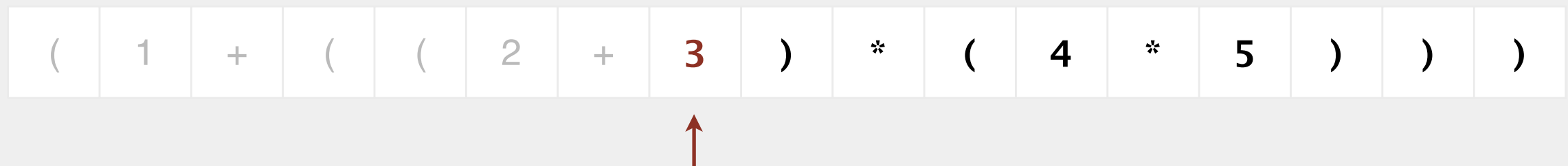
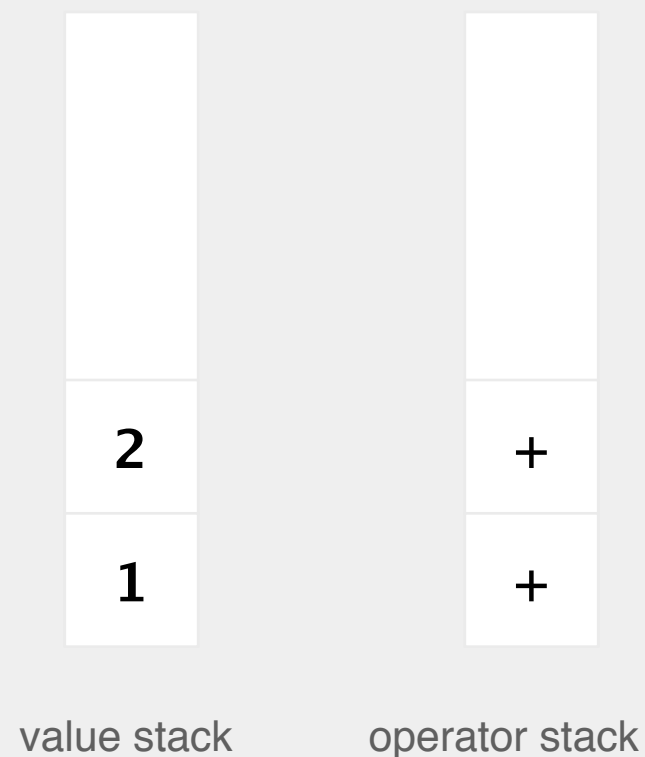
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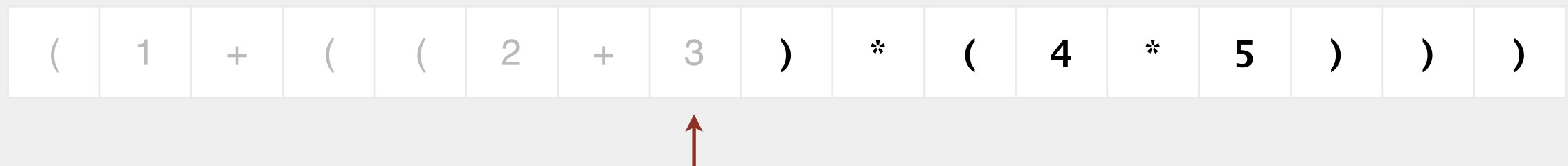
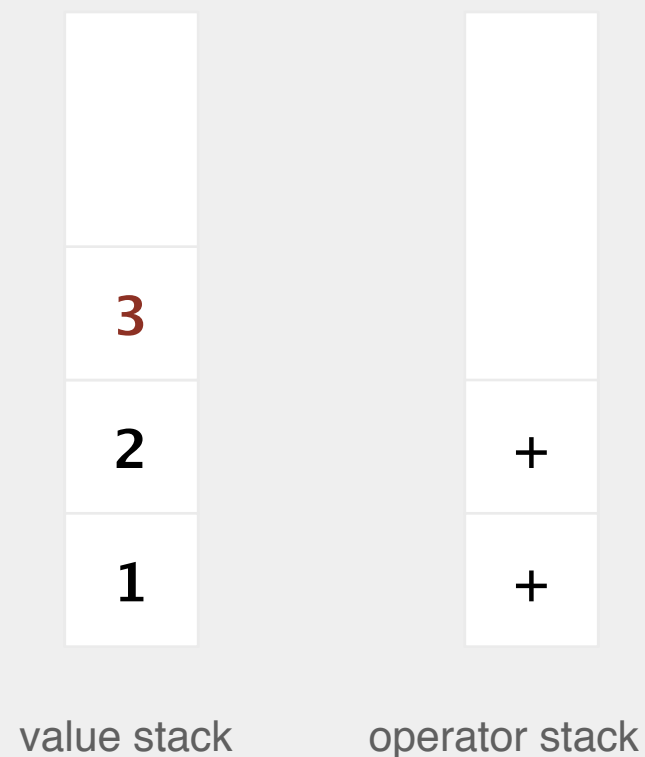
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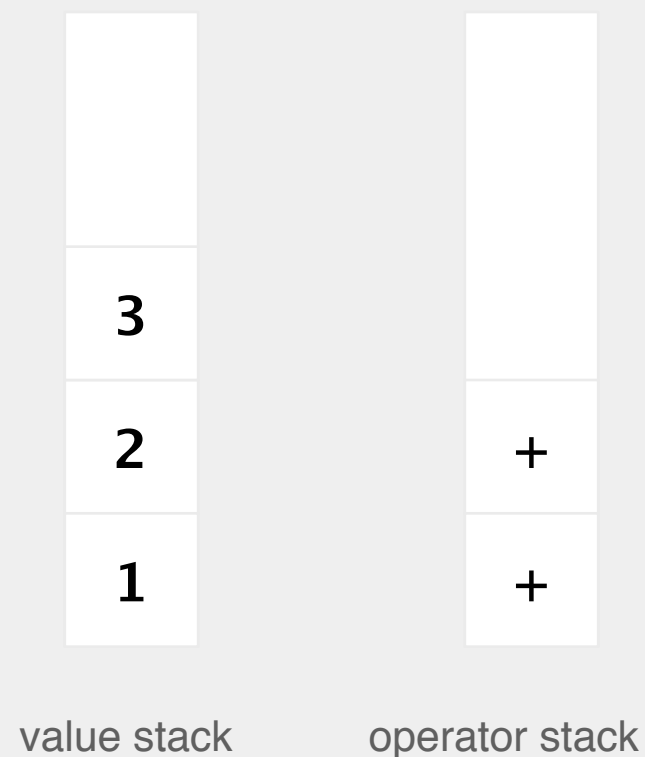
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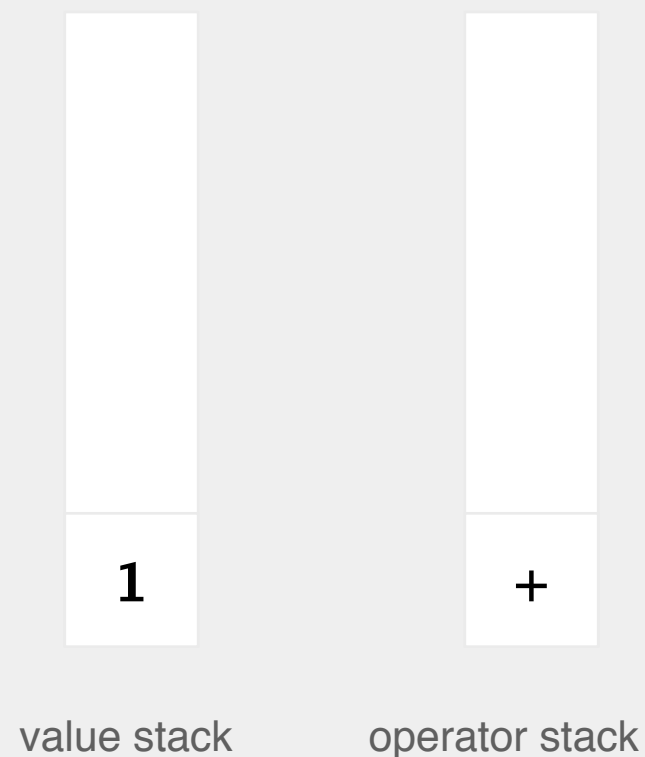
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3 + 2

