

# Physics 341 - Lecture 23

$$\left\{ \begin{array}{l} N_{\text{total}}^{\text{dof}} = N - 1 = a - 1 \\ N_{\text{treatment}}^{\text{dof}} = a - 1 \\ N_{\text{error}}^{\text{dof}} = N_{\text{total}}^{\text{dof}} - N_{\text{treatment}}^{\text{dof}} \end{array} \right.$$

$$\begin{aligned} SS_{\text{TOTAL}} &= (N - 1) * \text{VAR}(\dots) \\ SS_{\text{TREATMENT}} &= \sum_{i=1}^a n (\bar{x}_i - \bar{\bar{x}})^2 \\ SS_{\text{ERROR}} &= SS_{\text{TOTAL}} - SS_{\text{TREATMENT}} \end{aligned}$$

$$SS_{TOTAL} = \sum_{i,j} x_{ij}^2 - N \cdot \bar{x}^2$$

MS

$$MS_{TRT} = \frac{SS_{TRT}}{N_{TRT}^{df}}$$

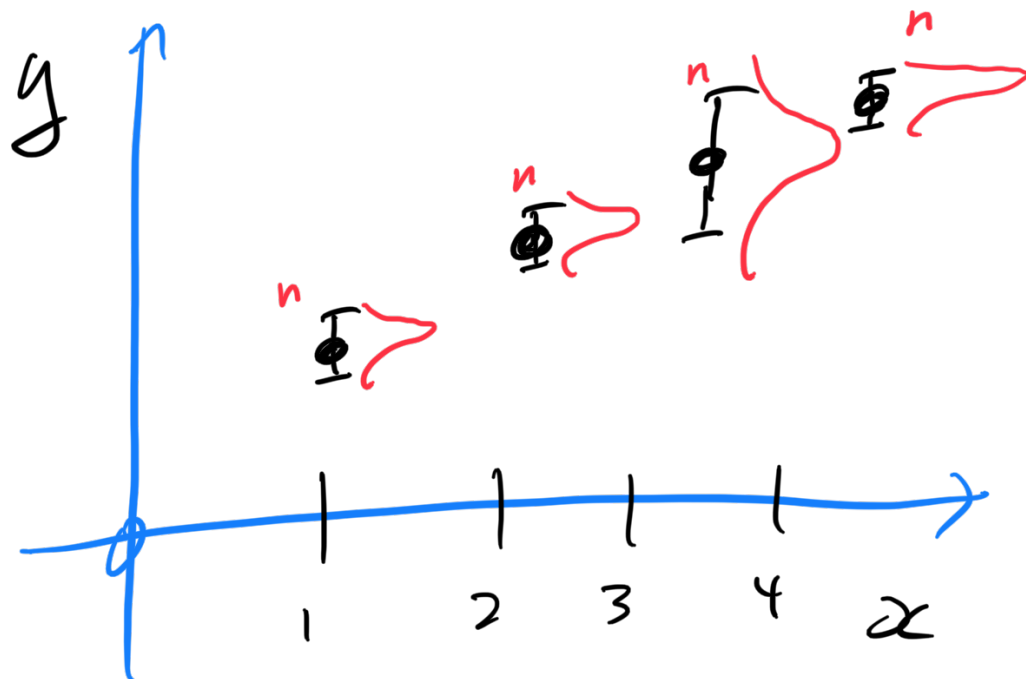
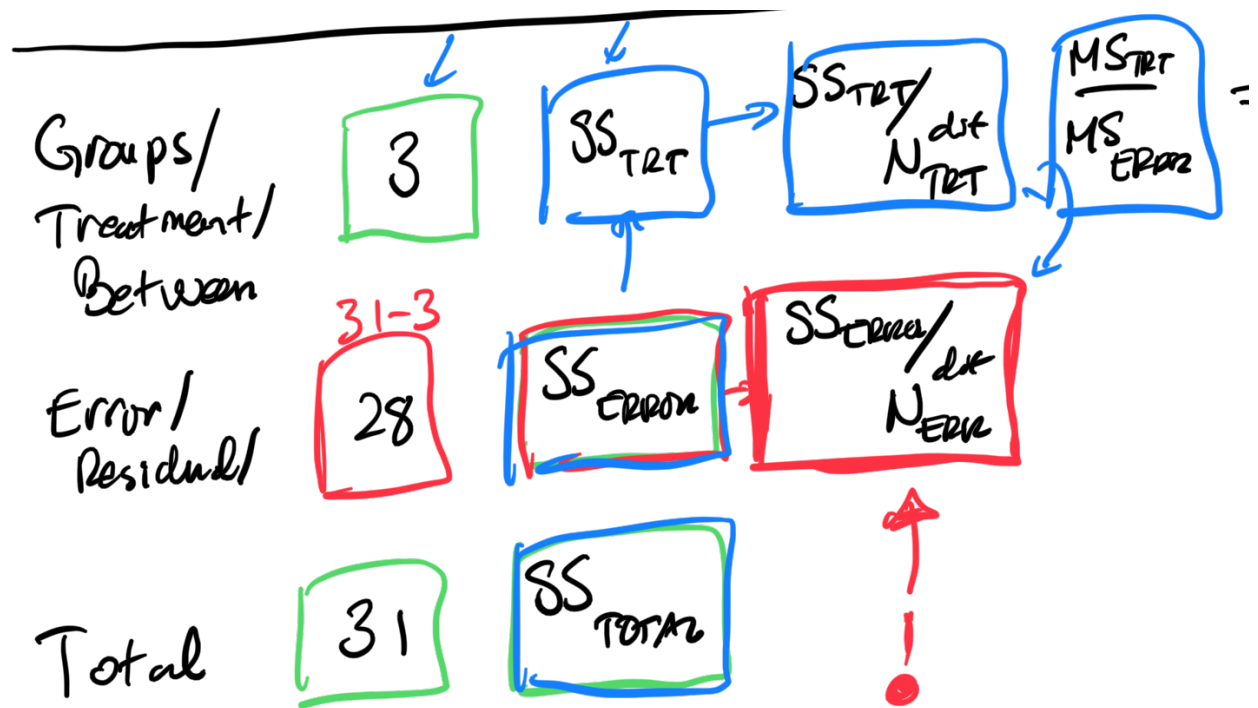
$$MS_{ERROR} = \frac{SS_{ERROR}}{N_{ERROR}^{df}}$$

