



Electronics Systems (938II)

Lecture 2.2

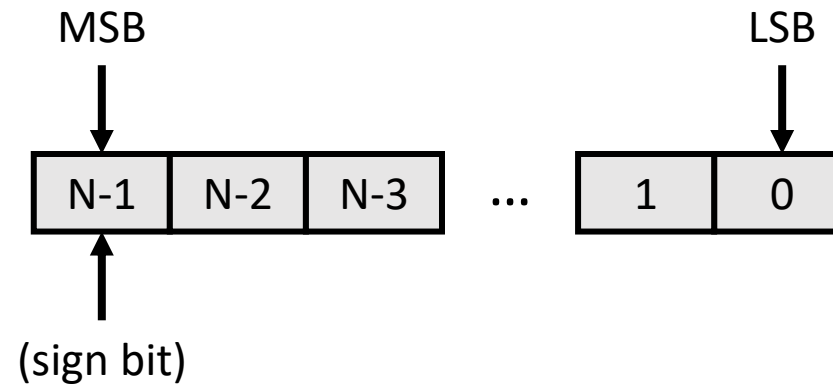
Building Blocks of Electronic Systems – Arithmetic operations

Combinational circuits for arithmetic operations

- Let's assume arithmetic operations on **integers (with sign)**
 - Addition
 - Subtraction
 - Multiplication
 - Division
- For this purpose, integers are represented using **two's complement (C2)**

Two's complement representation (of integers with sign)

- Assume N bits
 - Most significant bit (MSB), the leftmost one, is the sign bit



Two's complement representation (of integers with sign)

- Positive numbers
 - Natural binary representation
 - Sign bit = 0

• Example: $1 \rightarrow 000\dots01$



Two's complement representation (of integers with sign)

- Negative numbers

1. Get absolute binary representation (i.e. corresponding positive value)
2. Invert (or complement) all bits
3. Add 1 (ignoring overflow)

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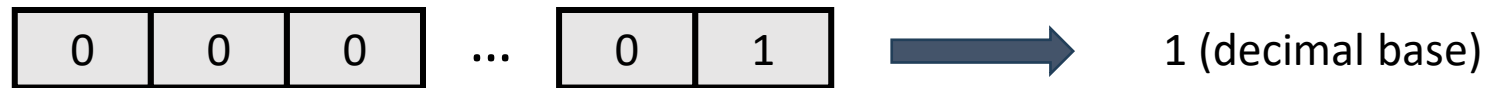
- Example: -1

Two's complement representation (of integers with sign)

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- Example: -1

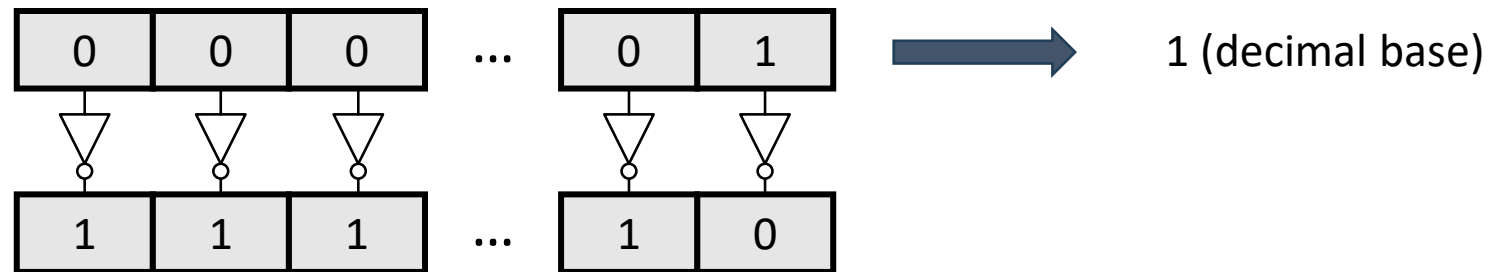


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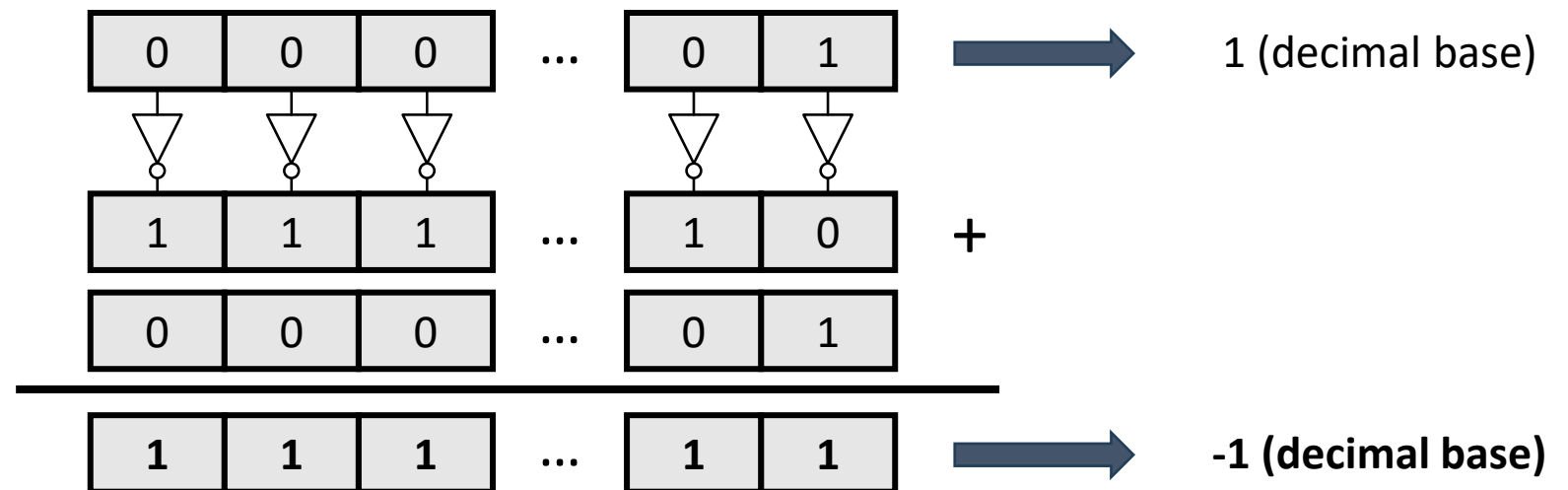


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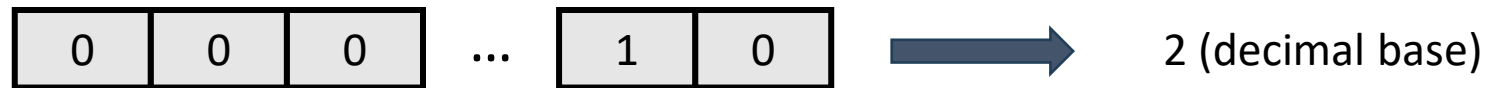
- Example: -2

Two's complement representation (of integers with sign)

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- Example: -2

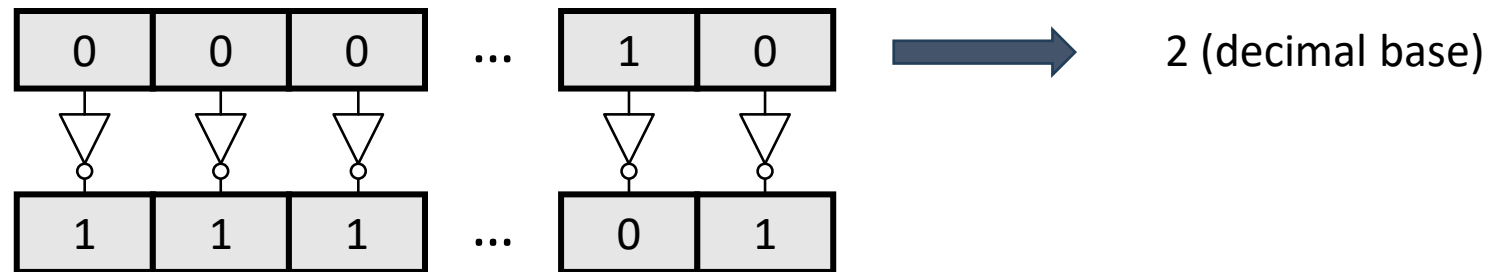


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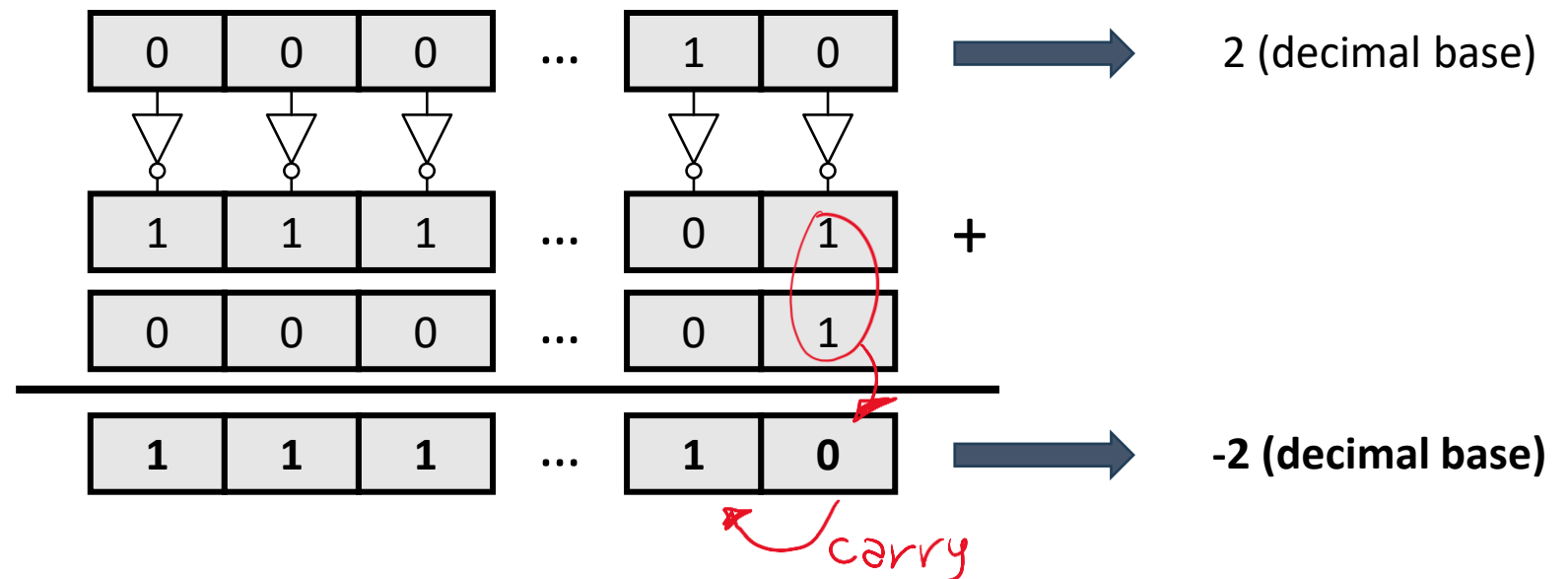


