# Machine-Level Programming II: Arithmetic & Control

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(Slides include copyright materials from *Computer Systems: A Programmer's Perspective*, by Bryant and O'Hallaron, and from *The C Programming Language*, by Kernighan and Ritchie)

# **Today**

- Complete addressing modes and address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops

### **Complete Memory Addressing Modes**

- Most General Form
- D(Rb,Ri,S) Mem[Reg[Rb]+S\*Reg[Ri]+D]
  - D: Constant "displacement" 1, 2, or 4 bytes
  - Rb: Base register: Any of 8 integer registers
  - Ri: Index register: Any, except for %esp
    - Unlikely you'd use %ebp, either
  - S: Scale: 1, 2, 4, or 8 (why these numbers?)
- Special Cases
- (Rb,Ri) Mem[Reg[Rb]+Reg[Ri]]
- D(Rb,Ri) Mem[Reg[Rb]+Reg[Ri]+D]
- (Rb,Ri,S) Mem[Reg[Rb]+S\*Reg[Ri]]

# **Address Computation Examples**

%edx	0xf000
%ecx	0x0100

Expression	Address Computation	Address
0x8 (%edx)		
(%edx,%ecx)		
(%edx,%ecx,4)		
0x80(,%edx,2)		

### **Address Computation Instruction**

### leal Src,Dest

- Src is address mode expression
- Set Dest to address denoted by expression

#### Uses

- Computing addresses without a memory reference
  - E.g., translation of p = &x[i];
- Computing arithmetic expressions of the form x + k\*y
  - k = 1, 2, 4, or 8

### Example

```
int mul12(int x)
{
    return x*12;
}
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```

### Converted to ASM by compiler:

```
leal (%eax,%eax,2), %eax ;t <- x+x*2
sall $2, %eax ;return t<<2</pre>
```

# **Today**

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops

### **Some Arithmetic Operations**

### **■ Two Operand Instructions:**

Format	Computation		
addl	Src,Dest	Dest = Dest + Src	
subl	Src,Dest	Dest = Dest – Src	
imull	Src,Dest	Dest = Dest * Src	
sall	Src,Dest	Dest = Dest << Src	Also called shil
sarl	Src,Dest	Dest = Dest >> Src	Arithmetic
shrl	Src,Dest	Dest = Dest >> Src	Logical
xorl	Src,Dest	Dest = Dest ^ Src	
andl	Src,Dest	Dest = Dest & Src	
orl	Src,Dest	Dest = Dest   Src	

- Watch out for argument order!
- No distinction between signed and unsigned int (why?)

### **Some Arithmetic Operations**

One Operand Instructions

```
incl     Dest     Dest = Dest + 1
decl     Dest     Dest = Dest - 1
negl     Dest     Dest = - Dest
notl     Dest     Dest = ~Dest
```

See book for more instructions

# **Arithmetic Expression Example**

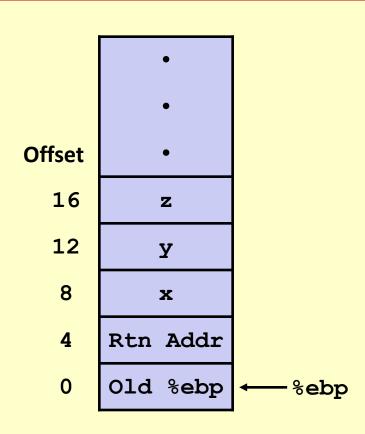
```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```

```
arith:
 pushl %ebp
                             Set
 movl %esp, %ebp
 movl 8(%ebp), %ecx
 movl 12(%ebp), %edx
  leal (%edx,%edx,2), %eax
 sall $4, %eax
                              Body
  leal 4(%ecx, %eax), %eax
 addl %ecx, %edx
 addl 16(%ebp), %edx
  imull %edx, %eax
        %ebp
 popl
  ret
```

# Understanding arith

```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```

```
movl 8(%ebp), %ecx
movl 12(%ebp), %edx
leal (%edx,%edx,2), %eax
sall $4, %eax
leal 4(%ecx,%eax), %eax
addl %ecx, %edx
addl 16(%ebp), %edx
imull %edx, %eax
```



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# Understanding arith