( 1 + ( ( 2 + 3 ) \* ( 4 \* 5 ) ) )



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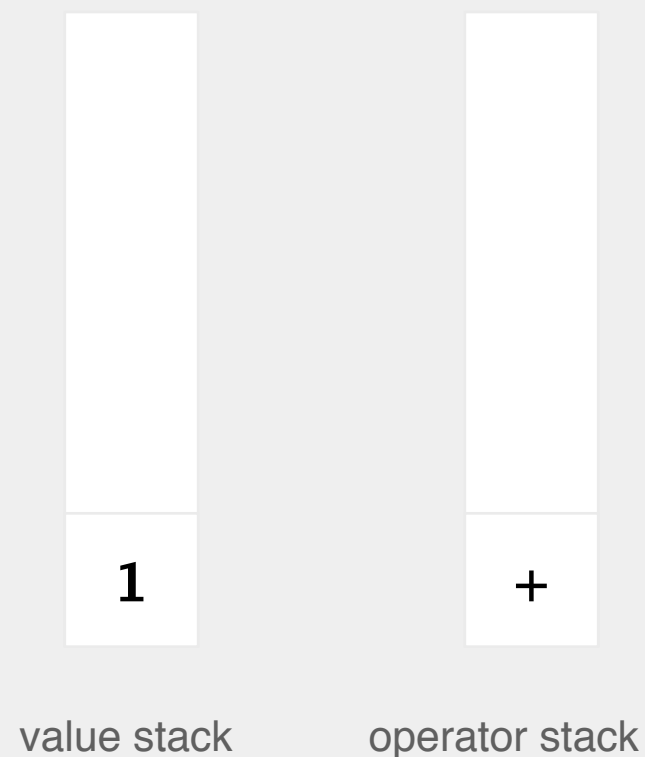
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3 + 2 = 5

( 1 + ( ( 2 + 3 ) \* ( 4 \* 5 ) ) )

