

A Brief Overview of Powder Diffraction

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BCA Intensive Course in X-Ray Structural Analysis
Trevelyan College, Durham 2005.

- Historical background
- Diffraction: physical phenomenon
- Samples, experiment and data obtained
- Applications
- Conclusions

Historical background

- 1895: Röntgen discovers X-rays (Nobel Prize 1901)
- 1912: von Laue discovers X-ray diffraction on crystals (Nobel Prize 1914)
- 1913: Bragg & Bragg discover structure analysis by XRD, NaCl (Nobel Prize 1915)
- 1916: Debye & Scherrer discover powder X-ray diffraction, LiF
- 1963: Zachariasen solves the structure of β -Pu from PXRD by direct methods
- 1969: Rietveld method
- 1990: direct space approaches to structure solution
- 2000: work on 100+ atom structures, proteins

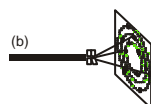
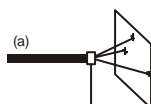
Diffraction: physical phenomenon

- Crystalline state of matter
 - long-range 3D order
- Diffraction
 - scattering on periodic arrays
- Crystallography
 - $2d_{hkl} \sin \theta = \lambda$
 - $F_{hkl} = \sum f_j e^{2\pi i(hx_j + ky_j + lz_j)}$

Samples

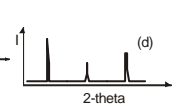
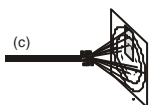


Single crystal



Four differently oriented single crystals

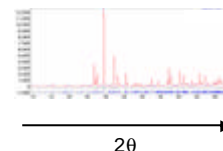
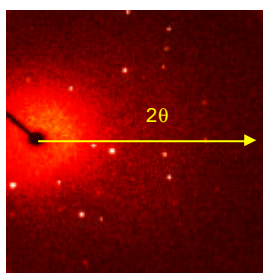
Polycrystalline material



Experiment



'...data compressed into one dimension...'



A modern take

"Probably the best known and widely used application of powder diffraction is as an analytical tool for both qualitative and quantitative analysis of crystalline materials".

(Fundamentals of Crystallography, ed. by C. Giacovazzo, pg. 297)

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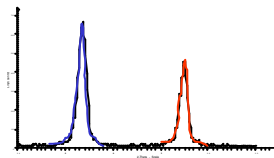
Not quite as simple as this...

Qualitative analysis

➤ JCPDS cards



Quantitative analysis

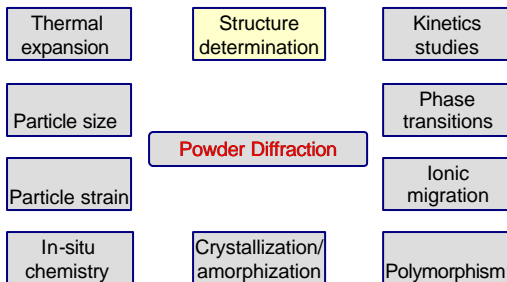


Many multibillion £££££ drug patents based on this!!!!



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...but it does much more

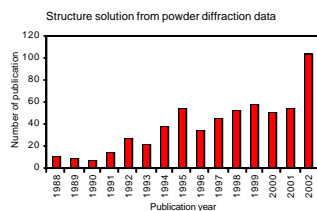


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Crystal structure publications



~ 100



~ 20,000

⇒ try hard to grow crystals!

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Structure determination

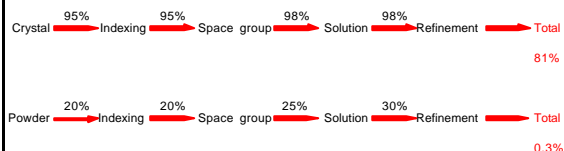


Indexing
Space group determination
Extraction of integrated intensities (?)
Structure solution
Structure refinement

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What is the difficulty?

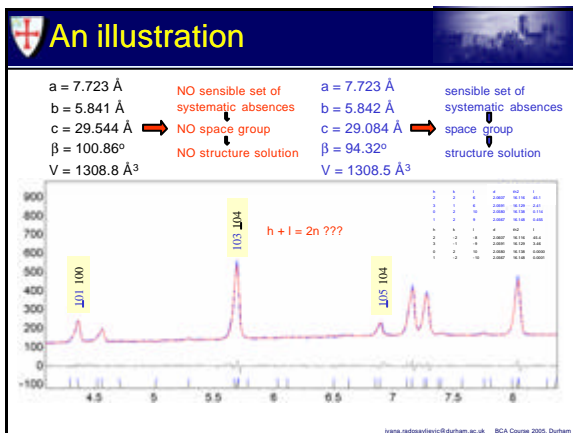
This slide illustrates personal experience – the only serious statement is the final line!



81% : 0.3% ~ 270 ⇒ comparable to the ratio of publications!!!!

⇒ every step is difficult!!!!