```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```

```
Stack
Offset
  16
            Z
  12
           У
   8
            X
   4
       Rtn Addr
       Old %ebp -
   0
```

```
movl 8(%ebp), %ecx # ecx = x
movl 12(%ebp), %edx # edx = y
leal (%edx,%edx,2), %eax # eax = y*3
sall $4, %eax # eax *= 16 (t4)
leal 4(%ecx,%eax), %eax # eax = t4 +x+4 (t5)
addl %ecx, %edx # edx = x+y (t1)
addl 16(%ebp), %edx # edx += z (t2)
imull %edx, %eax # eax = t2 * t5 (rval)
```

### Observations about arith

```
int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
```

- Instructions in different order from C code
- Some expressions require multiple instructions
- Some instructions cover multiple expressions
- Get exact same code when compile:
- (x+y+z)\*(x+4+48\*y)

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```
\# ecx = x
movl
      8(%ebp), %ecx
movl
      12 (%ebp), %edx
                       \# edx = y
leal (%edx, %edx, 2), %eax # eax = y*3
sall $4, %eax
                            \# eax *= 16 (t4)
leal 4(\%ecx,\%eax), \%eax # eax = t4 + x + 4 (t5)
addl %ecx, %edx
                            \# edx = x+y (t1)
addl 16(%ebp), %edx
                            \# edx += z (t2)
imull
      %edx, %eax
                            \# eax = t2 * t5 (rval)
```

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}</pre>
```

```
logical:
    pushl %ebp
    movl %esp,%ebp

    movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

    popl %ebp
    ret

    Finish
```

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax # eax = t1>>17 (t2)
andl $8185,%eax # eax = t2 & mask (rval)
```

```
int logical(int x, int y)
{
   int t1 = x^y;
   int t2 = t1 >> 17;
   int mask = (1<<13) - 7;
   int rval = t2 & mask;
   return rval;
}</pre>
```

```
logical:
    pushl %ebp
    movl %esp,%ebp

movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

popl %ebp
    ret

Finish
```

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax # eax = t1>>17 (t2)
andl $8185,%eax # eax = t2 & mask (rval)
```

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}</pre>
```

```
logical:
    pushl %ebp
    movl %esp,%ebp

movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

popl %ebp
    ret

Finish
```

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax # eax = t1>>17 (t2)
andl $8185,%eax # eax = t2 & mask (rval)
```

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```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}</pre>
```

```
2^{13} = 8192, 2^{13} - 7 = 8185
```

```
logical:
    pushl %ebp
    movl %esp,%ebp

movl 12(%ebp),%eax
    xorl 8(%ebp),%eax
    sarl $17,%eax
    andl $8185,%eax

popl %ebp
    ret

Finish
```

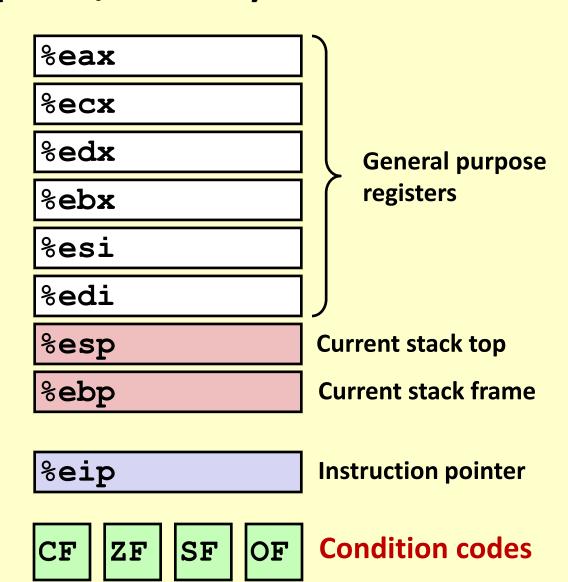
```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax # eax = t1>>17 (t2)
andl $8185,%eax # eax = t2 & mask (rval)
```

# **Today**

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- Loops

### **Processor State (IA32, Partial)**

- Information about currently executing program
  - Temporary data (%eax, ...)
  - Location of runtime stack (%ebp,%esp)
  - Location of current code control point (%eip, ...)
  - Status of recent tests( CF, ZF, SF, OF )



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# **Condition Codes (Implicit Setting)**

Single bit registers

```
    CF Carry Flag (for unsigned)
    SF Sign Flag (for signed)
    Zero Flag
    OF Overflow Flag (for signed)
```

Implicitly set (think of it as side effect) by all arithmetic operations

```
Example: add1/addq Src,Dest ↔ t = a+b

CF set if carry out from most significant bit (unsigned overflow)

ZF set if t == 0

SF set if t < 0 (as signed)

