

Math Notation

see [conventional math notation](#)

this note describes my own [math notation](#), meant to solve inconsistencies in [conventional math notation](#). it is not meant to be a fully formal system of [mathematics](#); rather, it is built to be easy to understand and intuitive to use by mere humans.

this [math notation](#) obviously cannot be used to communicate ideas to people who do not know it, but it has made my own experience of using [mathematics](#) much more enjoyable. being able to use a single relatively well defined notation in various [mathematics fields](#) that conventionally use their own made up notation has been invaluable

principles

- all equality [operators](#) check for equality and return a [boolean](#), and it is implied that an [expression](#) on its own must evaluate to \top . this allows for [boolean logic operators](#) to be applied on equalities explicitly as opposed informally
- [sets](#) are [functions](#) that return a [boolean](#) ([sets](#) are [predicates](#)). this way, [boolean logic operators](#) and [set operators](#) are one and the same. other [data structures](#) that work similarly include [vectors](#), [matrixes](#), [sequences](#), [multisets](#), [ordered pairs](#)...
- some [operators](#) are identical but have different precedence as "more brackets means more explicit, but less brackets means less complex and less confusing"
- $[a]$ returns both positive and negative square roots ($[q^2] \equiv \pm q$). the same is true for other reciprocals
- superscripts are modifiers (subscripts with special meanings). this distinction is extremely useful when working with [forward propagation](#) and [backpropagation](#) in [neural networks](#), for example
- [derivatives](#) are not to be written as y' , but rather as their complete form $\delta y - \delta x$. this makes [calculus notation](#) way more intuitive
- all indices start at 0, as they always should have
- [rank polymorphism](#) is supported over all [operators](#)

notation

also see [trigonometric functions](#) and [calculus notation](#)

let:

- M be a [matrix](#)

- V be a vector
- P be an ordered pair
- M' be a multiset
- G be a graph
- E be an expression
- x be a variable
- f be a function
- A be a sequence
- B be a series
- a, b be any mathematical objects
- A, B be any mathematical objects with rank greater than 1
- n, i be natural numbers
- b be a boolean
- ω be any number
- \circ be any operator

operator descriptions

notation	description	notes
$a : b$	addition or disjoint union	
$a \cdot b$	subtraction	
\pm and \mp	\pm and \mp	
$a b$ and $a \mid b$	multiplication	
$a \div b$ and $a \div b$	division	
$[a]b$	exponentiation	represents a power by convention
$a[b]$	exponentiation	represents an exponential by convention
$\lfloor a \rfloor b$	b th root of a	$b = 2$ if b is omitted
$\lceil a \rceil b$	base- b <u>logarithm</u> of a	$b = e$ if b is omitted
$x \rightarrow E$	<u>function</u> literal	$f = x \rightarrow E \equiv f \leftarrow x = E$
$f \leftarrow E$	<u>function</u> application	uncommon, shorthand preferred
$a = b$	equality	numerical equality by convention
$a < b$ and $a > b$	strict inequality	
$a \leq b$ and $a \geq b$	non-strict inequality	

notation	description	notes
$a \wedge b$	logical AND or min function	
$a \vee b$	logical OR or max function	
a / b	logical difference	$a \wedge b = \perp$
$a \equiv b$	equality	logical equality by convention
$a \times b$	nonequality	also serves as logical XOR
$a \vdash b$	implication, subset	a implies b , b for all a
$a \dashv b$	reverse implication, superset	a for all b , b implies a
$a_0 \circ a_1 \circ \dots a_n$	with $n = 3$, $a_0 \circ a_1 \circ a_2 \circ a_3$	step size is $\therefore 1$ if $a_1 \circ$ is omitted
$a_0 \dots a_n$	with $n = 3$, a_0, a_1, a_2, a_3	step size is $\therefore 1$ if a_1 is omitted
$a \circ \dots$	the <u>reduce function</u> of \circ on a	
$f \dot{\vdash} a \circ \dots b$	$f(a \dots b) \circ \dots$	
$f \dot{\vdash} x \rightarrow a$	the <u>limit</u> of f as x approaches a	
x_{sub}	the <u>variable</u> x with a subscript sub	
V^n	the n th component of V	
A^i	the i th element of A	
B^i	the i th element of B	
$M^{(i,j)}$	the i, j th element of M	uncommon, shorthand preferred
M^\top	the transpose <u>matrix</u> of M	
$-M$	the multiplicative inverse of M	
P^b	the b th element of P	
$S a$	whether a is element of S	
$M' a$	the number of elements a in M'	
$G a$	whether vertex a is in G	
$G^{(a,b)}$	the number of edges from a to b in G	uncommon, shorthand preferred

