



Electronics Systems (938II)

Lecture 4.1

Programmable Logic Devices – Principles and PAL

Introduction

- **PLD = Programmable Logic Device**
 - **Programming HW, not SW!**
 - **Configurable logic elements that can implement different circuits**
 - Configuration #1 → circuit/logic function #1
 - Configuration #2 → circuit/logic function #2
 - ...
 - **Not different pieces of HW, but the same piece of HW used in different ways!**

Introduction

- **PLD**

- We have already seen some examples of programmable connections
 - Fuses/anti-fuses
 - MOS transistors
 - ...
- And how to program logic functions?

Principles of programmable logic

- Any combinational logic function can be represented by a Boolean expression
 - Operators
 - $+$ \rightarrow OR (gate)
 - \cdot \rightarrow AND (gate)
 - $-$ \rightarrow NOT (gate)
 - Forms
 - Sum-of-Products (SP)
 - Product-of-Sums (PS)

Principles of programmable logic

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 - **Sum-of-Products (SP)** \rightarrow AND gates feeding an OR gate
 - **Product-of-Sums (PS)**

Principles of programmable logic

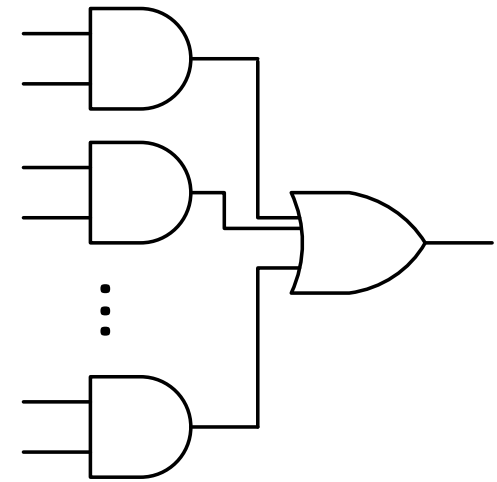
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Principles of programmable logic

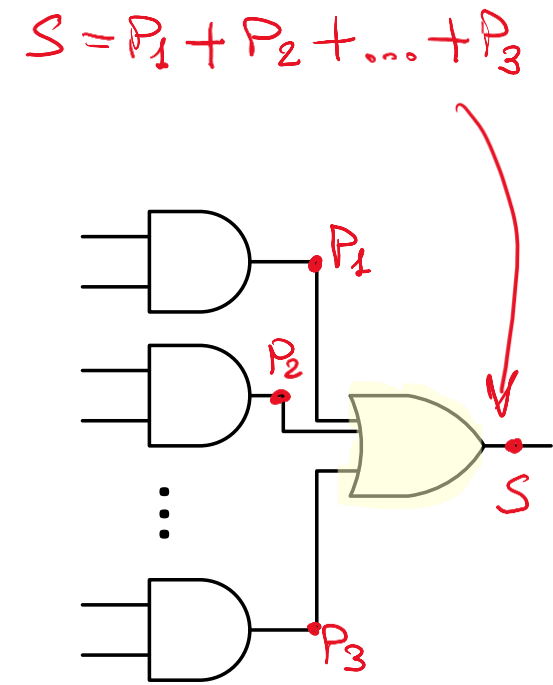
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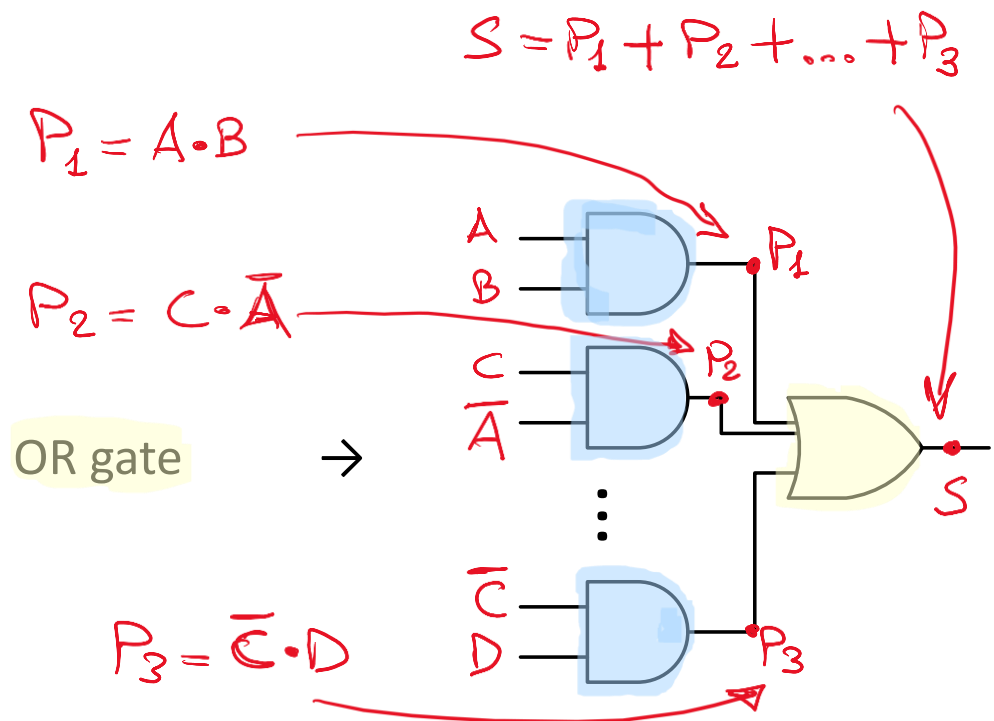
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AND gates feeding an OR gate



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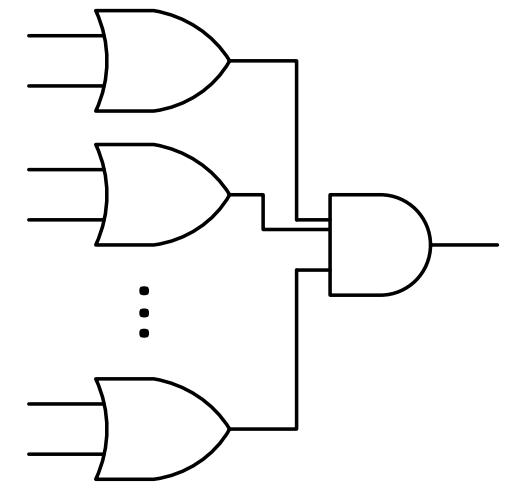
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Principles of programmable logic

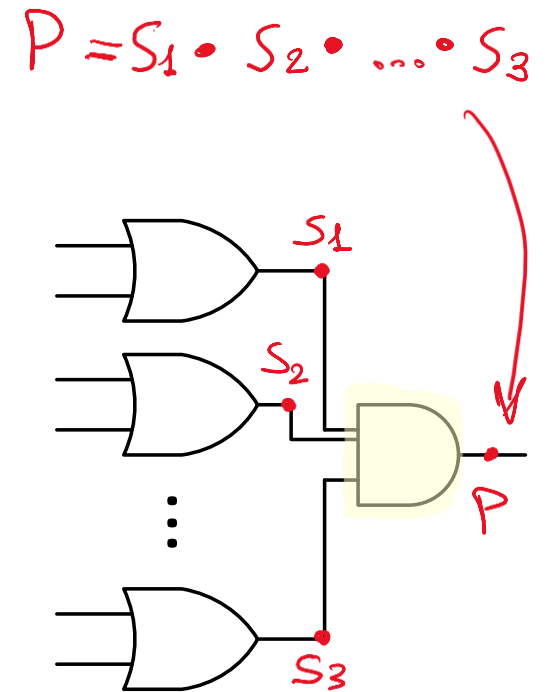
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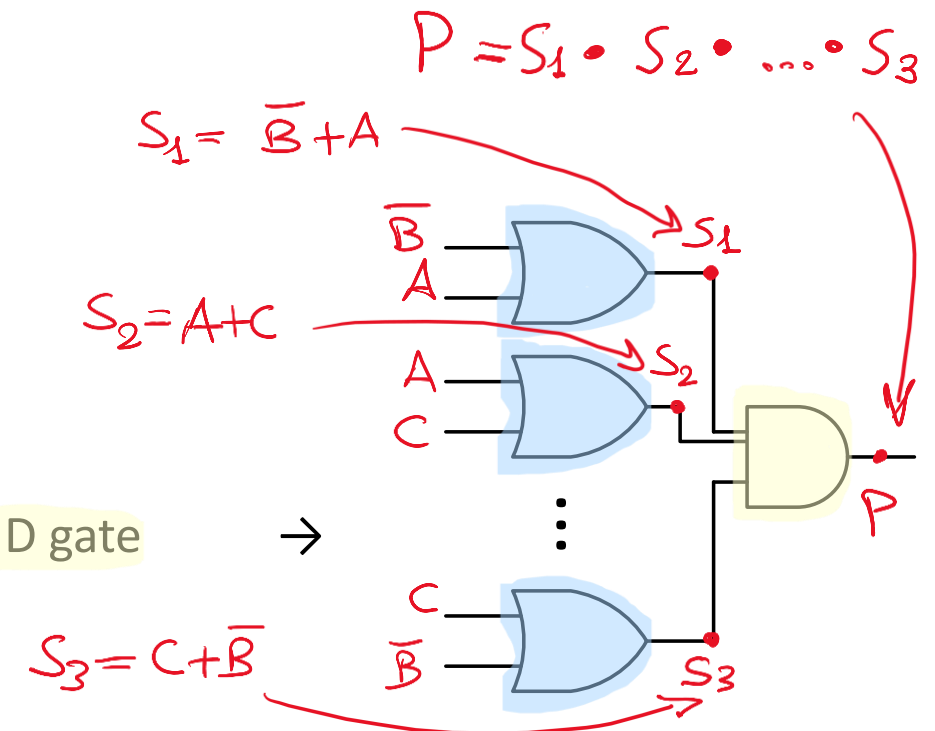
- Forms

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→

OR gates feeding an AND gate

→



Principles of programmable logic

- Example(s)
 - **Karnaugh map** (KM or K-map) = graphical method to express logic functions as SP or PS

Principles of programmable logic

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 - **Karnaugh map (KM or K-map)** = graphical method to express logic functions as SP or PS
 - Showing SP case *Usually associated to active high*

Principles of programmable logic

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 - $f_1(a, b) = a \cdot b$
 - AND gate/function

Principles of programmable logic

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 - $f_1(a, b) = a \cdot b$
 - AND gate/function
 - Truth table \longrightarrow
 - KM

a	b	y
0	0	0
0	1	0
1	0	0
1	1	1

Principles of programmable logic

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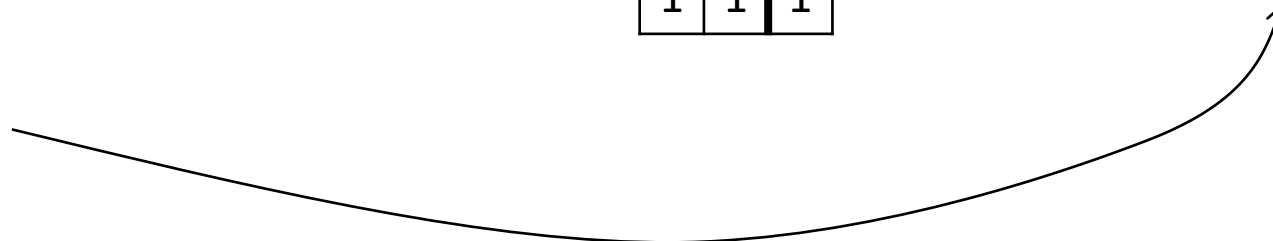
- Truth table

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	b	
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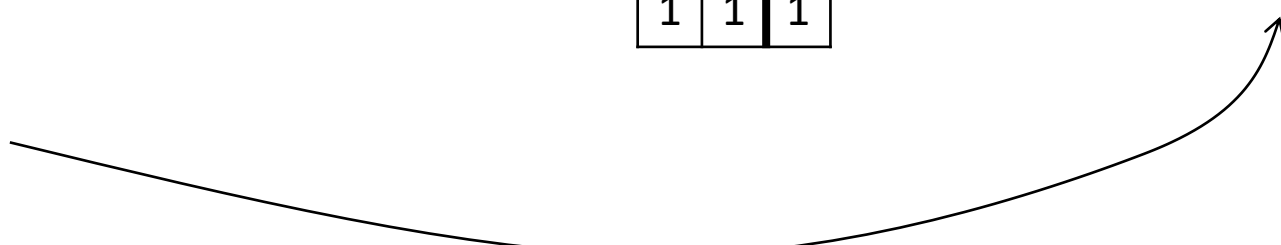
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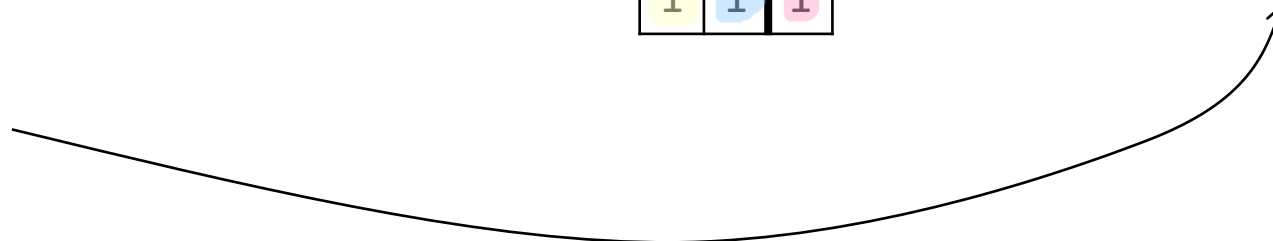
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- How to

1. Find all the largest group(s) of contiguous 1s
2. For each group, select only the inputs whose value does not change
3. Complement surviving inputs whose value is 0
4. Multiply the surviving inputs \rightarrow products P_i
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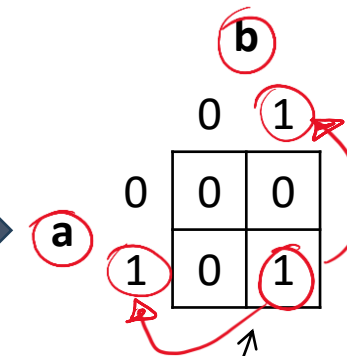
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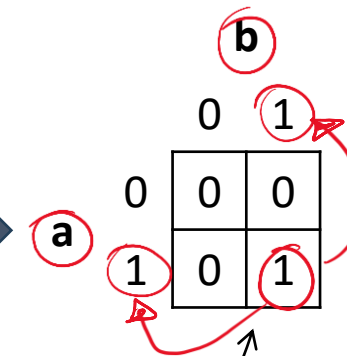
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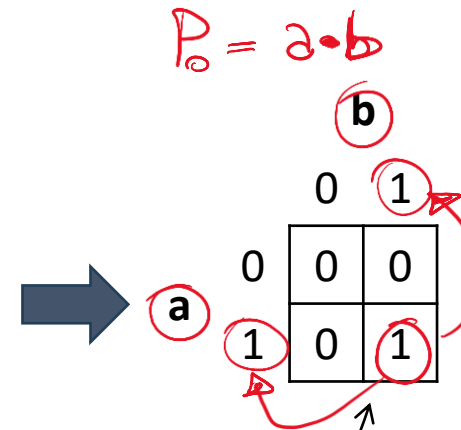
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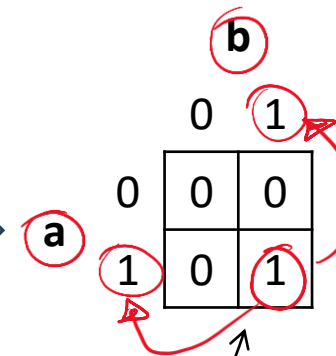
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$$P_0 = a \cdot b$$



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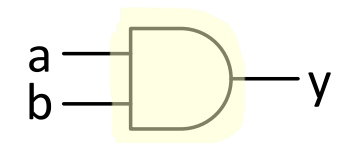
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	b	
	0	1
0	0	0
1	0	1



Logic circuit



- KM

Principles of programmable logic

- Example(s)

- **Karnaugh map (KM or K-map)** = graphical method to express logic functions as SP or PS
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- Example #2

