



WRITE GRAPH ALGORITHMS LIKE A BOSS

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Graph Theory

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- SQL
- GraphX

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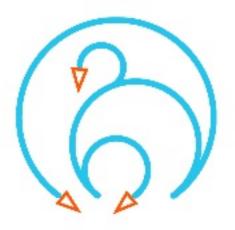
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AGILE DATA SCIENCE



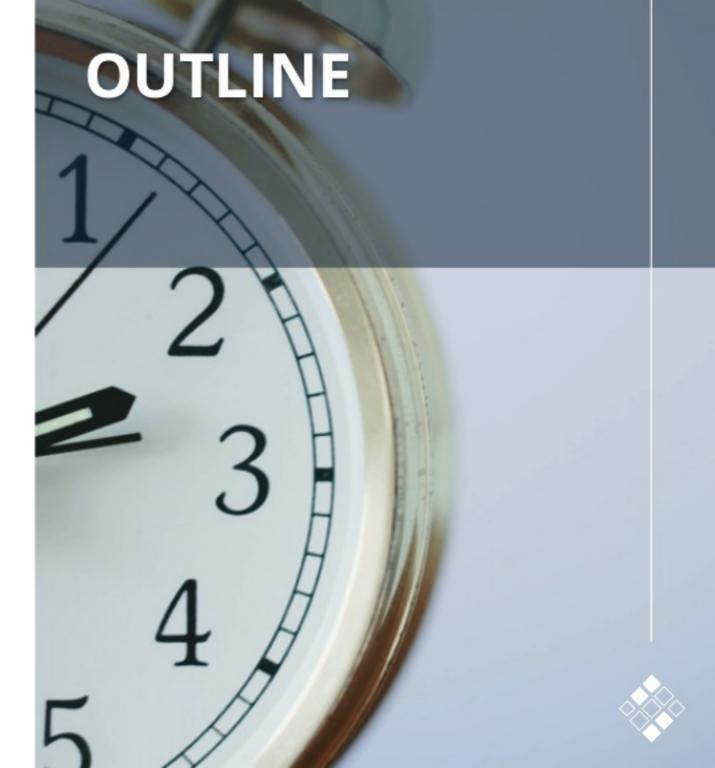


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- Graph-parallel
- Examples
- Pregel
- PowerGraph
- GraphX



There will be code





GRAPH-PARALLEL



- Data-parallel for graphs
- Use the entire graph
- Can be worked on from a local context in parallel
- Usually compute a value for every vertex/edge
- Needed for large graphs on distributed systems
- Pregel, PowerGraph, and GraphX provide graphparallel abstractions