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Two's complement representation (of integers with sign)

- Range of signed integer numbers (in decimal base) = $[-2^{N-1} \div 2^{N-1} - 1]$

Two's complement representation (of integers with sign)

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C2 representation
011...11
...
000...01
000...00
111...11
111...01
...
100...00

Two's complement representation (of integers with sign)

- Range of signed integer numbers (in decimal base) = $[-2^{N-1} \div 2^{N-1} - 1]$
 - Example: $N = 3$
 - $2^{N-1} - 1 = 2^2 - 1 = 4 - 1 = 3$
 - $-2^{N-1} = -2^2 = -4$

Two's complement representation (of integers with sign)

- Range of signed integer numbers (in decimal base) = $[-2^{N-1} \div 2^{N-1} - 1]$

- Example: $N = 3$



- $2^{N-1} - 1 = 2^2 - 1 = 4 - 1 = 3$
- $-2^{N-1} = -2^2 = -4$

C2 representation	Decimal base
011	3
010	2
001	1
000	0
111	-1
110	-2
101	-3
100	-4

Two's complement representation (of integers with sign)

- Why this?
 - Because it allows to perform arithmetic operations without particular (or dedicated) resources to handle the sign
 - Lower costs
 - Lower delays
 - **Subtraction** can be implemented as the **addition with the opposite number**; for examples ...
 - $10 - 18 = 10 + (-18)$
 - $12 - (-7) = 12 + 7$
 - ...
- Let's see some examples
 - Assuming $N = 3$ bits

Two's complement representation (of integers with sign)

<div style="border: 1px dashed black; padding: 5px; margin-bottom: 10px; text-align: center;">$1 + 1$</div> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(1)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>0</td><td>0</td><td>1</td></tr> </table> <div style="margin: 0 10px;">+</div> </div> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(1)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>0</td><td>0</td><td>1</td></tr> </table> </div> <hr style="border: 1px solid black; margin: 5px 0;"/> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(2)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>0</td><td>1</td><td>0</td></tr> </table> </div>	0	0	1	0	0	1	0	1	0	<div style="border: 1px dashed black; padding: 5px; margin-bottom: 10px; text-align: center;">$1 + (-1) \rightarrow 1 - 1$</div> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(1)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>0</td><td>0</td><td>1</td></tr> </table> <div style="margin: 0 10px;">+</div> </div> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(-1)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>1</td><td>1</td><td>1</td></tr> </table> </div> <hr style="border: 1px solid black; margin: 5px 0;"/> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(0)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>0</td><td>0</td><td>0</td></tr> </table> </div>	0	0	1	1	1	1	0	0	0	<div style="border: 1px dashed black; padding: 5px; margin-bottom: 10px; text-align: center;">$1 + (-2) \rightarrow 1 - 2$</div> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(1)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>0</td><td>0</td><td>1</td></tr> </table> <div style="margin: 0 10px;">+</div> </div> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(-2)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>1</td><td>1</td><td>0</td></tr> </table> </div> <hr style="border: 1px solid black; margin: 5px 0;"/> <div style="display: flex; align-items: center;"> <div style="text-align: right; margin-right: 10px;">(-1)</div> <table border="1" style="border-collapse: collapse; text-align: center; width: 60px;"> <tr><td>1</td><td>1</td><td>1</td></tr> </table> </div>	0	0	1	1	1	0	1	1	1
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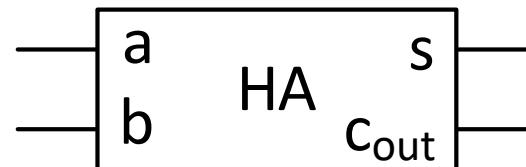
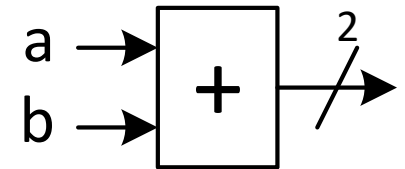
Adder

- The sum of 2 N-bit numbers requires N+1 bits to be represented
 - $N = 1 \rightarrow 2$ bits to represent the sum
- The simplest adder is the **Half Adder (HA)**
 - Just the sum of the two 1-bit inputs (a, b)
 - Output must be 2-bit

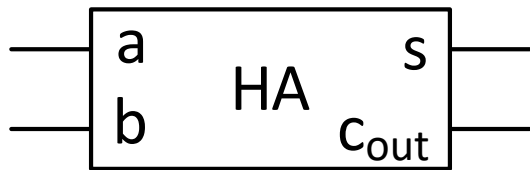


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 - Output must be 2-bit
 - s
 - c_{out} = carry (output)



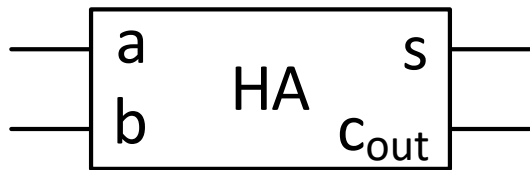
Half Adder (HA)



HA truth table

a	b	s	c _{out}
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

Half Adder (HA)



HA truth table

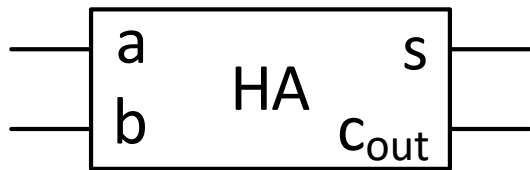
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0	0	0	0
0	1	1	0
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$s = 1$, when $a \neq b$

Half Adder (HA)

Does this remind you a logic operator we have seen before?



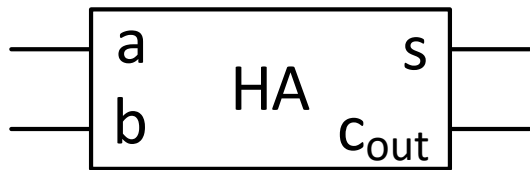
HA truth table

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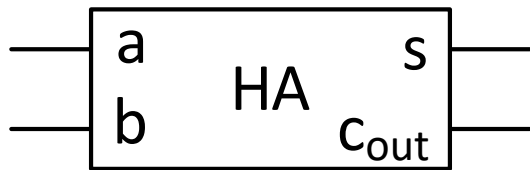


$s = 1$, when $a \neq b$



$$s = a \oplus b$$

Half Adder (HA)



HA truth table

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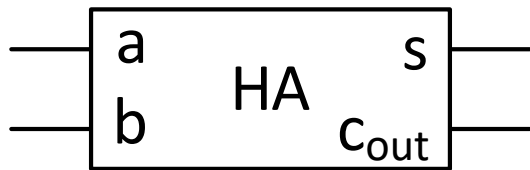


$$s = a \oplus b$$



$C_{out} = 1$, when
 $a = 1$ and $b = 1$

Half Adder (HA)



HA truth table

a	b	s	C _{out}
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



$s = 1$, when $a \neq b$



$$s = a \oplus b$$

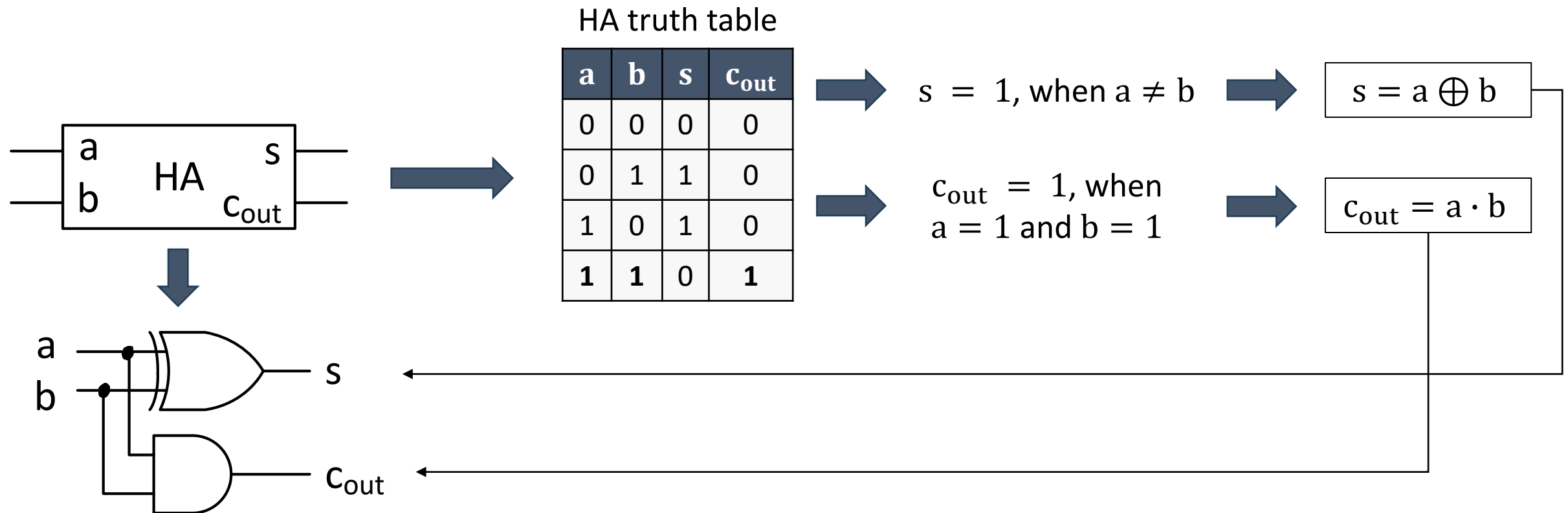


$C_{out} = 1$, when
 $a = 1$ **and** $b = 1$



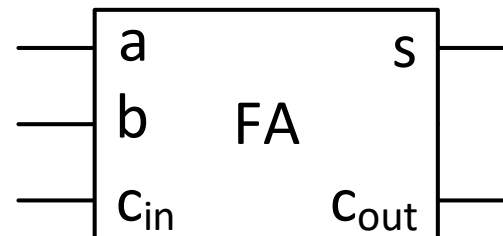
$$C_{out} = a \cdot b$$

Half Adder (HA)



Adder

- But, as we saw earlier, when summing two multi-bit vectors, it may happen that the carry is generated by the sum of the previous bits
 - To fully support the addition, also a carry input must be considered
 - c_{in} = carry (input)
- The corresponding (1-bit) adder is called **Full Adder (FA)**

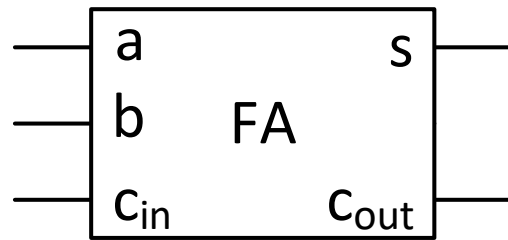


Full Adder (FA)