- $f_2(a, b) = ??$

- Truth table

a	b	y
0	0	0
0	1	0
1	0	1
1	1	1

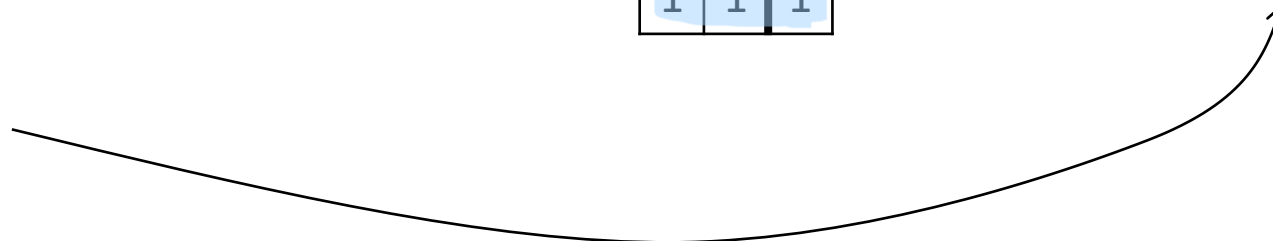


	b	
	0	1
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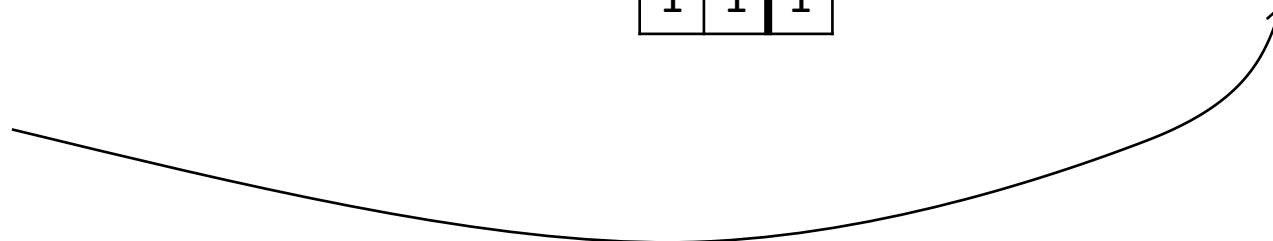


	b	
	0	1
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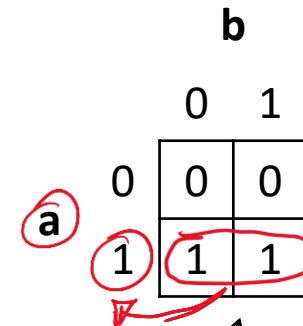
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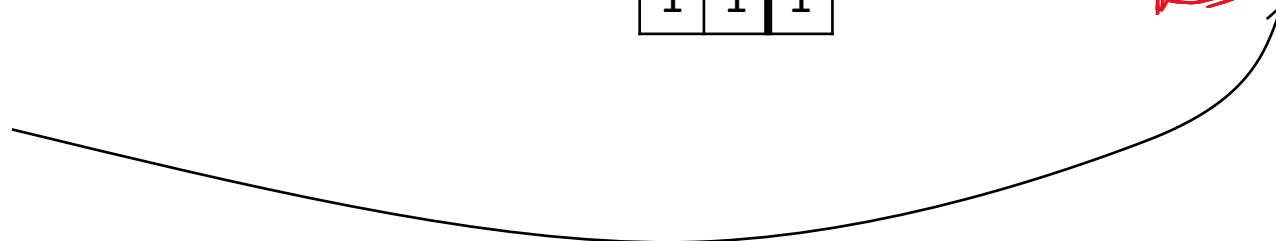
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b

	0	1
0	0	0
1	1	1

Diagram showing the Karnaugh map for the function $f_2(a, b)$. The map is a 2x2 grid with inputs 'a' and 'b' on the axes. The output 'y' is shown in the cells. The cells (1,0) and (1,1) are circled in red, indicating the surviving inputs for the product term a . A red arrow points from the label 'a' to the circled cells.

- KM

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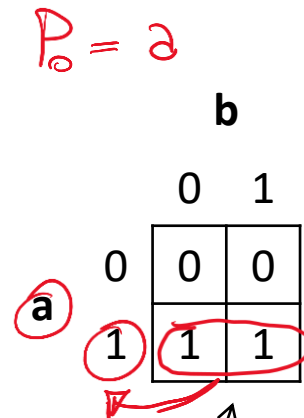
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- Example #2

- $f_2(a, b) = ??$

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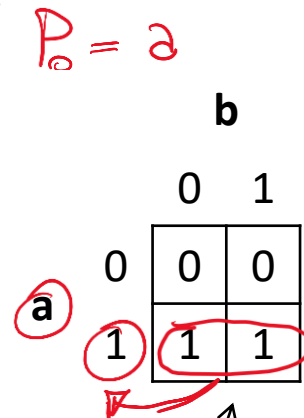
- Example #2

- $f_2(a, b) = a$

- Truth table

a	b	y
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- KM



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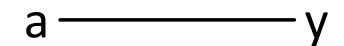
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	b	
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Logic circuit



- KM

Principles of programmable logic

- Example(s)

- **Karnaugh map (KM or K-map)** = graphical method to express logic functions as SP or PS
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- Example #3

- $f_3(a, b) = ??$

- Truth table

a	b	y
0	0	1
0	1	1
1	0	0
1	1	0



	b	
	0	1
0	1	1
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- KM

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1	1	0

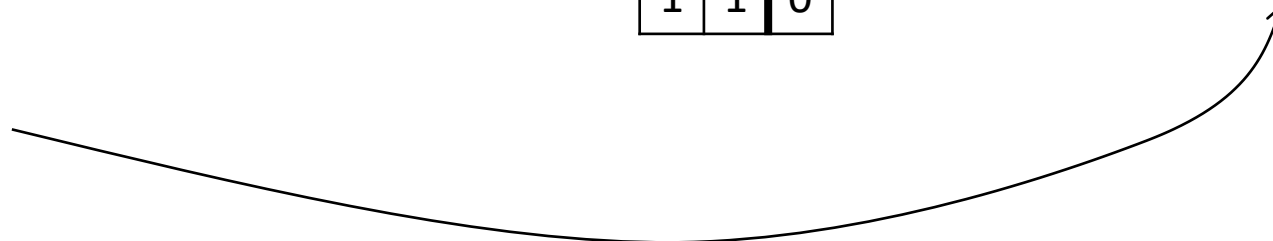


	b	
	0	1
0	1	1
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- How to

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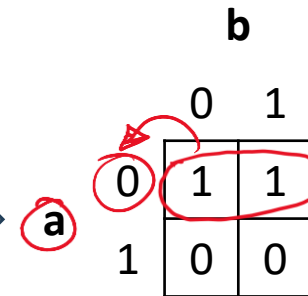
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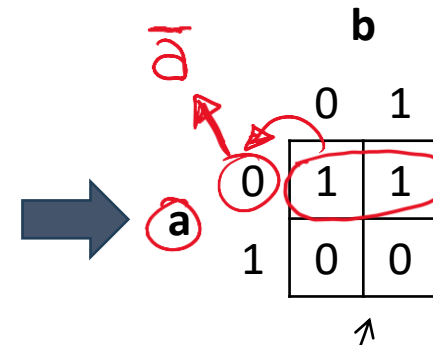
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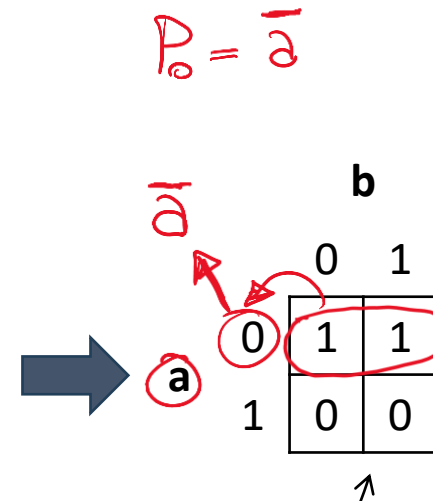
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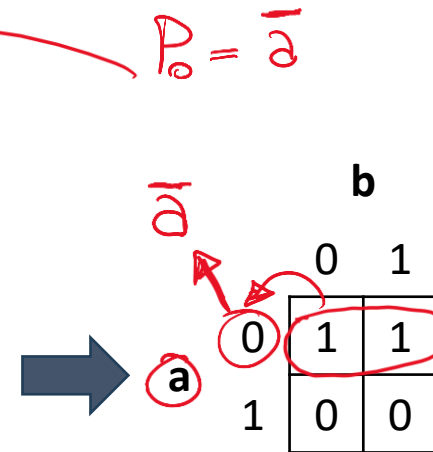
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- $f_3(a, b) = \bar{a}$

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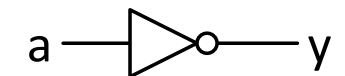
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	b	
	0	1
0	1	1
1	0	0



Logic circuit



- KM

Principles of programmable logic

- Example(s)

- **Karnaugh map (KM or K-map)** = graphical method to express logic functions as SP or PS
 - Showing SP case

- Example #4

- $f_4(a, b) = ??$

- Truth table

a	b	y
0	0	1
0	1	1
1	0	0
1	1	1



	b	
	0	1
0	1	1
1	0	1

- KM

- How to

1. Find all the largest group(s) of contiguous 1s
2. For each group, select only the inputs whose value does not change
3. Complement surviving inputs whose value is 0
4. Multiply the surviving inputs \rightarrow products P_i
5. Sum the products

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b

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0	1	1
1	0	1

a

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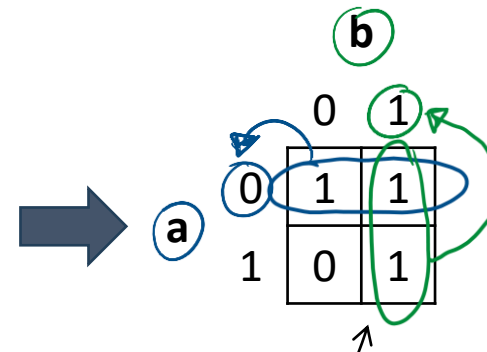
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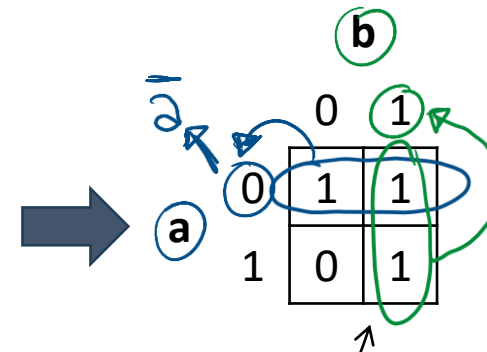
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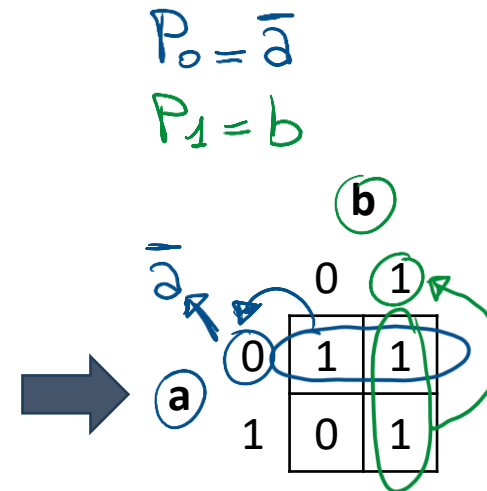
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Principles of programmable logic

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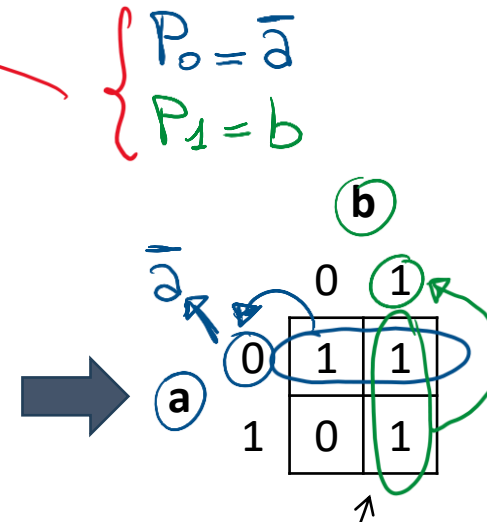
- Example #4

- $f_4(a, b) = \bar{a} + b$

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a	b	y
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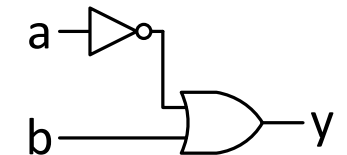
a	b	y
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0	1	1
1	0	0
1	1	1



	b	
	0	1
0	1	1
1	0	1



Logic circuit



- KM

Principles of programmable logic

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- **Karnaugh map (KM or K-map)** = graphical method to express logic functions as SP or PS

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- $f_5(a, b) = ??$

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0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1



		bc			
		00	01	11	10
a	0	0	1	1	0
	1	0	0	1	0

Gray code:
only one bit
must change
between two
adjacent values

- KM

Principles of programmable logic

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0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1



			<u>$b\bar{c}$</u>	
	00	0 <u>1</u>	<u>1<u>1</u></u>	10
<u>a</u> 0	0	1	1	0
1	0	0	1	0

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0	1	1	1
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1	0	1	0
1	1	0	0
1	1	1	1



		00	01	11	10
0	a	0	1	1	0
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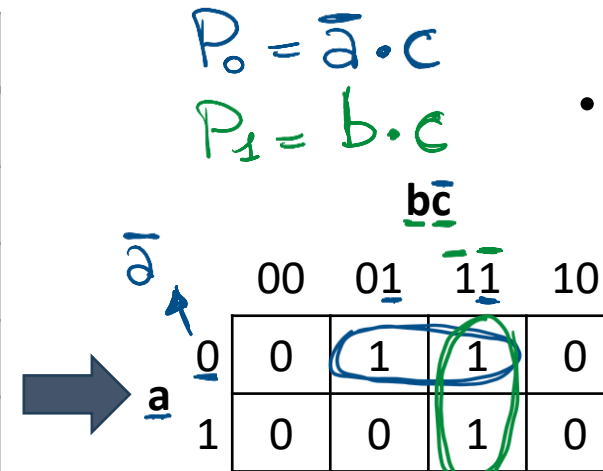
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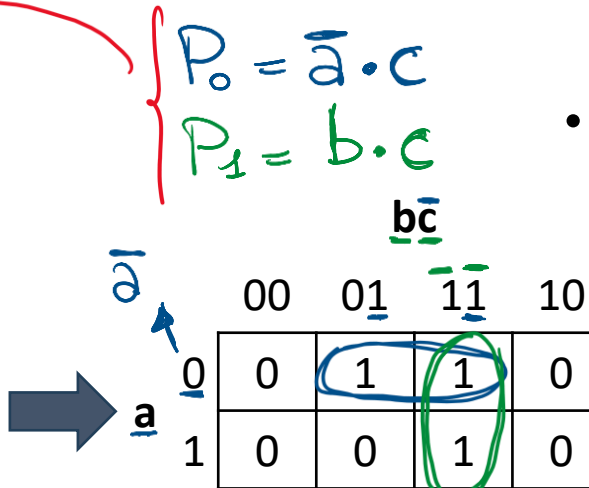
- Example #5

- $f_5(a, b) = (\bar{a} \cdot c) + (b \cdot c)$

- Truth table

a	b	c	y
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

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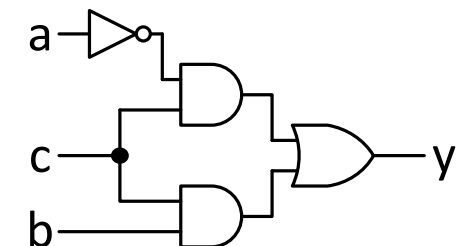
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a	b	c	y
0	0	0	0
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0	1	0	0
0	1	1	1
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		bc			
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a	0	0	1	1	0
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Logic circuit

Principles of programmable logic

- Example(s)
 - Karnaugh map (KM or K-map) = graphical method to express logic functions as SP or PS
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 - Similar approach can be used for PS
 - However, the goal is not to learn how to use Karnaugh maps, but ...