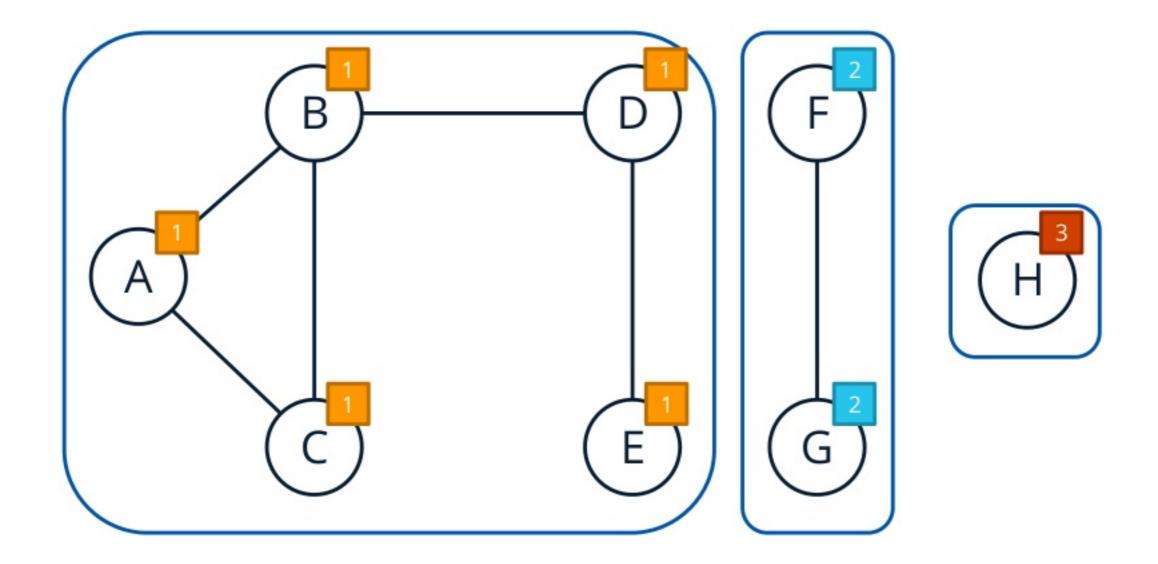


EXAMPLES

- Connected Components
- Single Source Shortest Path
- PageRank

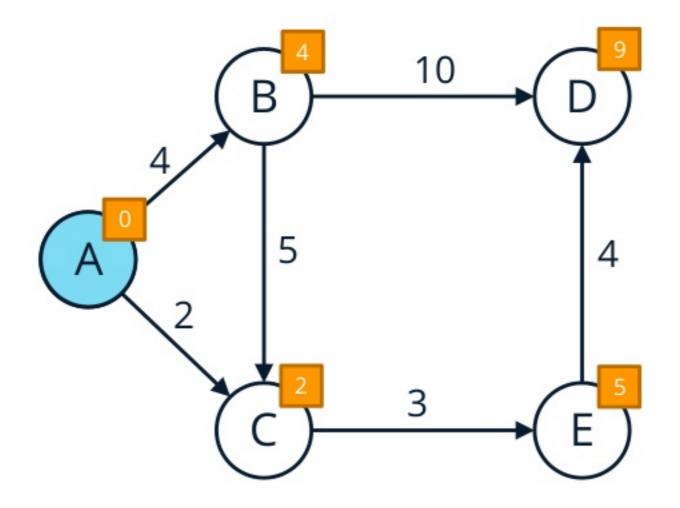


CONNECTED COMPONENTS



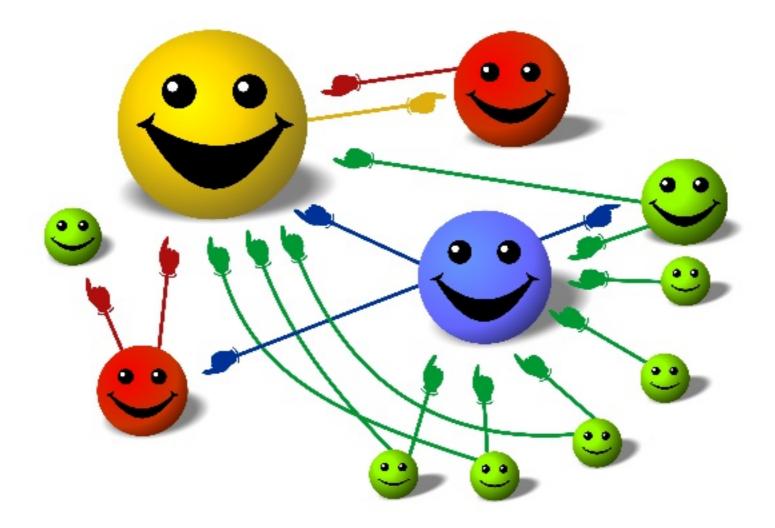


SINGLE SOURCE SHORTEST PATH





PAGERANK







- Message passing with "supersteps"
- Vertex program
 - Processes messages
 - Updates vertex state
 - Sends messages
 - Can vote to halt
- Optional message combiner
- Global aggregators





CONNECTED COMPONENTS

Initial vertex state: Unique integer vertex id

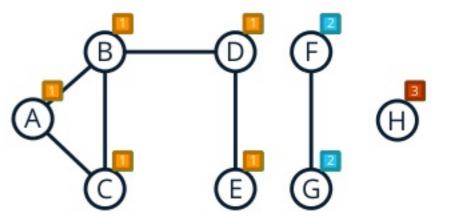
```
compute(messages):
```

```
min_label = min(messages)
if min_label < state:
    state = min_label</pre>
```



```
vote_to_halt()
```

send_message_to_all_neighbors(state)







SINGLE SOURCE SHORTEST PATH

Initial vertex state: source is 0, all others ∞

Edge data: distance between vertices

compute(messages):

min_dist = min(messages)

if min_dist < state:</pre>

state = min_dist

for neighbor in neighborhood:

send_message(neighbor, state + edge_weight)

else:

vote_to_halt()



