## The Greatest Thesis in the World



#### **Author Name**

School of Electrical & Electronic Engineering

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# Statement of Originality

| Date                                 | Author Name                               |
|--------------------------------------|---|
|                                      |   |
|                                      |   |
|                                      |   |
|                                      |   |
| higher degree to any other Univer    | rsity or Institution.                     |
| uct of my original research work     | and has not been submitted for $\epsilon$ |
| I nereby certify that the intellectu | al content of this thesis is the prod-    |

# Acknowledgements

I wish to express my greatest gratitude to my advisor.

"If I had one hour to save the world, I would spend 55 minutes defining the problem and only five minutes finding the solution."

—Einstein, Albert

To my dear family

# Abstract

My abstracts

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# Symbols and Acronyms

# Symbols

| $\mathcal{R}^n$            | the <i>n</i> -dimensional Euclidean space                             |
|----------------------------|---|
| $\mathcal{H}$              | the Euclidean space   |
| $\ \cdot\ $                | the 2-norm of a vector or matrix in Euclidean space                   |
| $\ \cdot\ _G$              | the induced norm of a vector in G-space                               |
| $\ \cdot\ _E$              | the induced norm of a vector or matrix in probabilistic space         |
| ·· ·· <i>L</i>             | the Hadamard (component-wise) product                                 |
| $\otimes$                  | the Kronecker product   |
| $\langle\cdot,\cdot angle$ | the inner product of two vectors                                      |
| 0                          | the composition of functions  |
|                            |   |
| $\nabla f$                 | the gradient vector   |
| $\mathcal{C}^k$            | the function with continuous partial derivatives up to $k$ orders     |
| $x_{i,k}$                  | the $i$ -th component of a vector $x$ at time $k$                     |
| $\bar{x}$                  | the vector with the average of all components of $x$ as each element  |
| 1                          | all-ones column vector with proper dimension                          |
| $\mathcal{C}$              | the average space, i.e., $span\{1\}$                                  |
| $\mathcal{C}^{\perp}$      | the disagreement space, i.e., $span^{\perp}\{1\}$                     |
| $\Pi_{\parallel}$          | the projection matrix to the average space $\mathcal C$               |
| $\Pi_{\perp}$              | the projection matrix to the disagreement space $\mathcal{C}^{\perp}$ |
| $O(\cdot)$                 | order of magnitude or ergodic convergence rate (running average)      |
| $o(\cdot)$                 | non-ergodic convergence rate  |
| $\mathcal{N}_i$            | the index set of the neighbors of agent $i$                           |
|                            |   |

## Acronyms

DOP Distributed Optimization Problem

EDOP Equivalent Distributed Optimization Problem SDOP Stochastic Distributed Optimization Problem

OEP Optimal Exchange Problem
OCP Optimal Consensus Problem

DOCP Dynamic Optimal Consensus Problem

AugDGM Augmented Distributed Gradient Methods AsynDGM Asynchronous Distributed Gradient Methods

D-ESC Distributed Extremum Seeking Control

D-SPA Distributed Simultaneous Perturbation Approach
D-FBBS Distributed Forward-Backward Bregman Splitting

ADMM Alternating Direction Method of Multipliers

DSM Distributed (Sub)gradient Method

GAS Globally Asymptotically Stable

UGAS Uniformly Globally Asymptotically Stable

SPAS Semi-globally Practically Asymptotically Stable

USPAS Uniformly Semi-globally Practically Asymptotically Stable

HoS Heterogeneity of Stepsize

FPR Fixed Point Residual

OBE Objective Error

i.i.d. independent and identically distributed

a.s. almost sure convergence of a random sequence

## Chapter 1

## Introduction

#### 1.1 Some useful hints

My figure citation: Figure 1.1. (command: fref)

My section citation: Section 1.2. (command: sref)

My Chaptere citation: Chapter 1. (command: cref)

My Paper citation: [1]. (notice back reference to page from bibliograph)

My equation citation: (1.1). (command: eqref), or cite equation by tag: (DOP).

$$F(\theta) = \sum_{i=1}^{m} f_i(\theta)$$
 (DOP)

$$F(\theta) = \sum_{i=1}^{m} f_i(\theta)$$
 (1.1)

## 1.2 Major Contributions

Our main contributions can be stated as follows:

• First part: My first contributions, several lines



FIGURE 1.1: An illustration.

- Second: Second contributions, several lines
- Third name: Third contributions, several lines

## 1.3 Outline of the Thesis

Chapter 1 introduces  $\dots$ 

Chapter 2 reviews ...

More chapters ....

. . . .

# Chapter 2

## Literature Review

#### 2.1 Part 1

When you cite a paper [1], the back reference from bibgraph will apper as page number.

You can also cite paper with author name using the command 'citet': such as: Bauschke and Combettes [1].

#### 2.2 Part 2

cite another paper [2].

**Theorem 2.2.1** (My theorem). A great theorem.

$$c^2 = a^2 + b^2 (2.1)$$

*Proof.* the proof is intuitive.

# Chapter 3

# Chapter3 name

#### 3.1 Section1

See Figure 3.1



FIGURE 3.1: Another illustration.

Let's cite out first table: Table 3.1.

| Table | Group 1 |       | Group 2 |       |
|-------|---------|-------|---------|-------|
|       | Col 1   | Col 2 | Col 1   | Col 2 |
| Row 1 | 14.37   | 5.76  | 2.65    | 2.84  |
| Row 2 | 5.43    | 7.36  | 2.22    | 2.49  |
| Row 3 | 5.54    | 5.68  | 4.42    | 2.92  |

Table 3.1: My Table.

# Appendix A

## Proofs for Part I

#### A.1 Proof of Lemma

$$\psi^{av}(\theta) = \frac{1}{T} \int_0^T [\psi(\theta + \mu(\tau)) + C] \otimes \frac{\mu(\tau)}{a} d\tau$$

## A.2 Proof of another Lemma

$$\gamma_1(\|x\|) \le W(t, x) \le \gamma_2(\|x\|)$$

$$\frac{\partial W}{\partial t} + \frac{\partial W}{\partial x}\phi(t, x, 0) \le -\gamma_3(\|x\|)$$
(A.1)

# List of Author's Award, Patent, and Publication<sup>1</sup>

## Journal Articles

• My name and My colleague, "A Great System," Nature.

## Conference Proceedings

• My name, My colleague 1, My colleague 3 and My colleague 3, "Greater System," in *Conference of Vision*, 2018.

<sup>&</sup>lt;sup>1</sup>The superscript \* indicates joint first authors

# **Bibliography**

- [1] Heinz H Bauschke and Patrick L Combettes. Convex analysis and monotone operator theory in Hilbert spaces. Springer Science & Business Media, 2011. 1, 3
- [2] J. B. Rawlings and B. T. Stewart. Coordinating multiple optimization-based controllers: New opportunities and challenges. *Journal of Process Control*, 18: 839–845, 2008.