

# Stream Ciphers

Gianluca Dini

Dept. of Ingegneria dell'Informazione

University of Pisa

Email: [gianluca.dini@unipi.it](mailto:gianluca.dini@unipi.it)

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*Can we modify OTP to make it practical?*

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## STREAM CIPHERS

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## Making OTP practical (1/3)



- Instead of generating the key I could have a pseudo random generator
- Idea: replace the random key stream by a **pseudo-random key stream**
- Pseudo Random Generator **G** is an efficient and deterministic function

$$G : \{0,1\}^s \rightarrow \{0,1\}^n, n \gg s$$

Seed space                      Key-stream space

The key stream is computed from a seed

I have a small seed and function G gives me a long key as needed, called key stream.

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- 3 Intuition: for different messages I use different parts of the stream.

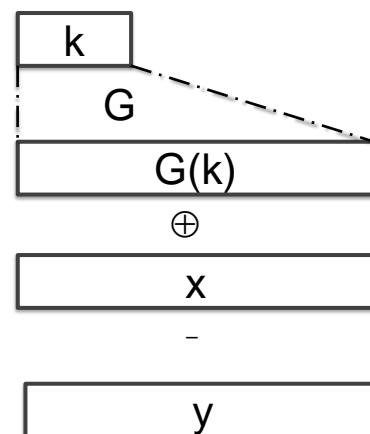
## Making OTP practical (2/3)



Encryption:  $y = G(k) \oplus x$

Decryption:  $x = G(k) \oplus y$

- Key  $k$  is a small secret (e.g., 100 bits)
- $G$  is pseudo-random so sender & receiver generate the same key stream



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## Making OTP practical (3/3)



- Is OTP-modified (stream cipher) still perfect?
  - NO!
    - $\#keys < \#msg \rightarrow$  Shannon's theorem is violated
  - We need a new definition of security!
- Security will depend on the specific PRG
  - PRG must look random, i.e., indistinguishable from a TRG for a limited adversary [We don't want impossible, just difficult]
    - It must be computationally unfeasible to distinguish PRNG output from a TRG output
  - Computational security (a new definition of security)

This will be considered secure (from a different pov) provided that the generation looks random. We need an output that cannot be distinguished by a true random output

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From your standpoint

## Computational security



- A new definition of security
- A cipher is computationally (practically) secure if the perceived level of computation required to defeat it, using the best attack known, exceeds, by a comfortable margin, the computation resources of the hypothesized adversary [LIMITED ADVERSARY] [WE ASSUME TO KNOW THE BEST KNOWN ATTACK]
- Now, the adversary is assumed to have a limited computation power

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## Computational security



- What is the best known attack?
- Even if a lower bound on the complexity of one attack is known, we don't know whether any other, more powerful attacks, are possible
- The best we can do is to design cryptosystem for which it is assumed that they are computationally secure

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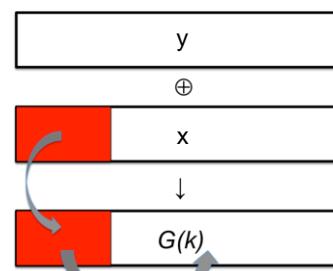
### 8 PROPERTIES A PRG MUST FOLLOW:

- THEY NEED VERY GOOD STATISTICS: They should produce a sequence of bits in which the # of 0s and 1s is approx the same, same for 00, 01, 10, 11 etc.
- THEY NEED TO BE UNPREDICTABLE  
THIS IS WHAT A PRG NEEDS TO LOOK RANDOM

## PRG must be unpredictable



- Not only a PRG must have good statistics, it must be also unpredictable
- If PRG is predictable, a stream cipher is not secure!
  - Assume an adversary can determine a prefix of  $x$  then
  - Then, (s)he can compute a prefix of the key stream
  - If  $G$  is predictable, (s)he can compute the rest of the key stream and thus decrypt  $y$



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9  $Cyph \oplus plant. = prefix of G(k)$ . If it is predictable, you can get bits of  $G(k)$ .

When we say that a **pseudorandom number generator (PRNG) must have good statistics**, we mean that the numbers it produces should **appear truly random** when analyzed using various statistical tests. Since PRNGs are deterministic algorithms, their output is not truly random, but it should be **indistinguishable from real randomness** for most practical purposes.

