

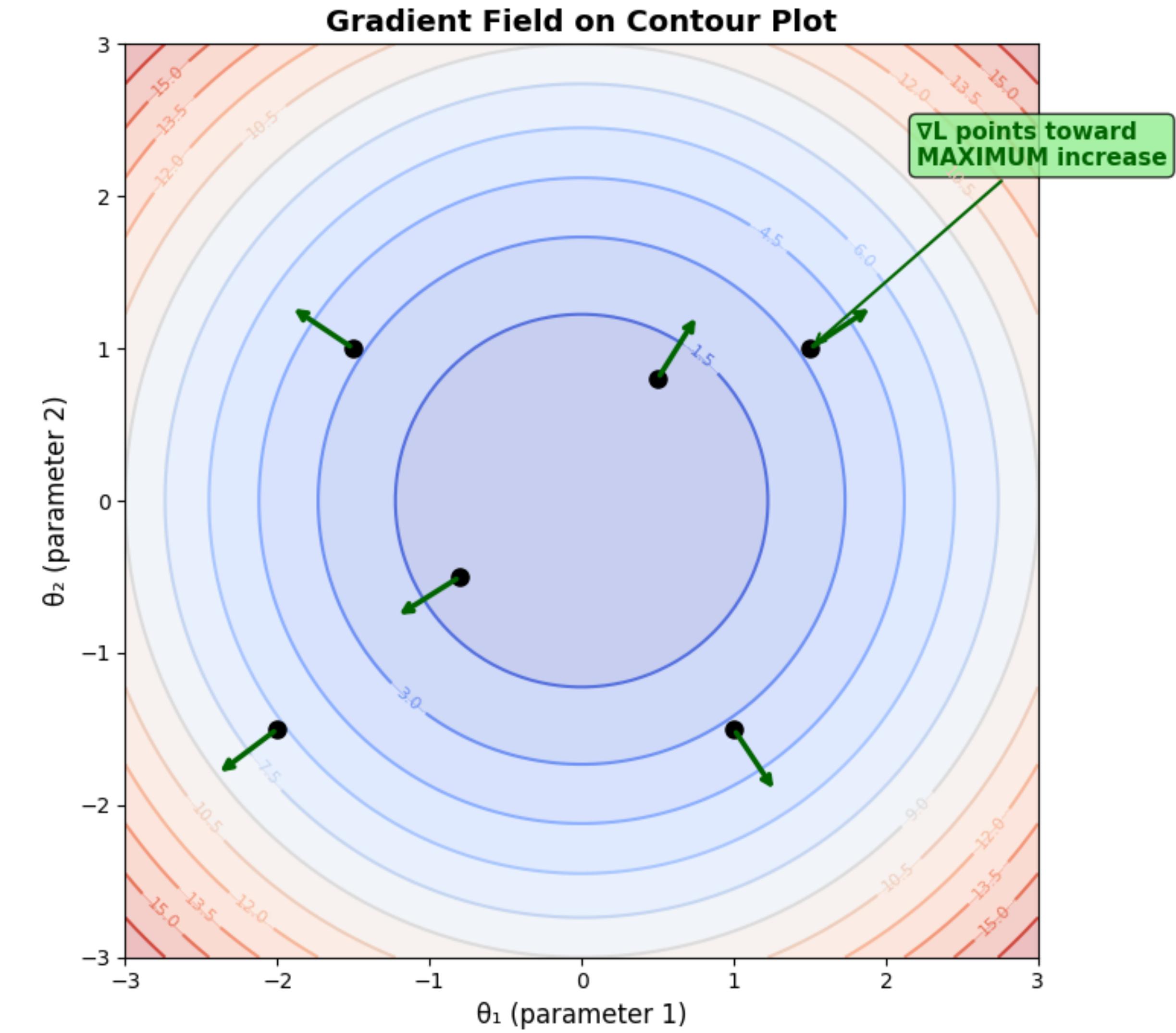
