

# Existence — Motion in Time

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## Abstract

### Existence as a Temporal Value

Existence is introduced as a primitive motion function distinct from magnitude (heat) and opposition (polarity). Where heat establishes motion in quantity and polarity establishes conserved opposition, existence establishes temporal state: whether motion is instantiated, absent, or transitioning. Existence is not reducible to duration, causality, or change; rather, it is the minimal condition required for any of these concepts to be defined.

This paper formalizes existence as a binary, time-indexed motion function, demonstrates its independence from other motion primitives, and shows how classical notions of time, persistence, and state arise only at higher descriptive layers.

## 1 Introduction — Why Motion Requires Existence

Motion cannot be meaningfully discussed without first establishing whether it is present. While magnitude may quantify motion and polarity may structure opposition, neither provides a mechanism for distinguishing between motion that is merely defined and motion that is instantiated. Any framework that omits this distinction implicitly assumes existence, thereby embedding temporal structure without formal acknowledgment.

In physical theories, this assumption often appears as an unexamined background time parameter. In computational systems, it appears as the silent distinction between allocated and executed state. In both cases, existence is treated as a side effect rather than a formal object of description.

The Motion Calendar rejects this implicit treatment. It asserts that existence is a prerequisite for motion to participate in time at all. Without existence, motion remains timeless, inert, and observationally inaccessible. Heat and polarity may describe potential motion, but existence determines whether that motion is realized at a given temporal index.

This distinction is not semantic. A motion with nonzero magnitude and well-defined polarity may nevertheless be non-existent. Conversely, existence does not alter magnitude or polarity; it merely determines whether they are expressed. Existence therefore cannot be derived from either quantity or opposition, nor can it be encoded as a property of them without circularity.

Crucially, existence is also not equivalent to change. A motion may exist without varying in magnitude or polarity, and it may cease to exist without undergoing transformation. Change, persistence, and causality all require existence, but existence requires none of them. It is the minimal temporal predicate upon which all higher motion descriptions depend.

For this reason, existence must be treated as a primitive motion function. It is the first function in the Motion Calendar that necessitates time, not because it measures duration, but because the distinction between presence and absence is undefined without temporal reference. Time enters the framework not as a dimension of motion, but as the index by which existence can be evaluated.

By formalizing existence explicitly, the Motion Calendar prevents the inadvertent introduction of temporal assumptions at lower descriptive layers. This separation enables a clean construction of time, state, and persistence as emergent structures rather than axiomatic givens.

## 2 What Existence Is Not

Because existence is introduced as a primitive motion function, it is especially susceptible to misinterpretation. Many familiar concepts—duration, causality, persistence, and logical truth—are commonly treated as inseparable from existence. In the Motion Calendar, this identification is explicitly rejected. Existence is defined minimally, and its scope is intentionally constrained.

### 2.1 Existence Is Not Duration

Existence does not measure how long motion persists. A motion may exist at a single temporal index without extending across adjacent indices. Duration requires comparison across time; existence only asserts presence at a specific time.

Treating existence as duration would introduce accumulation and continuity assumptions that are not warranted at this level. Duration emerges only when existence is evaluated across ordered temporal indices, and therefore cannot be primitive.

### 2.2 Existence Is Not Change

Existence does not imply variation. A motion may exist while remaining constant in magnitude and polarity, and it may cease to exist without undergoing transformation. Change requires at least two distinct existence evaluations; existence itself is singular and local in time.

Equating existence with change collapses temporal instantiation into dynamics, obscuring the distinction between being present and being altered. The Motion Calendar maintains this separation explicitly.

### 2.3 Existence Is Not Causality

Existence does not imply cause, effect, or dependency. The appearance or disappearance of motion under the existence function does not, by itself, establish a reason. Causality requires ordered relations between distinct states; existence merely identifies whether a state is instantiated.

By withholding causal structure at this layer, the Motion Calendar avoids embedding explanatory assumptions into foundational definitions. Causality is constructed later through composition with order and directional motion.

### 2.4 Existence Is Not Persistence

Persistence is the repeated satisfaction of existence across multiple temporal indices. It is a pattern, not a primitive. A motion that persists does so because existence evaluates to present over time, not because persistence is inherent to existence itself.

This distinction prevents persistence from being assumed as a default property of motion. Instead, persistence becomes an emergent phenomenon that must be explained rather than presumed.