Here's what "good statistics" typically involves:

## **1. Uniform Distribution**

Each possible number (or sequence of numbers) should appear with roughly equal probability over a large enough sample. If a PRNG generates numbers between 0 and 255, for example, each number should appear approximately **1/256 of the time**.

## **2. Independence**

# Unpredicability



- Forward unpredictability
  - If the seed is not known, the next output bit of a sequence must be unpredictable regardless of knowledge of any prefix of the sequence
- Backward unpredictability
  - It must not be possible to determine the seed from the knowledge of any generated sequence
- If a sequence is/appears random it is not possible to predict either the next bit(s) or the seed

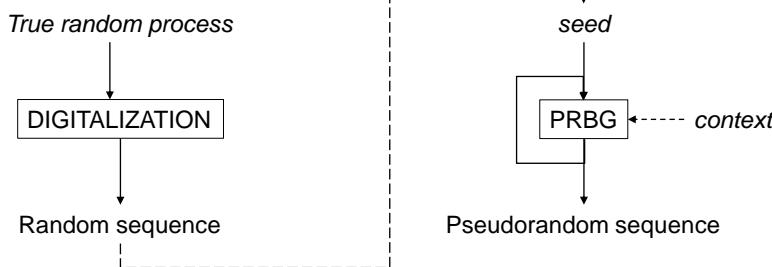
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# TRBG and PRBG



Idea is: I use seed with a PRBG, but how can I generate the seed?

I use a true random generator.

NOTE: adversary can always brute-force the possible seeds. So seeds need to be so large to discourage brute-force attacks.

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## STATE OF THE ART AND CASE STUDIES

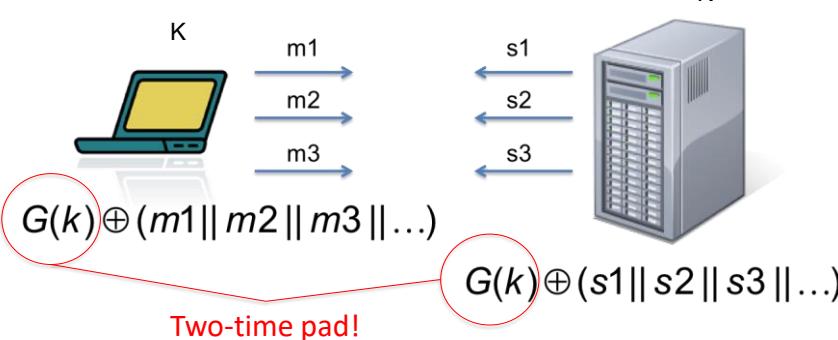
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## MS-PPTP (Windows NT)



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## MS-PPTP (Windows NT)



- The correct way to proceed is  $K = (K_{cs}, K_{sc})$
- $Z_{cs} = G(K_{cs})$ , key stream for encryption client → server
- $Z_{sc} = G(K_{sc})$ , key stream for encryption server → client

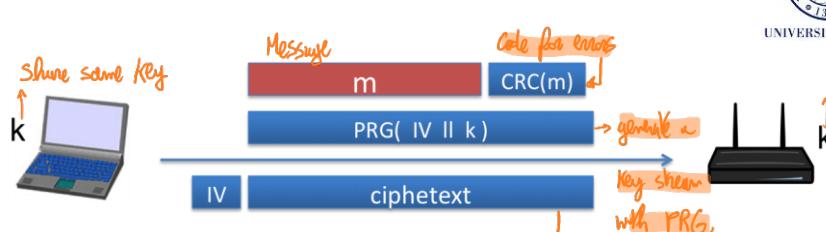
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## STANDARD 802.11b WEP



- A new IV for each new message
  - Key is fixed (104-bits)
  - IV avoids 2TP
- Length of IV: 24 bits (in the standard!)
  - Repeated IV after  $2^{24} \approx 16M$  frames
  - On some 802.11 cards IV resets to 0 after power cycle

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15 An application of stream ciphers is in WiFi WEP.