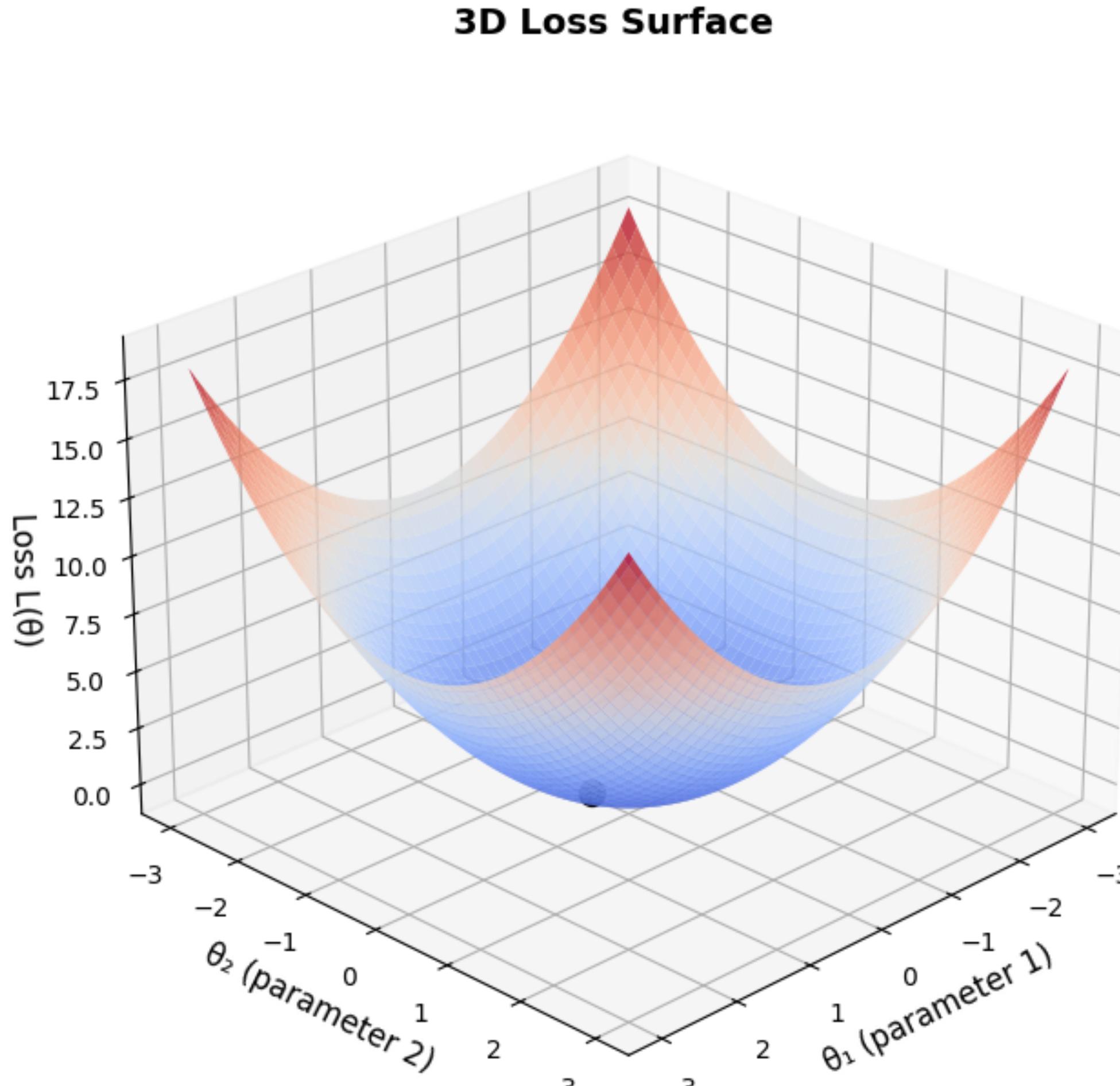
Deep Learning (1470)