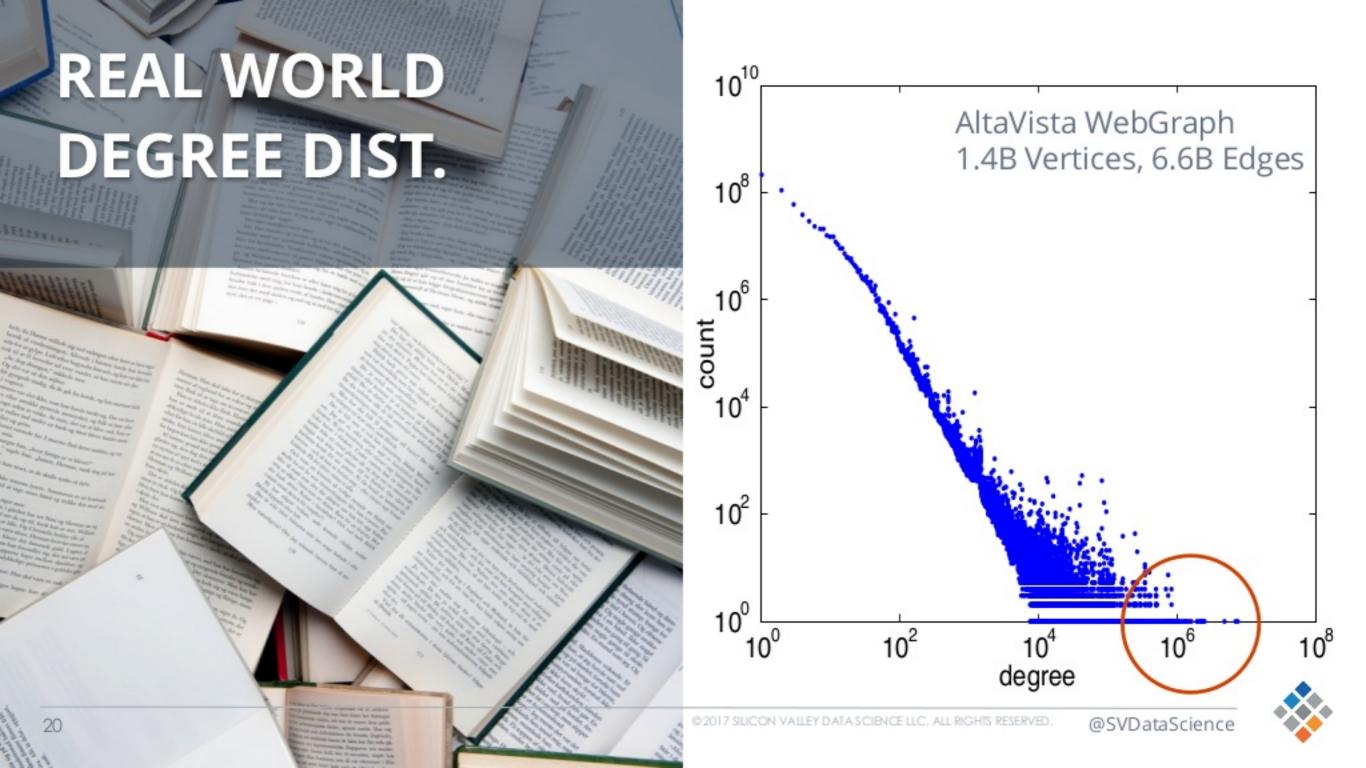


PAGERANK

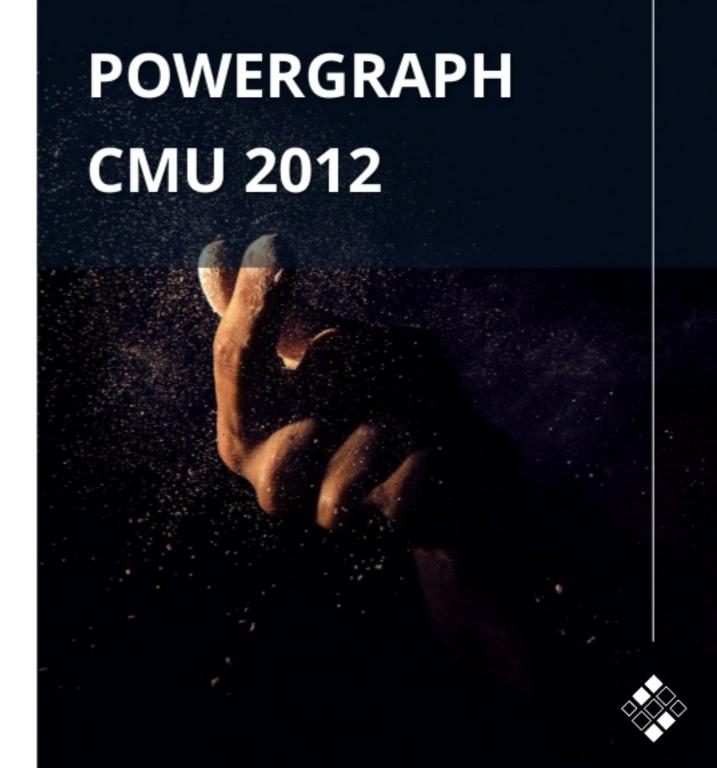
 Initial vertex state: 1 compute(messages): if superstep > 0: sum_messages = sum(messages) state = 0.15 + 0.85 * sum messagesif superstep < 30: send_message_to_all_neighbors(state/out_deg) else: vote to halt()







- Gather(D_u , $D_{(u,v)}$, D_v)
 - Function applied to each in/ out/both edge incident to u
 - Data from both vertices
- sum combiner
 - Combines gathered values for u
- Apply(D_u, sum)
 - Update vertex data D_u
- Scatter(D_u , $D_{(u,v)}$, D_v)
 - Update neighboring edge data
 - Activate neighbors
 - Optionally send a delta to v





CONNECTED COMPONENTS

Initial vertex data: Unique integer vertex id

```
gather(D_u, D_{(u,v)}, D_v)[all\_nbrs] = D_v
sum(a, b) = min(a, b)
apply(D_u, sum) = min(D_u, sum)
scatter(D_u, D_{(u,v)}, D_v)[all\_nbrs] = if D_v > D_u:
activate(v)
```





SINGLE SOURCE SHORTEST PATH

- Initial vertex data: source is 0, all others ∞
- Edge data: distance between vertices

```
gather(D_u, D_{(u,v)}, D_v)[in\_nbrs] = D_v + D_{(u,v)}

sum(a, b) = min(a, b)

apply(D_u, sum) = min(D_u, sum)

scatter(D_u, D_{(u,v)}, D_v)[out\_nbrs] =

if changed(D_u):

activate(v)
```