↑

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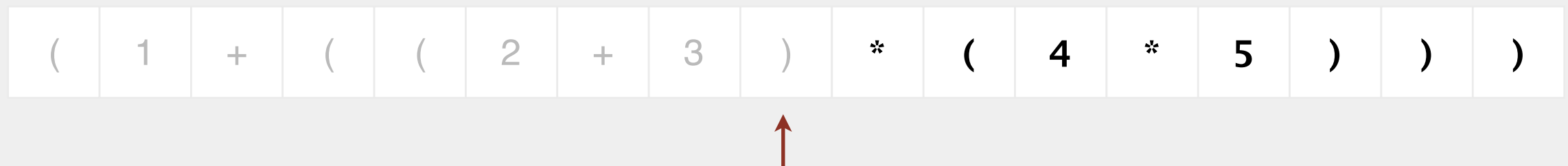
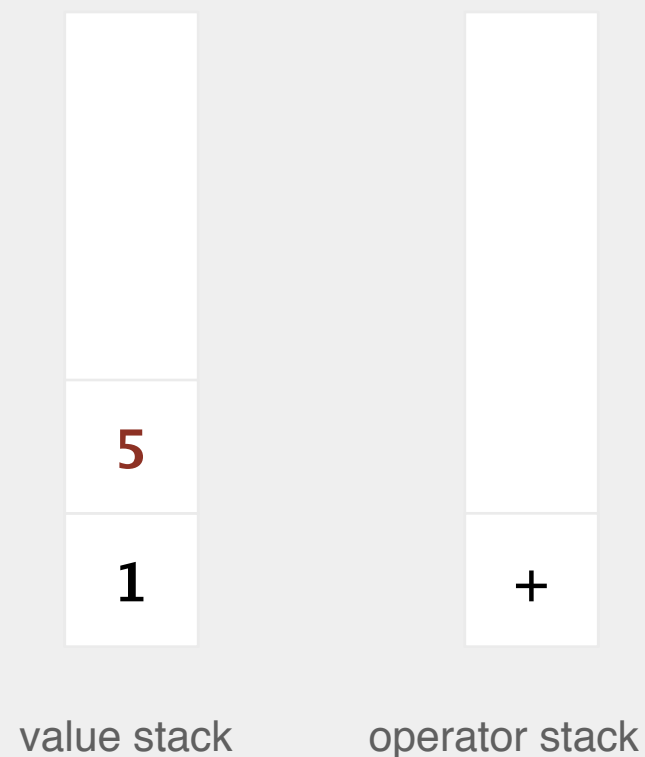
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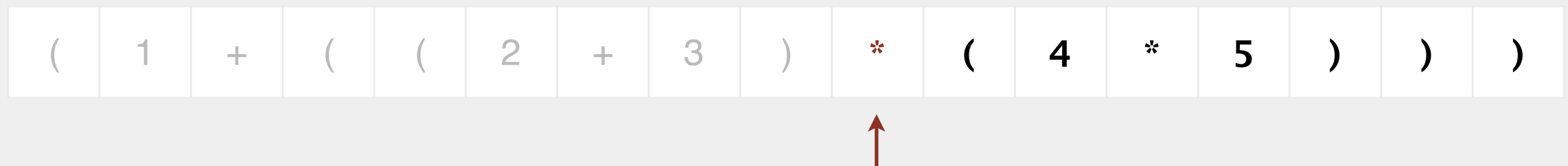
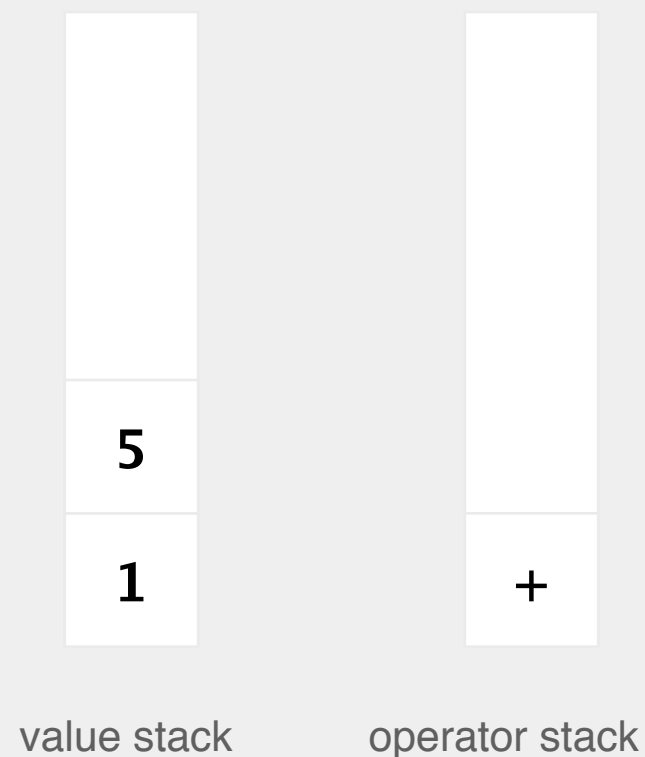
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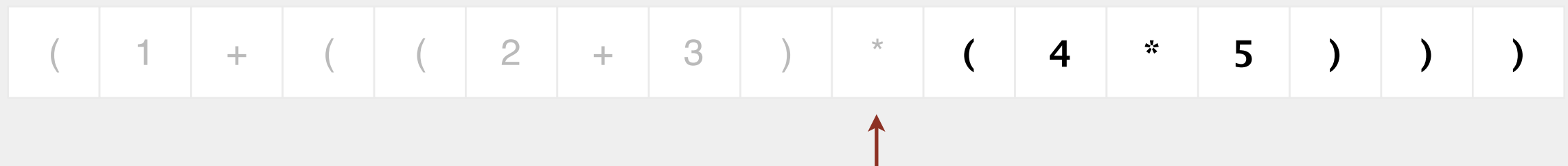
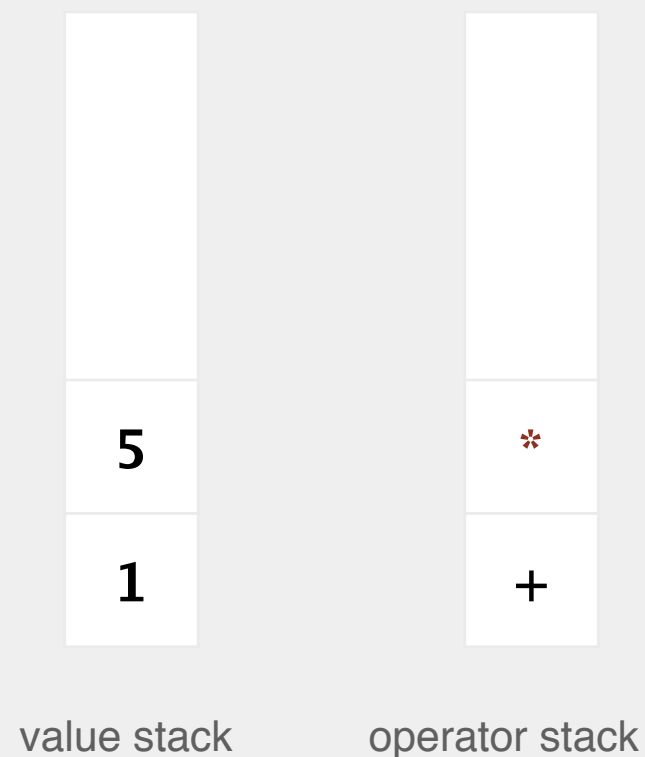
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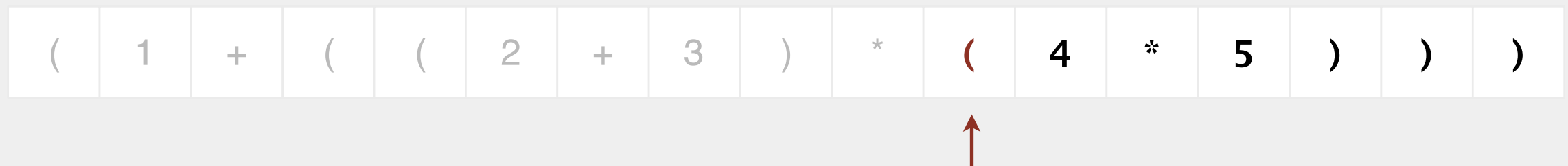
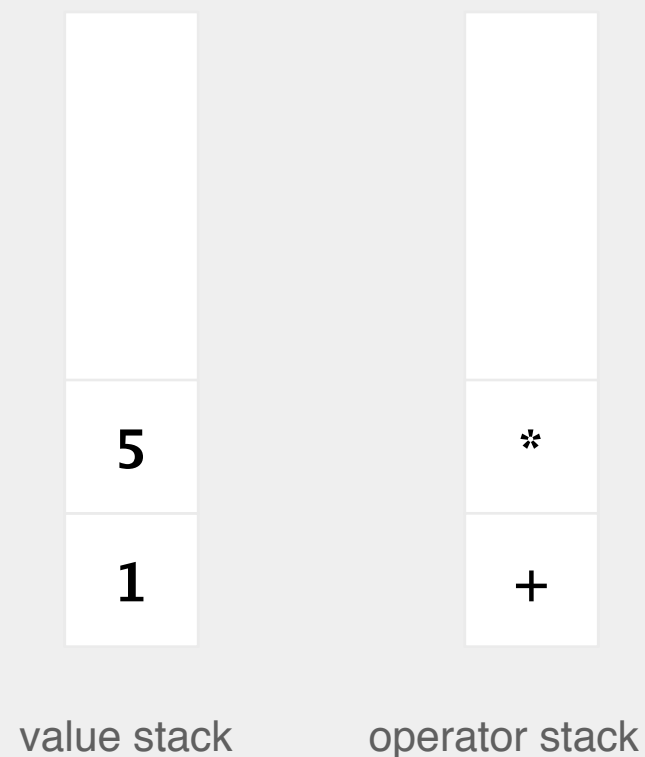
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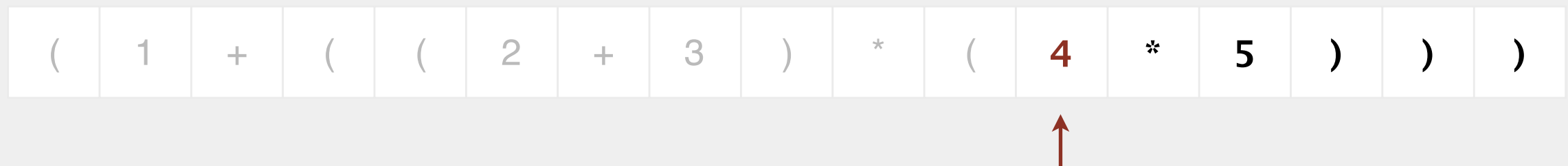