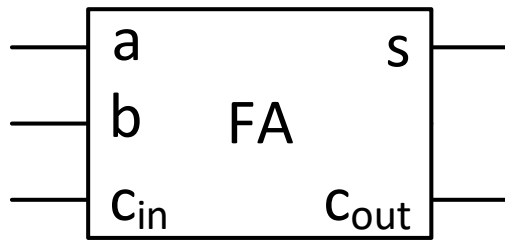
FA truth table

c_{in}	a	b	s	c_{out}
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

$$s = a \oplus b \oplus c_{in}$$



Full Adder (FA)



FA truth table

c_{in}	a	b	s	c_{out}
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
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1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
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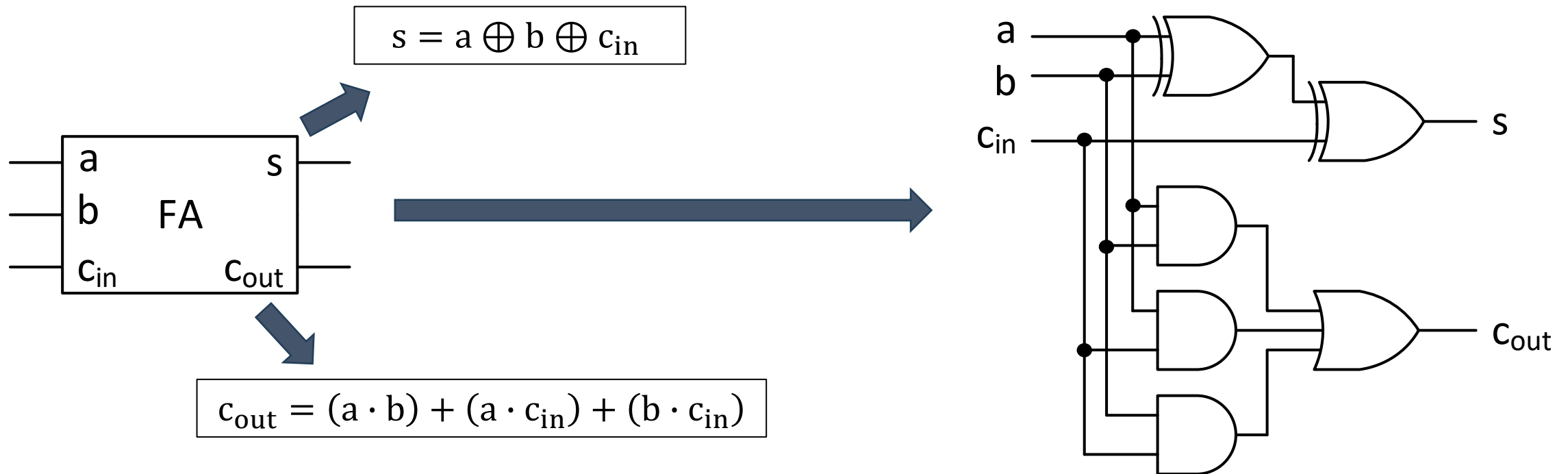


$$s = a \oplus b \oplus c_{in}$$



$$c_{out} = (a \cdot b) + (a \cdot c_{in}) + (b \cdot c_{in})$$

Full Adder (FA)



Adder (for multi-bit operands)

- A generic adder (for N-bit operands) can be built by cascading N FAs

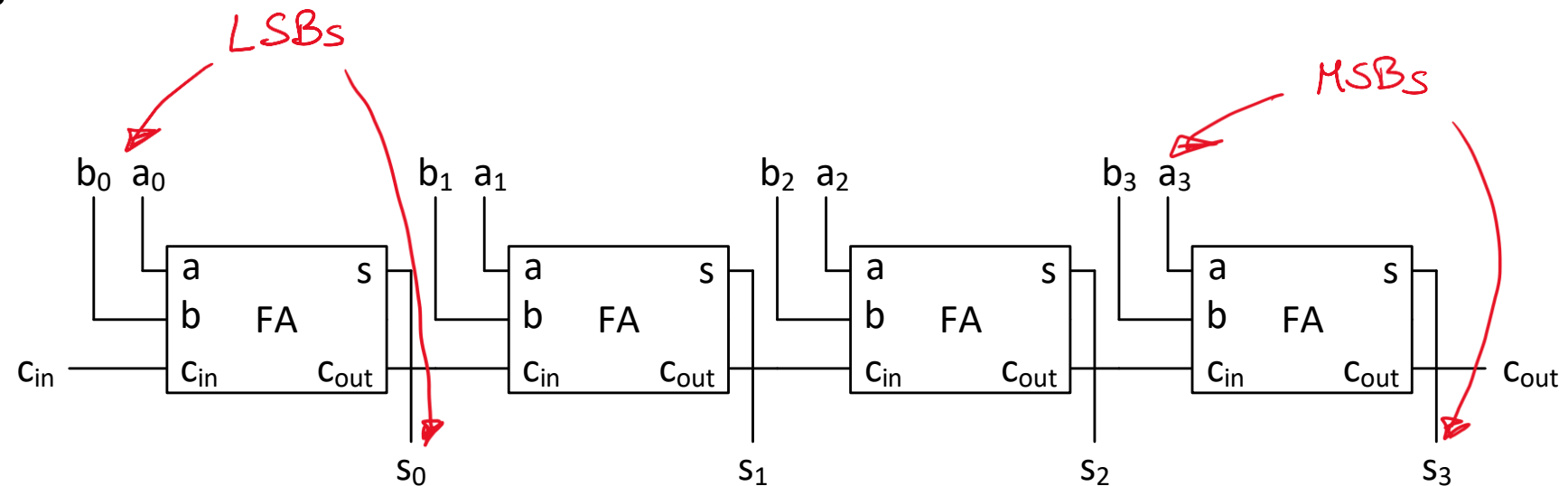
- Example: 4-bit adders

Inputs

- $a = \{a_3 a_2 a_1 a_0\}$
- $b = \{b_3 b_2 b_1 b_0\}$
- c_{in}

Outputs

- $s = \{s_3 s_2 s_1 s_0\}$
- c_{out}



Adder (for multi-bit operands)

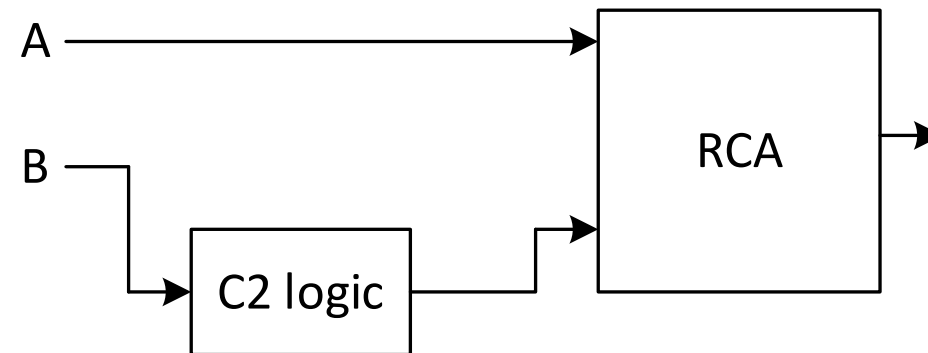
- The one saw before is called also Ripple Carry Adder (RCA)
 - The carry path propagate from the input to the output
 - Path is proportional to the bit width of the input operands
 - The delay path may be very high
- Other solutions (and architectures/circuits) for adders exist to solve this problem
 - Carry Save Adder (CSA)
 - Carry Bypass Adder (CBA), or Carry Skip Adder
 - Carry Lookahead Adder (CLA)

Adder (for multi-bit operands)

- CSA, CBA, CLA, ...: just for the sake of completeness
 - We are not going to analyze them
 - However, remember that each solution is a trade-off
 - They can be advantageous in terms of delay with respect to the RCA
 - But they can also present costs in other terms (e.g., resources)

Subtractor (for multi-bit operands)

- If you remember the properties of two's complement representation...
 - $A - B = A + (-B)$



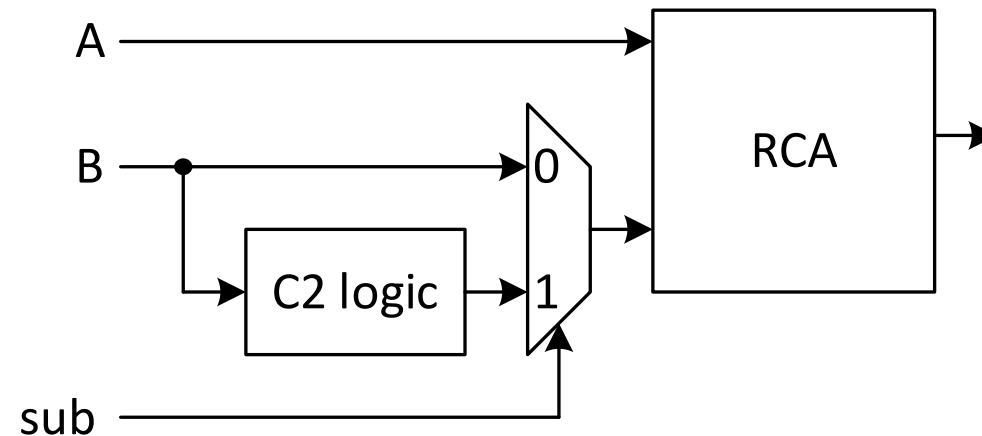
Adder/Subtractor (for multi-bit operands)

- For a full-case solution, i.e. adder/subtractor

- Inputs : A, B

- Control : sub

- If $\text{sub} = 0 \rightarrow A + B$
- If $\text{sub} = 1 \rightarrow A - B = A + (-B)$

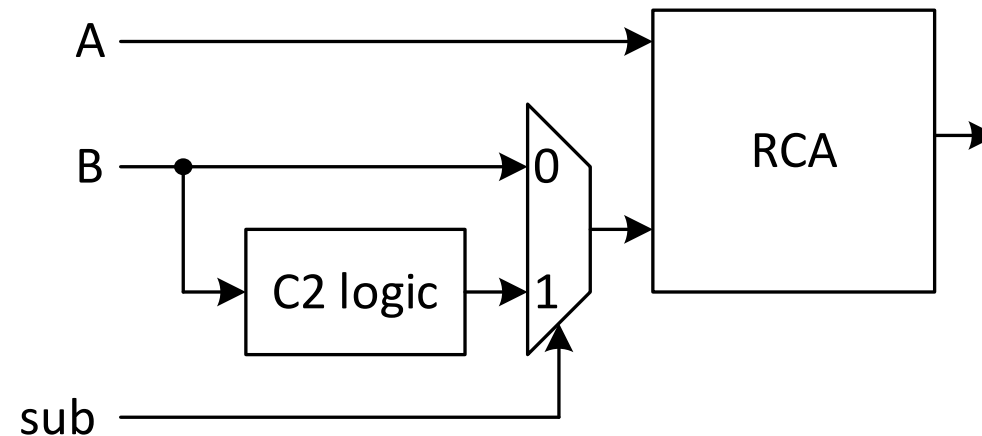


Adder/Subtractor (for multi-bit operands)