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 - However, the goal is not to learn how to use Karnaugh maps, but ...
- ... demonstrating that

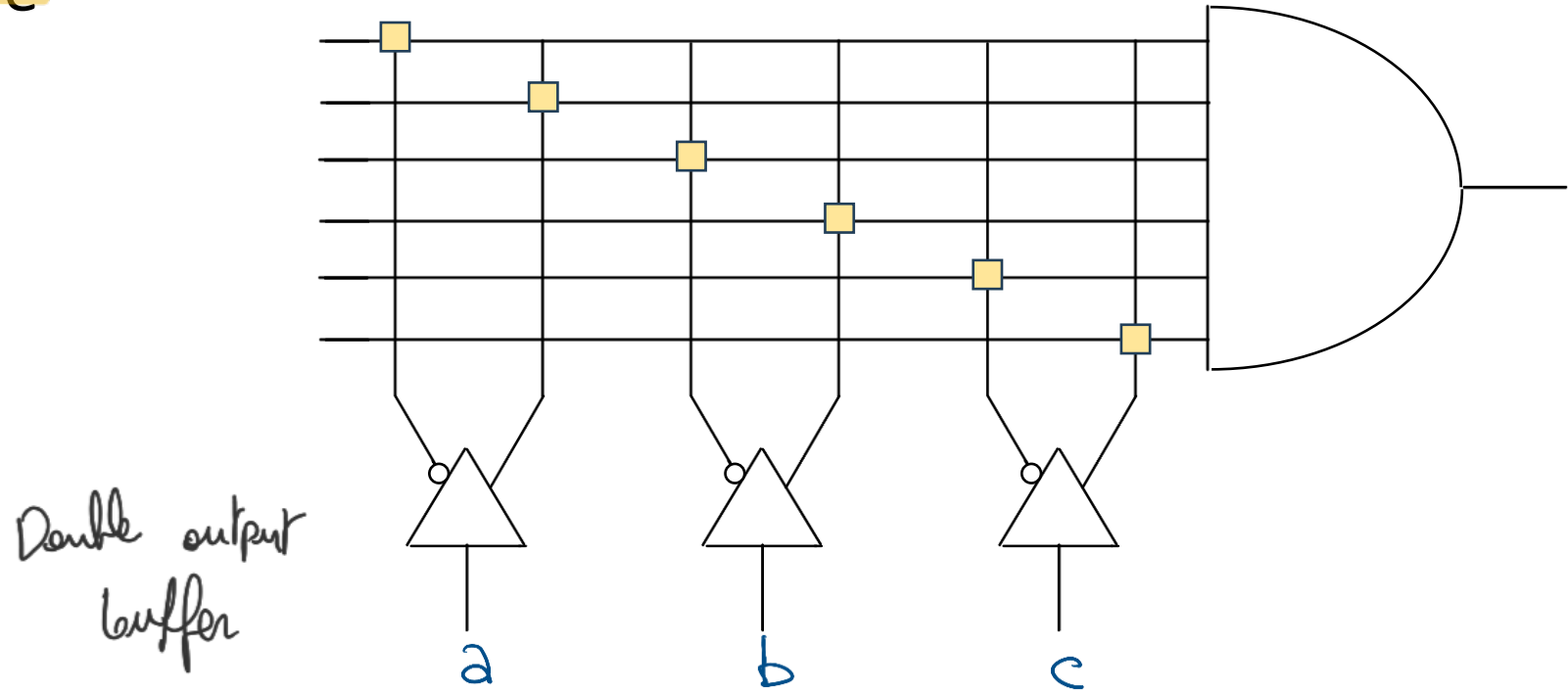
any logic function can be implemented as a network of AND and OR (and NOT) gates!

PAL

- Earliest PLDs were called Programmable Array Logic (PAL)
 - Programmable network of OR, AND, and NOT gates
 - Pre-defined network
 - Programmable connections among gates
 - PROM to program (and re-program) connections

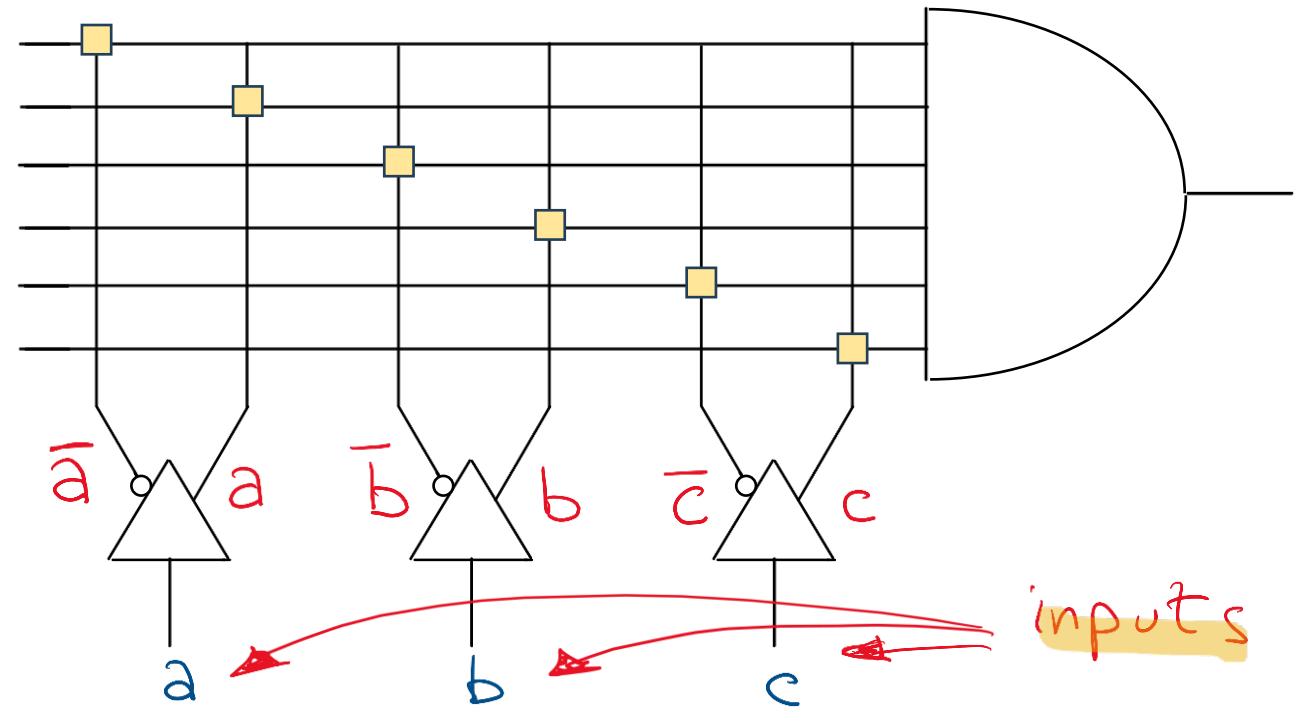
PAL

- Architecture outline



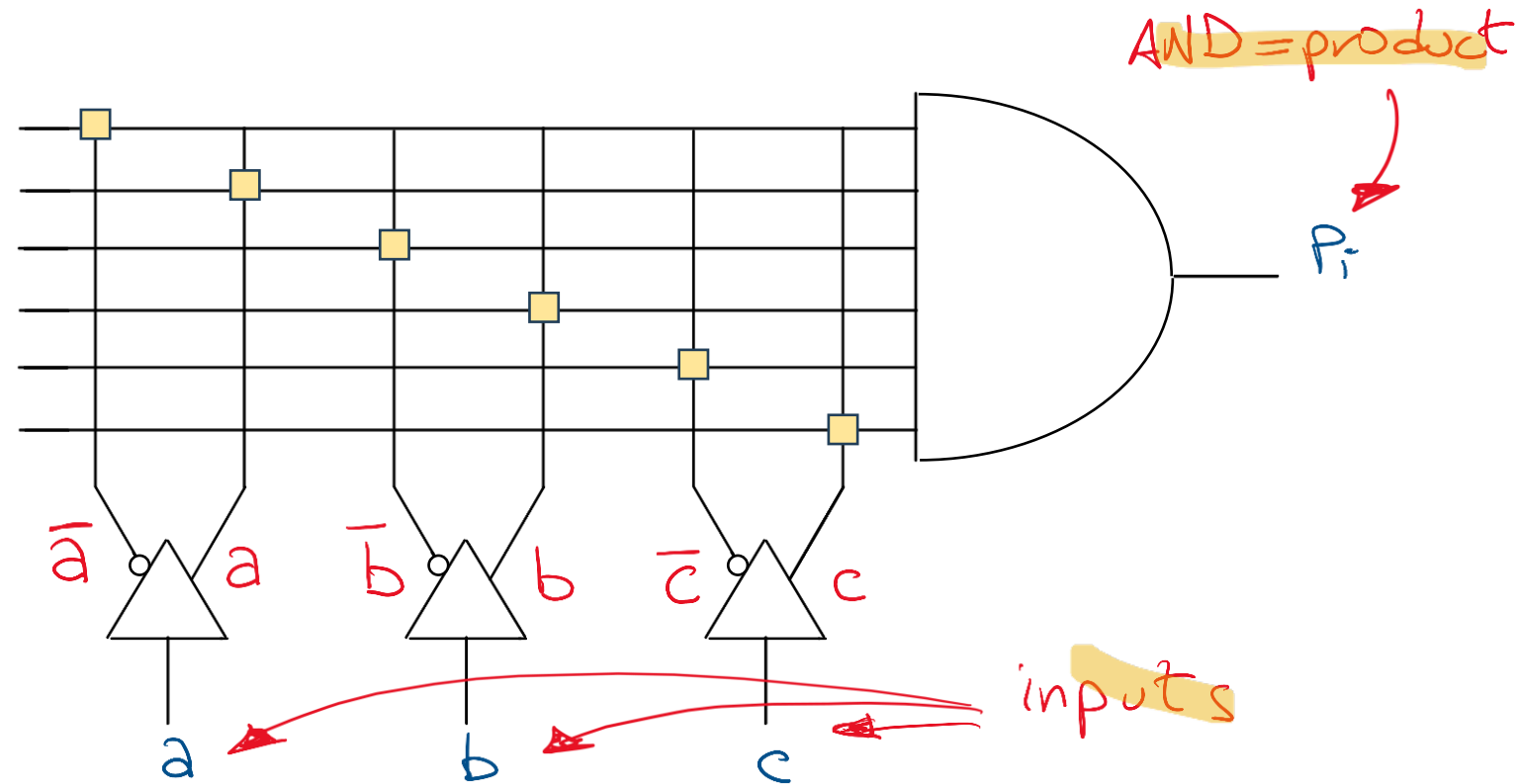
PAL

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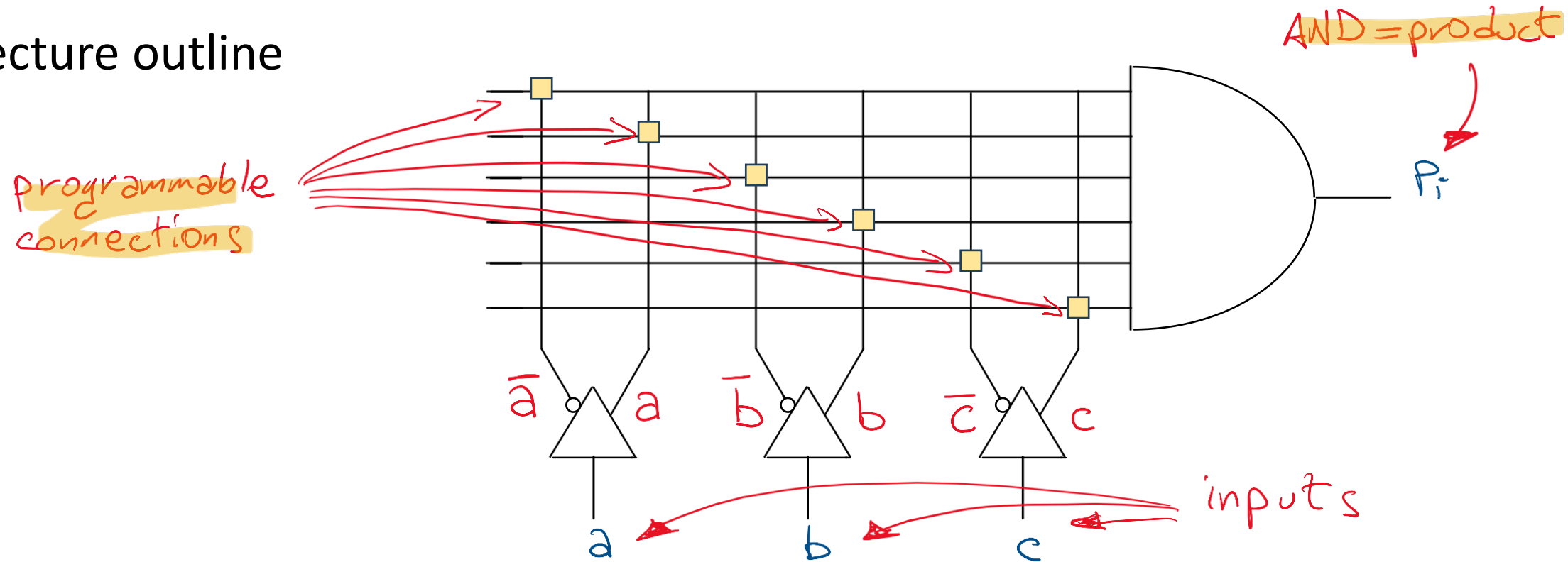
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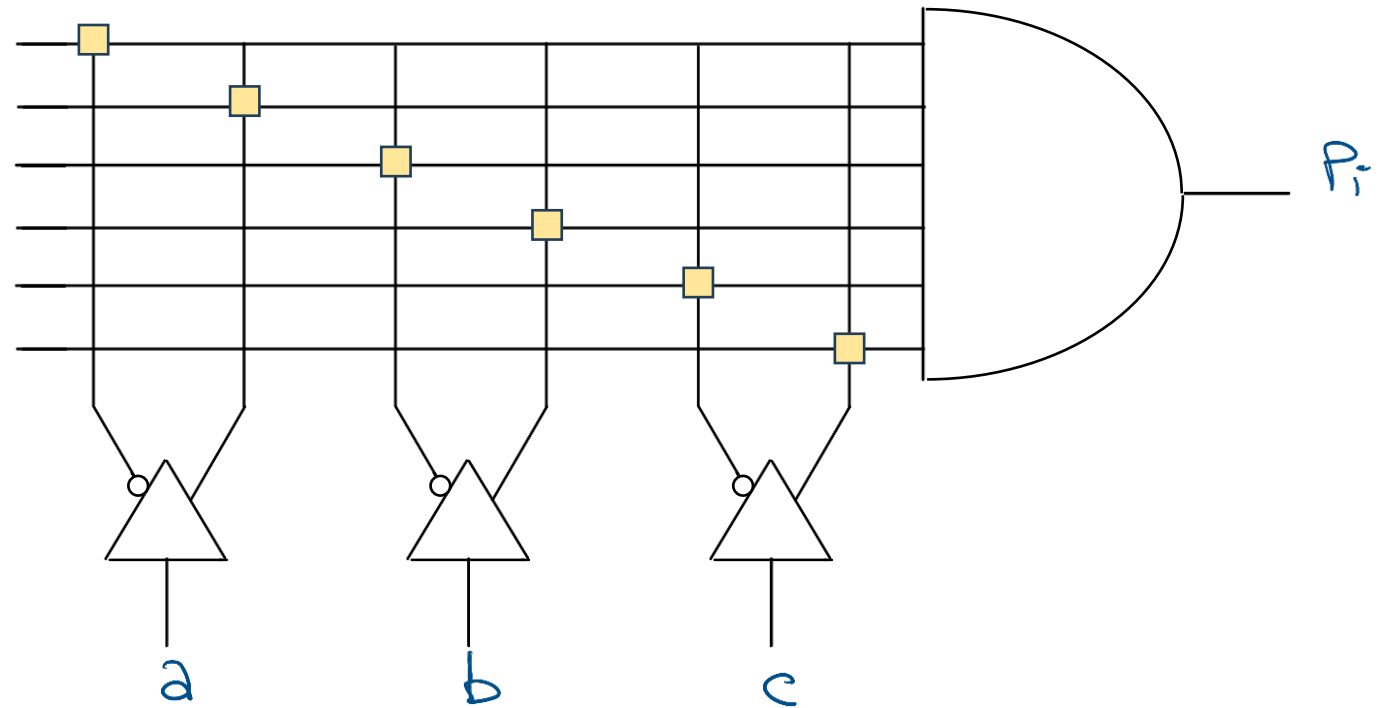
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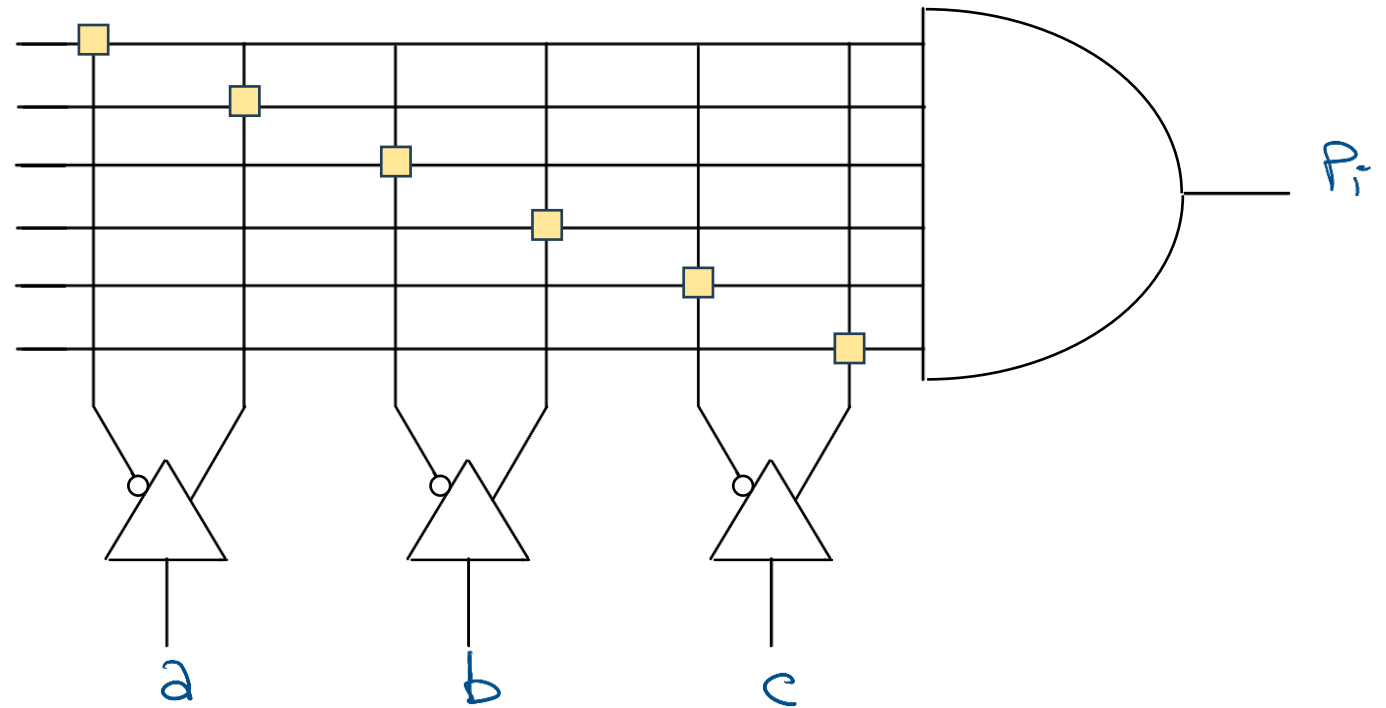
- Architecture outline
 - Do you see familiarity with previous examples?