## 2.5 Existence Is Not Logical Truth

Although existence is binary in value, it does not correspond to logical truth or falsity. Existence asserts instantiation, not correctness, validity, or semantic meaning. A motion may exist and still be false, contradictory, or incoherent at higher descriptive layers.

Separating existence from logic preserves ontological neutrality. Logical systems may operate on existing motion, but existence itself does not evaluate propositions.

## 2.6 Existence Is Not Information

Existence introduces no information beyond instantiation. It does not encode memory, identity, or state description. Any informational content arises from structure imposed on existing motion by higher motion functions.

This constraint ensures that existence cannot be used to smuggle complexity into the foundation. It gates motion into time without enriching it.

# 3 Existence as a Motion Function

## 3.1 Primitive Definition

Let  $m$  denote a motion-instance, and let  $T$  denote a temporal index set. Existence  $\varepsilon$  is defined as a primitive motion function:

$$\varepsilon : M \times T \rightarrow \{0, 1\}.$$

The interpretation is:

$$\varepsilon(m, t) = 1 \quad \text{motion is instantiated at temporal index } t,$$

$$\varepsilon(m, t) = 0 \quad \text{motion is not instantiated at temporal index } t.$$

This definition is intentionally minimal. It introduces neither dynamics nor persistence. It only provides the ability to evaluate instantiation at a time.

## 3.2 Time Enters Only as an Index

Time is not defined as a substance, dimension, or causal medium. In this layer it is only the index required to evaluate existence.

We require only that  $T$  support distinguishability of indices:

$$t_1 \neq t_2.$$

No metric, continuity, or ordering is assumed yet. Ordering may be introduced later as part of the order function; here, time is only an address space for instantiation.

## 3.3 Existence-Gated Motion Expression

Let  $\kappa(m)$  denote the heat (magnitude) of motion  $m$ . Define the expressed magnitude of  $m$  at time  $t$  as:

$$\kappa_t(m) = \varepsilon(m, t) \kappa(m).$$

This produces the correct gating behavior:

If  $\varepsilon(m, t) = 0$ , then  $\kappa_t(m) = 0$  (unexpressed magnitude, not negated heat).

If  $\varepsilon(m, t) = 1$ , then  $\kappa_t(m) = \kappa(m)$ .

This makes explicit the core claim: existence does not modify magnitude; it only gates whether magnitude is expressed in time.

### 3.4 Existence with Polarity

Let polarity be represented as a sign operator  $\sigma$  acting on a magnitude  $\kappa$ , yielding a signed expression  $\sigma\kappa$ .

Existence gates this expression identically:

$$\varepsilon(m, t) (\sigma\kappa).$$

Thus, polarity is definable without time, but its instantiation in time requires existence.

### 3.5 Transition and the Minimal “Motion in Time” Operator

To speak about transition without importing dynamics, define the existence difference operator over two temporal indices:

$$\Delta\varepsilon(m; t_1, t_2) = \varepsilon(m, t_2) - \varepsilon(m, t_1).$$

Then:

$$\Delta\varepsilon = 1 \text{ birth / instantiation event,}$$

$$\Delta\varepsilon = -1 \text{ cessation event,}$$

$$\Delta\varepsilon = 0 \text{ no existence change.}$$

This defines transition purely as a relation between existence evaluations, without duration, cause, or persistence.

### 3.6 Constraints and Non-Interference

Existence must satisfy the following non-interference constraints with lower primitives:

1. No magnitude modification:

$$\varepsilon(m, t) \kappa(m) \neq \kappa'(m).$$

2. No polarity modification:

$$\varepsilon(m, t) (\kappa, \sigma) \neq (\kappa, \sigma').$$

3. No information injection: existence introduces only the bit-valued instantiation outcome at  $(m, t)$ .

4. No causal entailment: the mapping  $\varepsilon$  is not constrained by causal laws at this layer.

### 3.7 Minimal Existence Algebra

Since  $\varepsilon \in \{0, 1\}$ , the following identities hold for all  $(m, t)$ :

Idempotence:

$$\varepsilon^2 = \varepsilon.$$

Gating stability:

$$\varepsilon(m, t) \varepsilon(m, t') = \varepsilon(m, t) \varepsilon(m, t').$$

Complement: Define  $\bar{\varepsilon} = 1 - \varepsilon$ , interpreted as non-instantiation.