- For a full-case solution, i.e. adder/subtractor

- If you remember, to get $-B$ from B :

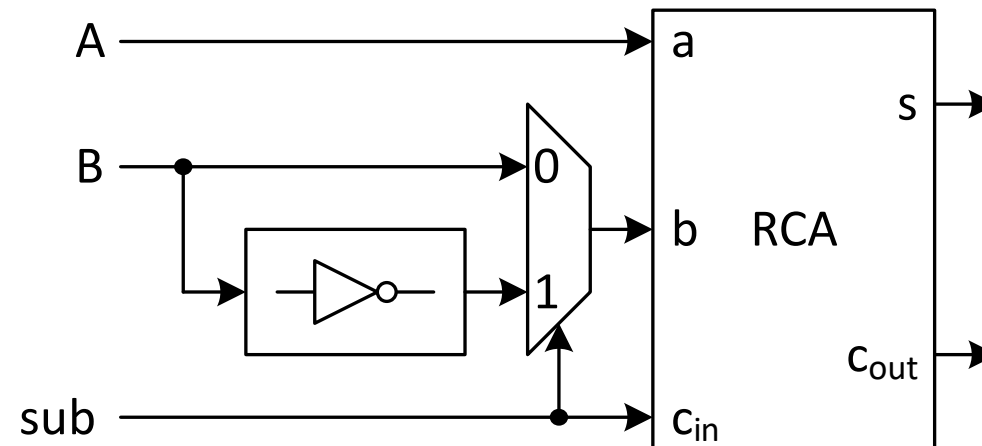
- Complement all bits of B
- Add 1
 - This can be done by exploiting the c_{in} input of RCA



Adder/Subtractor (for multi-bit operands)

- For a full-case solution, i.e. adder/subtractor
 - If you remember, to get $-B$ from B :

- Complement all bits of B
- Add 1
 - This can be done by exploiting the c_{in} input of RCA



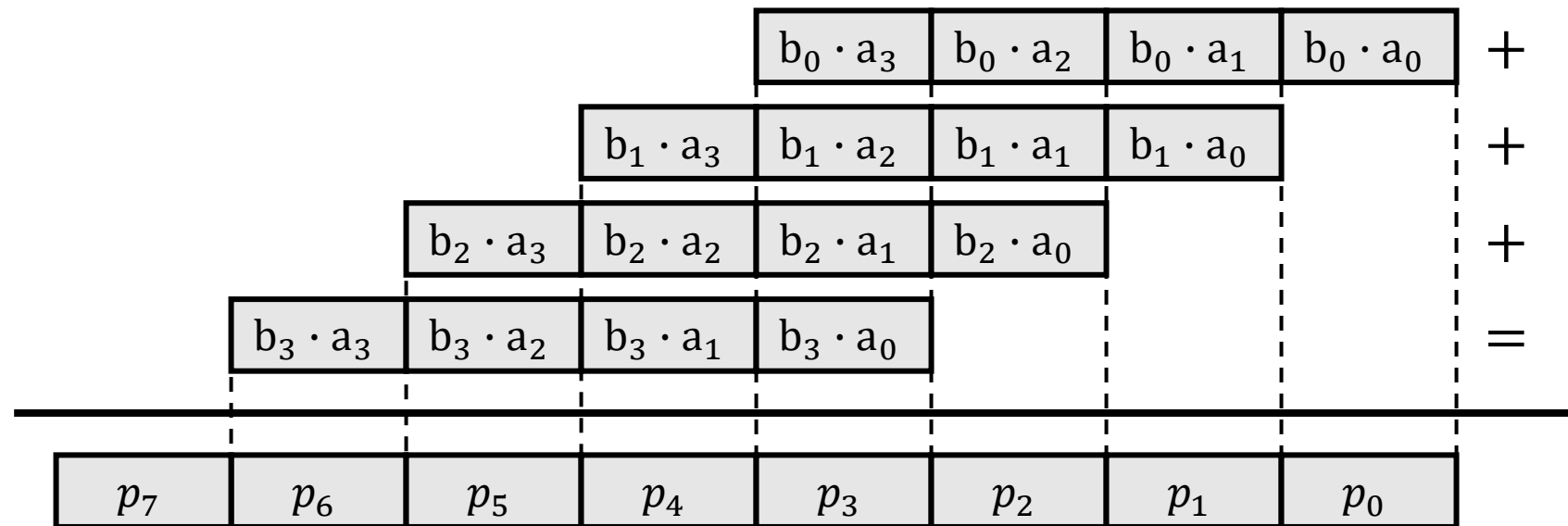
Multiplier

- The multiplication of a N -bit number by an M -bit number requires $N+M$ bits to be represented
 - Typically, $N = M \rightarrow 2N$ bits to represent the product
- The simplest way: shift-and-add algorithm
 - Similar to the paper-and-pencil method for decimal multiplication

Multiplier

- Assume $N = 4$ and calculate $p = a * b$

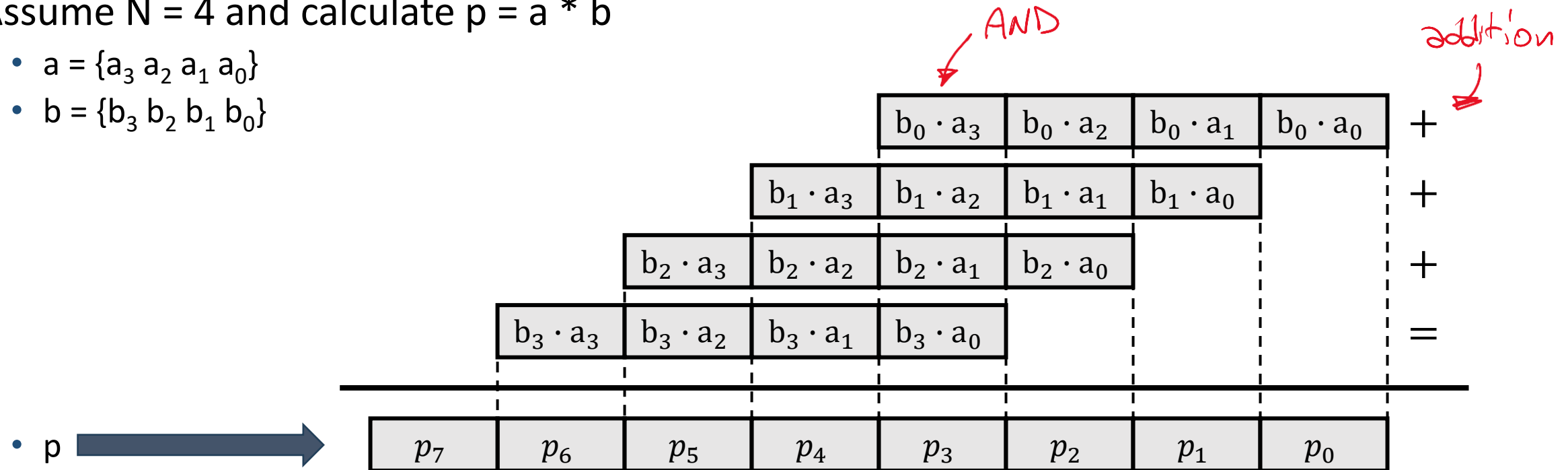
- $a = \{a_3 \ a_2 \ a_1 \ a_0\}$
- $b = \{b_3 \ b_2 \ b_1 \ b_0\}$



Multiplier

- Assume $N = 4$ and calculate $p = a * b$

- $a = \{a_3 \ a_2 \ a_1 \ a_0\}$
- $b = \{b_3 \ b_2 \ b_1 \ b_0\}$



Multiplier

- Assume $N = 4$ and calculate $p = a * b$

- $a = \{a_3 a_2 a_1 a_0\}$
- $b = \{b_3 b_2 b_1 b_0\}$

We can see AND each row as a 7 bit vector.

0	0	0	$b_0 \cdot a_3$	$b_0 \cdot a_2$	$b_0 \cdot a_1$	$b_0 \cdot a_0$	+
0	0	$b_1 \cdot a_3$	$b_1 \cdot a_2$	$b_1 \cdot a_1$	$b_1 \cdot a_0$	0	+
0	$b_2 \cdot a_3$	$b_2 \cdot a_2$	$b_2 \cdot a_1$	$b_2 \cdot a_0$	0	0	+
$b_3 \cdot a_3$	$b_3 \cdot a_2$	$b_3 \cdot a_1$	$b_3 \cdot a_0$	0	0	0	=

- p



p_7	p_6	p_5	p_4	p_3	p_2	p_1	p_0
-------	-------	-------	-------	-------	-------	-------	-------

- $N - 1$ additions of numbers with a bit width of $2N - 1$



Sequential multiplier

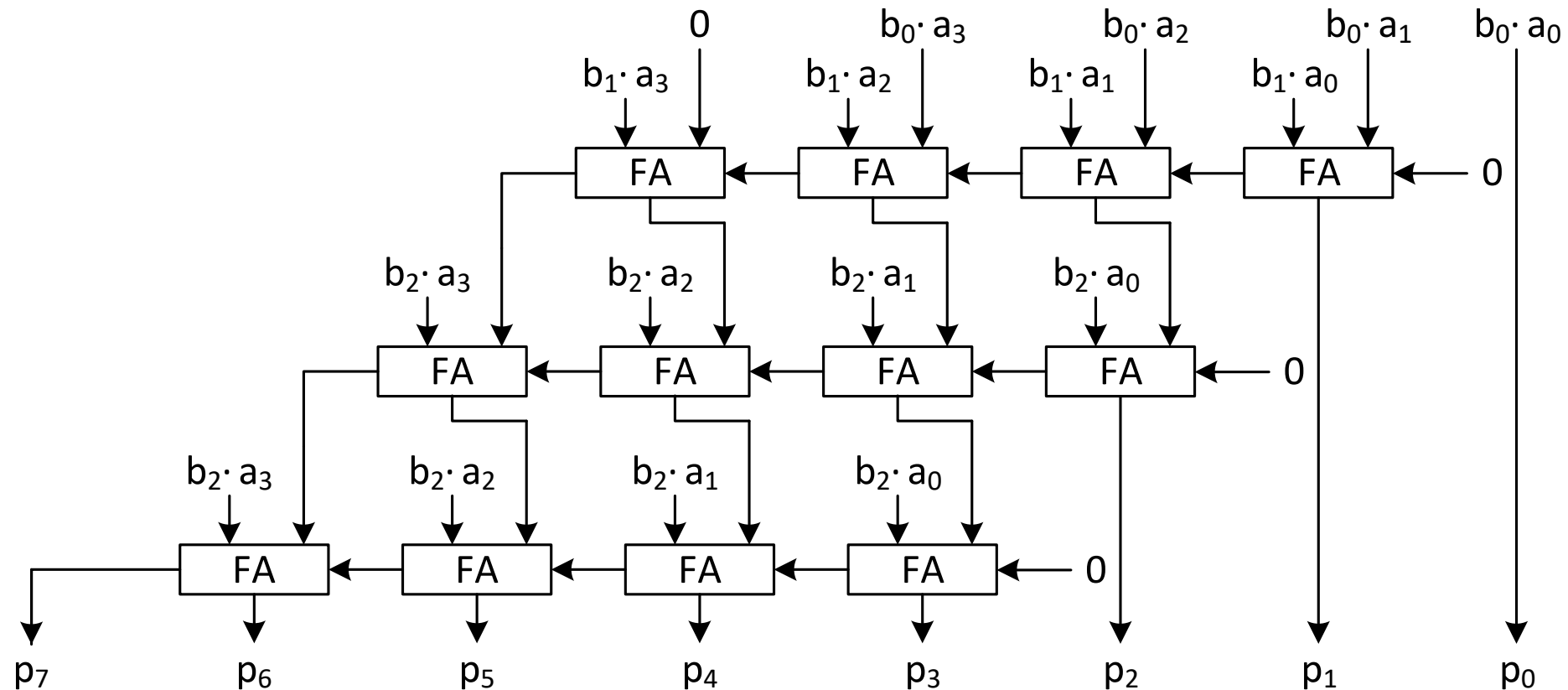
Sequential multiplier

1 DRAWBACK: Delay !

- Logic for calculation of AND products
- One adder
 - The RCA we saw before
- A register to store partial products
- Requiring $N - 1$ steps/cycles to perform the multiplication