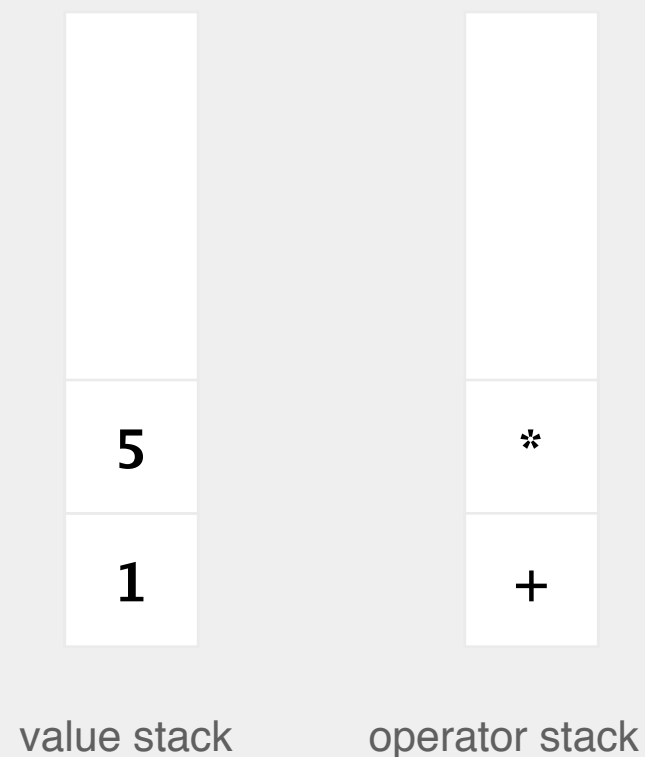
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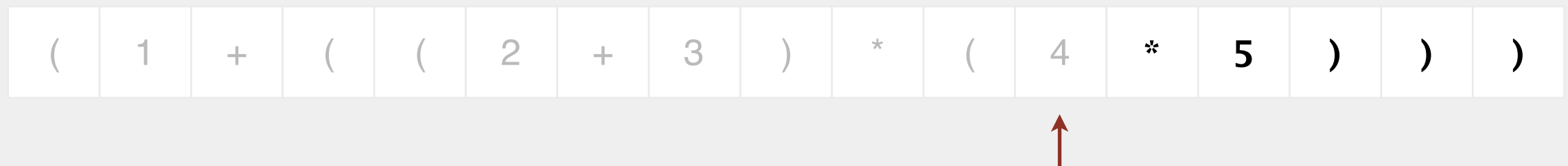
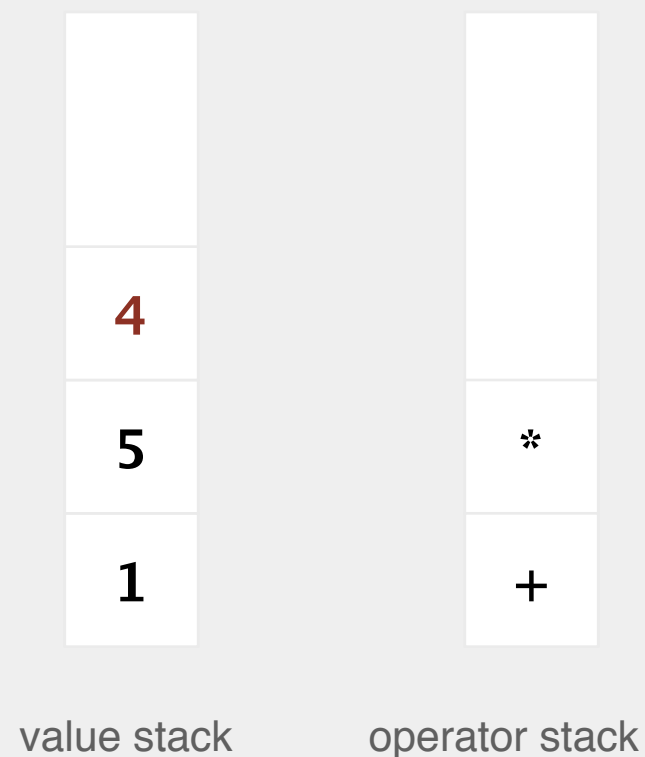
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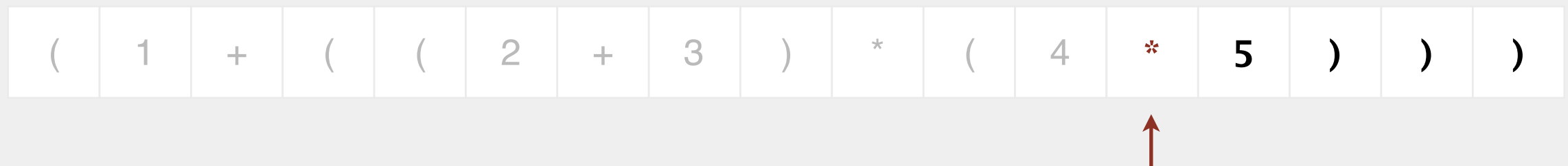
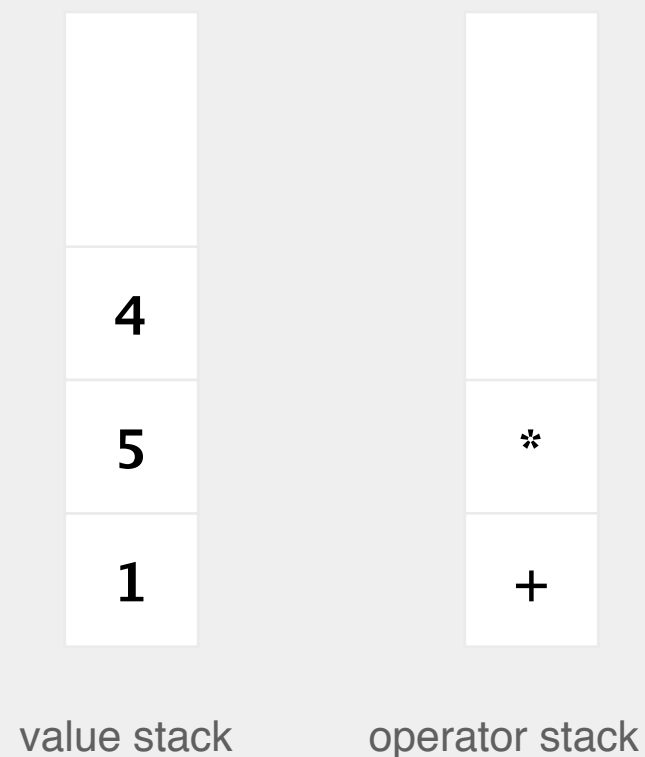
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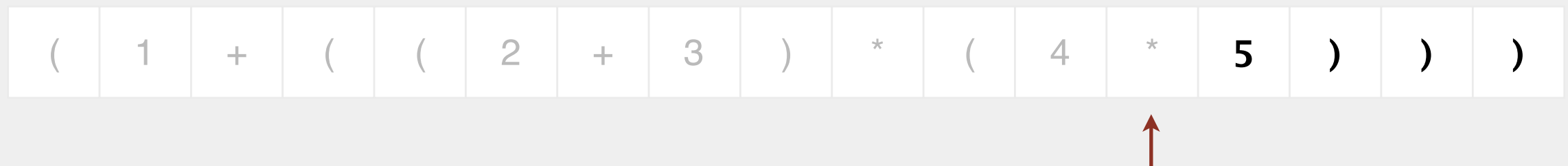
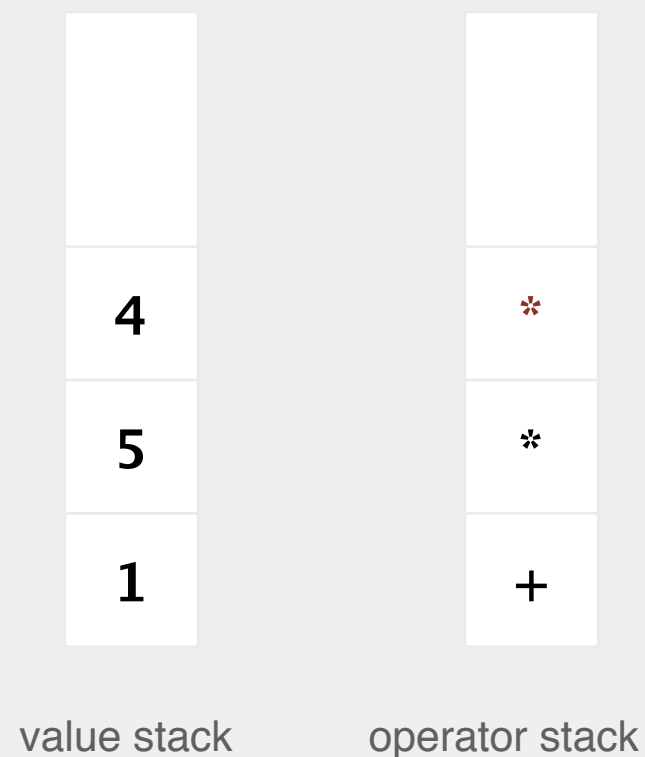
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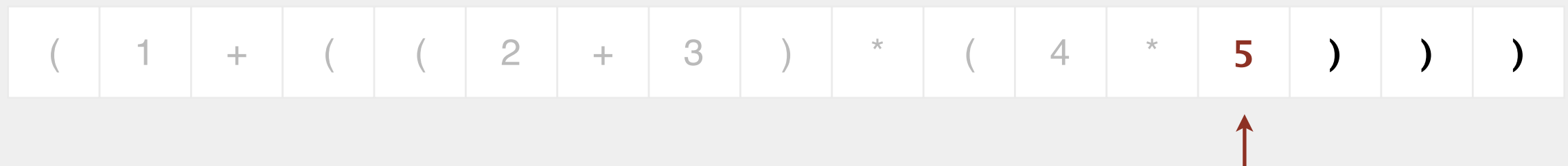