How to generate seed? Made by 2 quantities: IV (initialization vector) | key

$\downarrow$  24bit       $\downarrow$  Conc.  
104bit  $\rightarrow$  128bits for seed.

\* To avoid 2 TIME PAD: we don't want to reuse twice the same key stream

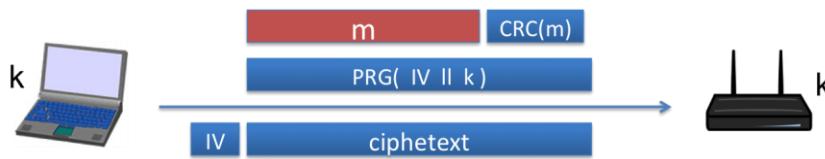
\* I have  $2^{24}$  possible IVs, so 16 million frames. But this is a small traffic.

You can obtain 16M frames even in a network of medium size. Consider the key is shared in the whole network.

When I run out of IVs a full set 2 time pads.

△ IV has to be new for each message. So they implemented it by means of a counter.

## 802.11b WEP



Key for frame #1: 1||k  
 Key for frame #2: 2||k  
 Key for frame #3: 3||k  
 ...

- Related keys, not random
- FMS 2001 attack can recover K in  $10^6$  frames (now 40 Kframes) → 1M frames
- Avoid related keys! → optimised later

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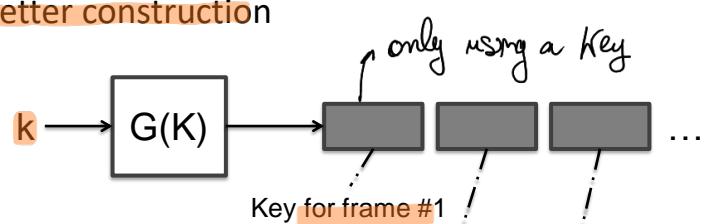
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## 802.11b: WEP



- A better construction



- Each frame has its own key
- Keys are pseudo-random

But here you need a large key.

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- For PRG they used a generator called RC4. Considered quite good but it has some defects. If you use related keys, it becomes predictable.
- Another mistake was using CRC, which is linear with respect to XOR. Cryptosystem is malleable, I could apply modifications on plaintext and CRC to make them match. This was used to modify the destination address of the packet.

## RC4



- RC4 (1987)
  - Used in HTTPS and WEP
  - Variable seed; output: 1 byte
- Weaknesses
  - Bias
    - $\Pr[2\text{nd byte} = 0] = 2/256$  (twice as random)
    - Other bytes are biased too (e.g., 1st, 3rd)
    - It is recommended that the first 256 bytes are ignored
  - $\Pr[00] = 1/256^2 + 1/256^3$ 
    - Bias starts after several gigabytes but it is still a distinguisher
  - Related keys
- It is recommended not to use RC4 but modern CSPRNG

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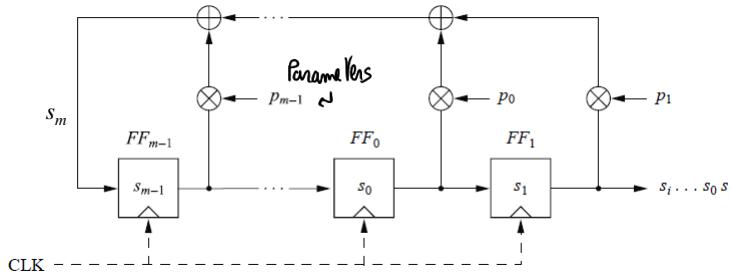
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Way to make pseudo random # gen

## Linear Feedback Shift Register



- $p_i$  = feedback coefficient (If  $p_i == 1$ , the feedback is active; otherwise it is not)



$$s_m \equiv p_{m-1}s_{m-1} + \dots + p_1s_1 + p_0s_0 \pmod{2}$$

$$s_{m+1} \equiv p_{m-1}s_m + \dots + p_1s_2 + p_0s_1 \pmod{2}$$

$$s_{i+m} \equiv \sum_{j=0}^{m-1} p_j \cdot s_{i+j} \pmod{2}, s_i, p_j \in \{0,1\}, i = 0, 1, 2, \dots$$