PAL

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 - Do you see familiarity with previous examples?
 - Recalling example #5

$$- f_5(a, b) = (\bar{a} \cdot c) + (b \cdot c)$$



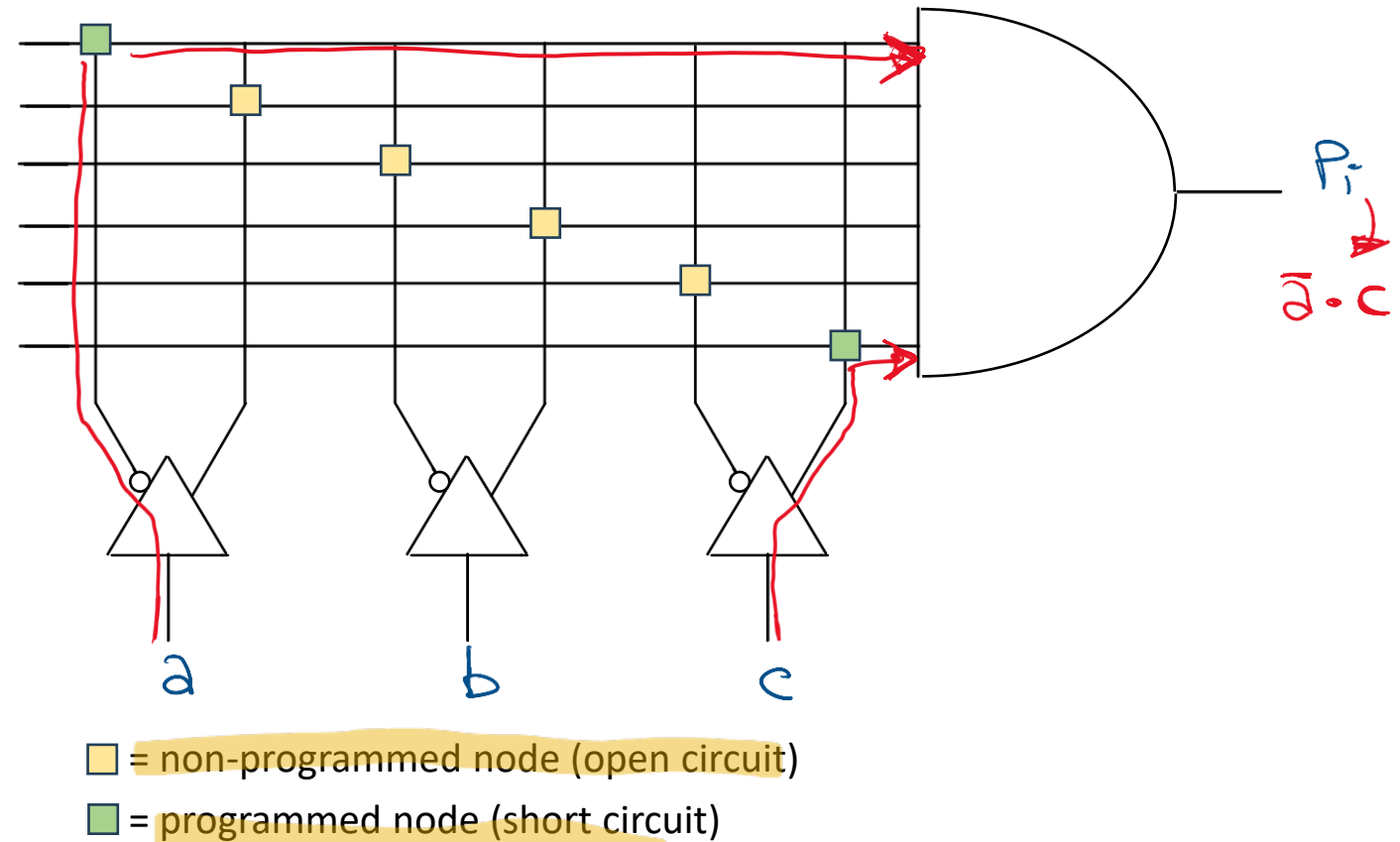
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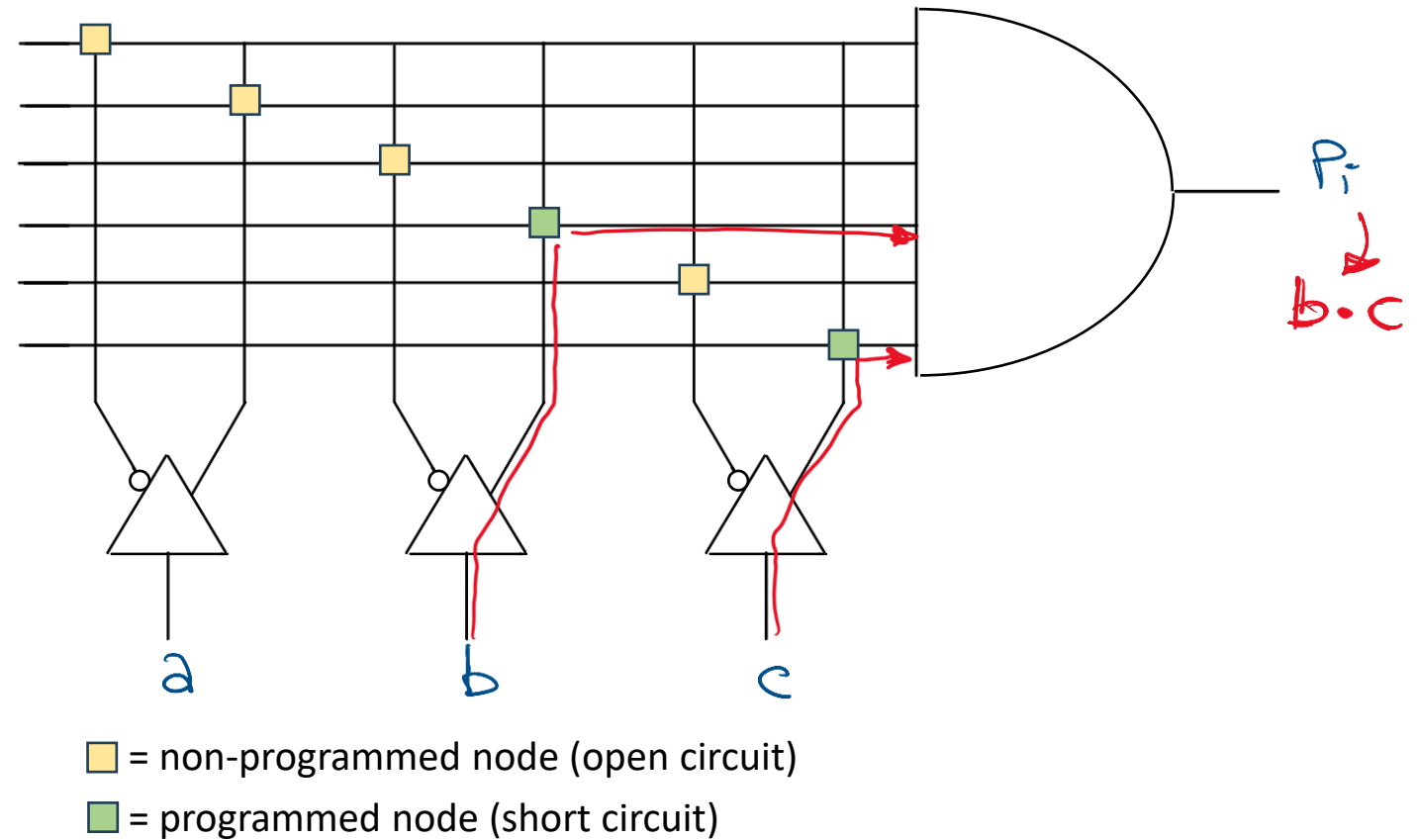
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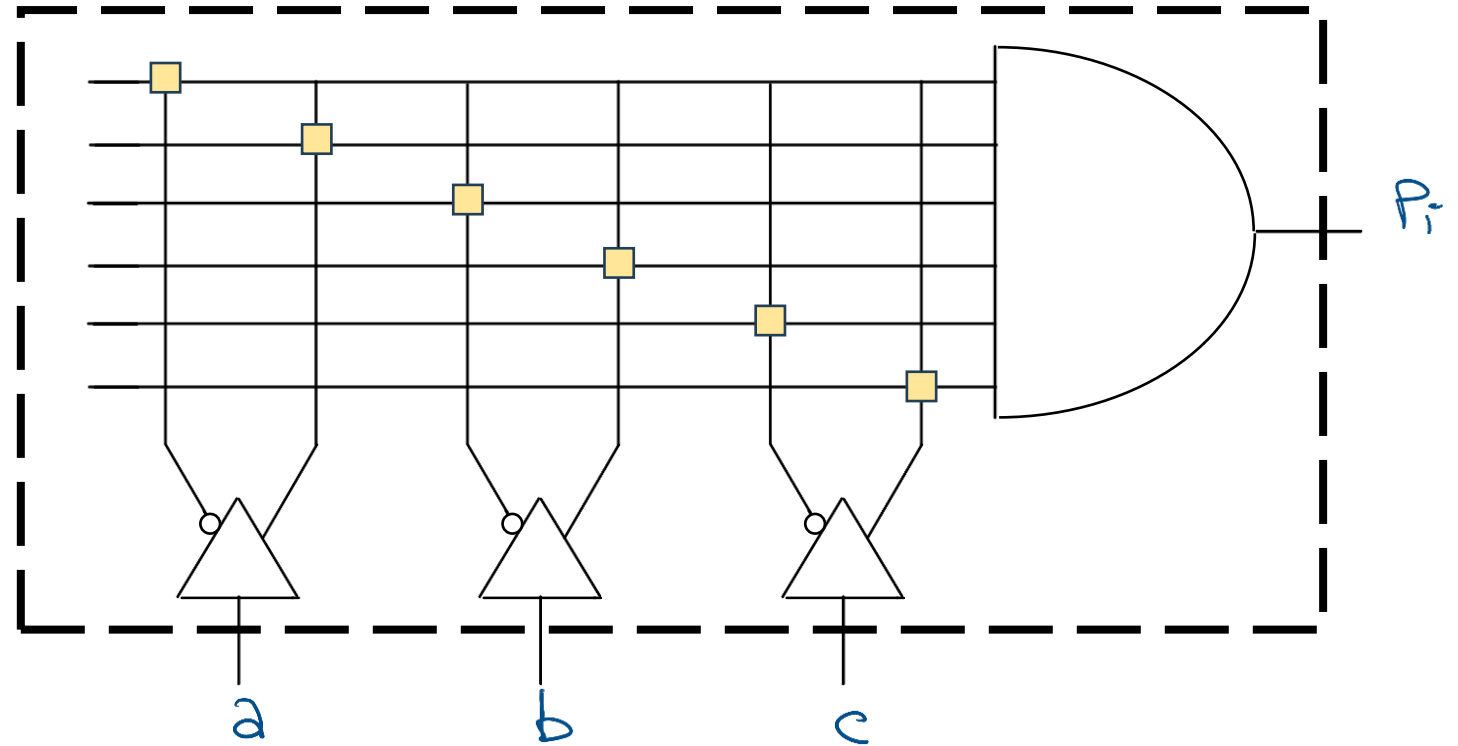
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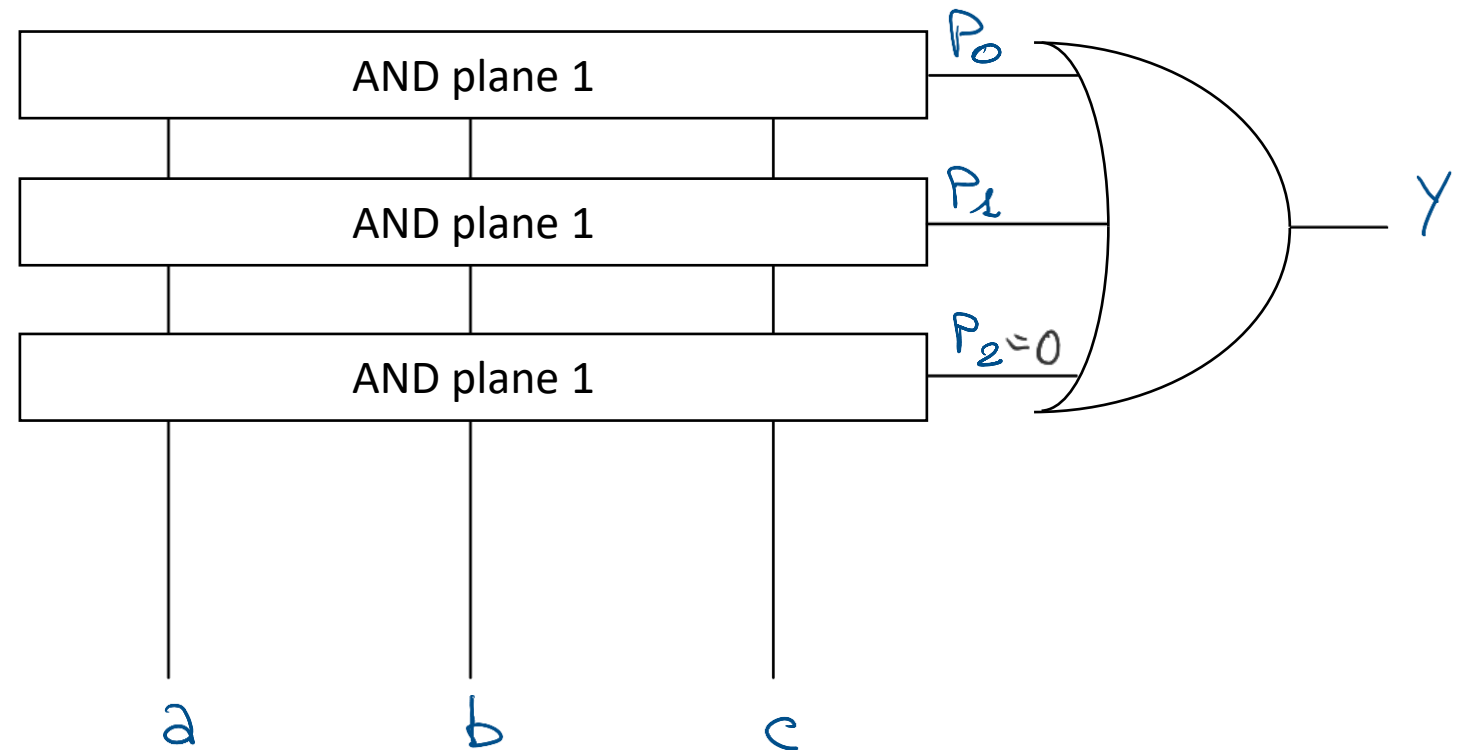
PAL