OF set if two's-complement (signed) overflow

(a>0 && b>0 && t<0) || (a<0 && b<0 && t>=0)
```

- Not set by lea instruction
- Full documentation (IA32) (follow this link)

### **Condition Codes (Explicit Setting: Compare)**

- Explicit Setting by Compare Instruction
  - empl/cmpq Src2, Src1
  - **cmpl** b, a like computing a-b without setting destination
  - •CF set if carry out from most significant bit (used for unsigned comparisons)
  - "ZF set if a == b
  - "SF set if (a-b) < 0 (as signed)</pre>
  - ■OF set if two's-complement (signed) overflow
    (a>0 && b<0 && (a-b)<0) || (a<0 && b>0 && (a-b)>0)

### **Condition Codes (Explicit Setting: Test)**

- Explicit Setting by Test instruction
  - test1/testq Src2, Src1

test1 b, a like computing a&b without setting destination

- Sets condition codes based on value of Src1 & Src2
- Useful to have one of the operands be a mask
- "ZF set when a&b == 0
- ■SF set when a&b < 0

# **Questions?**

### **Reading Condition Codes**

#### SetX Instructions

Set single byte based on combinations of condition codes

SetX	Condition	Description
sete	ZF	Equal / Zero
setne	~ZF	Not Equal / Not Zero
sets	SF	Negative
setns	~SF	Nonnegative
setg	~ (SF^OF) &~ZF	Greater (Signed)
setge	~(SF^OF)	Greater or Equal (Signed)
setl	(SF^OF)	Less (Signed)
setle	(SF^OF)   ZF	Less or Equal (Signed)
seta	~CF&~ZF	Above (unsigned)
setb	CF	Below (unsigned)

%ah

용dh

%al

%dl

### **Reading Condition Codes (continued)**

#### SetX Instructions:

 Set single byte based on combination of condition codes

### %ecx %ch %cl

%eax

%edx

### One of 8 addressable byte registers

- Does not alter remaining 3 bytes
- Typically use movzbl to finish job

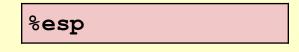
```
int gt (int x, int y)
{
  return x > y;
}
```

### %ebx %bh %bl

### %esi

### **Body**

```
movl 12(%ebp),%eax  # eax = y
cmpl %eax,8(%ebp)  # Compare x : y
setg %al  # al = x > y
movzbl %al,%eax  # Zero rest of %eax
```



```
%ebp
```

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### **Reading Condition Codes: x86-64**

#### SetX Instructions:

- Set single byte based on combination of condition codes
- Does not alter remaining 3 bytes

```
int gt (long x, long y)
{
  return x > y;
}
```

```
long lgt (long x, long y)
{
  return x > y;
}
```

#### **Bodies**

```
cmpl %esi, %edi
setg %al
movzbl %al, %eax
```

```
cmpq %rsi, %rdi
setg %al
movzbl %al, %eax
```

Is %rax zero?

Yes: 32-bit instructions set high order 32 bits to 0!

# **Today**

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- Control: Condition codes
- Conditional branches & Moves
- Loops

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# **Jumping**

### jX Instructions

Jump to different part of code depending on condition codes

jΧ	Condition	Description
jmp	1	Unconditional
je	ZF	Equal / Zero
jne	~ZF	Not Equal / Not Zero
js	SF	Negative
jns	~SF	Nonnegative
jg	~(SF^OF) &~ZF	Greater (Signed)
jge	~(SF^OF)	Greater or Equal (Signed)
j1	(SF^OF)	Less (Signed)
jle	(SF^OF)   ZF	Less or Equal (Signed)
ja	~CF&~ZF	Above (unsigned)
jb	CF	Below (unsigned)

### **Conditional Branch Example**

```
int absdiff(int x, int y)
{
    int result;
    if (x > y) {
       result = x-y;
    } else {
       result = y-x;
    }
    return result;
}
```

```
absdiff:
   pushl
          %ebp
                           Setup
   movl
          %esp, %ebp
   movl
         8(%ebp), %edx
   movl
          12(%ebp), %eax
   cmpl %eax, %edx
                           Body1
   jle
         .L6
   subl %eax, %edx
                           Body2a
   movl
          %edx, %eax
   jmp .L7
.L6:
   subl %edx, %eax
.L7:
   popl %ebp
   ret
```

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```
int goto_ad(int x, int y)
{
   int result;
   if (x <= y) goto Else;
   result = x-y;
   goto Exit;
Else:
   result = y-x;
Exit:
   return result;
}</pre>
```