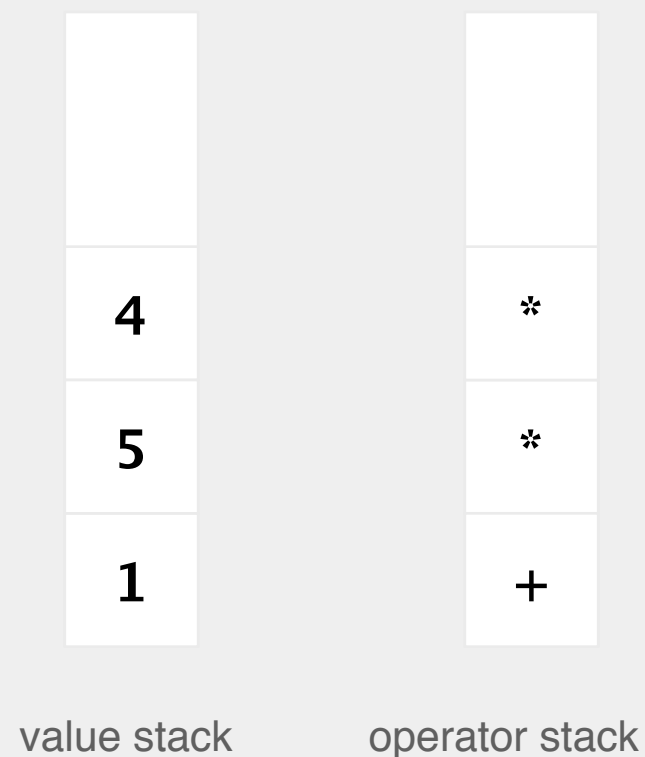
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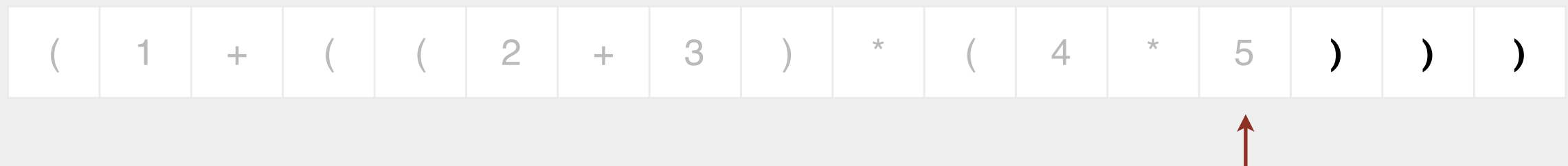
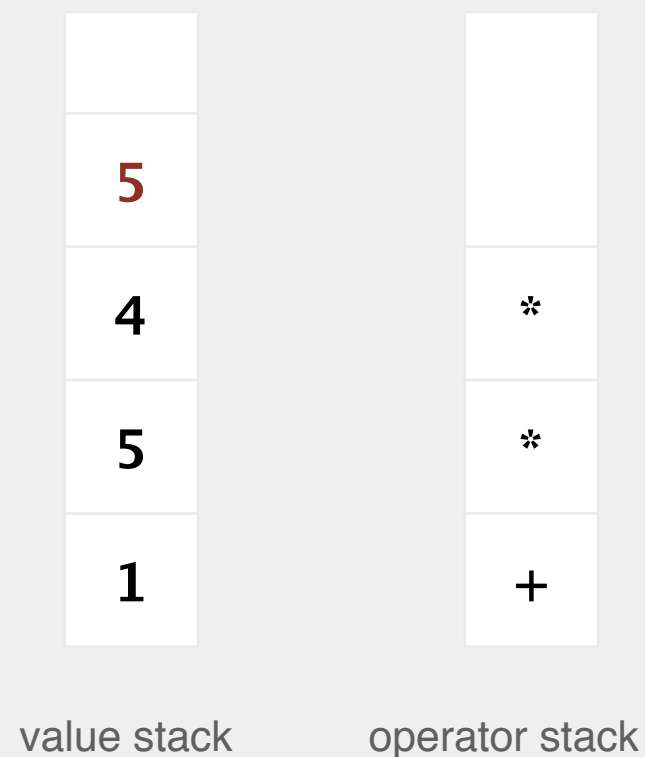
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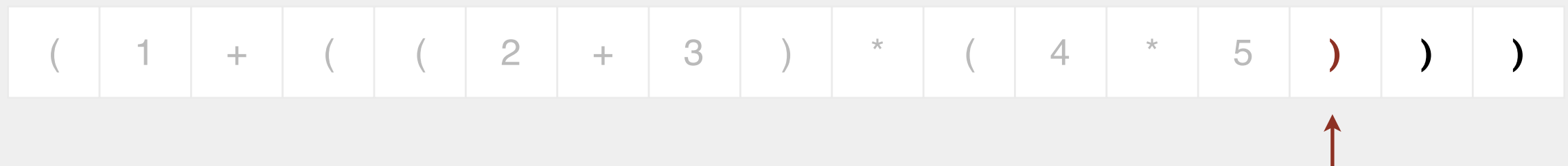
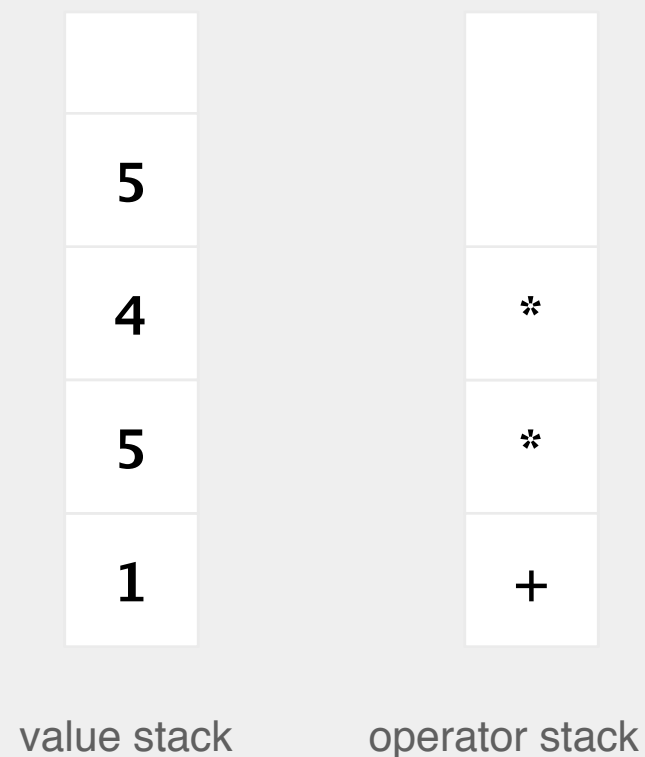
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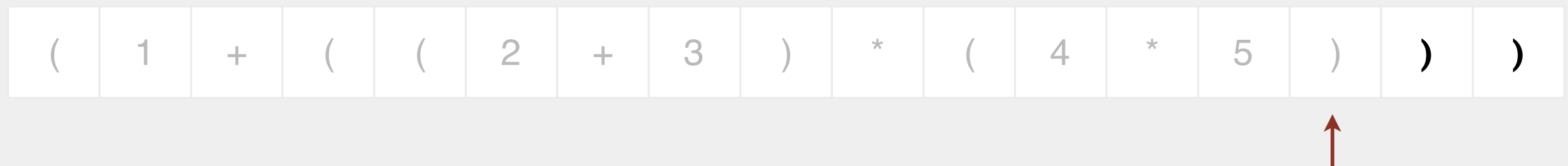
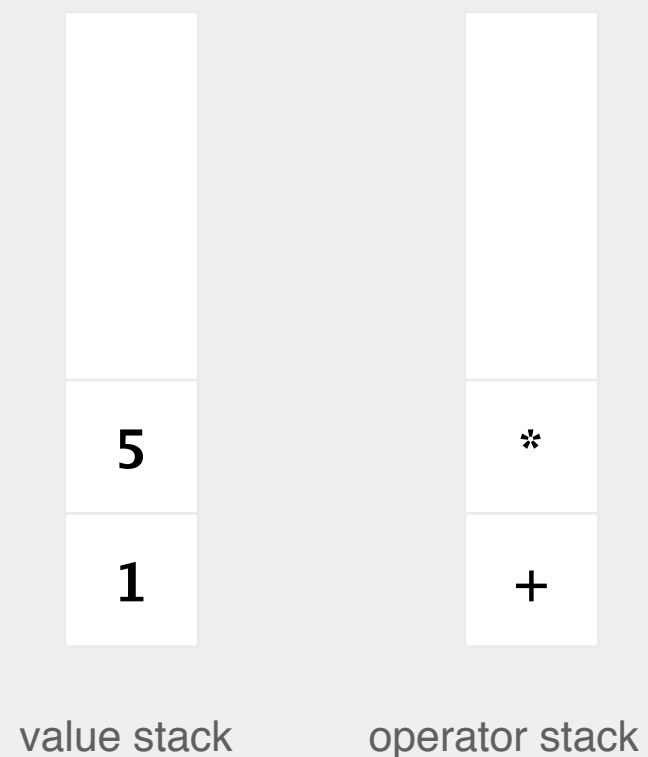
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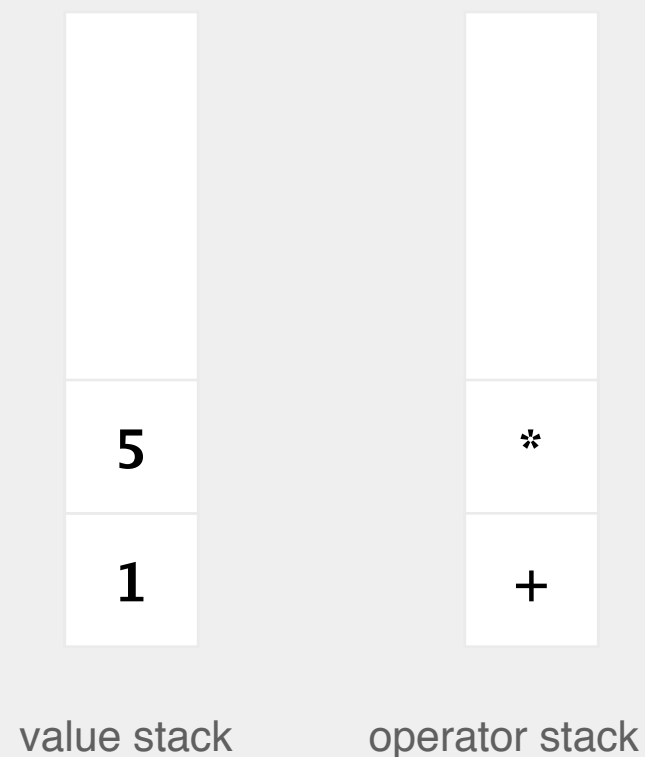
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5 \* 4 = 20