$f_{\%}$

$$f_{\%} = \frac{MS_{TRT}}{MS_{ERROR}}$$

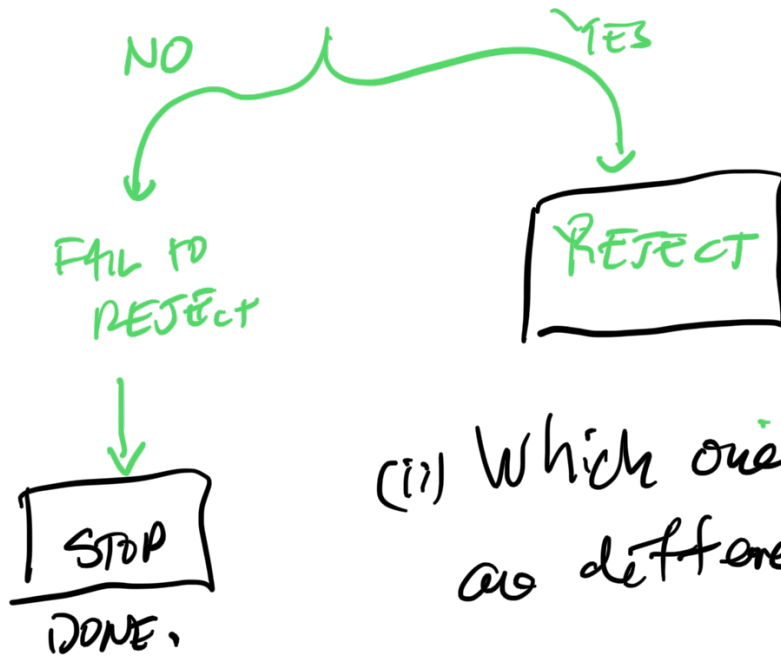
ANOVA TABLE

Source	df	SS	MS	f	i
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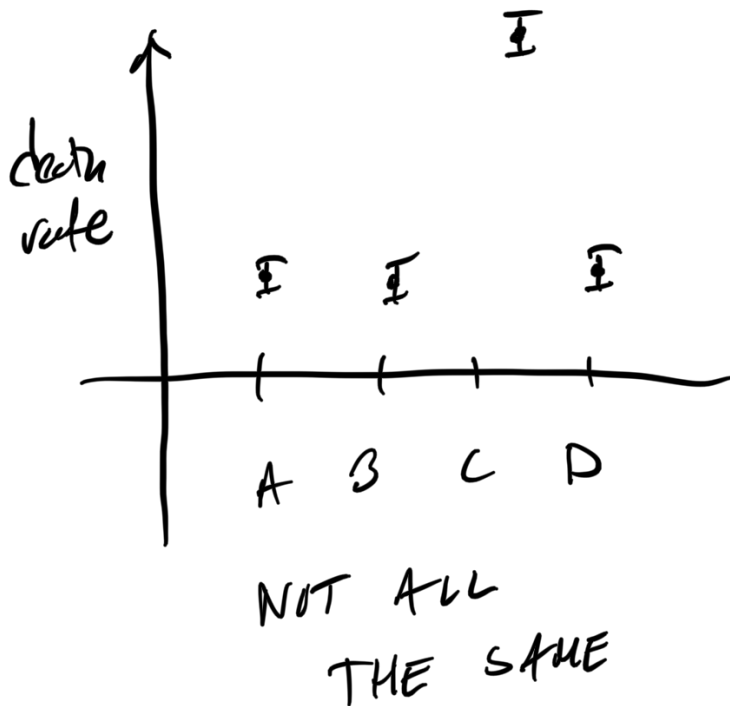


what do we do next?

(i) Are the different settings  
different?



(ii) Which ones  
are different?



... ON THE DATA!

→ PLDT (100%)

## Tukey's HSD Test.

Honestly Significant Difference.

### Procedure

(1) Standard Error

$$SEM = \sqrt{\frac{MS_{error}}{n}}$$

Size of "error bar"