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 - AND plane



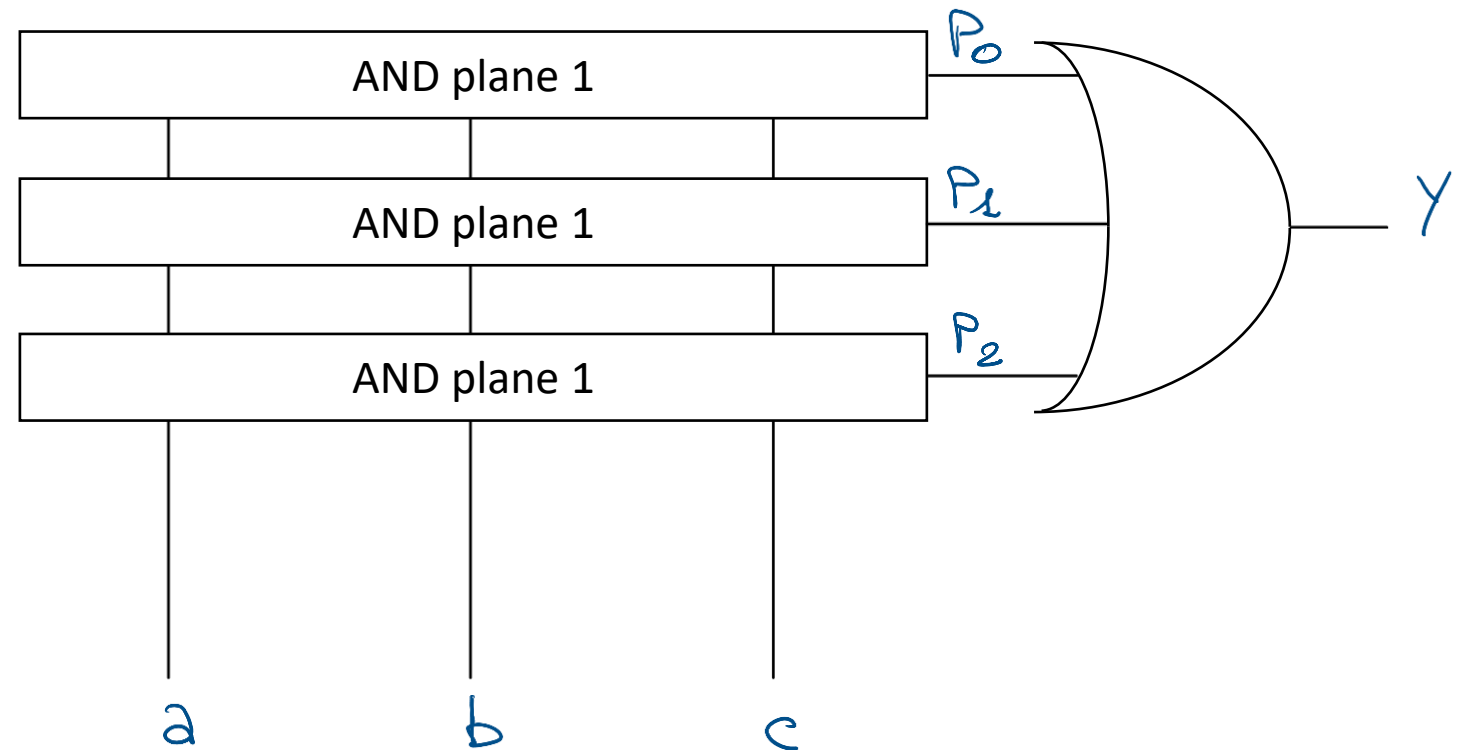
PAL

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PAL

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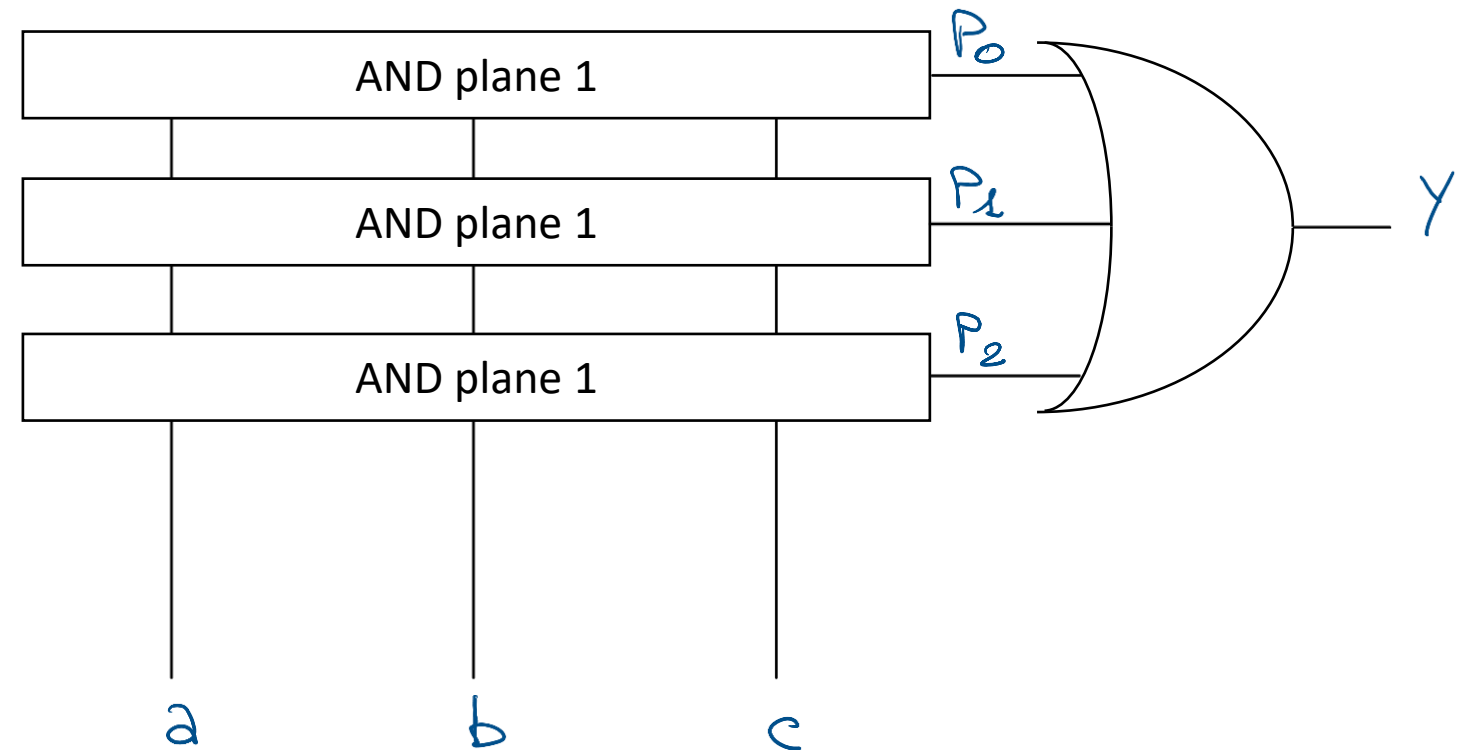
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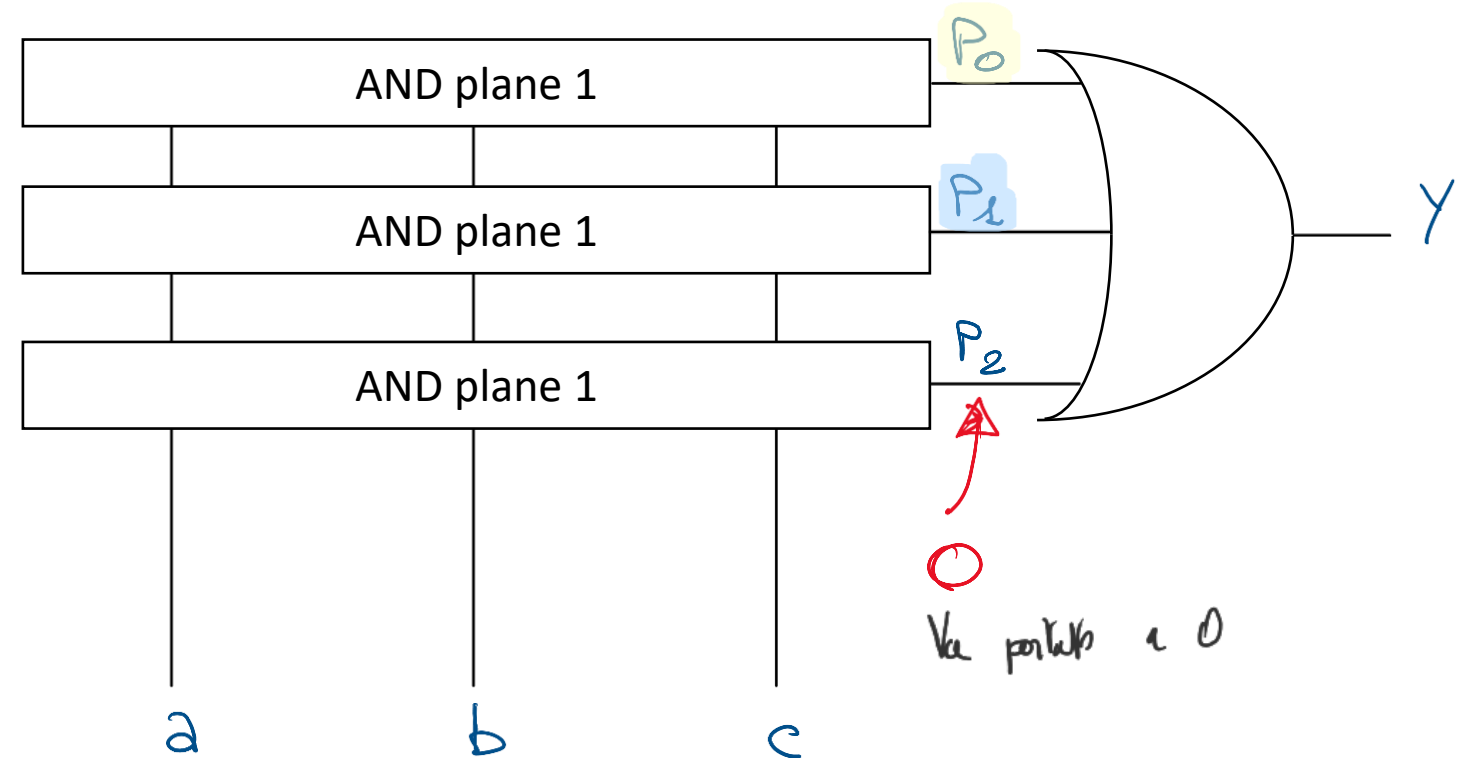
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$$f_5(a, b) = \underbrace{(\bar{a} \cdot c)}_{P_0} + \underbrace{(b \cdot c)}_{P_1}$$



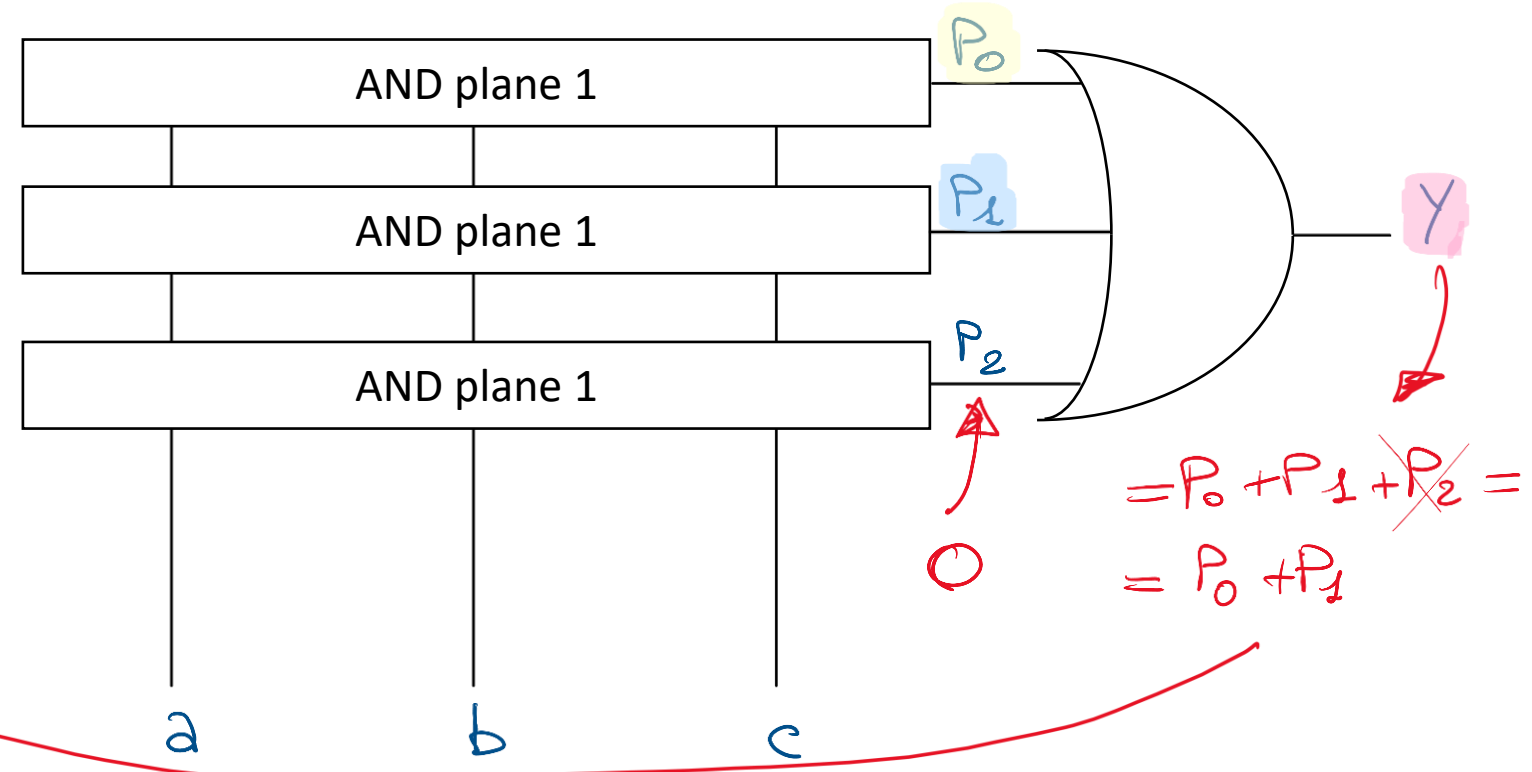
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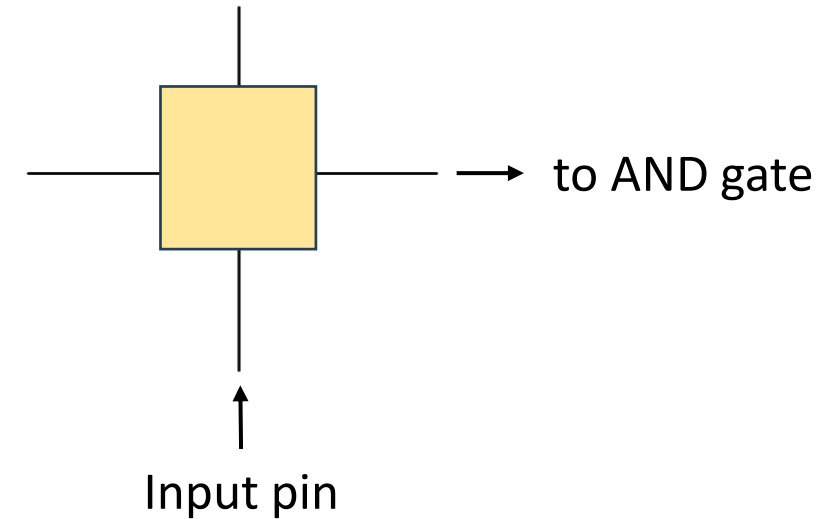
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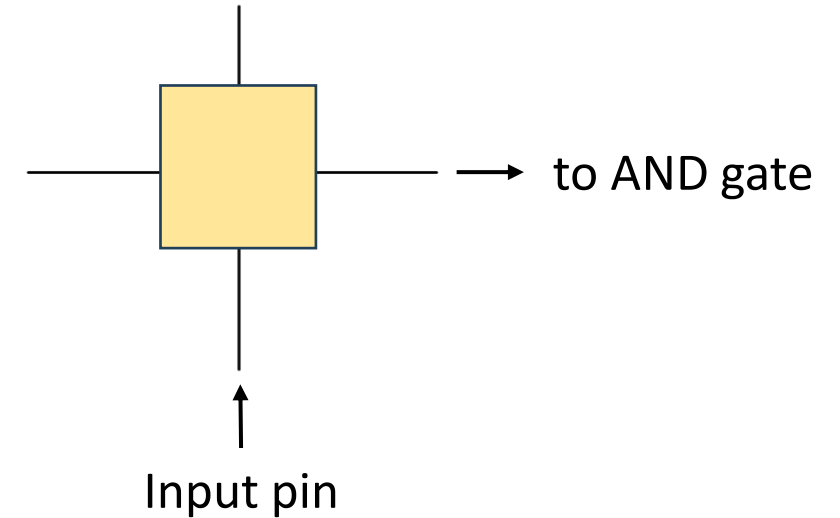
PAL