- C allows "goto" as means of transferring control
  - Closer to machine-level programming style
- Generally considered bad coding style

```
absdiff:
   pushl
          %ebp
                            Setup
          %esp, %ebp
   movl
   movl
          8(%ebp), %edx
   movl
          12 (%ebp), %eax
   cmpl %eax, %edx
                            Body1
   jle
          .L6
   subl
          %eax, %edx
                            Body2a
   movl
          %edx, %eax
   jmp .L7
.L6:
   subl %edx, %eax
.L7:
   popl %ebp
   ret
```

```
int goto_ad(int x, int y)
{
   int result;
   if (x <= y) goto Else;
   result = x-y;
   goto Exit;
Else:
   result = y-x;
Exit:
   return result;
}</pre>
```

```
absdiff:
   pushl
          %ebp
                           Setup
   movl
          %esp, %ebp
   movl
         8(%ebp), %edx
   movl
          12 (%ebp), %eax
   cmpl %eax, %edx
                           Body1
   jle
         .L6
          %eax, %edx
   subl
                           Body2a
   movl
          %edx, %eax
   jmp .L7
.L6:
   subl %edx, %eax
.L7:
   popl %ebp
   ret
```

```
int goto_ad(int x, int y)
{
   int result;
   if (x <= y) goto Else;
   result = x-y;
   goto Exit;
Else:
   result = y-x;
Exit:
   return result;
}</pre>
```

```
absdiff:
   pushl
          %ebp
                           Setup
   movl
          %esp, %ebp
   movl
         8(%ebp), %edx
   movl
          12 (%ebp), %eax
   cmpl %eax, %edx
                           Body1
   jle
         .L6
   subl
          %eax, %edx
                           Body2a
   movl
          %edx, %eax
   jmp .L7
.L6:
   subl %edx, %eax
.L7:
   popl %ebp
   ret
```

```
int goto_ad(int x, int y)
{
   int result;
   if (x <= y) goto Else;
   result = x-y;
   goto Exit;
Else:
   result = y-x;
Exit:
   return result;
}</pre>
```

```
absdiff:
   pushl
          %ebp
                            Setup
   movl
          %esp, %ebp
   movl
          8(%ebp), %edx
   movl
          12 (%ebp), %eax
   cmpl %eax, %edx
                            Body1
   jle
         .L6
   subl
          %eax, %edx
                            Body2a
   movl
          %edx, %eax
   jmp .L7
.L6:
   subl %edx, %eax
.L7:
   popl %ebp
                            Finish
   ret
```



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# **General Conditional Expression Translation**

#### C Code

```
val = Test ? Then_Expr : Else_Expr;
```

```
val = x>y ? x-y : y-x;
```

#### **Goto Version**

```
nt = !Test;
if (nt) goto Else;
val = Then_Expr;
goto Done;
Else:
  val = Else_Expr;
Done:
    . . .
```

- Test is expression returning integer
  - = 0 interpreted as false
  - ≠ 0 interpreted as true
- Create separate code regions for then & else expressions
- Execute appropriate one

### **Using Conditional Moves**

#### Conditional Move Instructions

- Instruction supports:
  if (Test) Dest ← Src
- Supported in post-1995 x86 processors
- GCC does not always use them
  - Wants to preserve compatibility with ancient processors
  - Enabled for x86-64
  - Use switch -march=686 for IA32

### Why?

- Branches are very disruptive to instruction flow through pipelines
- Conditional move do not require control transfer

#### C Code

```
val = Test
    ? Then_Expr
    : Else_Expr;
```

#### **Goto Version**

```
tval = Then_Expr;
result = Else_Expr;
t = Test;
if (t) result = tval;
return result;
```

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# **Conditional Move Example: x86-64**

```
int absdiff(int x, int y) {
    int result;
    if (x > y) {
        result = x-y;
    } else {
        result = y-x;
    }
    return result;
}
```

```
x in %edi
y in %esi
```

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### **Bad Cases for Conditional Move**

#### **Expensive Computations**

```
val = Test(x) ? Hard1(x) : Hard2(x);
```

- Both values get computed
- Only makes sense when computations are very simple

### **Risky Computations**

```
val = p ? *p : 0;
```

- Both values get computed
- May have undesirable effects

#### **Computations with side effects**

```
val = x > 0 ? x*=7 : x+=3;
```

Both values get computed

## **Today**

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- **■** Control: Condition codes
- Conditional branches and moves
- Loops