### 3.8 Summary

Existence  $\varepsilon$  is a binary time-indexed function that gates motion into temporal reality without introducing duration, change, causality, persistence, or meaning. Heat and polarity remain timeless descriptors of motion content; existence determines when that content is instantiated.

## 4 Time as an Emergent Index Structure

### 4.1 Time Is Required by Existence, Not Prior to It

Time is introduced in the Motion Calendar solely because existence requires an index against which instantiation can be evaluated. There is no notion of time independent of existence; without the ability to distinguish between present and absent, temporal reference collapses.

Accordingly, time is not treated as a primitive dimension of motion. It is an emergent structure whose minimal role is to support repeated evaluation of the existence function.

### 4.2 Minimal Temporal Structure

The weakest structure sufficient for existence is a set:

$$T.$$

Such a set allows evaluation of  $\varepsilon$  but supports no comparison between indices. In this regime, instantiation is defined, transition can be stated relationally, and duration, order, and causality are undefined.

### 4.3 Ordered Time as a Derived Structure

If an order relation  $\prec$  is introduced on  $T$ , then temporal succession becomes meaningful:

$$t_1 \prec t_2.$$

With ordering, transitions gain directionality, and persistence becomes interpretable as sustained instantiation across ordered indices.

### 4.4 Metric Time and Duration

Only when a metric  $d$  is imposed does duration become definable:

$$\text{duration}(t_1, t_2) = d(t_1, t_2).$$

Duration is therefore a higher-order construct dependent on existence, ordering, and metric structure.

### 4.5 Time Has No Dynamics at This Layer

No assumption is made that time flows, advances, or progresses. Time is a static index space necessary for instantiation to be meaningful.

### 4.6 Summary

Time enters the Motion Calendar only because existence demands an evaluative index. Its structure may be progressively enriched, but none of these enrichments are primitive.

## 5 Instantiation and Potential Motion

### 5.1 The Necessity of Non-Instantiated Motion

Motion may be fully specified yet non-instantiated:

$$\forall t \in T, \quad \varepsilon(m, t) = 0.$$

Such motion is potential, not contradictory or null.

### 5.2 Instantiated Motion

A motion  $m$  is instantiated at time  $t$  if and only if:

$$\varepsilon(m, t) = 1.$$

Instantiation permits motion to participate in temporal relations, interaction, and observation.

### 5.3 Potential Motion

Potential motion possesses defined heat and polarity but is not instantiated at a given time. Potential motion may be evaluated or composed without entering temporal reality.

### 5.4 Transition Between Potential and Instantiated Motion

The transition between potential and instantiated motion is governed entirely by  $\varepsilon$ .

No additional mechanism is required at this layer.

### 5.5 Separation of Evaluation and Realization

Evaluation of motion structure is distinct from realization in time. This separation prevents collapse of imagination into action or description into execution.

### 5.6 Summary

Existence divides motion into potential and instantiated regimes. This division is ontological, not semantic.

## 6 Existence and Identity

### 6.1 Identity Requires Persistence

Identity is not primitive. It requires repeated instantiation across time.

### 6.2 Identity as a Function of Existence

Let  $I(m)$  denote the identity support set:

$$I(m) = \{t \in T \mid \varepsilon(m, t) = 1\}.$$

If  $I(m)$  contains more than one ordered element, identity becomes definable.

### 6.3 Identity Mass

Define identity mass as:

$$\mu(m) = \sum_{t \in T} \varepsilon(m, t),$$

or, in metric time, as an integral over  $T$ .

### 6.4 Identity Without Memory

Identity does not require memory. Memory is informational and arises later.

### 6.5 Identity Is Not Essence

Identity is sameness of existence support, not sameness of structure.

### 6.6 Summary

Identity emerges from existence evaluated over time.

## 7 Existence and Causality

### 7.1 Causality Is Not Primitive

Causality is derived, not fundamental.

### 7.2 Causal Preconditions

Causality requires ordered time, persistent identity, and relational constraints.

### 7.3 Causal Chains

Existence supplies the *when*; causality requires an added *because*.

### 7.4 No Spontaneous Causation

Existence transitions do not imply cause.

### 7.5 Directionality and Asymmetry

Causal asymmetry arises only with ordered time and persistent identity.

### 7.6 Summary

Causality is an emergent relational structure imposed on ordered existence transitions among persistent identities. Existence enables causality but does not enforce it.

The need to evaluate multiple co-present existences within a shared relational frame motivates the introduction of righteousness as the next motion function.