Randall Balestriero

Class 4

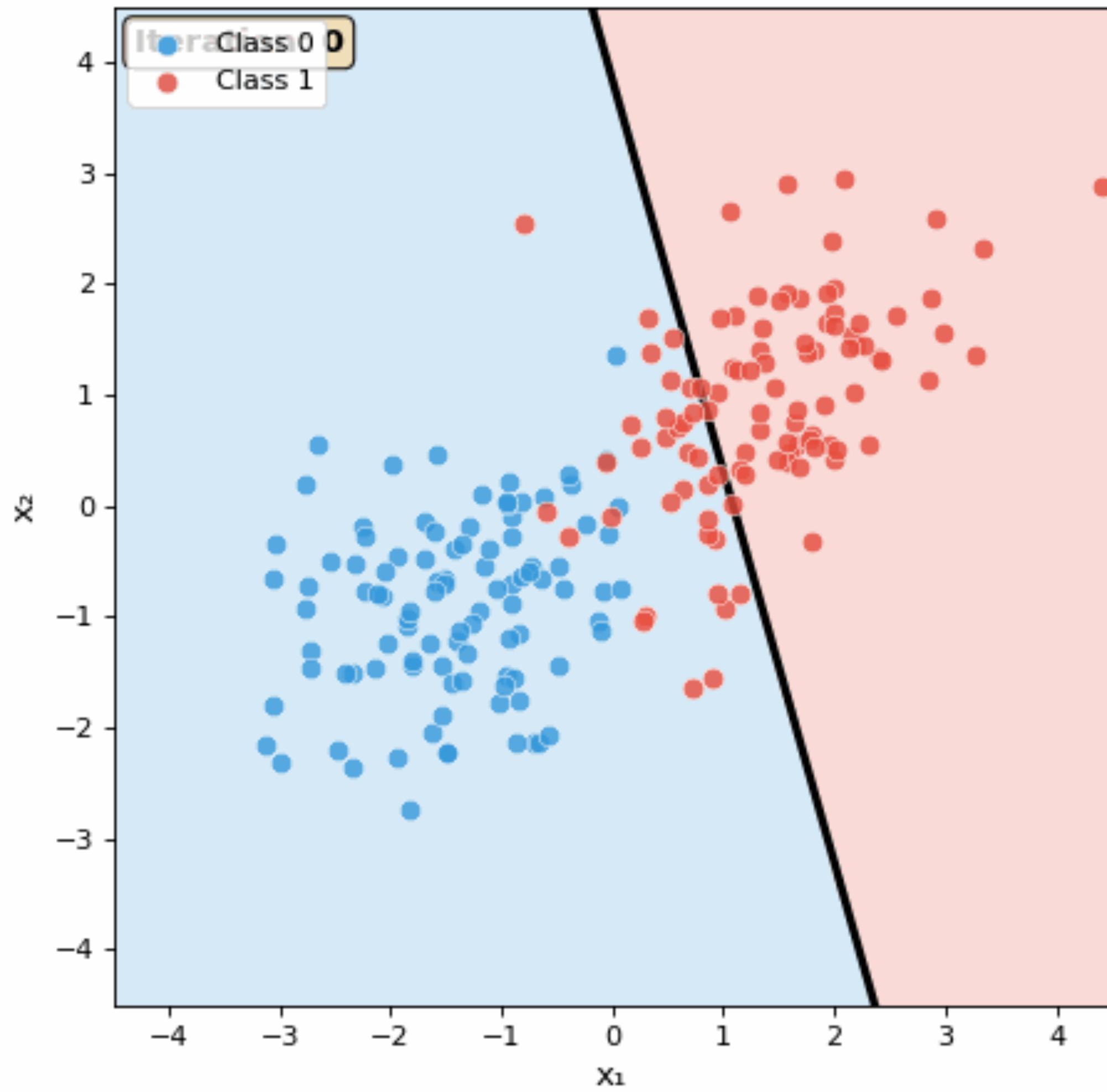
Rewind!