## "Do-While" Loop Example

#### C Code

```
int pcount_do(unsigned x)
{
  int result = 0;
  do {
    result += x & 0x1;
    x >>= 1;
  } while (x);
  return result;
}
```

```
int pcount_do(unsigned x)
{
  int result = 0;
loop:
  result += x & 0x1;
  x >>= 1;
  if (x)
    goto loop;
  return result;
}
```

- Count number of 1's in argument x ("popcount")
- Use conditional branch to either continue looping or to exit loop

## "Do-While" Loop Compilation

```
int pcount_do(unsigned x) {
  int result = 0;
loop:
  result += x & 0x1;
  x >>= 1;
  if (x)
    goto loop;
  return result;
}
```

```
Registers:
%edx x
%ecx result
```

```
movl $0, %ecx # result = 0
.L2:  # loop:
  movl %edx, %eax
  andl $1, %eax # t = x & 1
  addl %eax, %ecx # result += t
  shrl %edx # x >>= 1
  jne .L2 # If !0, goto loop
```

### General "Do-While" Translation

#### C Code

```
do

Body

while (Test);
```

```
Body: {
    Statement<sub>1</sub>;
    Statement<sub>2</sub>;
    ...
    Statement<sub>n</sub>;
}
```

```
loop:

Body

if (Test)

goto loop
```

- Test returns integer
- = 0 interpreted as false
- ≠ 0 interpreted as true

# **Questions?**

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## "While" Loop Example

#### C Code

```
int pcount_while(unsigned x) {
  int result = 0;
  while (x) {
    result += x & 0x1;
    x >>= 1;
  }
  return result;
}
```

```
int pcount_do(unsigned x) {
  int result = 0;
  if (!x) goto done;
loop:
  result += x & 0x1;
  x >>= 1;
  if (x)
    goto loop;
done:
  return result;
}
```

- Is this code equivalent to the do-while version?
  - Must jump out of loop if test fails

### **General "While" Translation**

#### While version

```
while (Test)
Body
```



### **Do-While Version**

```
if (!Test)
    goto done;
do
    Body
    while (Test);
done:
```



```
if (!Test)
    goto done;
loop:
    Body
    if (Test)
       goto loop;
done:
```

# "For" Loop Example

#### C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
   int i;
   int result = 0;
   for (i = 0; i < WSIZE; i++) {
      unsigned mask = 1 << i;
      result += (x & mask) != 0;
   }
   return result;
}</pre>
```

■ Is this code equivalent to other versions?

## "For" Loop Form

#### **General Form**

```
for (Init; Test; Update)

Body
```

```
for (i = 0; i < WSIZE; i++) {
   unsigned mask = 1 << i;
   result += (x & mask) != 0;
}</pre>
```

#### Init

```
i = 0
```

#### **Test**

```
i < WSIZE
```

### **Update**

```
i++
```

### **Body**

```
{
  unsigned mask = 1 << i;
  result += (x & mask) != 0;
}</pre>
```

# "For" Loop → While Loop

#### **For Version**

```
for (Init; Test; Update)

Body
```



### While Version

```
Init;
while (Test) {
    Body
    Update;
}
```

# "For" Loop $\rightarrow ... \rightarrow$ Goto

#### **For Version**

```
for (Init; Test; Update)

Body
```

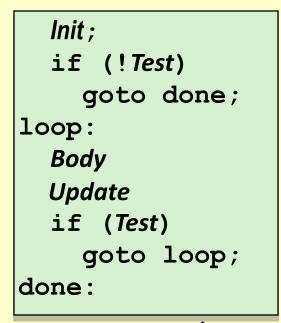


#### While Version

```
Init;
while (Test) {
    Body
    Update;
}
```

```
Init;
if (!Test)
  goto done;
do
  Body
  Update
  while(Test);
done:
```

Machine-Level Programming II



## "For" Loop Conversion Example

#### C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
   int i;
   int result = 0;
   for (i = 0; i < WSIZE; i++) {
      unsigned mask = 1 << i;
      result += (x & mask) != 0;
   }
   return result;
}</pre>
```

Initial test can be optimized away

```
int pcount for gt(unsigned x) {
  int i;
  int result = 0;
                    Init
  i = 0;
       (i < WSIZE)
    goto done
loop:
                     Body
    unsigned mask = 1 << i;
    result += (x \& mask) != 0;
  i++; Update
  if (i < WSIZE) Test
    goto loop;
done:
  return result;
```

## **Summary**

### Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches & conditional moves
- Loops

### Next Topic

- Switch statements
- Stack
- Call / return
- Procedure call discipline