

## PROCESS DYNAMICS – CPN 321

### SEMESTER TEST 2

Chemical Engineering  
Engineering and the Built Environment

Examiner: Carl Sandrock

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90 minutes

*Instructions – Read carefully*

- Answer all the questions.
- This is a closed book test. All the information you may use is contained in the paper and the attached formula sheet.
- Make sure that you motivate all your answers and write legibly.



# 1 Linearisation

The following equations represent a chemical system.

$$\frac{d}{dt}[x(t)y(t)] = 2x(t)^2 + 3\frac{y(t)}{x(t)} \quad (1)$$

$$\frac{dy(t)}{dt} = \sqrt{y(t)} + \frac{x(t) - 1}{2} \quad (2)$$

1. Rewrite the system as a linearised model in terms of deviation variables. 4
2. Rewrite the linearised system in matrix form. 2
3. Consider the right hand side of equation 1. Use a graph on the attached graph paper to indicate the accuracy of the linear approximation given that  $y$  stays near the steady state value ( $\bar{x} \approx -1.23$ ,  $\bar{y} \approx 1.24$ ) 4

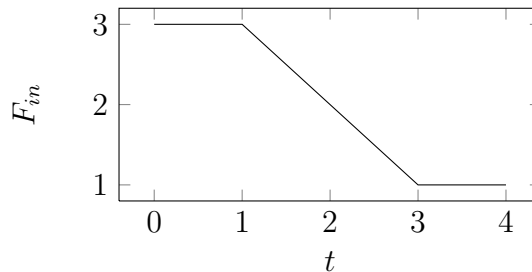
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# 2 First order response

A tank system described by equation 3

$$\frac{dh}{dt} = 3F_{in}(t) - 2h(t) + 1 \quad (3)$$

is subjected to a change in  $F_{in}$  as shown in figure 1.



**Figure 1:** Flowrate for system response in question 2

1. If the system starts at steady state, calculate the initial height  $h_0$ . 1
2. Express the input signal shown in figure 1 as a linear combination, with optional time-shifting, of steps and/or ramps. Use qualitative graphs to explain your answer. 3
3. Sketch the system's response ( $h(t)$ ) to the input signal qualitatively and indicate the time constant on your graph. 2
4. Calculate the system response ( $h(t)$ ) analytically. 4

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### 3 Second order response

Consider the following equations describing a heat exchanger system with feedback control.  $a$  and  $b$  are positive constants.

$$\begin{aligned}\frac{dT}{dt} &= aF \\ \frac{dF}{dt} &= K \left( \frac{dT}{dt} + b(T - T_S) \right)\end{aligned}$$

1. Find a single second-order differential equation that describes the response of  $T$  to changes in  $T_S$ . 2
2. Determine the values for  $K$  for which the system will be stable. 4
3. Sketch a qualitative step response of the system for  $K = 2$ . 2
4. Sketch a qualitative step response for the system given critically damped behaviour. 2

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Full Marks 30