Gradient: Intuition

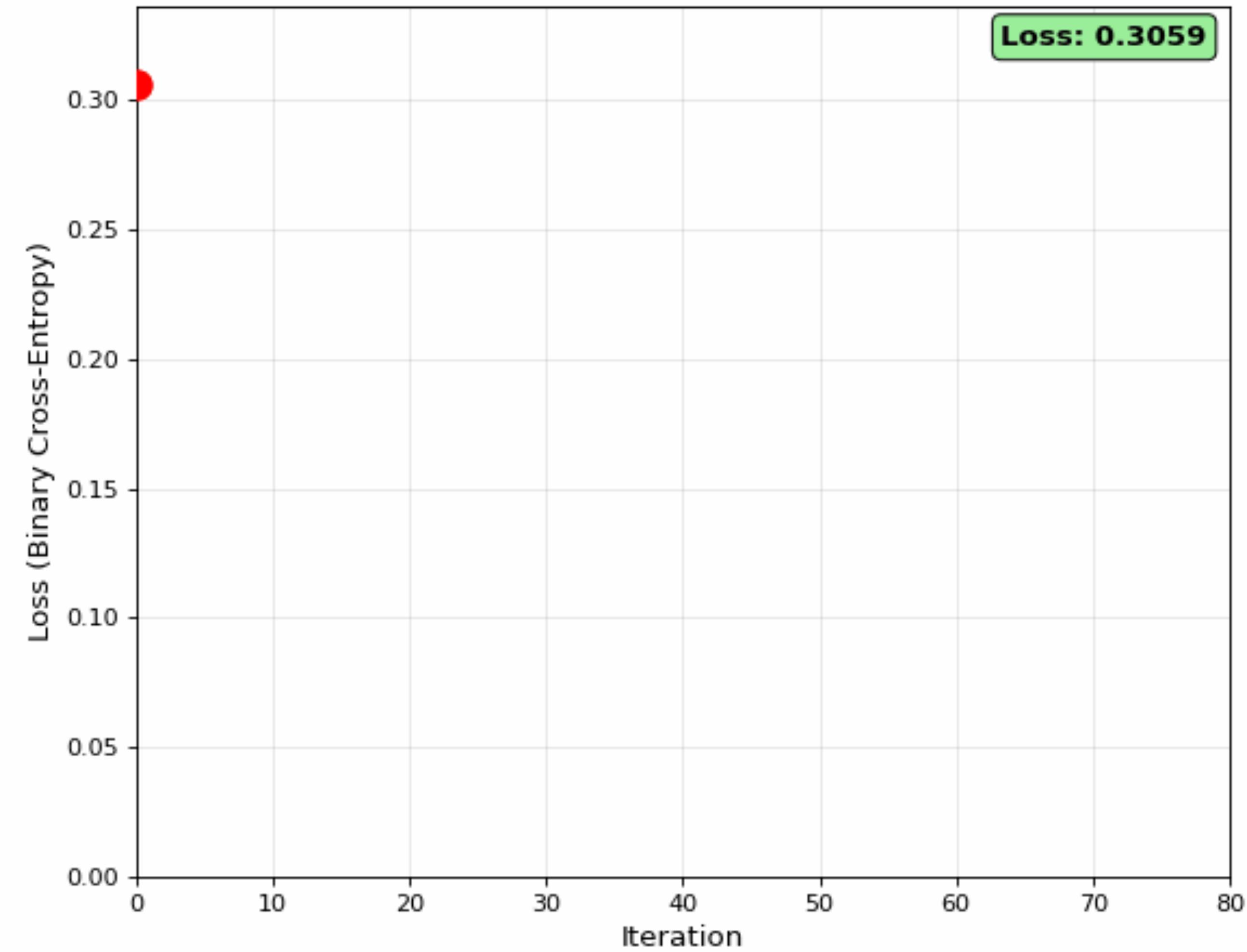


Gradient: Intuition

Linear Classifier Decision Boundary

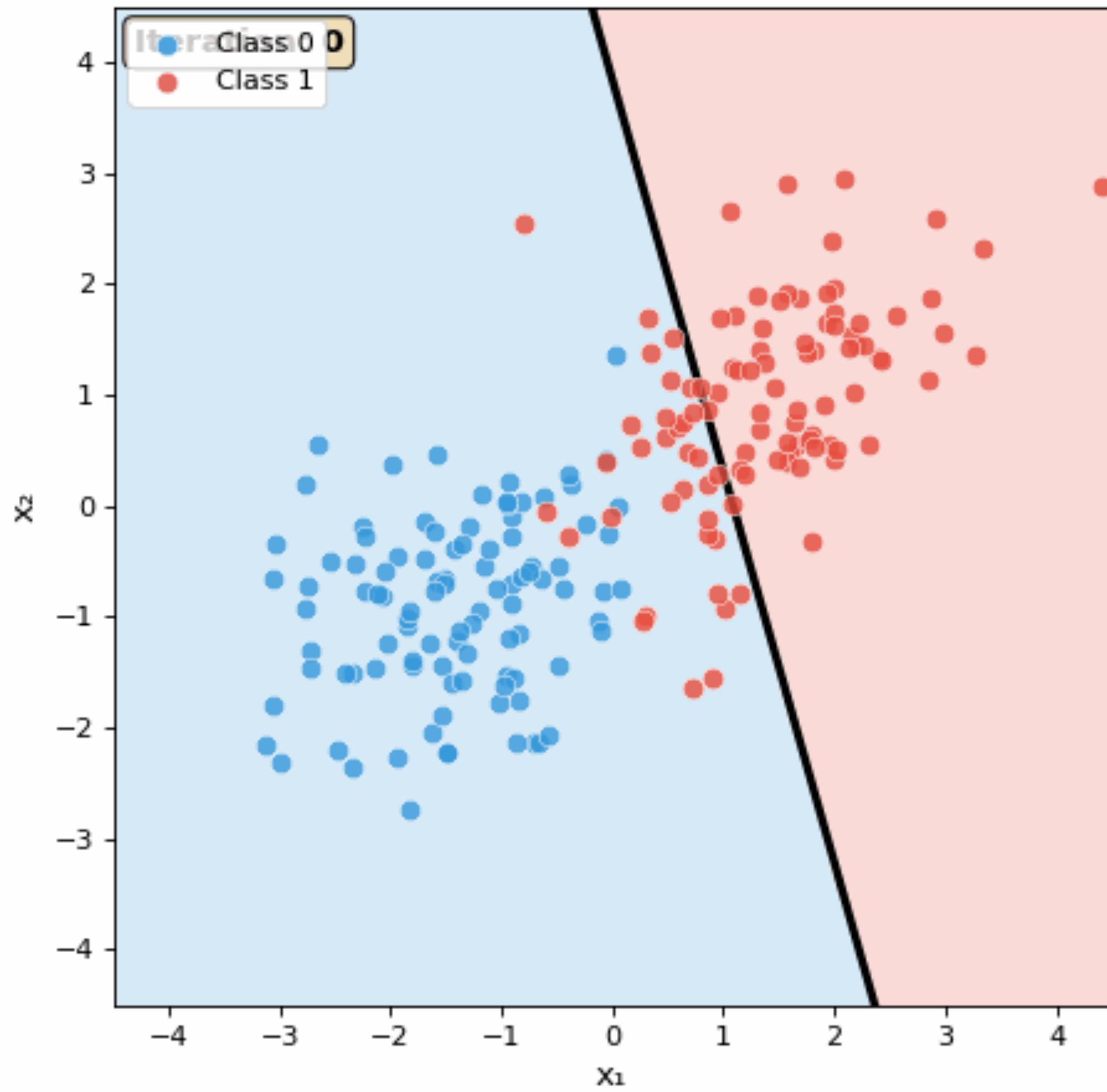


Training Loss Evolution

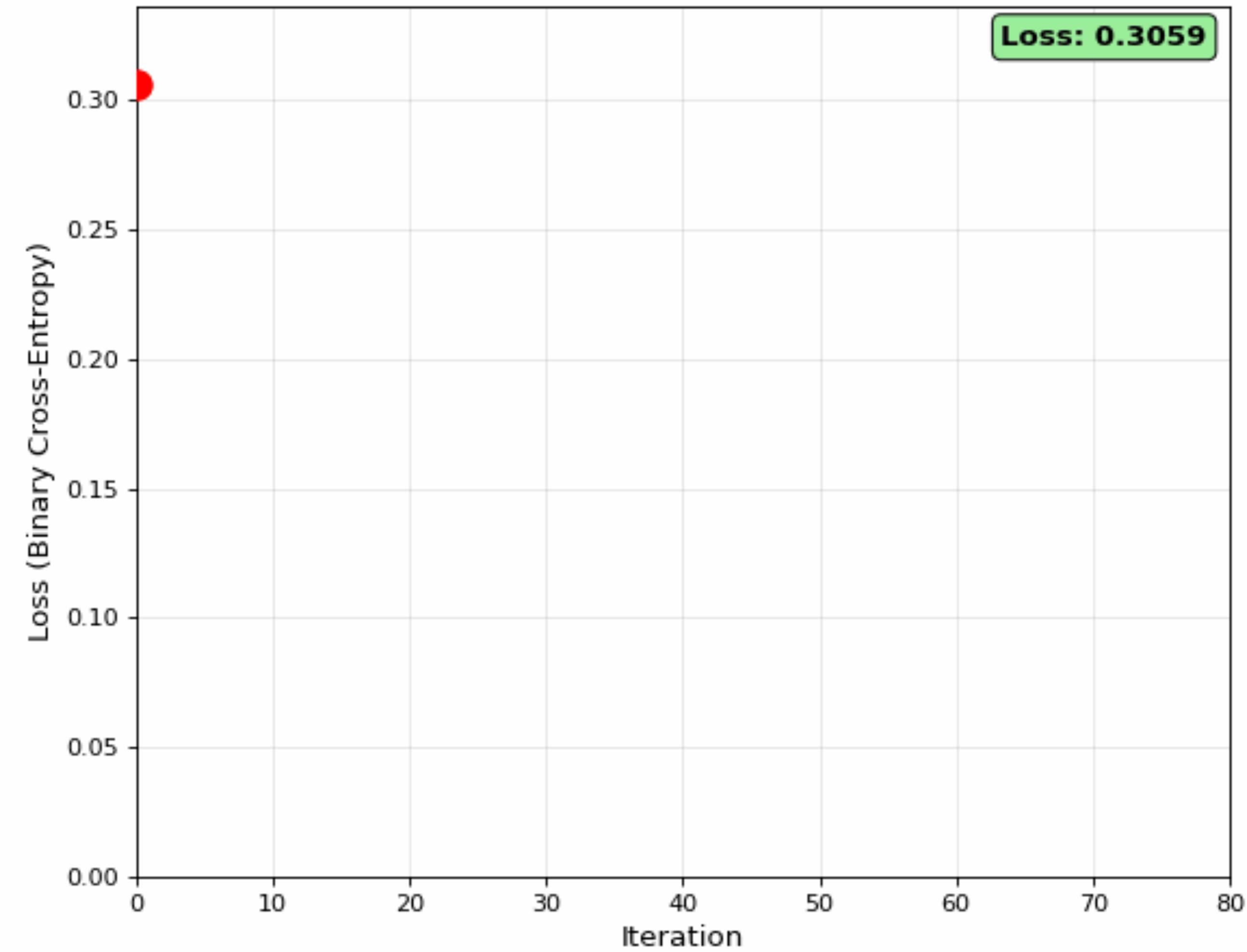


Gradient: Intuition

Linear Classifier Decision Boundary



Training Loss Evolution