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Structure solution

Examples of approaches to structure solution include:

- Reciprocal space methods
 - direct methods
 - Patterson methods
- Direct space methods
 - simulated annealing
 - genetic algorithm

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Refinement: pre Rietveld

➤ Integrated intensity refinement

- State of the art until late 60's early 70's
- Poor observation-to- parameter ratio
- Problems due to overlap
- Limited applicability
- Suitable for high symmetry systems
- Used extensively for high T nonstoichiometric phases

| hkl | F_{0-220}^2 | R_{0-220} | R_{0-220} | hkl |
|-------|---------------|-------------|-------------|-------|
| 111 | 6092 | 6315 | 111 | |
| 200 | 89766 | 89604 | 200 | |
| 220 | 79186 | 79285 | 220 | |
| 311 | 3378 | 3484 | 311 | |
| 222 | 26240 | 26139 | 222 | |
| 400 | 12697 | 13084 | 400 | |
| 331 | 1540 | 1377 | 331 | |
| 420 | 31104 | 31301 | 420 | |
| 422 | 23695 | 23438 | 422 | |
| 333 | 1081 | 898 | 333 | |
| 511 | 1081 | 6042 | 511 | |
| 440 | 5831 | 6042 | 511 | |
| 600 | 10394 | 10308 | 440 | |
| 442 | | | | |

$R(I) = 0.78\%$

- 12 observations
- 4 variables
 - Scale factor
 - $U_{iso}(Fe)$
 - $U_{iso}(O)$
 - $Occ(O)$

Cheetham et al., 1971.

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Refinement: the Rietveld method

➤ Rietveld, 1969: diffraction pattern analysis by a curve fitting procedure

➤ First proposed for constant wavelength neutron data

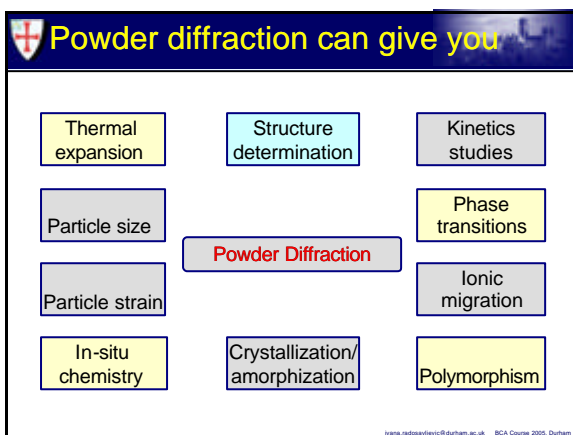
➤ The difference between the observed and calculated profiles is minimized

- typical Rietveld plot:

➤ Parameters refined:

- structural parameters (atomic positions, displacement parameters, occupancies, unit cell parameters)
- instrumental parameters (zero point, background parameters)
- peak shape function parameters

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Applications

$ZrMo_2O_8$

- NTE material
- Rich phase system
- Interesting behaviour vs T

Lab powder XRD data:

- In-situ chemistry
- Quantitative phase analysis
- Thermal expansion
- Phase transitions
- Polymorphism
- Structure solution

$(ZrMo_2O_8(OH)_2 \cdot 2H_2O)$ LT- $ZrMo_2O_8$ cub- $ZrMo_2O_8$ trig- $ZrMo_2O_8$

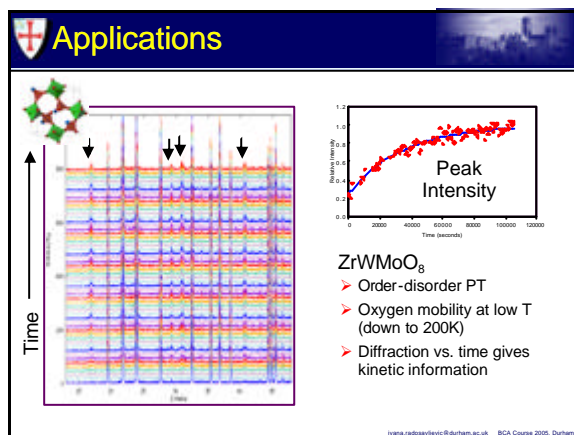
303 K 543 K 763 K 953 K

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Powder diffraction can give you

| | | |
|-------------------|-------------------------------|-------------------|
| Thermal expansion | Structure determination | Kinetics studies |
| Particle size | Powder Diffraction | Phase transitions |
| Particle strain | | Ionic migration |
| In-situ chemistry | Crystallization/amorphization | Polymorphism |

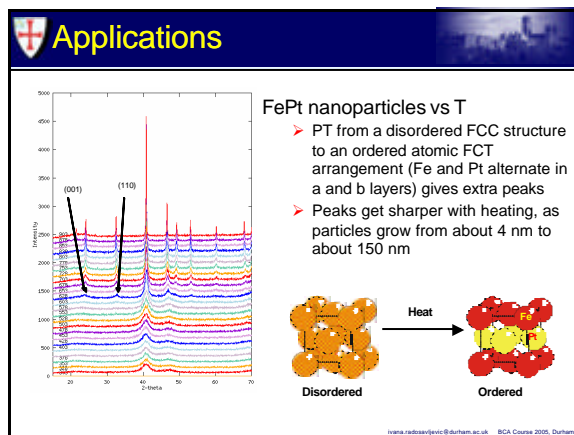
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Conclusions

- Single crystal diffraction superior for structure determination
- Powder diffraction more versatile
- For full and thorough characterization of functional materials - use both!!!

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