The Greatest Thesis in the World



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A thesis submitted to the Nanyang Technological University in partial fulfillment of the requirements for the degree of Doctor of Philosophy

Statement of Originality

Date	Author Name
higher degree to any other Univer	rsity or Institution.
uct of my original research work	and has not been submitted for ϵ
I nereby certify that the intellectu	al content of this thesis is the prod-

Acknowledgements

I wish to express my greatest gratitude to my advisor.

"If I had one hour to save the world, I would spend 55 minutes defining the problem and only five minutes finding the solution."

—Einstein, Albert

To my dear family

Abstract

My abstracts

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Symbols and Acronyms

Symbols

\mathcal{R}^n	the <i>n</i> -dimensional Euclidean space
\mathcal{H}	the Euclidean space
$\ \cdot\ $	the 2-norm of a vector or matrix in Euclidean space
$\ \cdot\ _G$	the induced norm of a vector in G-space
$\left\ \cdot \right\ _{E}$	the induced norm of a vector or matrix in probabilistic space
· · · · · · · · · · · · · · · · · · ·	the Hadamard (component-wise) product
\otimes	the Kronecker product
$\langle\cdot,\cdot angle$	the inner product of two vectors
0	the composition of functions
∇f	the gradient vector
\mathcal{C}^k	the function with continuous partial derivatives up to k orders
$x_{i,k}$	the i -th component of a vector x at time k
\bar{x}	the vector with the average of all components of x as each element
1	all-ones column vector with proper dimension
\mathcal{C}	the average space, i.e., $span\{1\}$
\mathcal{C}^\perp	the disagreement space, i.e., $span^{\perp}\{1\}$
Π_{\parallel}	the projection matrix to the average space \mathcal{C}
Π_{\perp}	the projection matrix to the disagreement space \mathcal{C}^{\perp}
$O(\cdot)$	order of magnitude or ergodic convergence rate (running average)
$o(\cdot)$	non-ergodic convergence rate
\mathcal{N}_i	the index set of the neighbors of agent i

Acronyms

DOP Distributed Optimization Problem

EDOP Equivalent Distributed Optimization Problem SDOP Stochastic Distributed Optimization Problem

OEP Optimal Exchange Problem
OCP Optimal Consensus Problem

DOCP Dynamic Optimal Consensus Problem

AugDGM Augmented Distributed Gradient Methods

AsynDGM Asynchronous Distributed Gradient Methods

D-ESC Distributed Extremum Seeking Control

D-SPA Distributed Simultaneous Perturbation Approach
D-FBBS Distributed Forward-Backward Bregman Splitting

ADMM Alternating Direction Method of Multipliers

DSM Distributed (Sub)gradient Method

GAS Globally Asymptotically Stable

UGAS Uniformly Globally Asymptotically Stable

SPAS Semi-globally Practically Asymptotically Stable

USPAS Uniformly Semi-globally Practically Asymptotically Stable

HoS Heterogeneity of Stepsize

FPR Fixed Point Residual

OBE Objective Error

i.i.d. independent and identically distributed

a.s. almost sure convergence of a random sequence

Chapter 1

Introduction

1.1 Some useful hints

My figure citation: Figure 1.1. (command: fref)

My section citation: Section 1.2. (command: sref)

My Chaptere citation: Chapter 1. (command: cref)

My Paper citation: [1]. (notice back reference to page from bibliograph)

My equation citation: (1.1). (command: eqref), or cite equation by tag: (DOP).

$$F(\theta) = \sum_{i=1}^{m} f_i(\theta)$$
 (DOP)

$$F(\theta) = \sum_{i=1}^{m} f_i(\theta)$$
 (1.1)

1.2 Major Contributions

Our main contributions can be stated as follows:

• First part: My first contributions, several lines



FIGURE 1.1: An illustration.

- Second: Second contributions, several lines
- Third name: Third contributions, several lines

1.3 Outline of the Thesis

Chapter 1 introduces \dots

Chapter 2 reviews ...

More chapters

. . . .

Chapter 2

Literature Review

2.1 Part 1

when you cite a paper [1], the back reference from bibgraph will apper as page number.

You can also cite paper with author name using the command 'citet': such as: Bauschke and Combettes [1].

2.2 Part 2

cite another paper [2].

Theorem 2.2.1 (My theorem). A great theorem.

$$c^2 = a^2 + b^2 (2.1)$$

Proof. the proof is intuitive.

Chapter 3

Chapter3 name

3.1 Section1

See Figure 3.1



FIGURE 3.1: Another illustration.

3.2 Section2

Appendix A

Proofs for Part I

A.1 Proof of Lemma

$$\psi^{av}(\theta) = \frac{1}{T} \int_0^T [\psi(\theta + \mu(\tau)) + C] \otimes \frac{\mu(\tau)}{a} d\tau$$

A.2 Proof of another Lemma

$$\gamma_1(\|x\|) \le W(t, x) \le \gamma_2(\|x\|)$$

$$\frac{\partial W}{\partial t} + \frac{\partial W}{\partial x}\phi(t, x, 0) \le -\gamma_3(\|x\|)$$
(A.1)

List of Author's Award, Patent, and Publication¹

Journal Articles

• My name and My colleague, "A Great System," Nature.

Conference Proceedings

• My name, My colleague 1, My colleague 3 and My colleague 3, "Greater System," in *Conference of Vision*, 2018.

¹The superscript * indicates joint first authors

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