MNIST

The most famous dataset in Deep Learning

Modified **N**ational Institute of **S**tandards and **T**echnology database

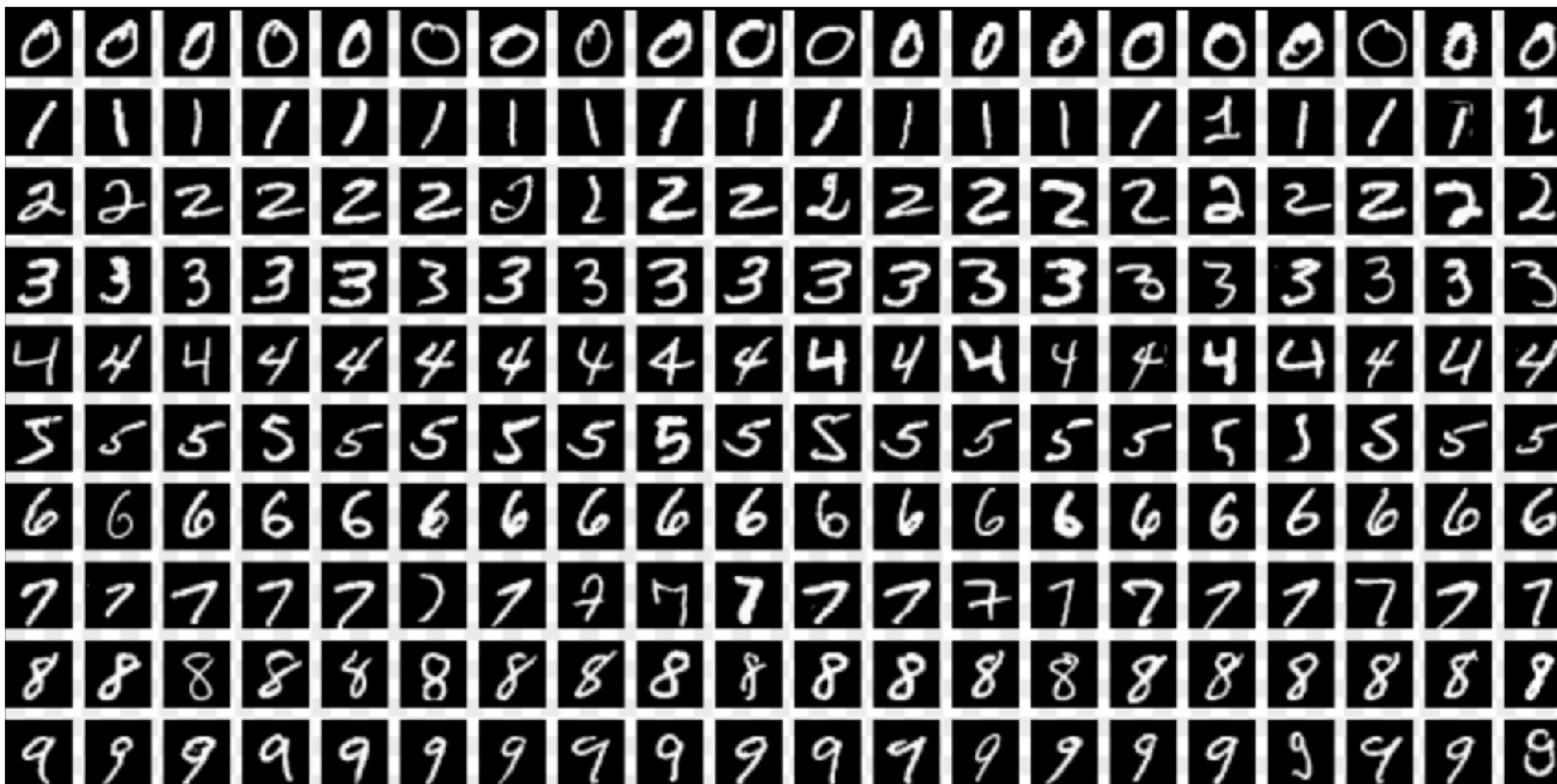


Image courtesy of Wikipedia

MNIST

MNIST

- What is D (dimension) of the samples?

MNIST

- What is D (dimension) of the samples?
- How many classes do we have?

MNIST

- What is D (dimension) of the samples?
- How many classes do we have?
- Do you think the classes are linearly separable?

MNIST

- What is D (dimension) of the samples?
- How many classes do we have?
- Do you think the classes are linearly separable?

A linear model reaches 94% accuracy!

Your First Deep Network!

Your First Deep Network!

- Why do we want to use a Deep Network?

Your First Deep Network!

- Why do we want to use a Deep Network?
- Could you think of “features” to extract by-hand that would improve linear model accuracy?

Your First Deep Network!