( 1 + ( ( 2 + 3 ) \* ( 4 \* 5 ) ) )

↑

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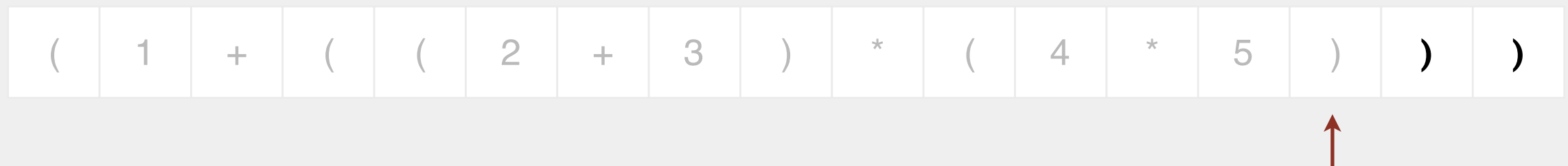
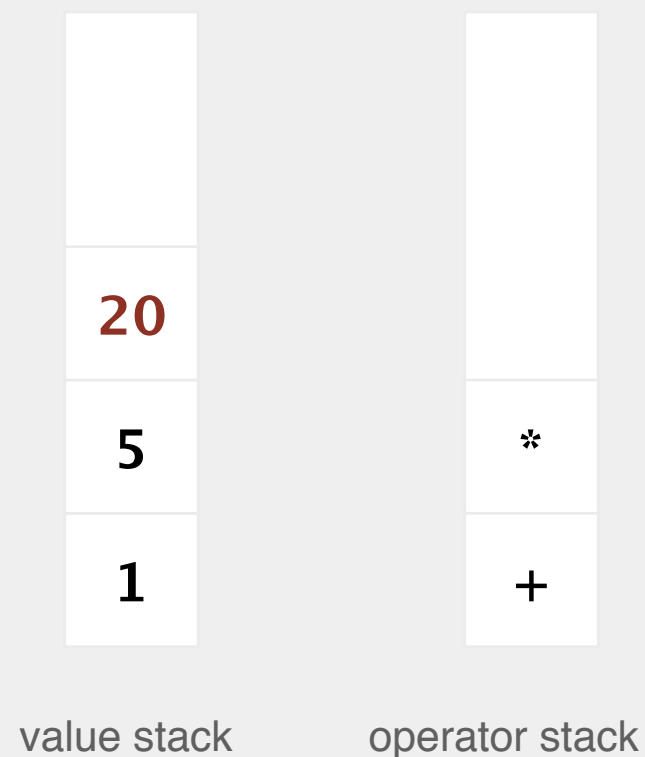
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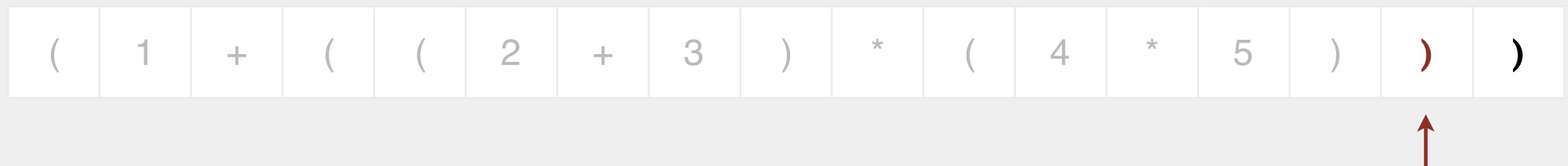
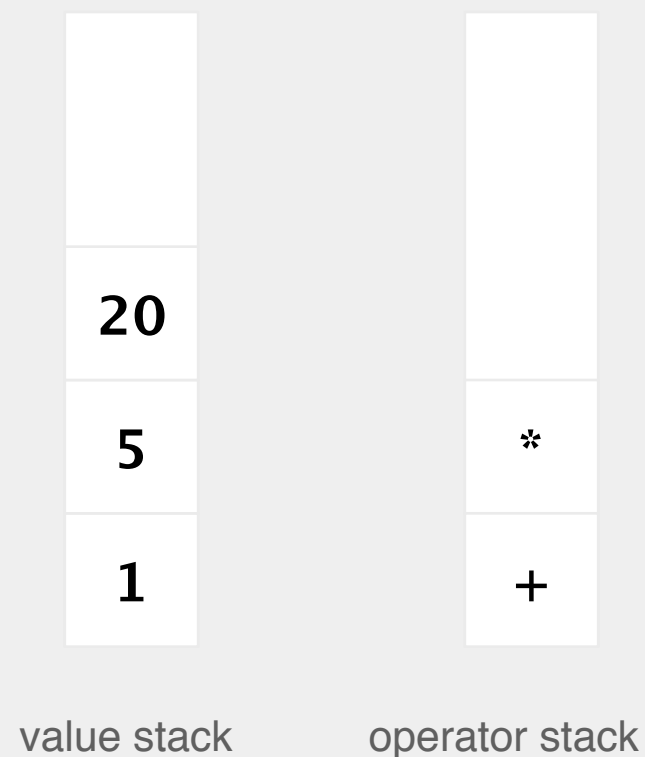
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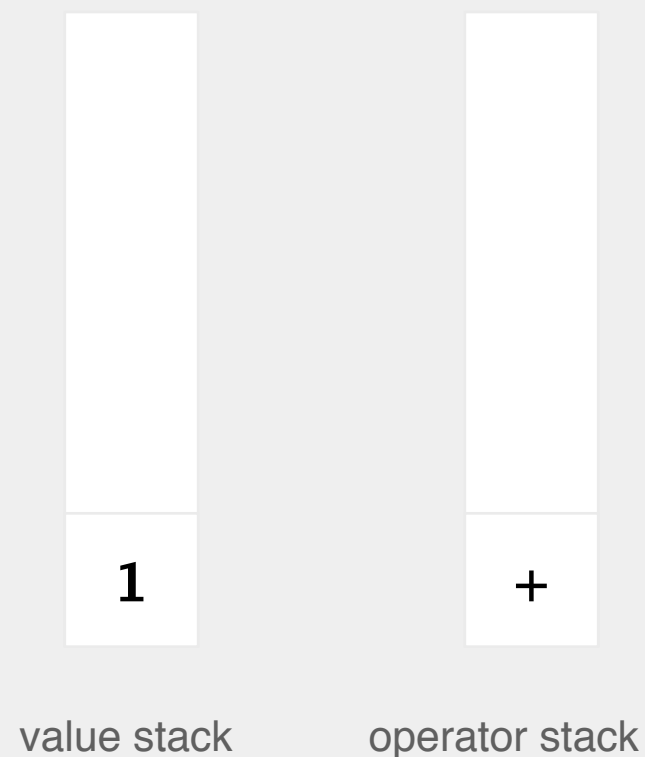
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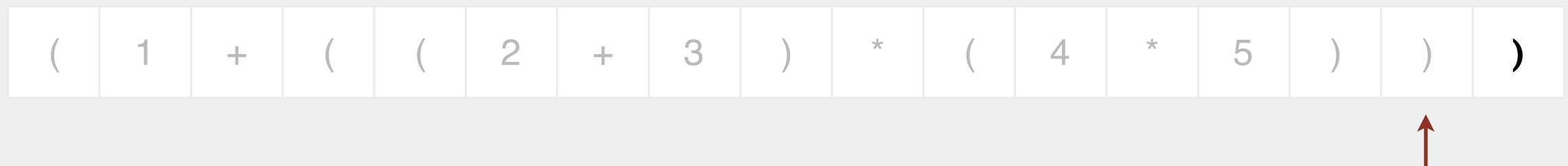
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20	*	5
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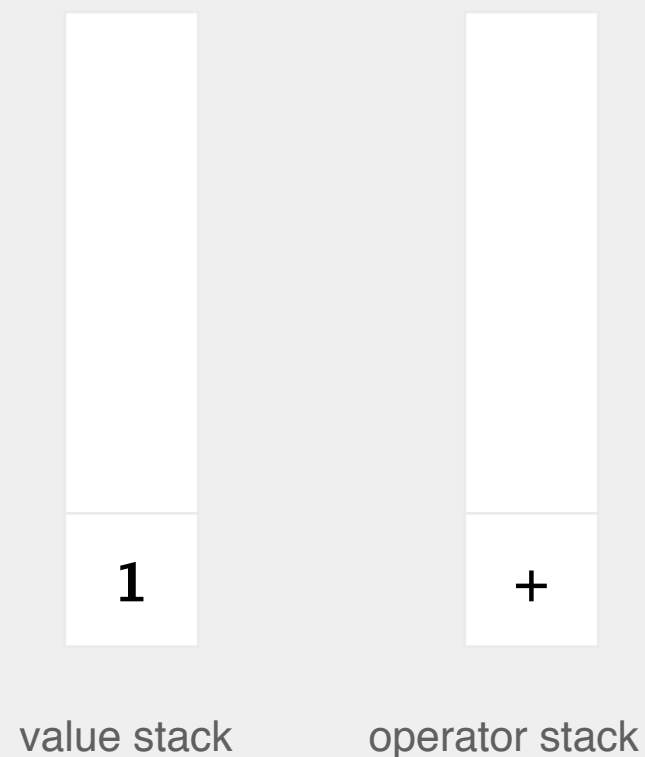
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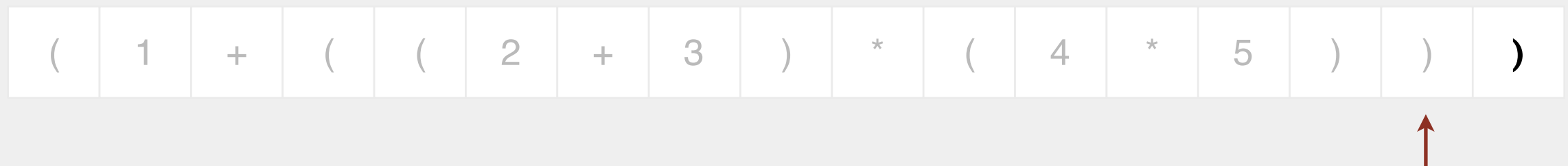
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20	*	5	=	100
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# Dijkstra's two-stack algorithm