From a security pov w/r  
is linear, so when you  
have enough points you  
can interpolate

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## LFSR is periodical

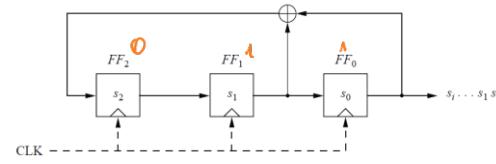


- LFSR
  - Degree: 3
- Sequence of states

clk	FF <sub>2</sub>	FF <sub>1</sub>	FF <sub>0</sub> = s <sub>t</sub>
0	1	0	0
1	0	1	0
2	1	0	1
3	1	1	0
4	1	1	1
5	0	1	1
6	0	0	1
7	1	0	0
8	0	1	0

← The initial state (*seed*)

← The sequence of states is *periodical*



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## LFSR - Properties



- **Properties**
  - **Seed** = initial state of the register
    - All 0's state must be avoided
  - **Degree** = number of storage units
    - Degree = 8
  - **Periodic**
- Maximum-length LFSR
  - **Theorem**
    - The maximum sequence length generated by an LFSR of degree m is  $2^m - 1$
  - Maximum-length LFSR can be easily found

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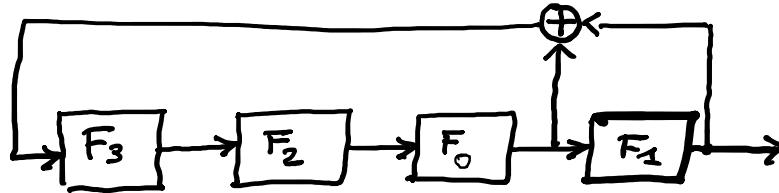
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## LFSR – example #1



- LFSR with maximum output sequence

- Degree  $m = 4$
- Coefficients:  $p_3 = 0, p_2 = 0, p_1 = 1, p_0 = 0$
- Period =  $2^m - 1 = 15$



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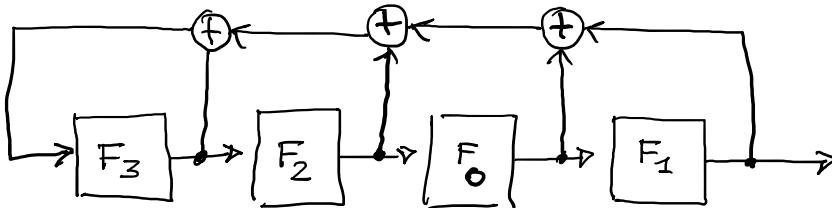
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## LFSR – example #2



- LFSR with non-maximum output sequence

- Degree  $m = 4$
- Coefficients:  $p_3 = 1, p_2 = 1, p_1 = 1, p_0 = 1$
- Period = 5



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## LFSRs are not good for crypto



- Pros:
  - LFSRs have good statistical properties
- Cons
  - Periodical (but any PRNG is periodical)
  - Linear

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## LFSRs are not good for crypto



- Known-Plaintext attack against LFSR
  1. Given  $2m$  pairs  $(pt, ct)$ , the adversary determines a prefix of the sequence  $s_i$ ,
  2. Then, the adversary determines feedback coefficients by solving a system of  $m$  linear equations in  $m$  unknowns
  3. Finally, the adversary can “build” the LFSR and produce the entire sequence

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## LSFRs are not good for crypto



- Have LSFRs to be thrown away?

– Use a non-linear combination of several LFSRs to build strong cryptosystems

• E.g., use AND

– E.g.: Trivium (2003)

Ex: remove XOR and add more

other ops like NAND, NOR etc.

This is good when you don't need unpredictability but random bits  
 If you know a prefix of adequate length you can find the generator

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## State of the art

- Software-oriented
  - RC4 and SEAL
    - Very well-investigated; secure
- Hardware-oriented
  - LFSR-based
    - Many have been broken
  - GSM A5/1 and A5/2
    - A5/1 used to be secret but was reverse-engineered
    - A5/2 has serious flaws
    - Neither of them is recommended nowadays
    - A5/3 (KASUMI) is used but it is a block cipher

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