shorthands

shorthand	definition	notes
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shorthand	definition	notes
$a \nmid b, a \neq b, a \not\leq b, a \not< b...$	$/(a \vdash b), /a = b, /a \leq b, /a < b...$	
$x\omega$	$[x]\omega$	
ax	$a \setminus x$	
$f\ x$	$f \leftarrow x$	common, longhand discouraged
$x\ y \rightarrow E$	$x \rightarrow y \rightarrow E$	
$\langle \rangle$	$\langle\langle \rangle\rangle$	see empty set
$()$	$(())$	see multiset
V^x, V^y, V^z	V^0, V^1, V^2	
$M^{i,j}$	$M^{(i,j)}$	common, longhand discouraged
$M^i,$	the i th row of M	
$M^{\cdot j}$	the j th column of M	
$P = \langle f, t \rangle$	$P^\perp = f \wedge P^\top = t$	see ordered pair
$S = \langle\langle a \dots b \rangle\rangle$	$S\ x \equiv x = a \vee \dots x = b$	see set
$V = (a \dots b)$	$V^0 = a \wedge \dots V^n = b$	see vector in rn
$M' = ((1, 2, 2, 2, 3, 3))$	multiset literal	see multiset
$M = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$	matrix literal	see matrix
$x \rightarrow (a < x < b)$	the interval from a to b	
$A \circ B$	$x \rightarrow A\ x \circ B\ x$	see rank polymorphism
$A \circ B$	$A\ x \circ B\ x$ for all x	$(\top \dots)$ is treated as \top
$\delta y - \delta x$	the derivative of y with respect to x	δ should be used instead of d
$\int y \mid \delta x$	the antiderivative of y with respect to x	δ should be used instead of d

constants

constant	definition	notes
\emptyset	<i>undefined</i>	see improved expression evaluation
\top	logical true	

constant	definition	notes
\perp	logical false	
τ	the ratio of the circumference of a circle to its radius	using π is discouraged
e	Euler's constant	see eulers constant
ι	$[\cdot 1]$	see imaginary , using i is discouraged
Π	the pi function	using fact is discouraged

operator properties

in order of high to low precedence

#todo fix asymmetry between $\neq > \geq < \leq$ and $\wedge \vee \dashv \vdash \equiv \times$

operator	associativity	unary identity	unary description
$() \langle \rangle \boxed{}$			
$\boxed{} \sqcup \sqcap$			
$\mid -$	left	1	inverse
$\delta \sin \# \leftarrow$	right-ish		
$: \cdot \therefore \therefore$	left	0	negation
$\mid -$	left	1	inverse
$\int \dot{} \dots \rightarrow \bmod$	right-ish		
$\neq > \geq < \leq$	AND	0	is (not) 0
$/$	left	\top	boolean logic NOT
$\wedge \vee$	left		
$\dashv \vdash$	left		
$\equiv \times$	AND	\top	boolean logic NOT
$,$			

note: above,

- x represents [variables](#)
- x_a^i represents subscripts and superscripts
- \leftarrow represents [function](#) application
- \rightarrow represents [function](#) literals

- \square represents matrix literals

note: unary operators have identical precedence to their binary counterparts, but are right associative

definition let \circ be an operator with *AND* associativity. then,

$$a \circ b \circ c \circ \dots \equiv a \circ b \wedge b \circ c \wedge c \circ \dots$$

variable scope

variable scope is currently entirely context-dependent. this is know to cause occasional issues, such as with derivatives: $\delta f x - \delta x$ could represent both the derivative of f with respect to x in the general sense, or the derivative of f with respect to x **at the point** x

examples

quadratic formula: $\cdot b : [b^2 \cdot 4ac] - 2a$

definition of the set of complex numbers: $\mathbb{C}x \equiv x = a : b\iota \wedge \mathbb{R}a \wedge \mathbb{R}b$

definition of the implication / subset / superset / "for all" symbol: $a \vdash b \equiv /a \vee b$ and $a \dashv b \equiv a \vee /b$

in set theory, if U is a subset of V and V is a subset of U , then V is U . in this math notation: $(U x \vdash V x) \wedge (U x \dashv V x) \equiv U = V$

the probability density of the normal distribution in conventional math notation:

$$\frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

compared to in my math notation: $-\lfloor \tau\sigma^2 \rfloor - e\lfloor [x \cdot \mu - \sigma]^2 - 2 \rfloor$

definition of factorials: $\text{fact } n = 1 \mid \dots n$

the negation of an implication in my math notation: $B \vdash C \times B / C$ (*B implying C equals not (B without C) or implication is the negation of set difference or the negation of "for all B, C" is "there exists a B such that not C"*)

compared to conventional math notation: $\neg(B \rightarrow C) = B \wedge \neg C$ or

$$(a \in B \rightarrow a \in C) \iff a \notin B \setminus C \text{ or } B \subset C \iff \forall a \in C, a \notin B$$

the resonant frequency of an LC circuit in conventional math notation: $f = \frac{1}{2\pi\sqrt{LC}}$

compared to in my math notation: $f = -\tau[LC]$

see random math notation formulas for more examples