$$\left( \frac{\sigma}{\sqrt{n}} \right)$$

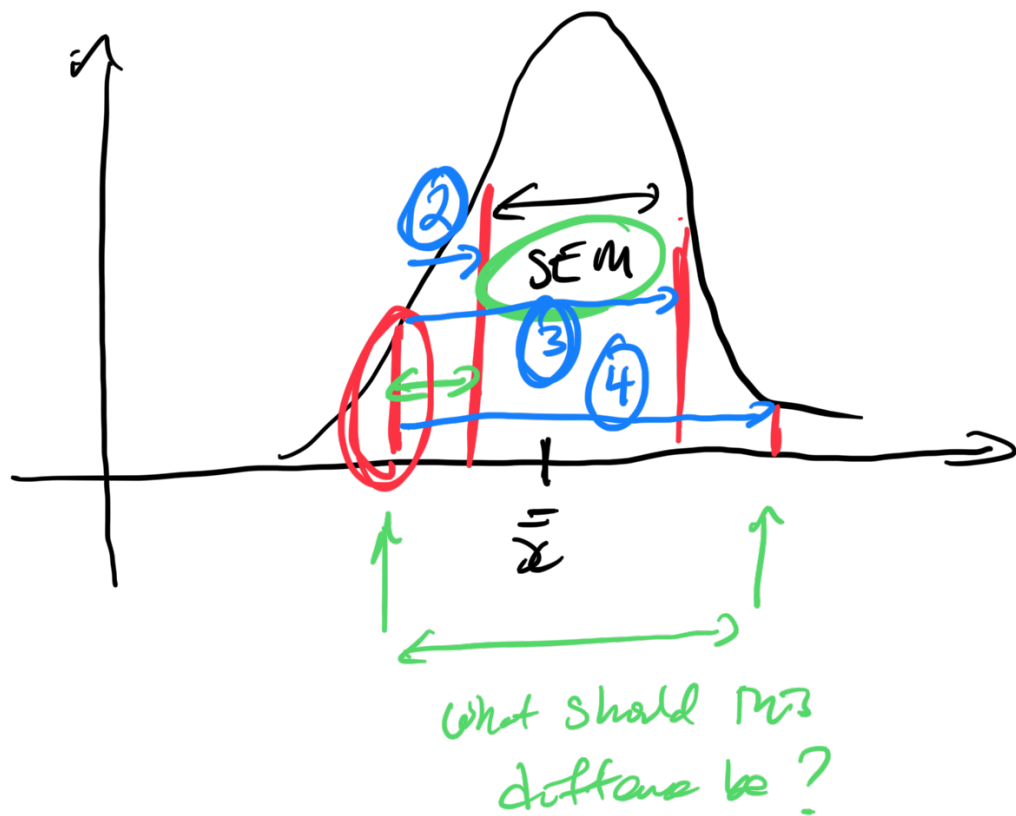
$\sqrt{\frac{\sigma^2}{n}}$

(2) Order the means from smallest to largest.

$$[4.28, 4.81, 5.39, 5.88]$$

$\bar{x} = 5.09$

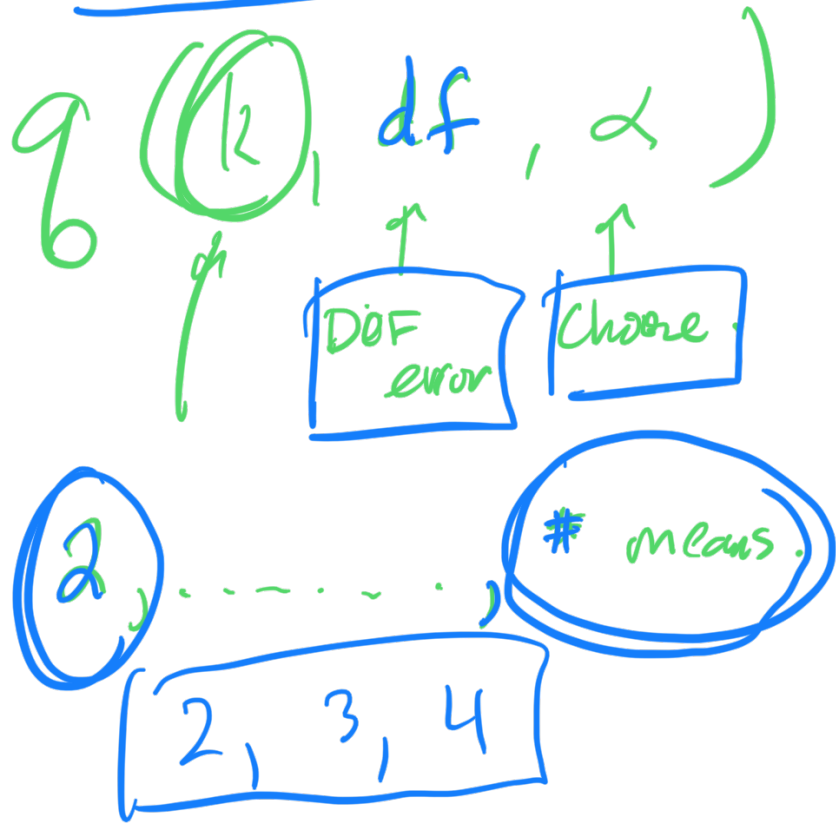
$$[5.07, 5.08, 5.09, 5.10]$$



Gossett

③ Studentized Range of values.