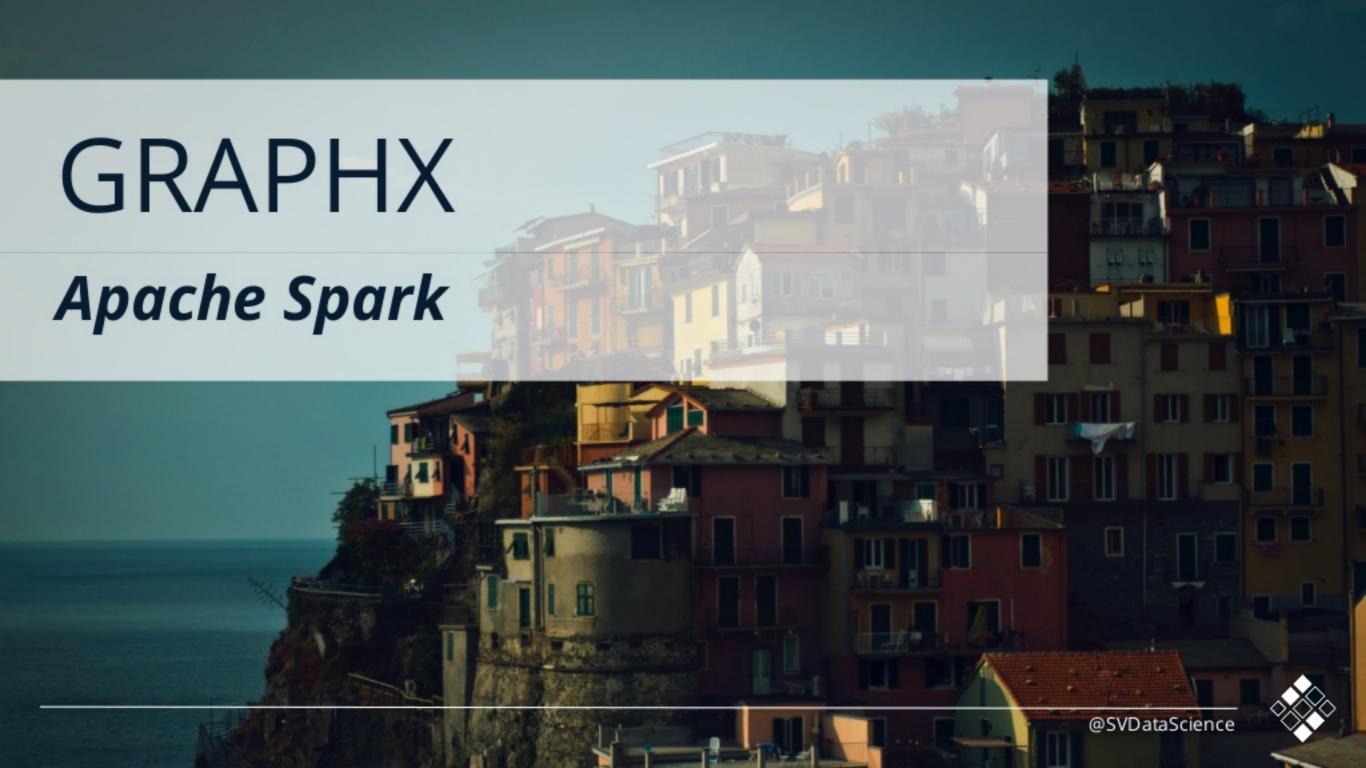


PAGERANK

Initial vertex data: 1

```
gather(D_u, D_{(u,v)}, D_v)[in\_nbrs] = D_v / out\_deg(v)
sum(a, b) = a + b
apply(D_u, sum) = 0.15 + 0.85 * sum
scatter(D_u, D_{(u,v)}, D_v)[out\_nbrs] = if |D_u.delta| > epsilon: activate(v)
```





GRAPHX AMPLAB 2013



- General Graph API built on Spark RDD's
 - Vertex RDD
 - Edge RDD
- Implementation of "Pregel"
 - Messages from edge triplet
 - Requires combiner
 - Implicit activation
- Lower level "Aggregate Messages" building block
 - Used to implement Pregel
- Normal RDD methods



Warning: Scala code ahead



"Pregel" in GraphX

```
def pregel[A: ClassTag](
    initialMsg: A,
    maxIterations: Int = Int.MaxValue,
    activeDirection: EdgeDirection = EdgeDirection.Either)(
    vprog: (VertexId, VD, A) => VD,
    sendMsg: EdgeTriplet[VD, ED] => Iterator[(VertexId, A)],
    mergeMsg: (A, A) => A)
    : Graph[VD, ED]
```





CONNECTED COMPONENTS

```
// Simplified version of org.apache.spark.graphx.lib.ConnectedComponents
def connectedComponents[VD: ClassTag, ED: ClassTag](graph: Graph[VD, ED]):
  Graph[VertexId, ED] = {
  graph
    .mapVertices { case (id, attr) => id }
    .pregel(initialMsg = Long.MaxValue)(
      vprog = (id, attr, msg) => math.min(attr, msg),
      sendMsg = edge => {
        if (edge.srcAttr < edge.dstAttr)</pre>
          Iterator((edge.dstId, edge.srcAttr))
        else if (edge.srcAttr > edge.dstAttr)
          Iterator((edge.srcId, edge.dstAttr))
        else
          Iterator.empty
      mergeMsg = (a, b) \Rightarrow math.min(a, b)
```