- Programmable connection(s)
 - Connecting input to AND gate
 - Determining the type of PAL/PLD
 - **OTP = One-Time Programmable**
 - Fuse/Anti-fuse
 - **Reprogrammable**
 - UV-EPROM style (FAMOS)
 - Flash memory style (Flash transistor)



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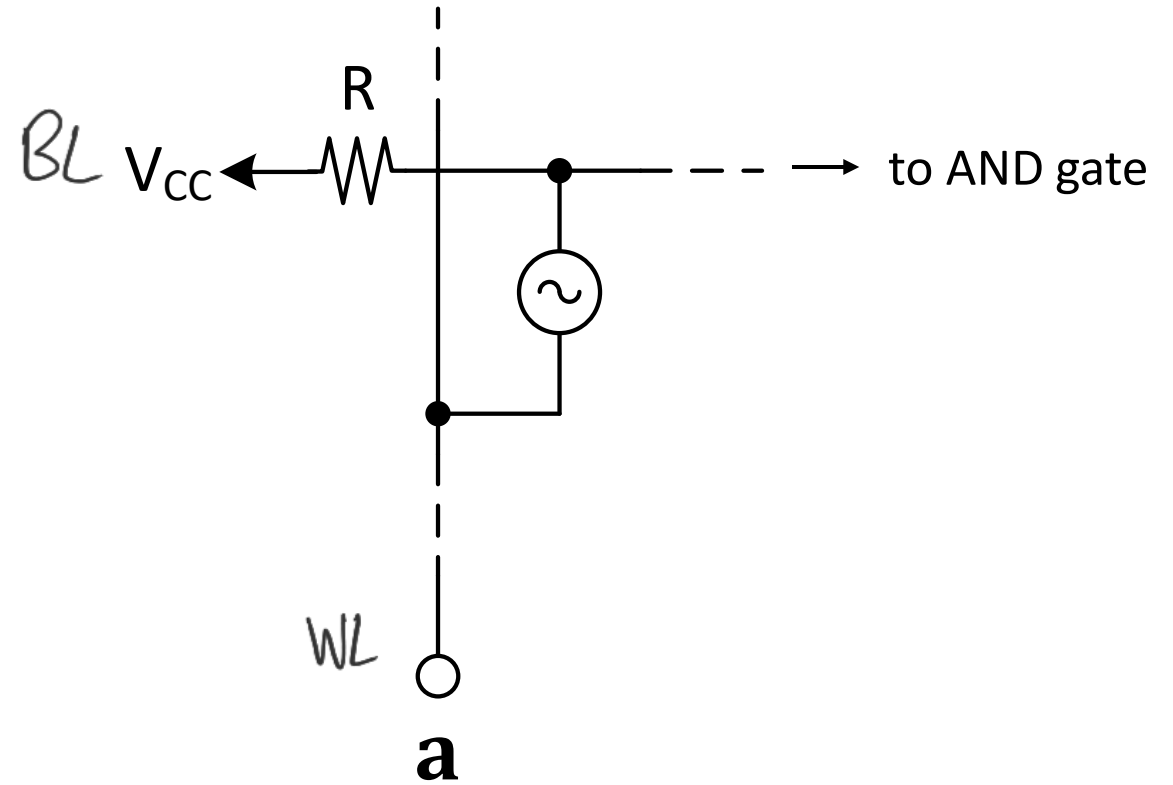


Similar to memory (ROM):

- Word Line = input pin
- Bit Line = AND gate input

PAL

- OTP PAL
 - Fuse

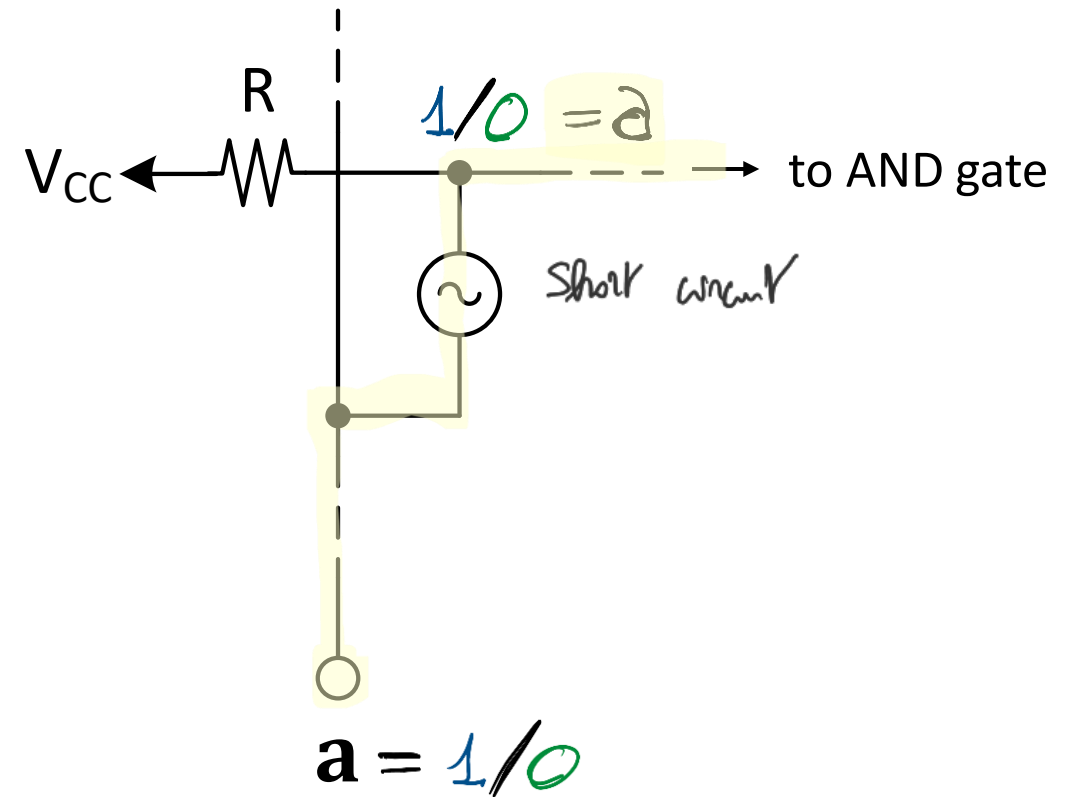


PAL

- OTP PAL

- Fuse

- Default (Fuse not vaporized)
 - Input pin (a) connected to the AND gate

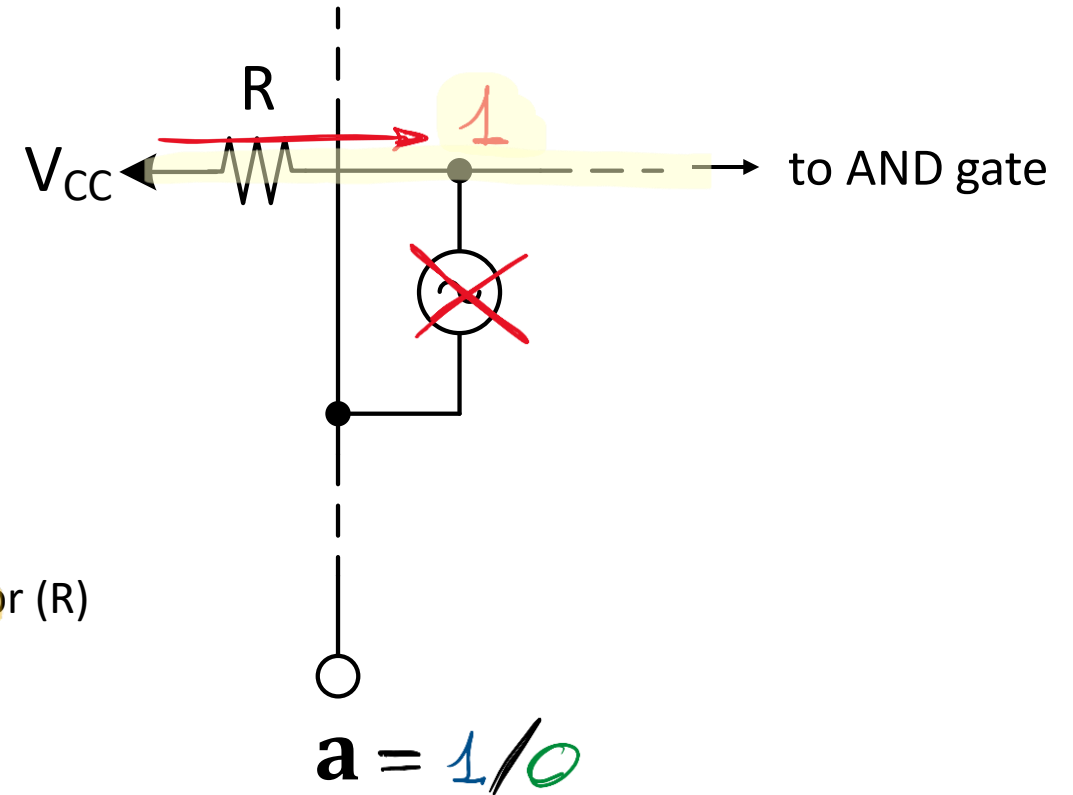


PAL

- OTP PAL

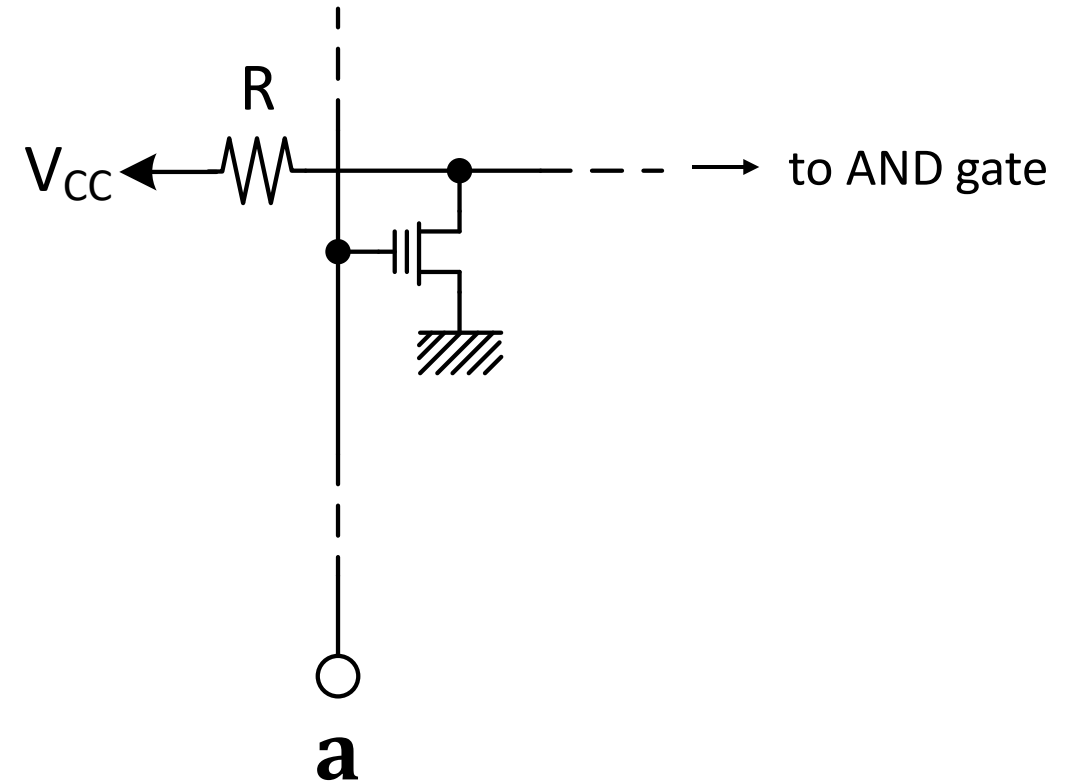
- Fuse

- Default (Fuse not vaporized)
 - Input pin (a) connected to the AND gate
- Fuse vaporized (after programming)
 - Link to the input pin broken
 - AND gate input connected only to the pull-up resistor (R)
 - Always logic 1
 - Not altering the AND gate functionality!!!



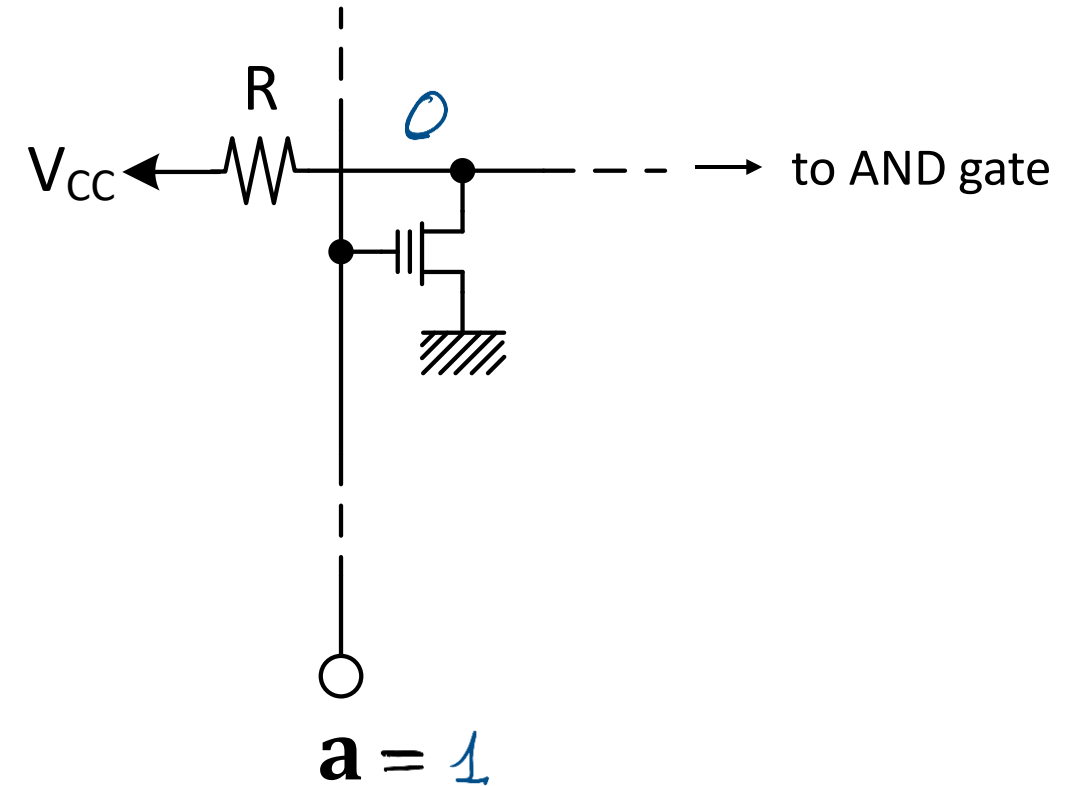
PAL

- Reprogrammable PAL
 - **UV erasable (FAMOS)**



PAL

- Reprogrammable PAL
 - **UV erasable (FAMOS)**
 - Default (FAMOS not programmed)
 - If input pin (a) = logic 1 ($V_{CC} > V_T$) → transistor **ON**
 - AND gate input = logic 0