Combinational multiplier

- Example: $N = 4$



The whole multiplication can be done in just 1 cycle

Combinational multiplier

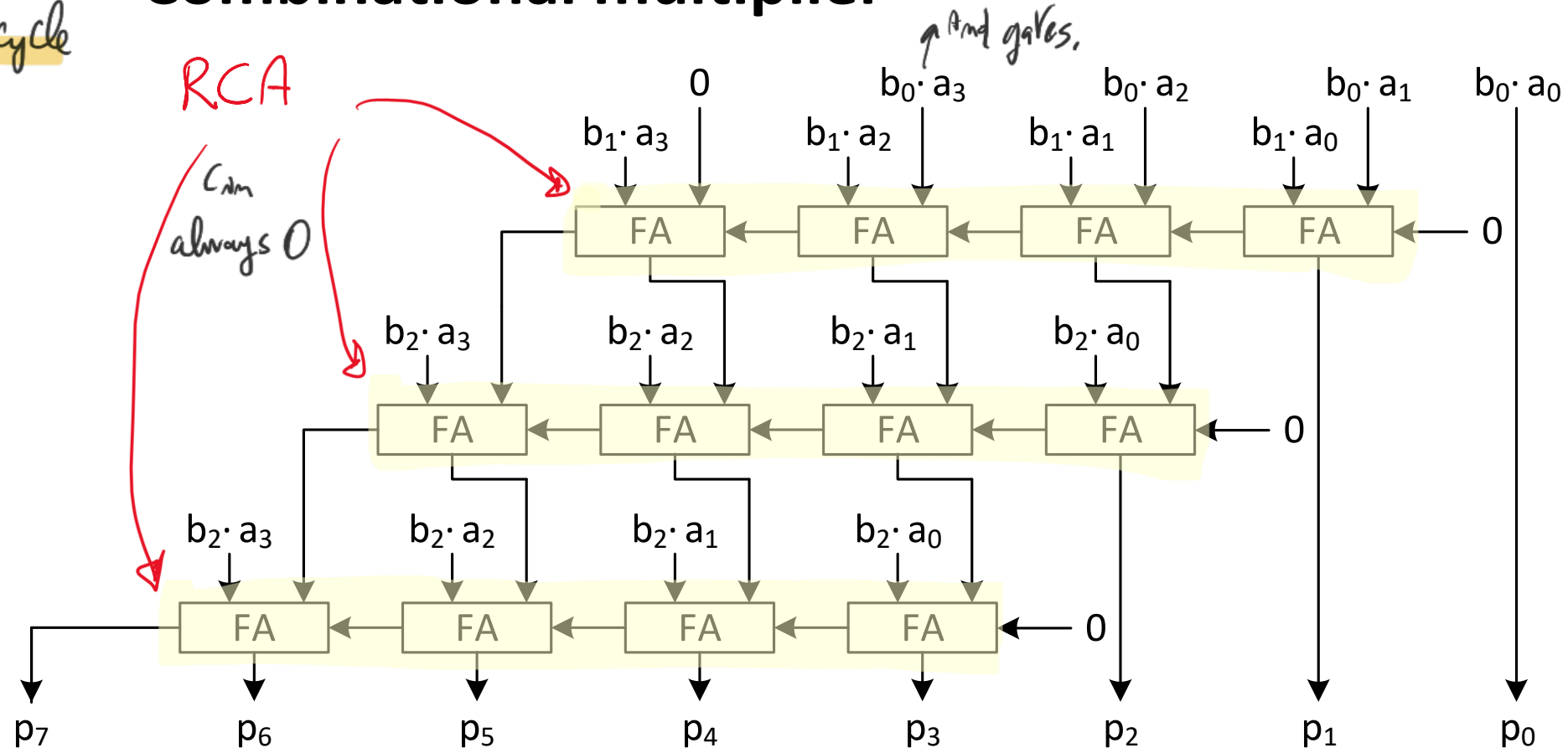
- Example: $N = 4$

- 3x 4-bit RCAs

- In general

- $N - 1$ x RCAs
- Each of N bits

- Plus logic for AND!!!



Here the number of ripple CA depends linearly on the number of bits.

And you can still have a long path. So long path means that you have lower frequencies.

Divisor

- Similarly to multiplier, the divisor can be implemented exploiting again an adder (RCA) supporting two's complement addition
- Division can be split in a sequence of subtractions and comparison
- Example: $63 / 12$
 - Quotient = 0
 - $63 - 12 = 51$ → Quotient += 1 (1), $51 > 12$? Yes
 - $51 - 12 = 39$ → Quotient += 1 (2), $39 > 12$? Yes
 - $39 - 12 = 27$ → Quotient += 1 (3), $27 > 12$? Yes
 - $27 - 12 = 15$ → Quotient += 1 (4), $15 > 12$? Yes
 - $15 - 12 = 3$ → Quotient += 1 (5), $3 > 12$? No → **Reminder = 3**
- Or other combinational circuits can be implemented

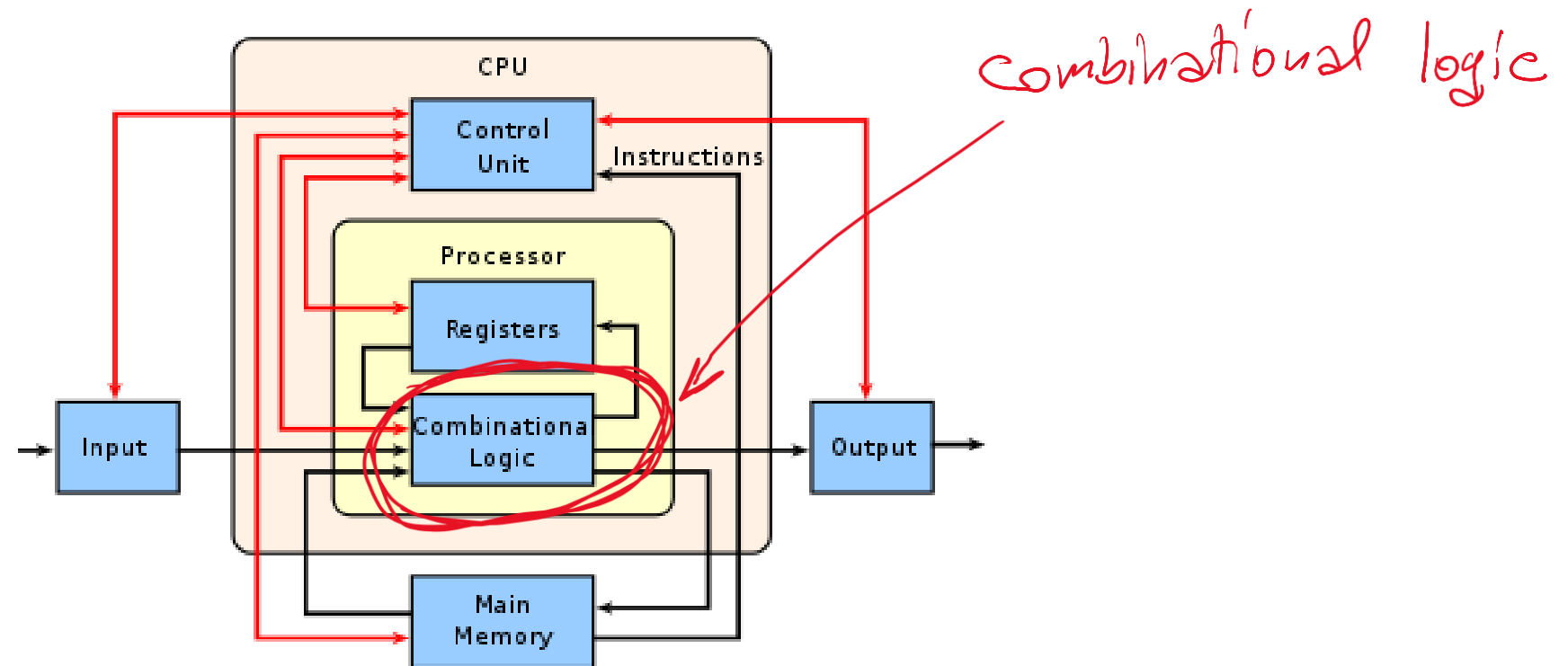
SEQUENTIAL NETWORK

Multiplicator/Divisor

- We are not going to see the circuit of a combinational divisor, however ...
- ... remember that multipliers and divisors are expansive
 - Resources and/or time (steps/cycles)

