

# Linear Convolution

Linear convolution is a mathematical operation used to combine two signals to produce a third signal. It's a fundamental operation in signal processing and systems theory. Mathematical Definition: Given two signals,  $x(t)$  and  $h(t)$ , their linear convolution is defined as:  $y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau)h(t-\tau) d\tau$

## Applications:

- Filtering: Convolution is used to filter signals, removing unwanted frequencies or noise.
- System Analysis: The impulse response of a system completely characterizes its behavior, and convolution can be used to determine the output of the system given a known input.
- Image Processing: Convolution is used for tasks like edge detection, blurring, and sharpening images.