Expected  $\neq$   $\pm$  error bars



④ **W**  $\leftarrow$  max. expected difference between largest and smallest.  
 $q(4) \neq \text{std-error}$   
 ↑  
 webassign

⑤ Pairwise Comparisons.  $q(2)$   
 $q(3) \leftarrow$   
 $q(4)$

1, 2, 3, 4

Smallest

largest

Actual

Expected

1 vs. 4

$$\bar{x}_4 - \bar{x}_1$$

$g(4) * \text{std. err.}$

1 vs. 3

$$\bar{x}_3 - \bar{x}_1$$

$g(3) * \text{std. err.}$

1 vs. 2

$$\bar{x}_2 - \bar{x}_1$$

$g(2) * \text{std. err.}$

2 vs. 4

$$\bar{x}_4 - \bar{x}_2$$

$g(3) * \text{std. err.}$

2 vs. 3

$$\bar{x}_3 - \bar{x}_2$$

$g(2) * \text{std. err.}$

3 vs. 4

$$\bar{x}_4 - \bar{x}_3$$

$g(2) * \text{std. err.}$

$(n-1)!$

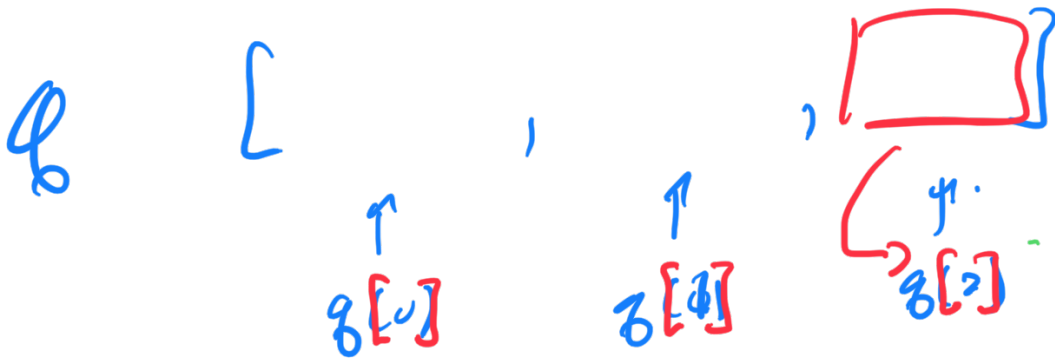
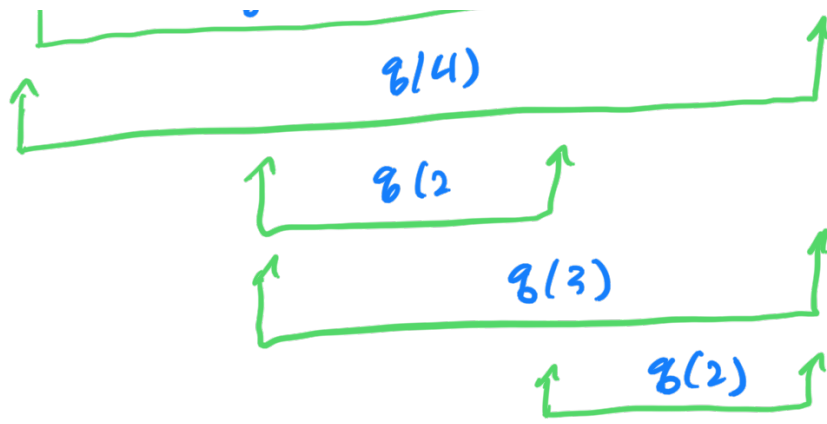
↑ ↑

ordered  
indices.

$\bar{x}_1, \bar{x}_2, \bar{x}_3, \bar{x}_4$

$g(2)$   $g(3)$





# moves = 4

4-2