SINGLE SOURCE SHORTEST PATH

```
// Based on example in https://spark.apache.org/docs/latest/graphx-programming-guide.html
// see also org.apache.spark.graphx.lib.ShortestPaths
def sssp[VD: ClassTag](graph: Graph[VD, Double], sourceId: VertexId):
  Graph[Double, Double] = {
  graph
    .mapVertices { (id, attr) =>
      if (id == sourceId) 0.0
      else Double.PositiveInfinity
    }.pregel(initialMsg = Double.PositiveInfinity)(
      vprog = (id, dist, msg) => math.min(dist, msg),
      sendMsg = edge => {
        if (edge.srcAttr + edge.attr < edge.dstAttr)</pre>
          Iterator((edge.dstId, edge.srcAttr + edge.attr))
        else
          Iterator.empty
      },
      mergeMsg = (a, b) \Rightarrow math.min(a, b)
```



"Aggregate Messages" in GraphX

```
def aggregateMessages[A: ClassTag](
    sendMsg: EdgeContext[VD, ED, A] => Unit,
    mergeMsg: (A, A) => A,
    tripletFields: TripletFields = TripletFields.All)
    : VertexRDD[A]
```





PAGERANK

```
// Simplified version of org.apache.spark.graphx.lib.PageRank
def pageRank[VD: ClassTag, ED: ClassTag](graph: Graph[VD,ED], numIter: Int):
  Graph[Double, Double] = {
  var rankGraph: Graph[Double, Double] = graph
    .outerJoinVertices(graph.outDegrees) { (id, vdata, deg) => deg.getOrElse(0) }
    .mapTriplets(e => 1.0 / e.srcAttr)
    .mapVertices((id, attr) => 1.0)
  for (i <- 1 to numIter) {</pre>
    val rankUpdates = rankGraph.aggregateMessages[Double](
      sendMsg = ctx => ctx.sendToDst(ctx.srcAttr * ctx.attr),
      mergeMsg = (a, b) \Rightarrow a + b
    rankGraph = rankGraph.outerJoinVertices(rankUpdates) {
      (id, oldRank, msgSumOpt) => 0.15 + 0.85 * msgSumOpt.getOrElse(0.0)
  rankGraph
```



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Almost done...

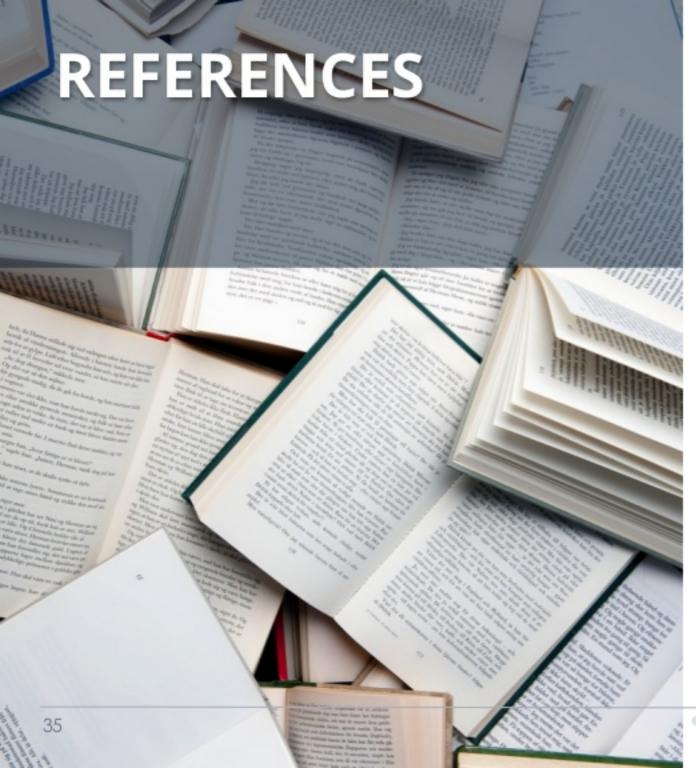




GRAPHX TIPS AND TRICKS

- Specify activeDirection for Pregel algorithms.
- Specify tripletFields for aggregate messages.
- Specify a PartitionStrategy (like EdgePartition2D)
 with the appropriate number of partitions.
- Use immutable data types for vertex/edge data.
- Don't use this example code for anything serious.





 Pregel: A System for Large-Scale Graph Processing (2010)

 PowerGraph: Distributed Graph-Parallel Computation on Natural Graphs (2012)

GraphX: A Resilient
 Distributed Graph System
 on Spark (2013)



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THANK YOU

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