Verified double-hashing hash map

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Outline

Introduction

Implementation

Modifications
Performance evaluation
Performance results

Verification

What to prove? Proof steps

Conclusion

Hash Table software Remaining work Side effects

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Performance evaluation

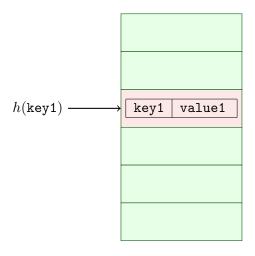
Verification

What to prove? Proof steps

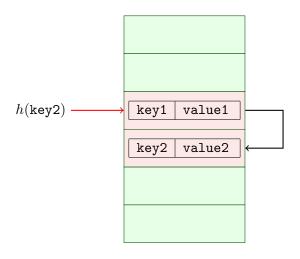
Conclusion

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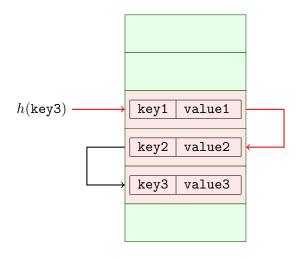
Naive hash table



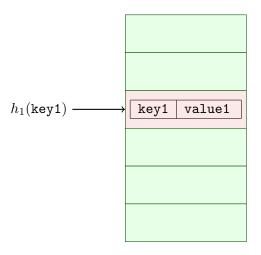
Naive hash table



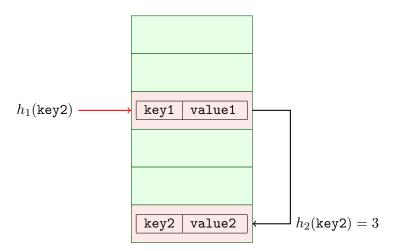
Naive hash table



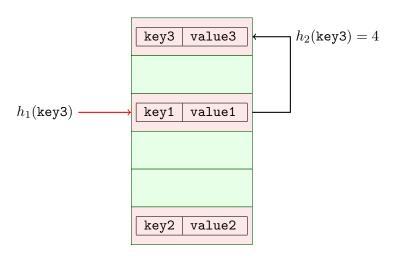
Double hashing



Double hashing



Double hashing

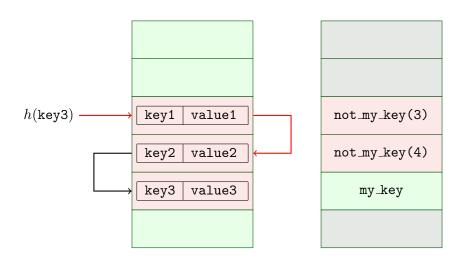


Provided implementation

- ▶ A naive implementation
- ▶ findEmpty, findKey perform the loops.

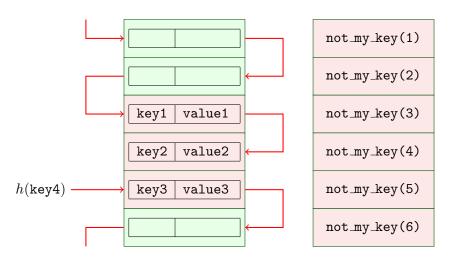
Provided verification

Example: successful search of key3



Provided verification

Example: unsuccessful search of key4



Provided verification

Part before and after " $\forall i.not_my_key(i) = true$ " provided.

For insertion:

- ► Same idea
- ► Property: findEmpty

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Modifications

▶ 64 bits hashes.

offset	entry
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Except type changes, only for loops modified.

Performance evaluation

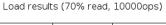
- ▶ Build a benchmark tool.
- ► Size, number of accesses, load, read/write ratio, etc...
- ▶ Converter to C file.
- ▶ First warms-up, then measures when target load is reached.

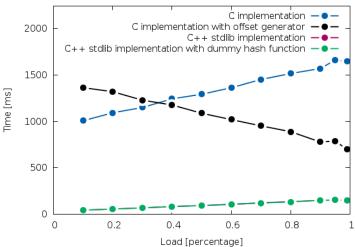
test_load.sh length read_ratio load1 [load2...]

Evaluation cases

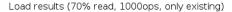
- ▶ Worst case: searching a non existing element.
- 1. Allow searching non existing element.
- 2. Search only existing element.

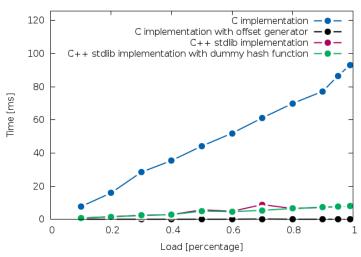
Result





Result – only existing





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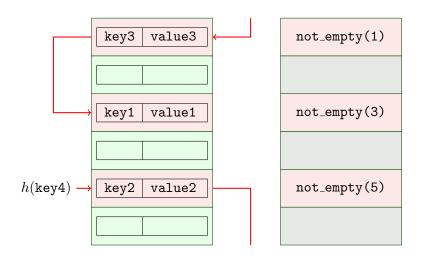
What to prove?

Goal: show that increment by offset covers all the map.

- ▶ Not always true (chinese remainder theorem).
- ▶ Requires: offset and capacity coprime (gcd = 1) (necessary and sufficient).

What to prove?

Insert key4: $h_1(\text{key4}) = 5$, $h_2(\text{key4}) = 2$: search empty?



Proof steps

If the number of iteration is less than the capacity:

- ▶ Build and updated a list<option<nat>> with the same pattern.
- ► Each cell is:
 - \triangleright some(n) if accessed after n iterations.
 - ▶ none if not accessed.
- ▶ Apply Chinese Remainder Theorem.
- ▶ Deduce that only none are updated to some.
- ▶ Hence, the number of some is the number of iteration.
- ▶ For capacity iteration, all cells are some.

Proof steps

If some(n), then prop(start+offset*n % capa).

_	
-2, iter=7)	none
	some(4)
offset=2	some(1)
stripe(capacity=7, of	some(5)
	some(2)
	none
	some(3)
Ω	

prop(2) holds
(0) 1 11
prop(3) holds
prop(4) holds
prop(4) noids
prop(5) holds
prop (e) notae
prop(7) holds

Proof steps

_	
iter=7)	some(7)
•	some(4)
7, offset=2	some(1)
	some(5)
city=	some(2)
tripe(capacity=7	some(6)
	some(3)

```
\Rightarrow \mathtt{count\_some} = \mathtt{iter} = 7
```

 \Rightarrow All cells are some.

Chinese Remainder Theorem

- ▶ Requires to implement gcd related functions.
- ▶ Almost proved.
- ▶ Last assumption: Coprime factorization lemma $(a \perp c \land b \perp c \Rightarrow (a \cdot b) \perp c)$.

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Hash-Table software

- ▶ Efficient (when key is present).
- ► Formally verified.
- ▶ Requires capacity and offset coprime.

Remaining work

- ▶ Coprime factorization lemma: $a \bot c \land b \bot c \Rightarrow (a \cdot b) \bot c$
- ► Logical operations (shift and bitwise_and)
- ▶ Some typing errors

Side effects

- ▶ 6 commits in Verifast tree (long long support).
- ▶ 9 issues on Verifast.
- ▶ A random access sequence generator & benchmark.

Q&A