Exercise 6:

Summary: Implement a software framework that allows you to set and compute some properties of triangles and rectangles. More specifically, you should be able to set the points of these shapes, to compute their unit normals and their area. **Exercise** is fully implemented.

Task 1: Implement the class Point and the interface AlgebraSupport (2 points)

The class **Point** has the class diagram shown below.

The instance variables are the point coordinates and are initialized in the constructor.

Their values are returned and set by the instance methods. The constructor uses them to set the coordinates.

toString() returns "Point = (" followed by the values of x, y, z separated by a comma and followed by the closing parenthesis")".

Point
-x, y, z : double
+Point(double, double, double)
+getX() : double
+getY() : double
+getZ() : double
+setX(double) : void
+setY(double) : void
+setZ(double) : void
+toString(): String

Create the interface **AlgebraSupport**. It declares two instance methods that all triangles and rectangles should have available. A method comparePoints(Point p1, Point p2) that compares two points. It returns true if p1 and p2 have identical coordinates and false otherwise.

It also declares the method $setNormal(double\ n1,\ double\ n2,\ double\ n3)$ with the return type void. It uses the 3 components in the argument list to set the normal and the area of a rectangle or triangle. It should set the area of the rectangle to the length of (n1,n2,n3) and it should set the area of the triangle to 0.5 times the length. It should also compute the unit normal from these values. The latter sets the values of nX, nY, nZ discussed below.

Task 2: Implement the shapes (6 points)

Develop the superclass **Shape**, which implements **AlgebraSupport**:

pointCounter is used by getPoint() and initialized to 0.

the Points is a static array for the corner points of a triangle or rectangle.

area corresponds to the area of the shape.

nX, nY, nZ are the components of the unit normal vector.

Shape
-pointCounter : int
#thePoints : Double[]
#area : double
#nX, nY, nZ : double
+Shape()
+getPoint(): Point
+setPoint(Point) · String

+toString(): String

getPoint() returns a point of the shape. It returns the point at the slot pointCounter of thePoints and increases pointCounter by 1. If the value of pointCounter exceeds the length of thePoints it should set pointCounter to 0.

setPoint(arg) compares arg to the points in thePoints. If arg is different from the ones of thePoints and if there is a free slot available in thePoints then it should add it to the array and return "Added". Otherwise it should return "not added".

The method toString() should return the string "has the area area and normal (nX, nY, nZ)" where the values of area, nX, nY, nZ are expressed using 4 digits, two of which come after the radix point.

The two subclasses **Rectangle** and **Triangle** have the class diagrams

Rectangle	Triangle
+Rectangle()	+Triangle()
+toString(): String	+toString(): String

The constructor in each class initializes the Points with the appropriate length.

The methods toString() return "The rectangle" or "The triangle" followed by the return value of the method toString() of the superclass.

One of the two methods declared in the interface should be implemented in **Shape** and the other in the subclasses. Remember that the area of a rectangle is given by the length of the cross product of its base vectors while the area of a triangle is given by half that value.

Task 2: Implement Algebra (2 points)

The class is the superclass of **Exercise** and has the class diagram

Algebra
+computeNormal(Shape): void
+createPoint(double, double, double): Point

The method createPoint(arg, arg, arg) creates an instance of **Point** using the three values in the argument list.

computeNormal(arg) computes the edge vectors with two consecutive points (point 0 and point 1 is one edge and point 1 and point 2 the second) and computes the cross product of both. The length of the vector is related to the area of the shape and the unit vector sets the normal.

Run Exercise to see if everything works.