Complete the following assignment prior to Meeting #16:

- A. Study our notes from Meeting #15.
- B. Comprehend Jim's sample response to Quiz 15.
- C. Comprehend Entry #036A–D of our *Glossary*.
- D*. Please solve each of the following problems; display the computations, and upload the resulting pdf document on the appropriate Canvas assignment link:
 - i In a certain region of western Asia, 75 % of the population live to be at least 80 years old. 63% of the population lives to be at least 90 years. What is the probability of a randomly selected person who is in her/his/their 80's survives to be 90 years old?

Sample computation:

Let A be the event that the selected person survives to be 90 years old \land let B be the event that the person is at least 80 years old. We need to compute p(A|B).

$$p(A|B) = \frac{p(A \cap B)}{p(B)}$$
. Since a 90-year old is also 80, $p(A \cap B) = p(A)$, thus we have:

$$p(A|B) = \frac{p(A \cap B)}{p(B)} = \frac{p(A)}{p(B)} = \frac{0.63}{0.75} = 0.84$$



ii. Assume that in a two-child family, all sex distributions are equally probable. An experiment is conducted in which a *family* is randomly selected from { families that have exactly two children }; the selected family has at least one girl. What is the probability that the second child is also a girl?

Sample computation:

Let A be the event that the selected family has two girls \land let B be the event that the family has a girl. For this family with exactly two children, let $\Omega = \{ (f, s) : f = \text{the sex of the first born } \land s \text{ is the sex of the second born } \} = \{ (g, g), (g, b), (b, g), (b, b) \}$. We need to compute p(A|B):

$$p(A|B) = \frac{p(A \cap B)}{p(B)} = \frac{0.25}{0.75} = \frac{1}{3}$$

iii. Assume that in a two-child family, all sex distributions are equally probable. An experiment is conducted in which a *child* is randomly selected from { families that have exactly two children } and that particular child is a girl. What is the probability that the second child is also a girl?

Sample computation:

Let B be the event that the randomly selected child is a girl \land let A be the event that her sibling is also a girl. We need to compute p(A|B):

$$p(A|B) = \frac{p(A \cap B)}{p(B)} = \frac{0.25}{0.50} = \frac{1}{2}$$

- E. From the Video Page of *Canvas*, view with comprehension "Bayes' theorem of conditional probability."
- F. Comprehend Jim's sample responses to the homework prompts that are posted on *Canvas*.