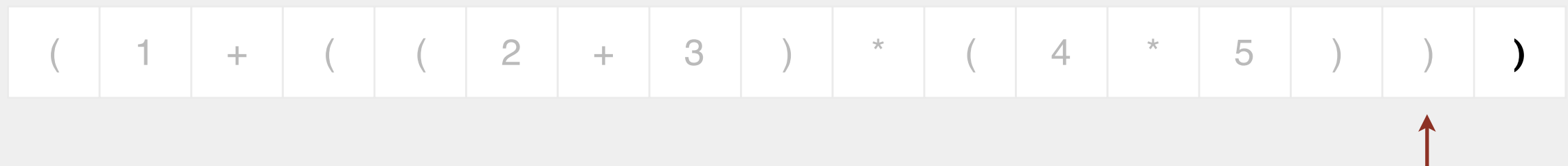
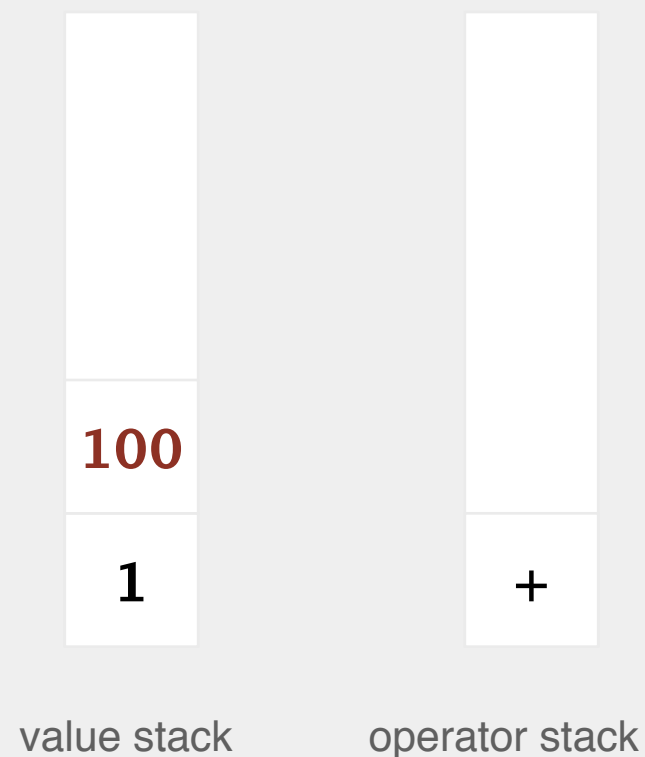
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**Value:** push onto the value stack.

**Operator:** push onto the operator stack.

**Left parenthesis:** ignore.

**Right parenthesis:** pop operator and two values; push the result of applying that operator to those values onto the value stack.