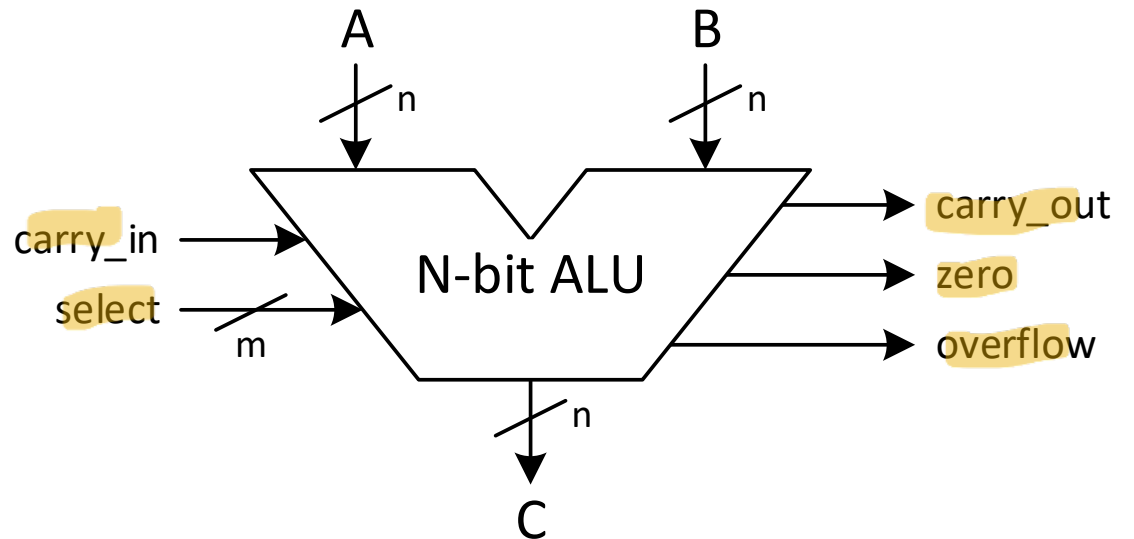
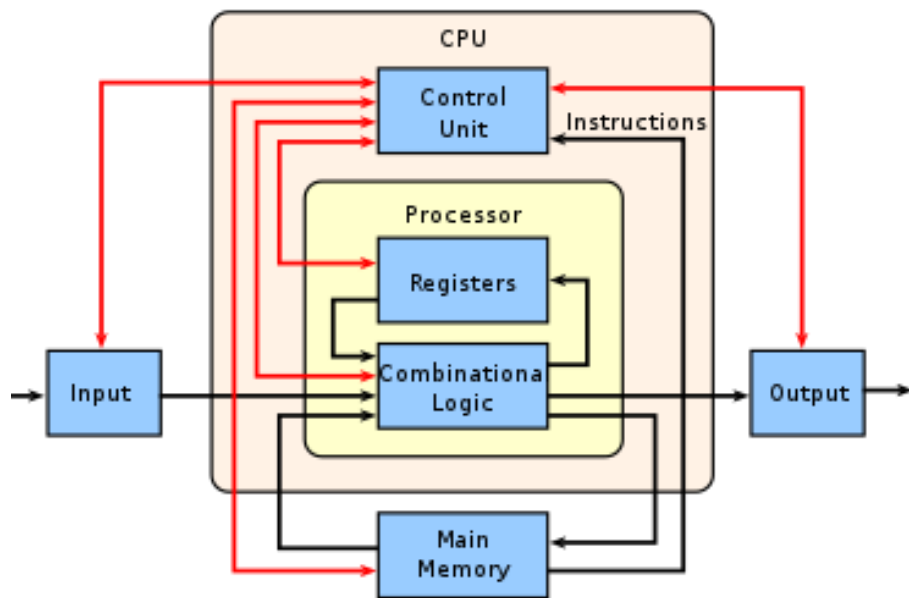
Combinational logic in modern processors

- If you remember the overall outline of a modern processor



Combinational logic in modern processors

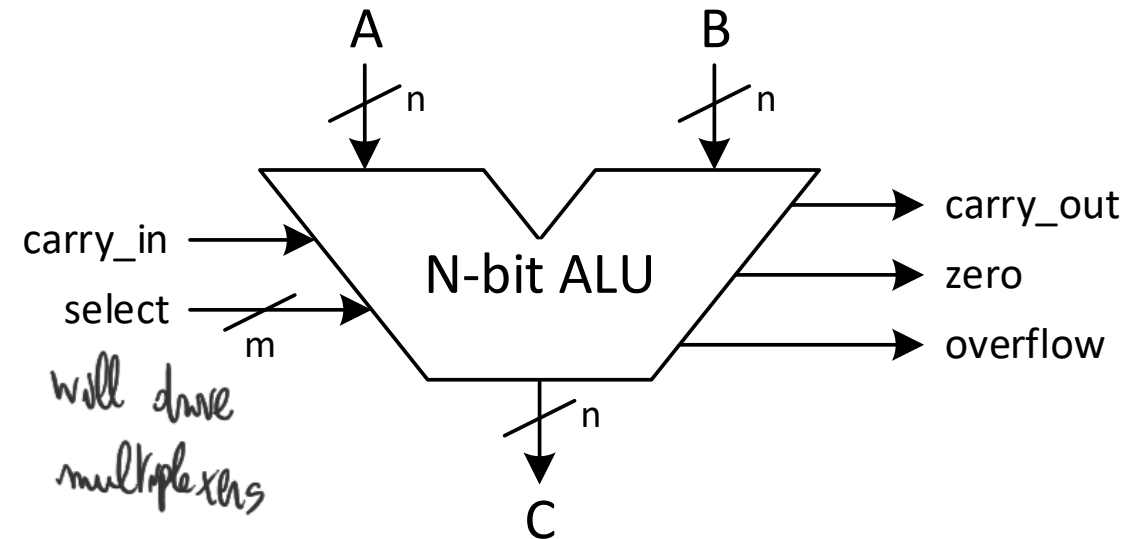
- The main component of the Combinational logic block is called **ALU**
 - ALU = Arithmetic Logic Unit** *ALU has comb. block*



ALU

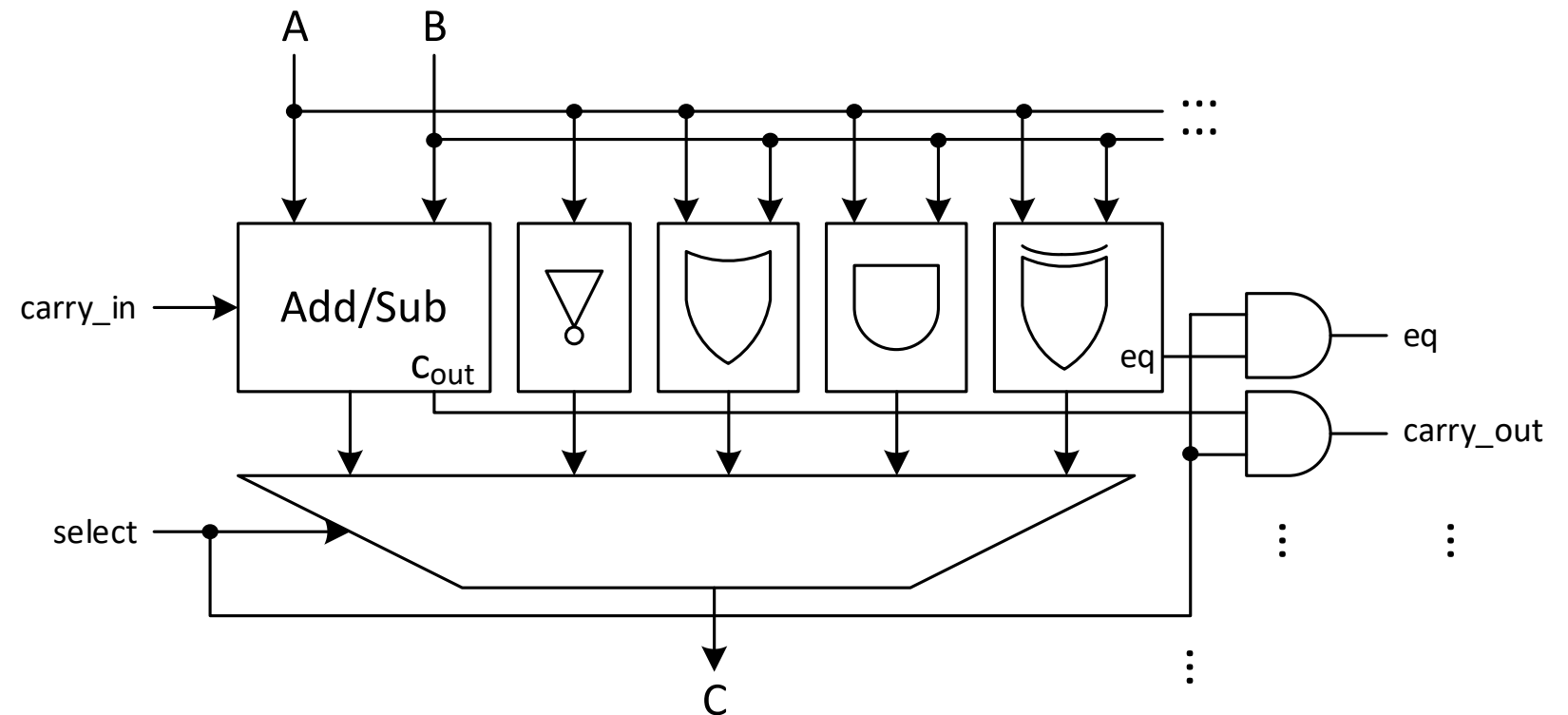
- Main operations (but not all) supported by an ALU

OPCODE (select)		Meaning
ADD	00001	$A + B$
SUB	00010	$A - B$
MULT	01000	$A * B$
NOT	10000	Complement A
AND	10001	Bit-wise AND
OR	10010	Bit-wise OR
XOR	10011	Bit-wise XOR
EQL	01011	Check $A == B$
...



ALU

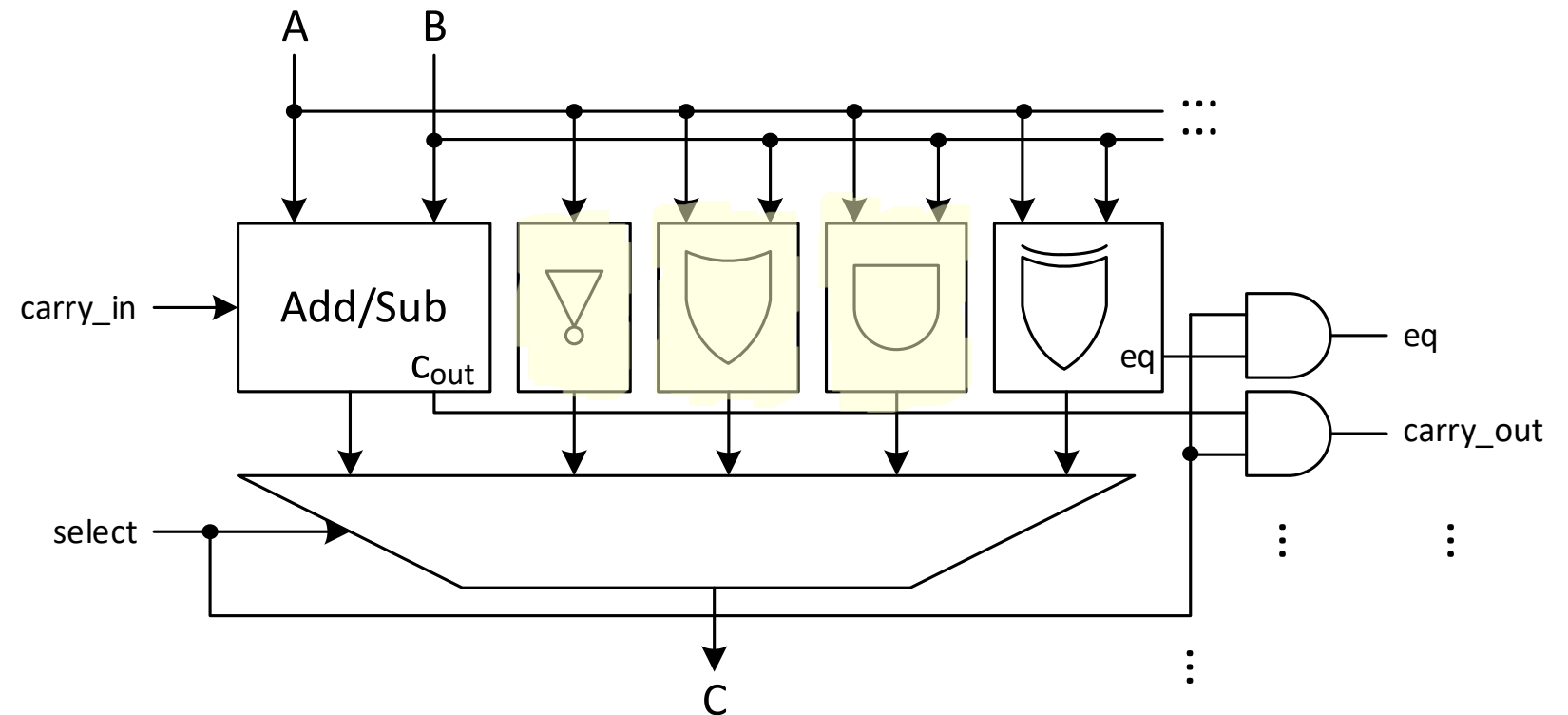
- Therefore, a possible architecture for an ALU can be the following one