PAL

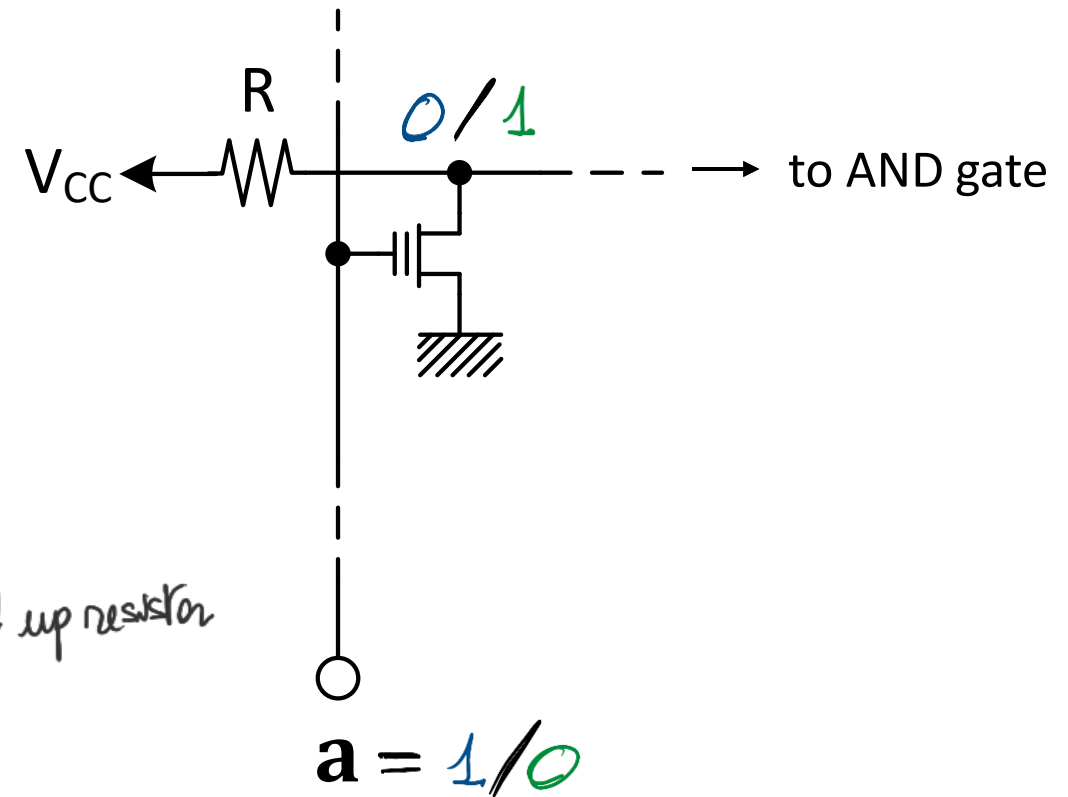
- Reprogrammable PAL

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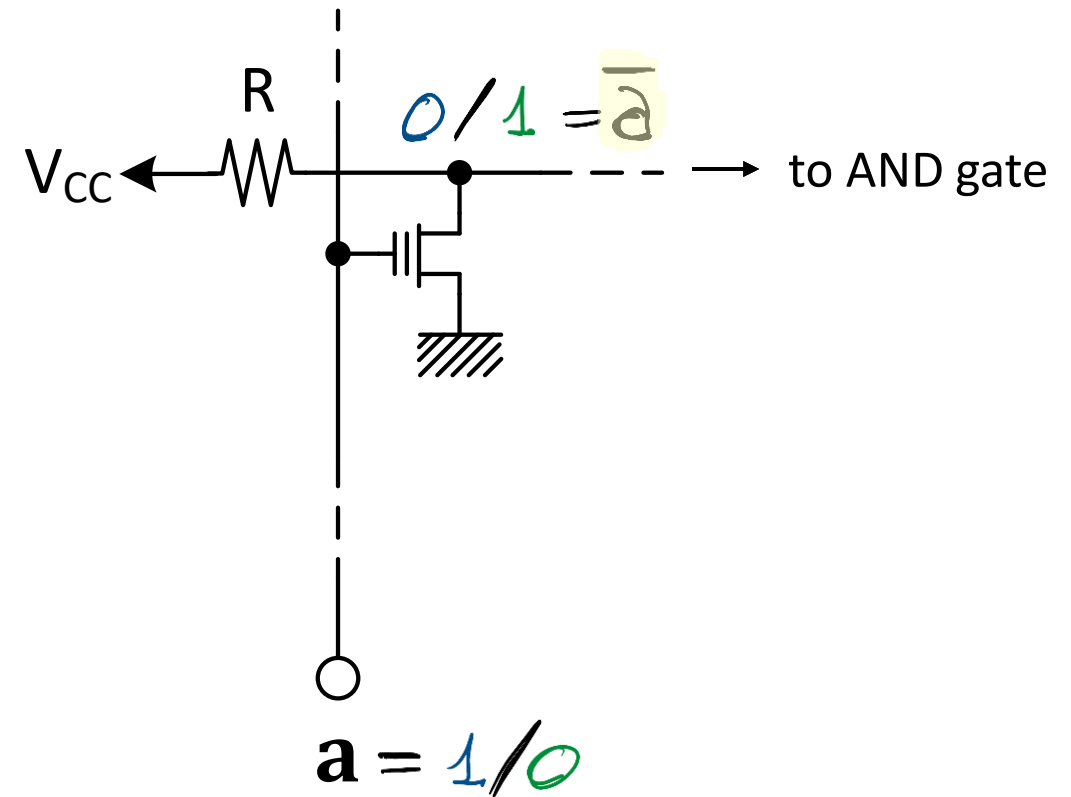
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↓ Because of the pull up resistor



PAL

- Reprogrammable PAL
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 - **Attention! Inverting logic / active-low logic!!!**

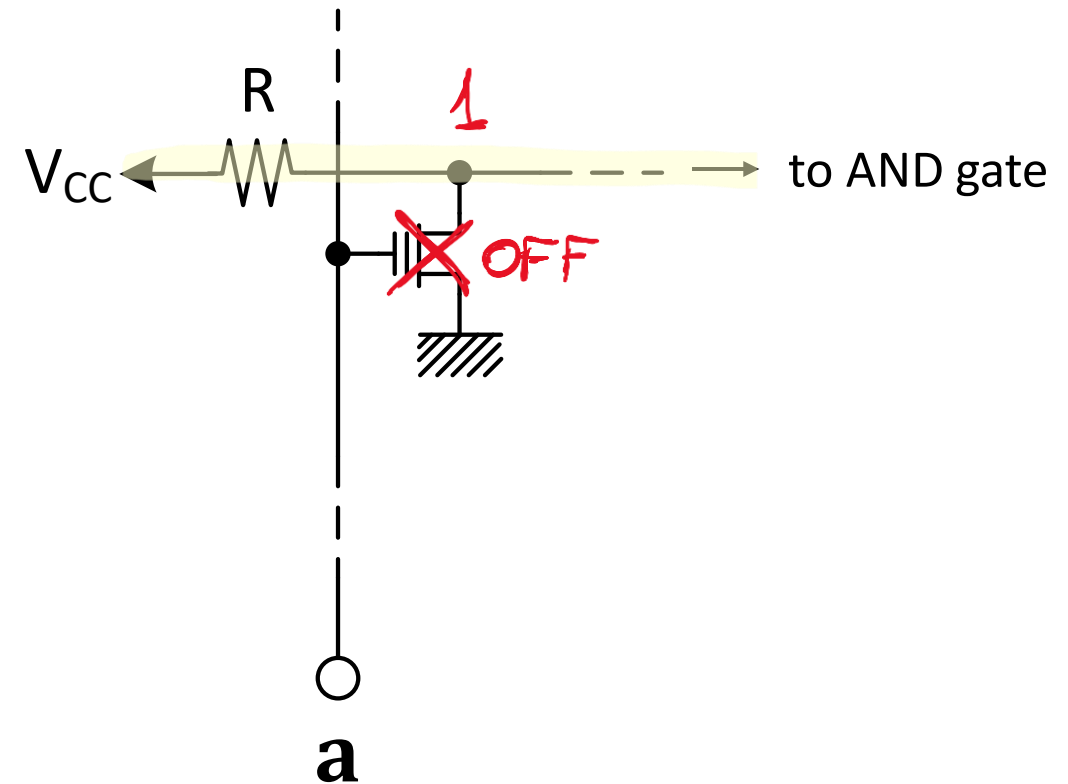


PAL

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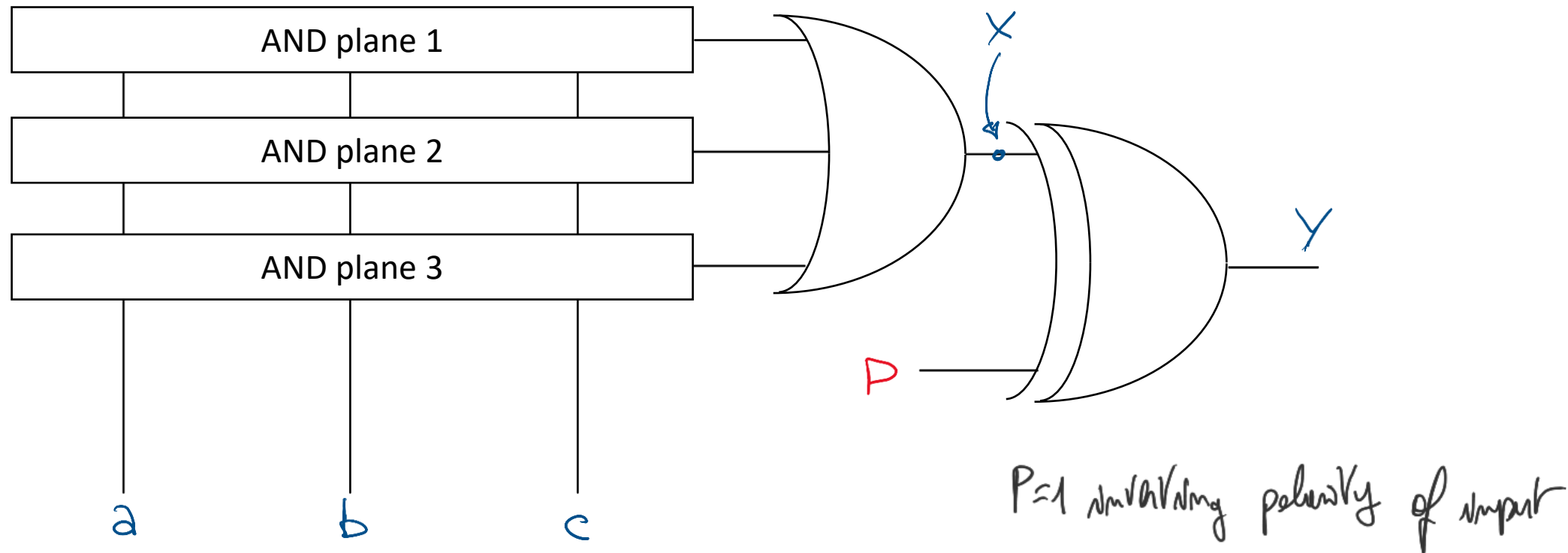
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 - AND gate input = logic 1
 - **Attention! Inverting logic / active-low logic!!!**
- FAMOS programmed ($V_T' > V_{CC}$)
 - Transistor always OFF
 - **AND gate input always logic 1** (through pull-up resistor to V_{CC})
 - **Not altering AND gate functionality!!!**



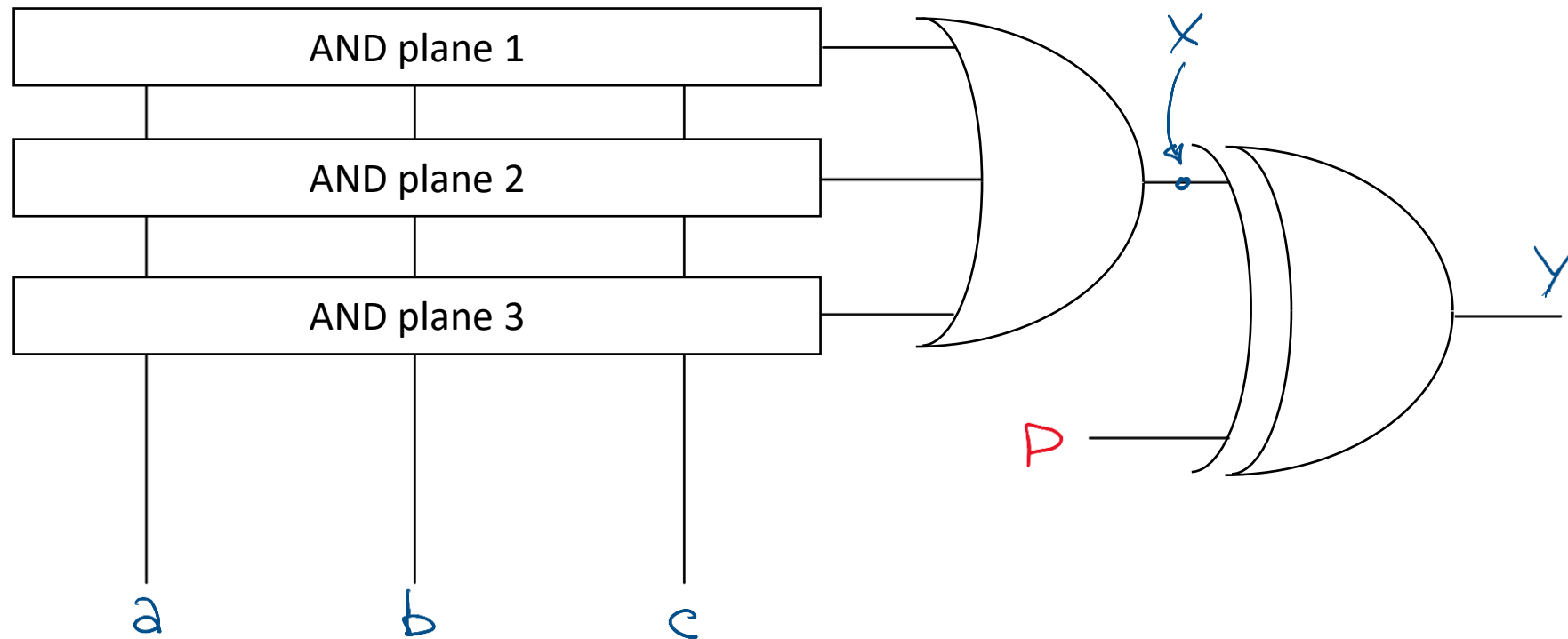
Evolution of PAL

- Output polarity configuration: active-high / active-low



Evolution of PAL

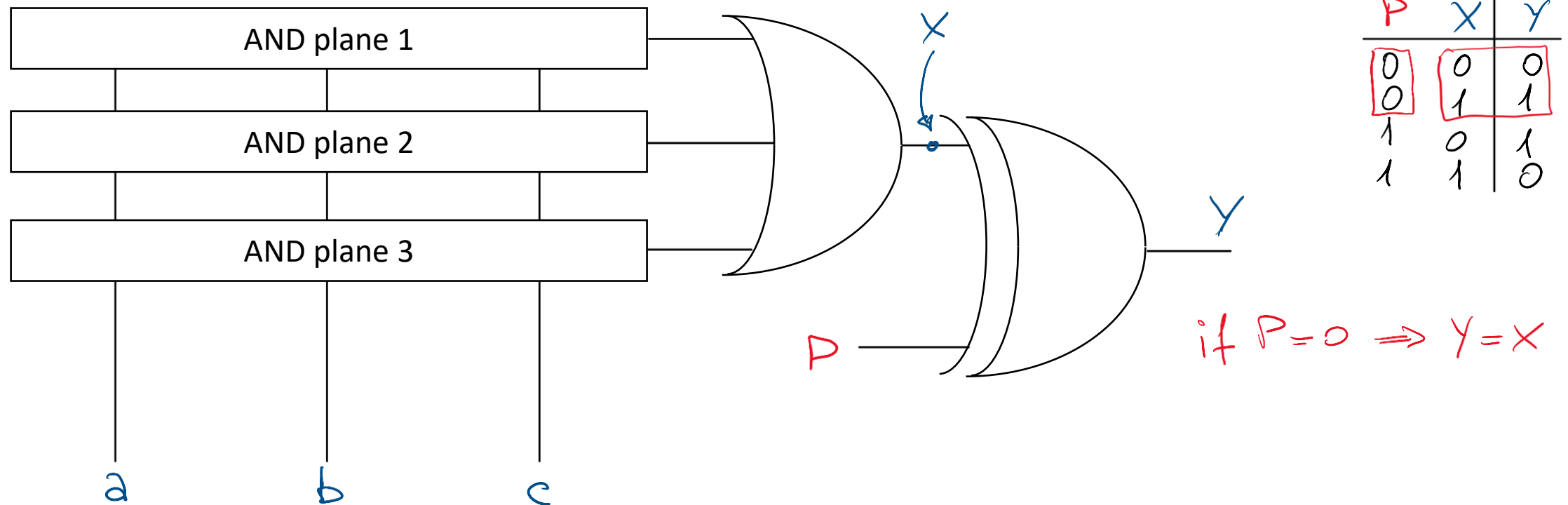
- Output polarity configuration: active-high / active-low