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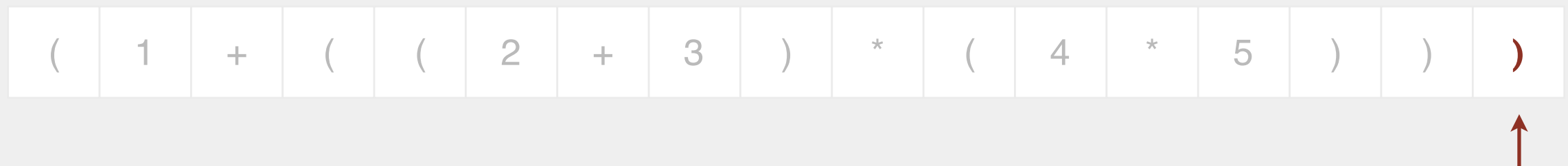
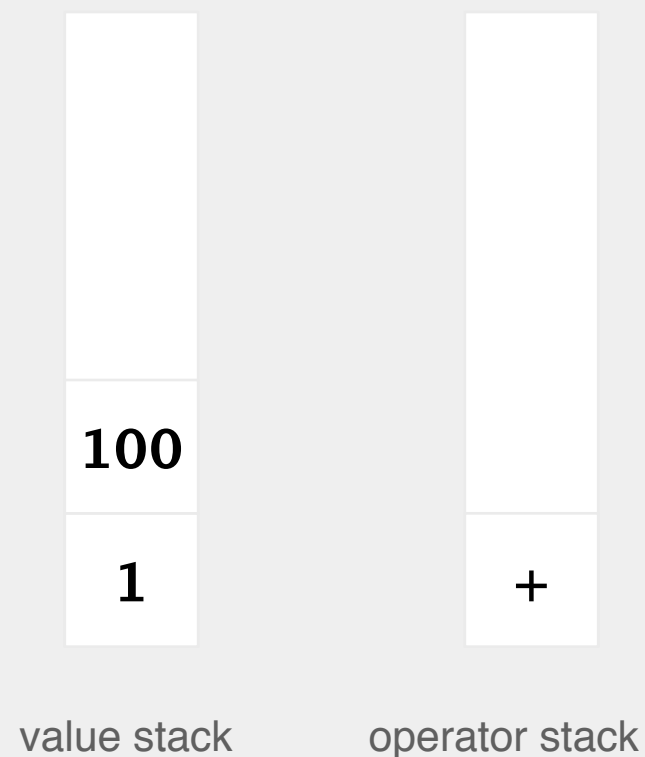
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100	+	1
-----	---	---

(	1	+	(	(	2	+	3	)	*	(	4	*	5	)	)	)
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---



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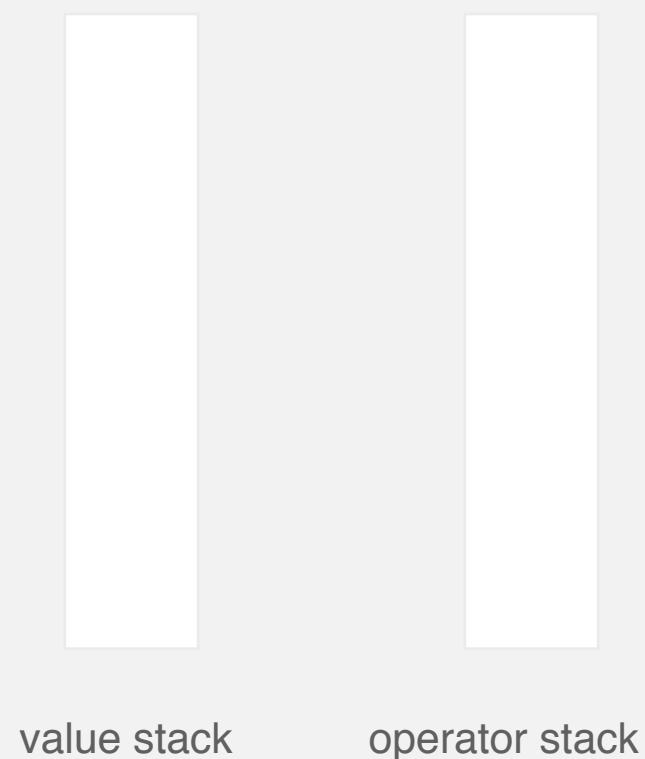
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100	+	1	=	101
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(	1	+	(	(	2	+	3	)	*	(	4	*	5	)	)	)
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# Dijkstra's two-stack algorithm

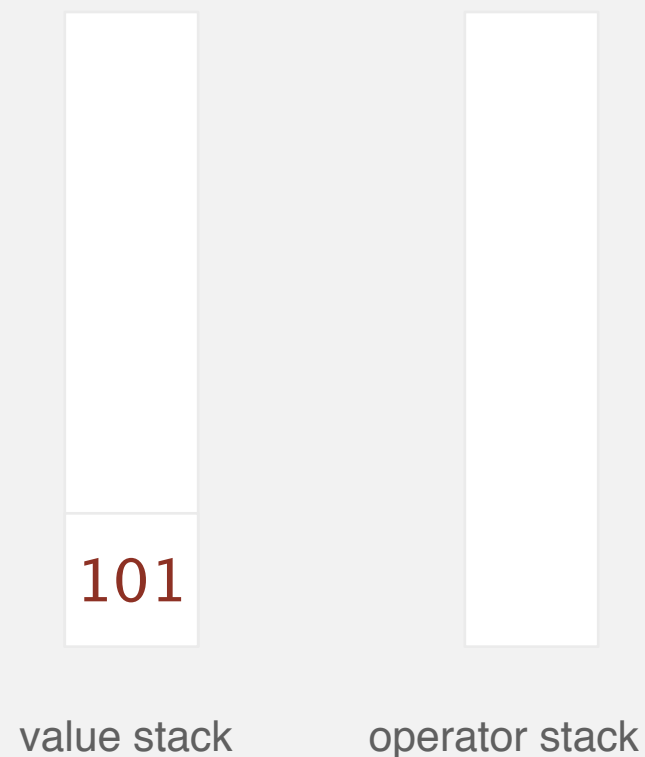
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(	1	+	(	(	2	+	3	)	*	(	4	*	5	)	)	)
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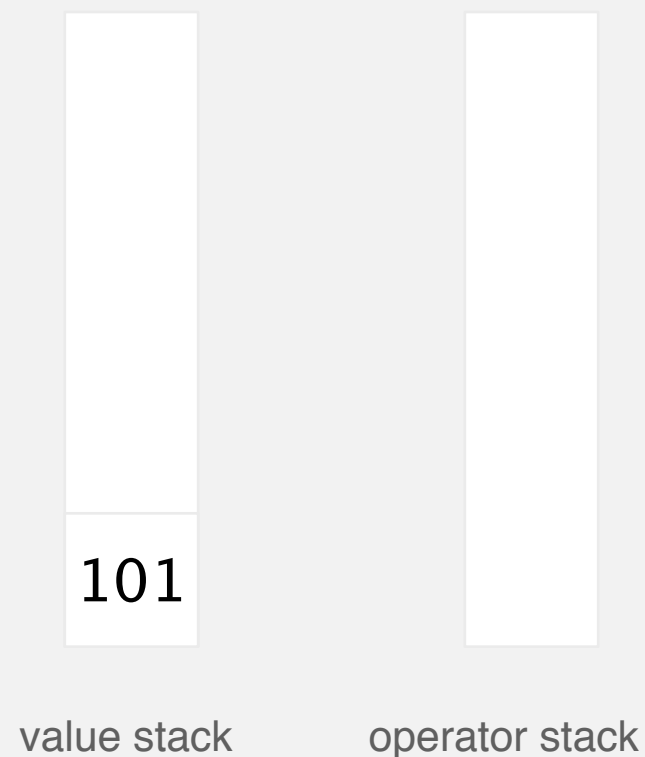
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(	1	+	(	(	2	+	3	)	*	(	4	*	5	)	)	)
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---



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**Operator:** push onto the operator stack.

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**Right parenthesis:** pop operator and two values; push the result of applying that operator to those values onto the value stack.

**End:** if there are any operators remaining in the operator stack, then implement them.

101

result

(	1	+	(	(	2	+	3	)	*	(	4	*	5	)	)	)
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---