ALU

- Therefore, a possible architecture for an ALU can be the following one

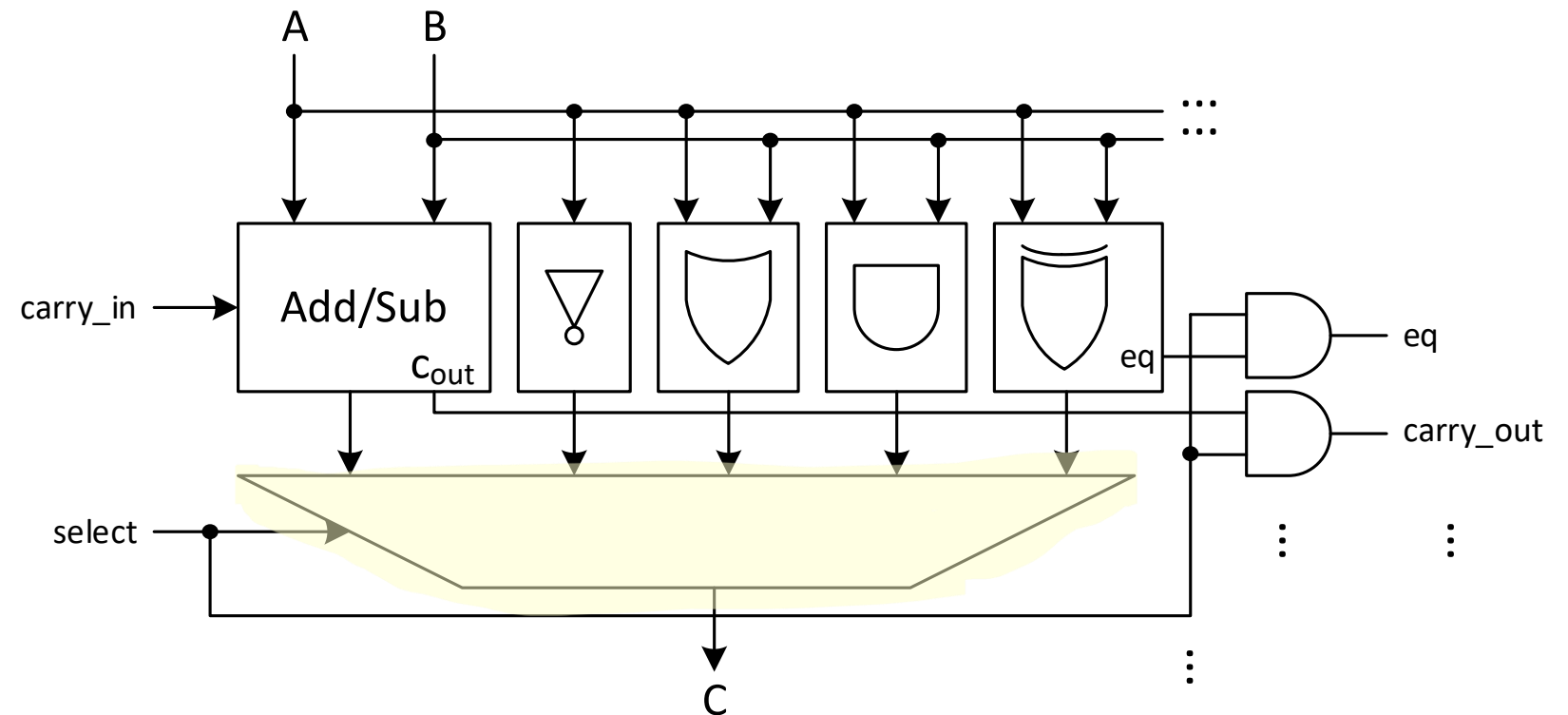
- Basic logic gates



ALU

- Therefore, a possible architecture for an ALU can be the following one

- Basic logic gates
- Multiplexers



ALU

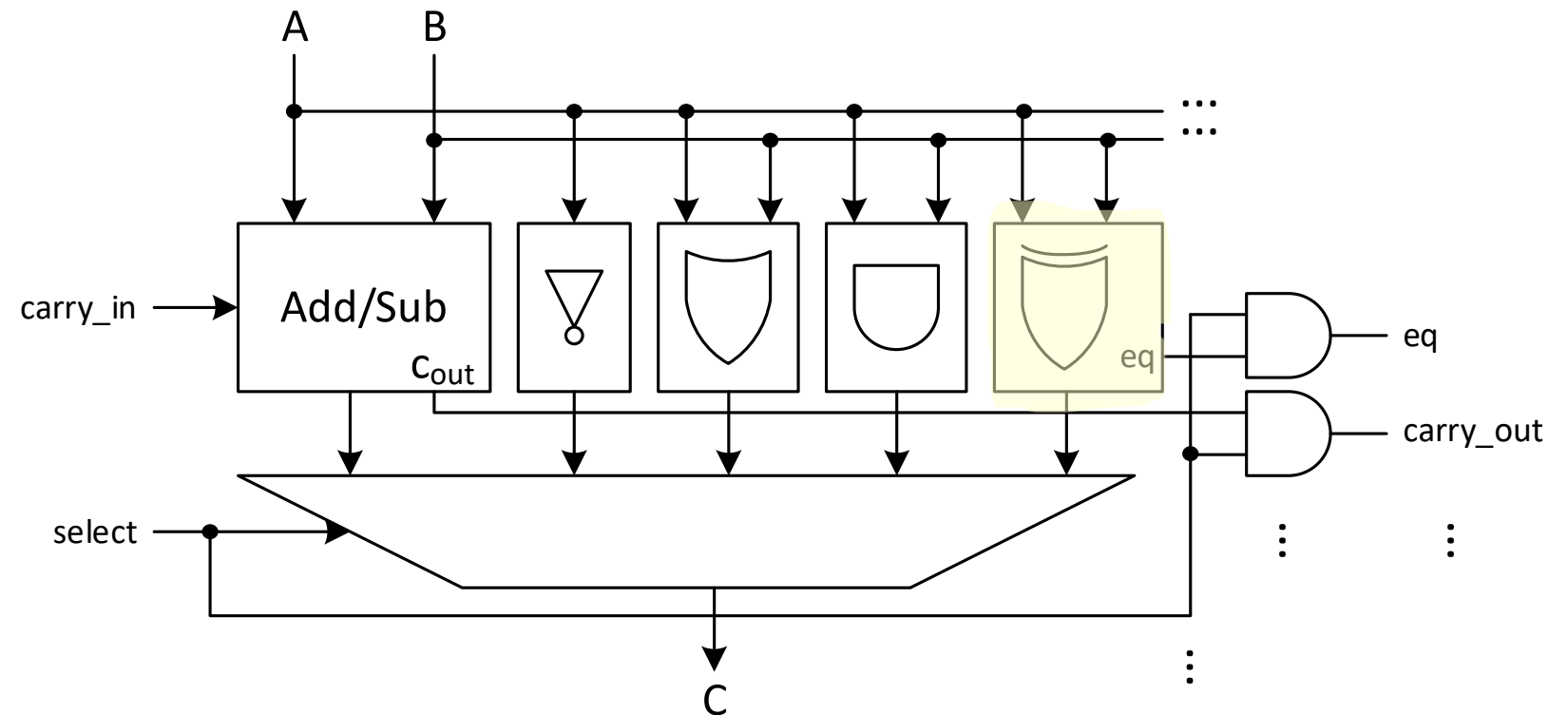
- Therefore, a possible architecture for an ALU can be the following one