P	X	Y
0	0	0
0	1	1
1	0	1
1	1	0

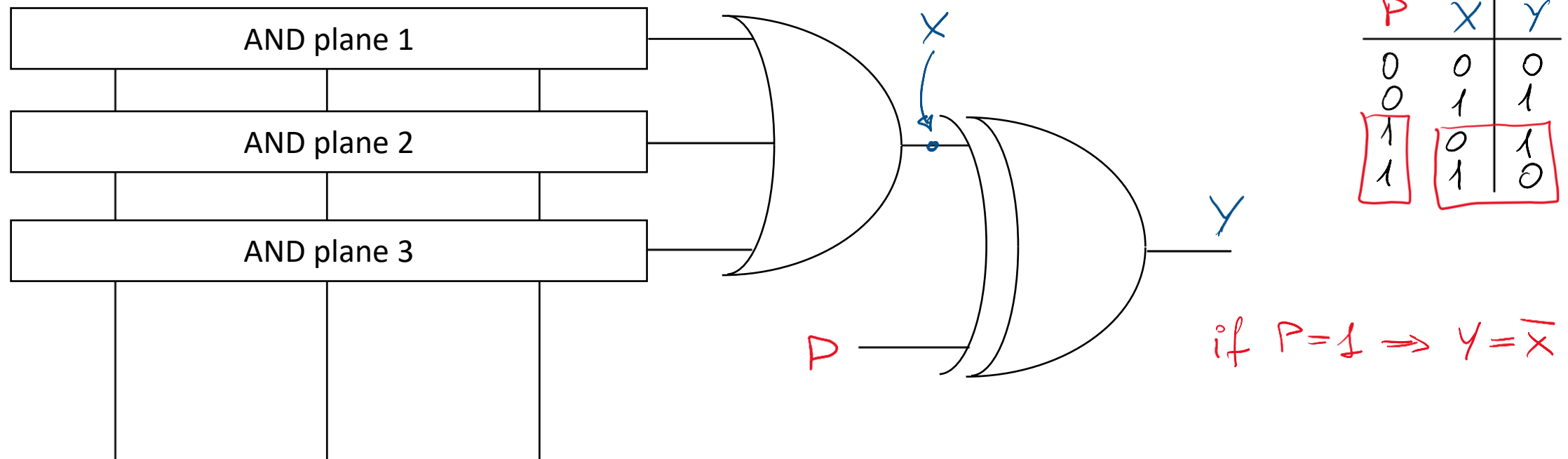
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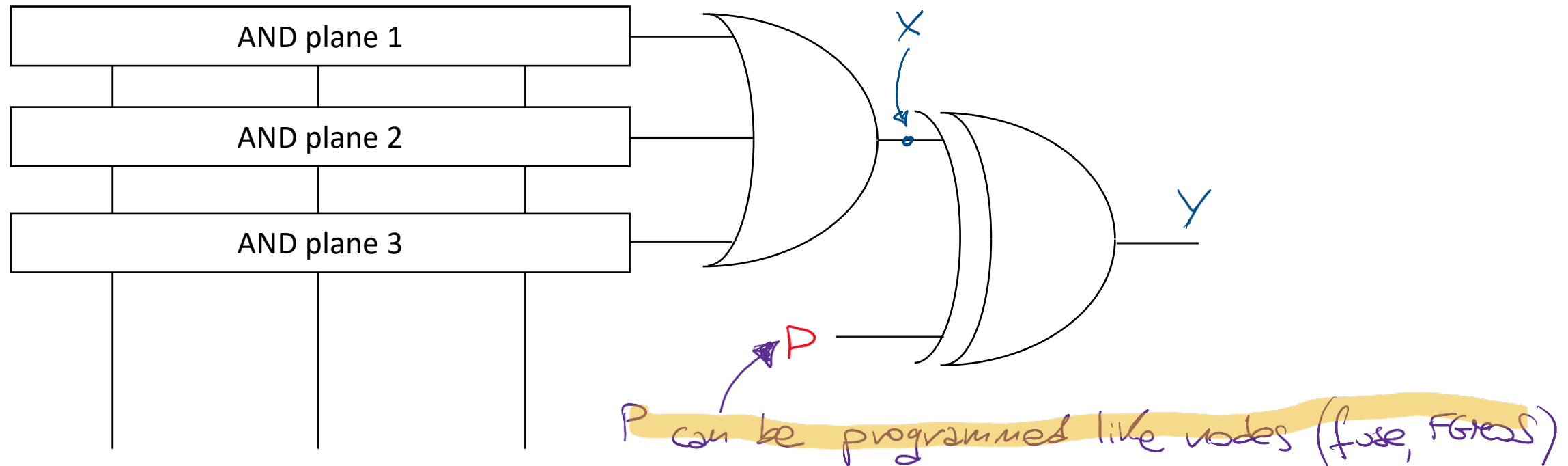
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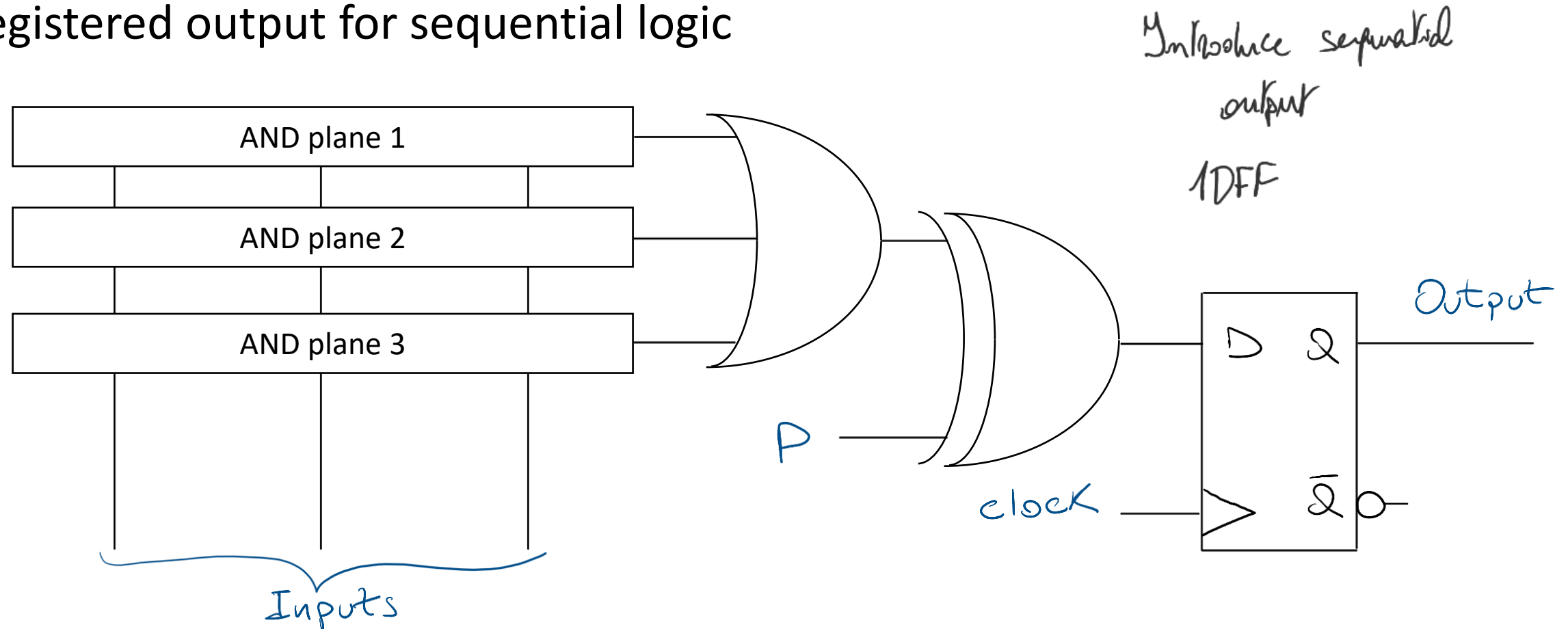
Evolution of PAL

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Evolution of PAL

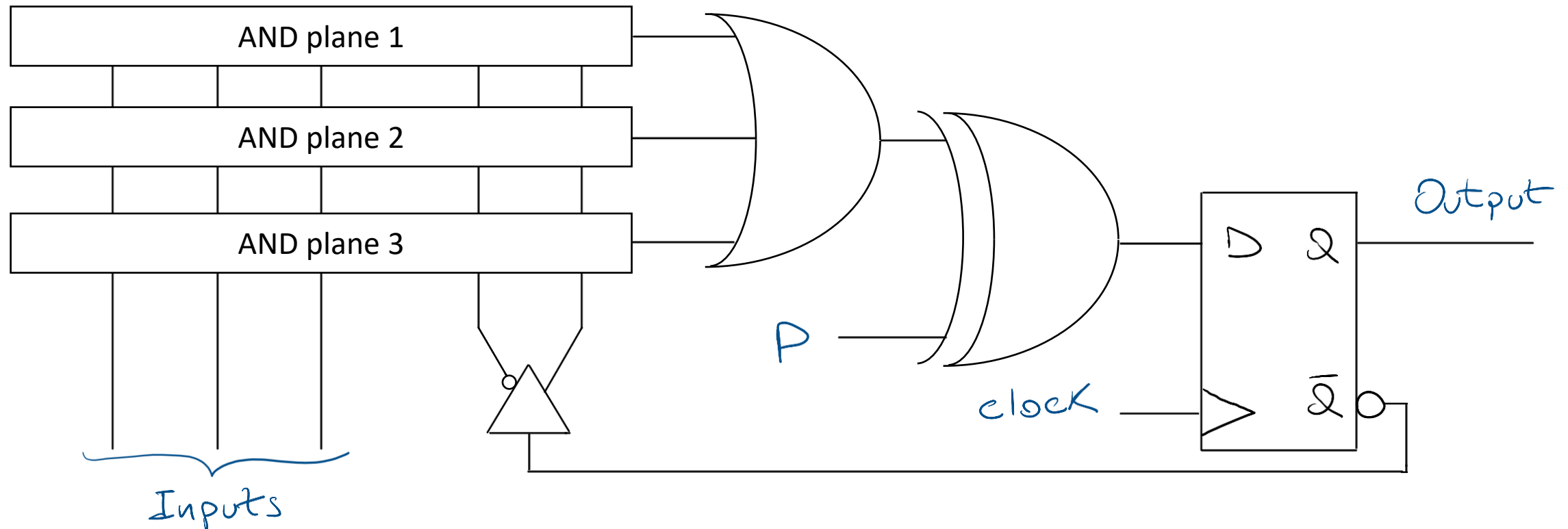
- Registered output for sequential logic



Evolution of PAL

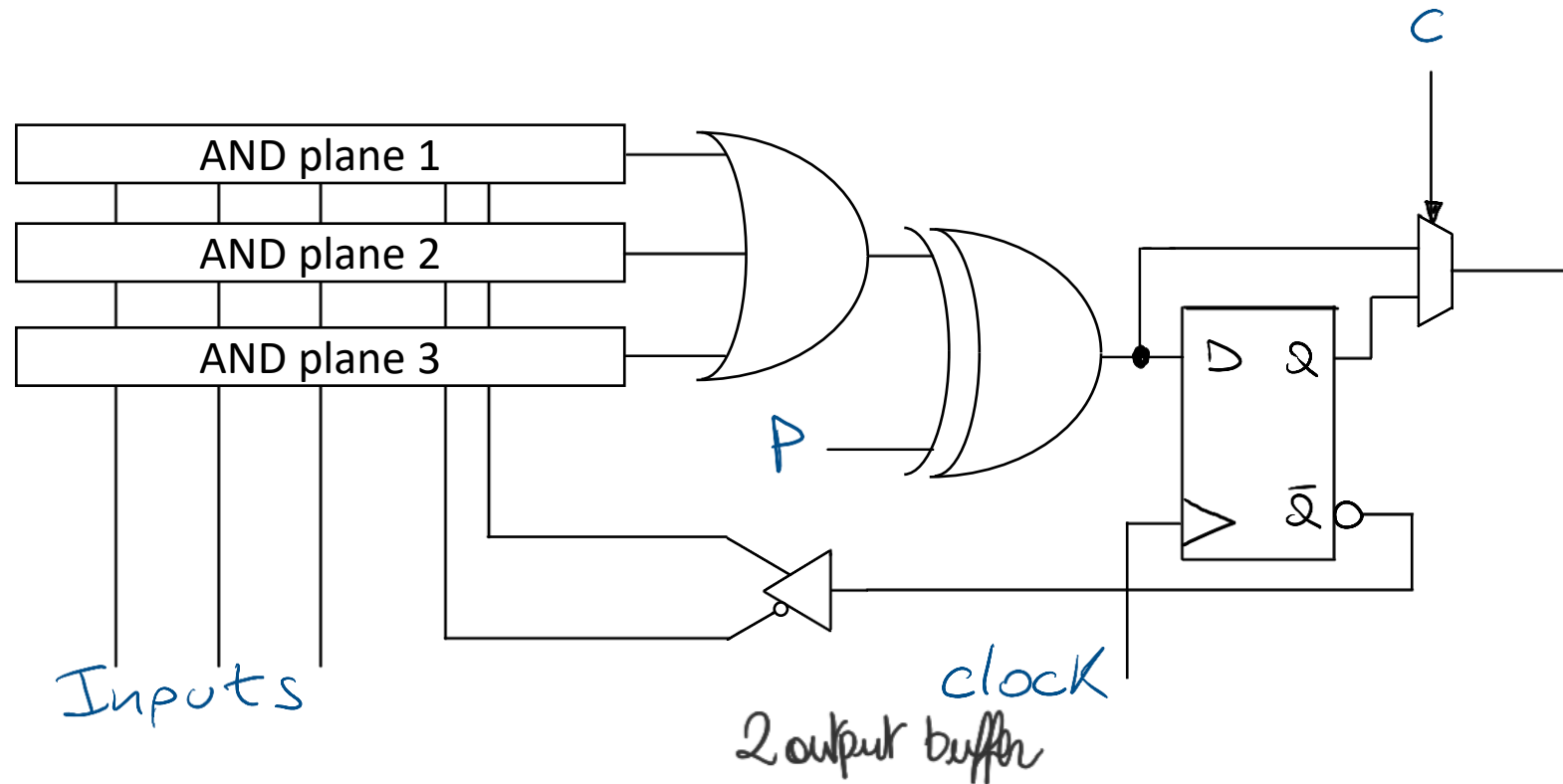
- Feedback path for FSM implementation

Finite state machine:
register for the state



Evolution of PAL

- MUX to select between combinational or sequential output



Evolution of PAL

- PAL has evolved by enriching its functionality/flexibility
Sometimes also architecture as tech moved forward
- Evolution to more complex PLDs (CPLDs) to the latest and most powerful configurable device
 - **FPGA = Field-Programmable Gate Array**



PAL – Last notes

- How PALs were programmed

- ^{Using:} Dedicated equipment *Now you can program them with USB*
- Programming language
 - PALASM (PAL Assembler)
 - CUPL (Compiler for Universal Programmable Logic)
 - ABEL (Advanced Boolean Expression Language)

PAL – Last notes

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PAL16R4 PAL PAL DESIGN SPECIFICATION
 CNT4SC
 4 bit counter with synchronous clear
 Michael Holley and Dave Pellerin

Clk	Clear	NC	NC	NC	NC	NC	NC	NC	NC	GND
OE	NC	NC	/Q3	/Q2	/Q1	/Q0	NC	NC	NC	VCC

```

Q3 := Clear
    + /Q3 * /Q2 * /Q1 * /Q0
    + Q3 * Q0
    + Q3 * Q1
    + Q3 * Q2

Q2 := Clear
    + /Q2 * /Q1 * /Q0
    + Q2 * Q0
    + Q2 * Q1

Q1 := Clear
    + /Q1 * /Q0
    + Q1 * Q0

Q0 := Clear
    + /Q0
  
```

FUNCTION TABLE

OE	Clear	Clk	/Q0	/Q1	/Q2	/Q3
L	H	C	L	L	L	L
L	L	C	H	L	L	L
L	L	C	L	H	L	L
L	L	C	H	H	L	L
L	L	C	L	L	H	L
L	H	C	L	L	L	L

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```
" 4 to 1 multiplexer design with case construct
"   SEL0,SEL1 pin;
"   A,B,C,D   pin;
"   MUX_OUT   pin istype 'com';
"
"   SEL = [SEL1,SEL0];

equations

when SEL==0 then MUX_OUT = A; else
when SEL==1 then MUX_OUT = B; else
when SEL==2 then MUX_OUT = C; else
when SEL==3 then MUX_OUT = D;
```

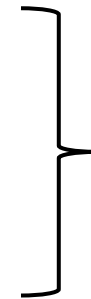
PAL – Last notes

- How PALs were programmed

- Dedicated equipment

- Programming language

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First examples of **HDL**



Thank you for your attention

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