- Basic logic gates

- Multiplexers

- XOR/Comparator

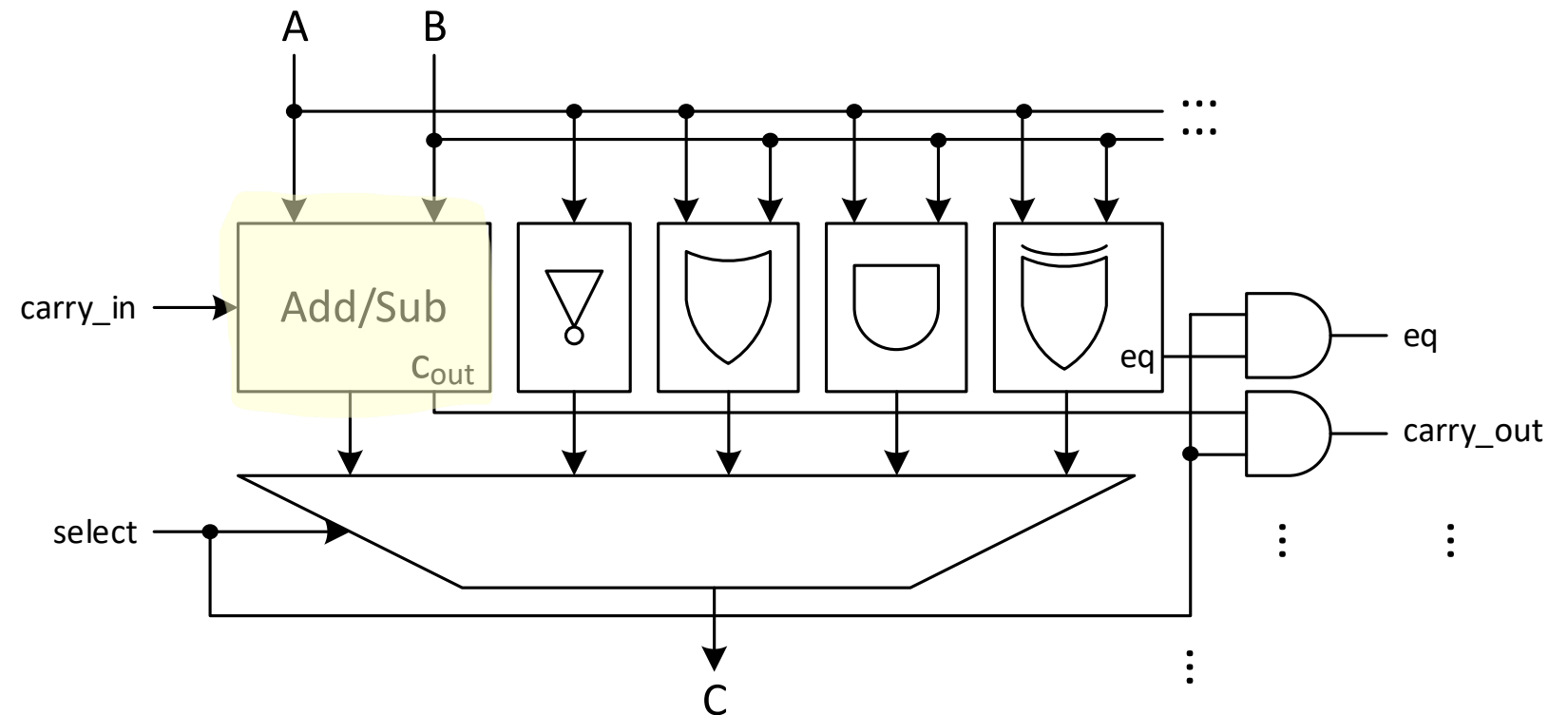
Comparator can be implemented cascading XOR gates



ALU

- Therefore, a possible architecture for an ALU can be the following one

- Basic logic gates
- Multiplexers
- XOR/Comparator
- Adder/Subtractor



Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder 4 bit (  
    input    [3:0] a  
    ,input    [3:0] b  
    ,output   [3:0] c  
);
```

4-bit signals

```
endmodule
```

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);
```

??



```
endmodule
```

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);
```

```
    assign c = a + b;
```

```
endmodule
```

- Continuous assignment (again)
 - assign <signal> = <expression>;
 - But using arithmetic operator (+) in <expression>

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);  
  
    assign c = a + b;  
  
endmodule
```

- **Some operators in SV**

- Arithmetic

- They can be use in any expression/assignment (also blocking or non-blocking)

- Addition +
 - Subtraction −
 - Multiplication *
 - Division /
 - Power ** (e.g., $a^{**}b = a^b$)
 - Mod % (e.g., $a \% b = a \bmod b$)

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);  
  
    assign c = a + b;  
  
endmodule
```

- **Some operators in SV**

- Bit-wise

- They can be use in any expression/assignment (also blocking or non-blocking)

- AND &
 - OR |
 - NOT ~

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);  
  
    assign c = a + b;  
  
endmodule
```

- **Some operators in SV**

- Logical

- They can be used in any control condition (if-else, ternary operator)

- AND &&
 - OR ||
 - NOT !

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);  
  
    assign c = a + b;  
  
endmodule
```

- **Some operators in SV**

- Relational
 - They can be used in any control condition (if-else, ternary operator)
- Equality ==
- Inequality !=
- Greater than >
- Greater than or equal >=
- Lower than <
- Lower than or equal <=

Exercise with SystemVerilog

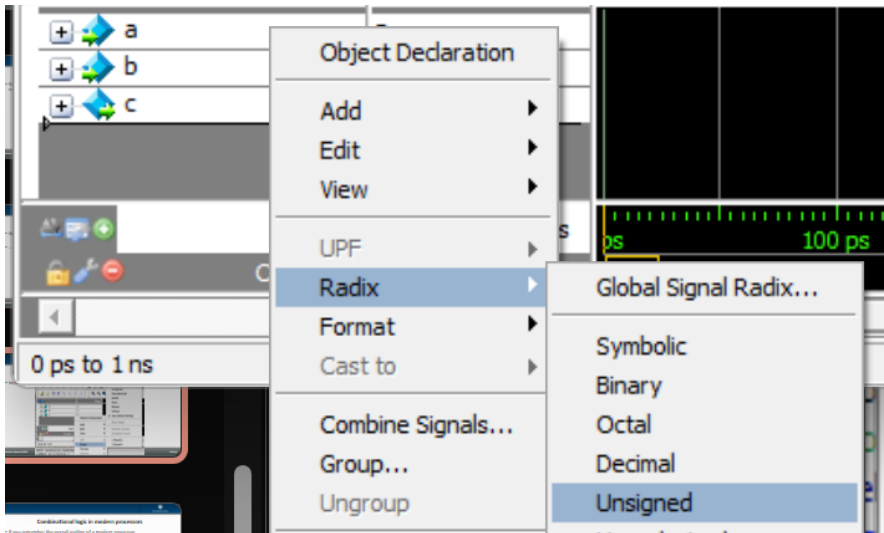
- Implementation of a 4-bit Adder and simulation with Modelsim

```
module adder_4_bit (  
    input  [3:0] a  
    ,input  [3:0] b  
    ,output [3:0] c  
);  
  
    assign c = a + b;  
  
endmodule
```

- Try to simulate it on Modelsim with the **force** and **run** command
 - To assign a multi-bit value with the force command use the syntax for constants in SV
 - force a 4'd0
 - force b 4'd3
 - ...

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim



- Try to simulate it on Modelsim with the **force** and **run** command
 - A suggestion: to plot the waveform, use the Unsigned radix (for a, b, and c)

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim
 - Signed version: supporting two's complement operands

```
module adder_c2_4_bit (  
    input  signed [3:0] a  
    ,input  signed [3:0] b  
    ,output signed [3:0] c  
);
```

```
    assign c = a + b;
```

```
endmodule
```

- Signals must be declared as **signed**
 - By default, all signals are unsigned

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim
 - Signed version: supporting two's complement operands

```
module adder_c2_4_bit (  
    input  signed [3:0] a  
    ,input  signed [3:0] b  
    ,output signed [3:0] c  
);
```

```
    assign c = a + b;
```

```
endmodule
```

- Signals must be declared as **signed**
 - By default, all signals are unsigned
 - It applies to both ports and internal signals

```
// ...  
wire signed [3:0] d;  
reg signed  [7:0] e;  
// ...
```

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim
 - Signed version: supporting two's complement operands

```
module adder_c2_4_bit (  
    input  signed [3:0] a  
    ,input  signed [3:0] b  
    ,output signed [3:0] c  
);
```

```
    assign c = a + b;
```

```
endmodule
```

- Signals must be declared as **signed**
 - By default, all signals are unsigned
 - It applies to both ports and internal signals

```
// ...  
wire signed [3:0] d;  
reg signed   [7:0] e;  
// ...
```

*Signed is declared
AFTER the type.*

- It must be specified after the type

Exercise with SystemVerilog

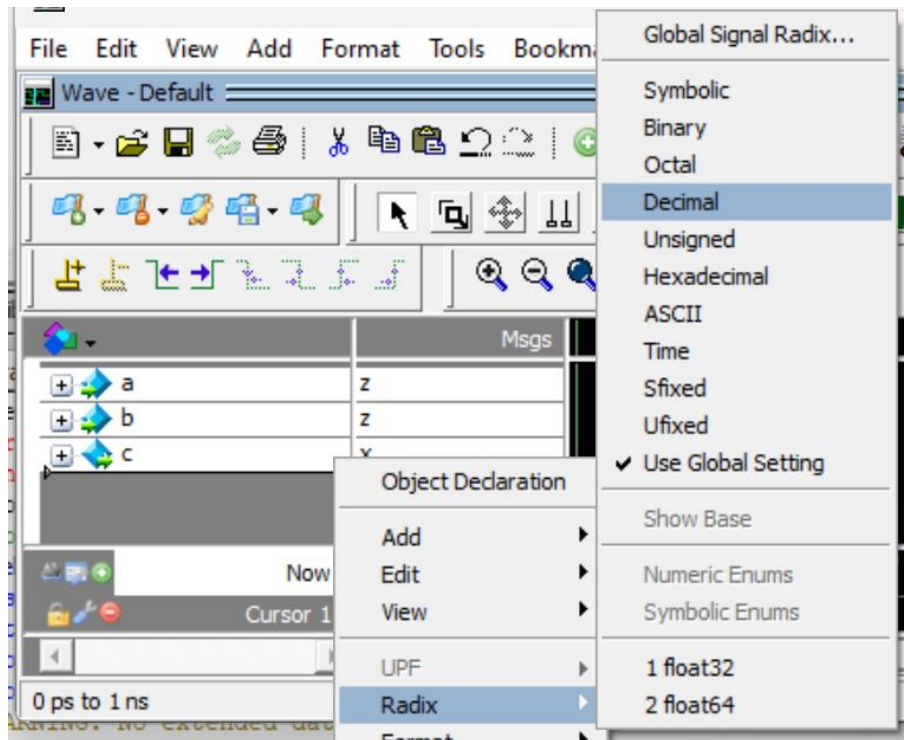
- Implementation of a 4-bit Adder and simulation with Modelsim
 - Signed version: supporting two's complement operands

```
module adder_c2_4_bit (  
    input  signed [3:0] a  
    ,input  signed [3:0] b  
    ,output signed [3:0] c  
);  
  
    assign c = a + b;  
  
endmodule
```

- Try to simulate it on Modelsim with the **force** and **run** command
 - To assign negative value with the force command use ...
 - `force a -4'd1`
 - `force b -4'd3`
 - ...
 - Remember of representable range!!!

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim
 - Signed version: supporting two's complement operands



- Try to simulate it on Modelsim with the **force** and **run** command
 - A suggestion: to plot the waveform, use the Decimal radix (for a, b, and c)

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim
 - You can find all the files about this exercise in the dedicated folder on the Team of the course
 - File > Electronics Systems module > Crocetti > Exercises > 2.2
 - Try to simulate on your own both unsigned and signed version of the 4-bit adder
 - Unsigned version → 'adder_4_bit'
 - Signed version → 'adder_c2_4_bit'

Exercise with SystemVerilog

- Implementation of a 4-bit Adder and simulation with Modelsim
 - For the signed version, you can find 'adder_c2_4_bit' two auxiliary .do files
 - 'wave_adder_c2.do'
 - 'sim_adder_c2.do'
 - Refer to README.txt file
 - However, you can run them using again the Transcript Tab and the **do** command
 - After having launched the simulation

```
VSIM 24> do wave_adder_c2.do  
VSIM 25> do sim_adder_c2.do
```



Thank you for your attention

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