- Why do we want to use a Deep Network?
- Could you think of “features” to extract by-hand that would improve linear model accuracy?
- Which accuracy do you think we can reach?

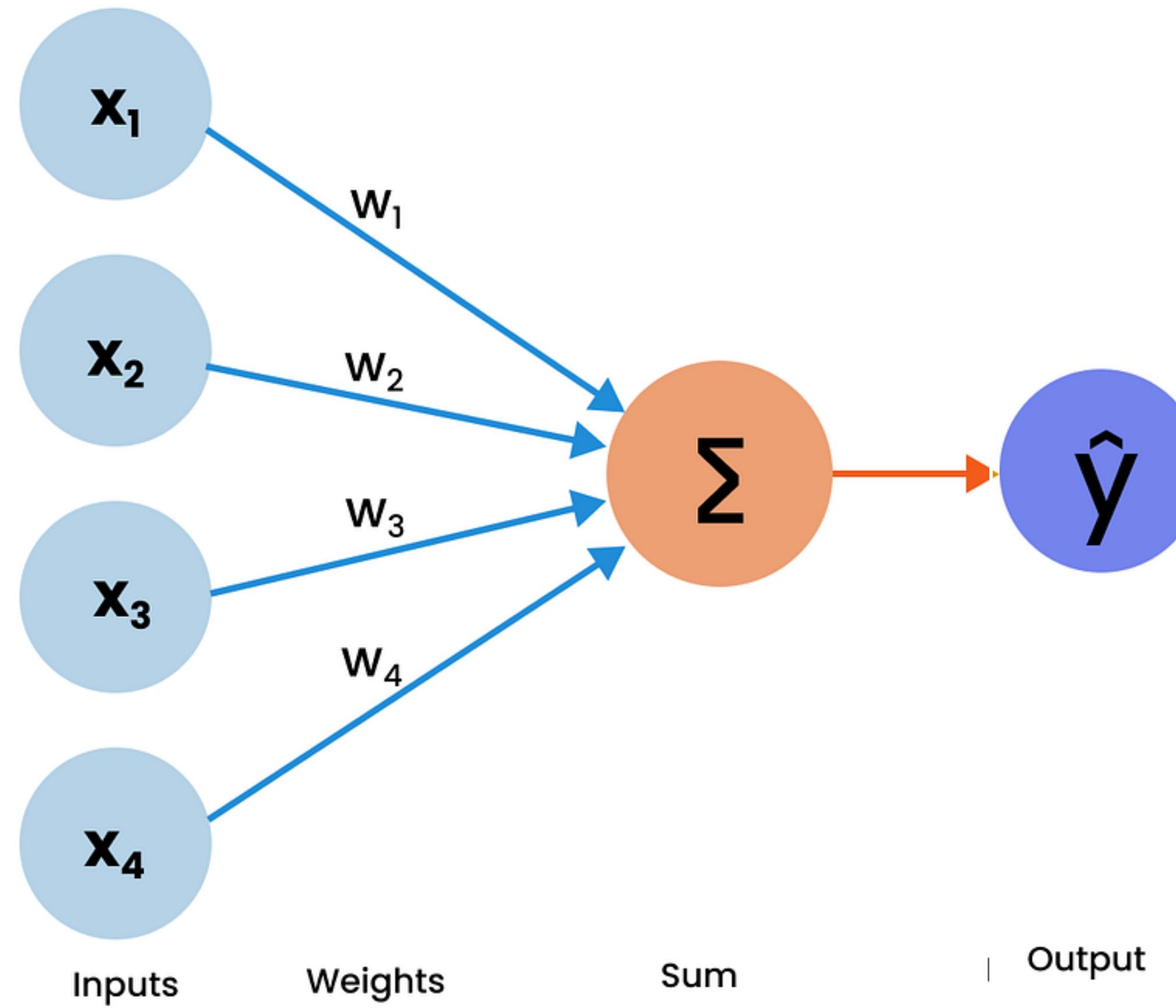
Your First Deep Network!

- Why do we want to use a Deep Network?
- Could you think of “features” to extract by-hand that would improve linear model accuracy?
- Which accuracy do you think we can reach?

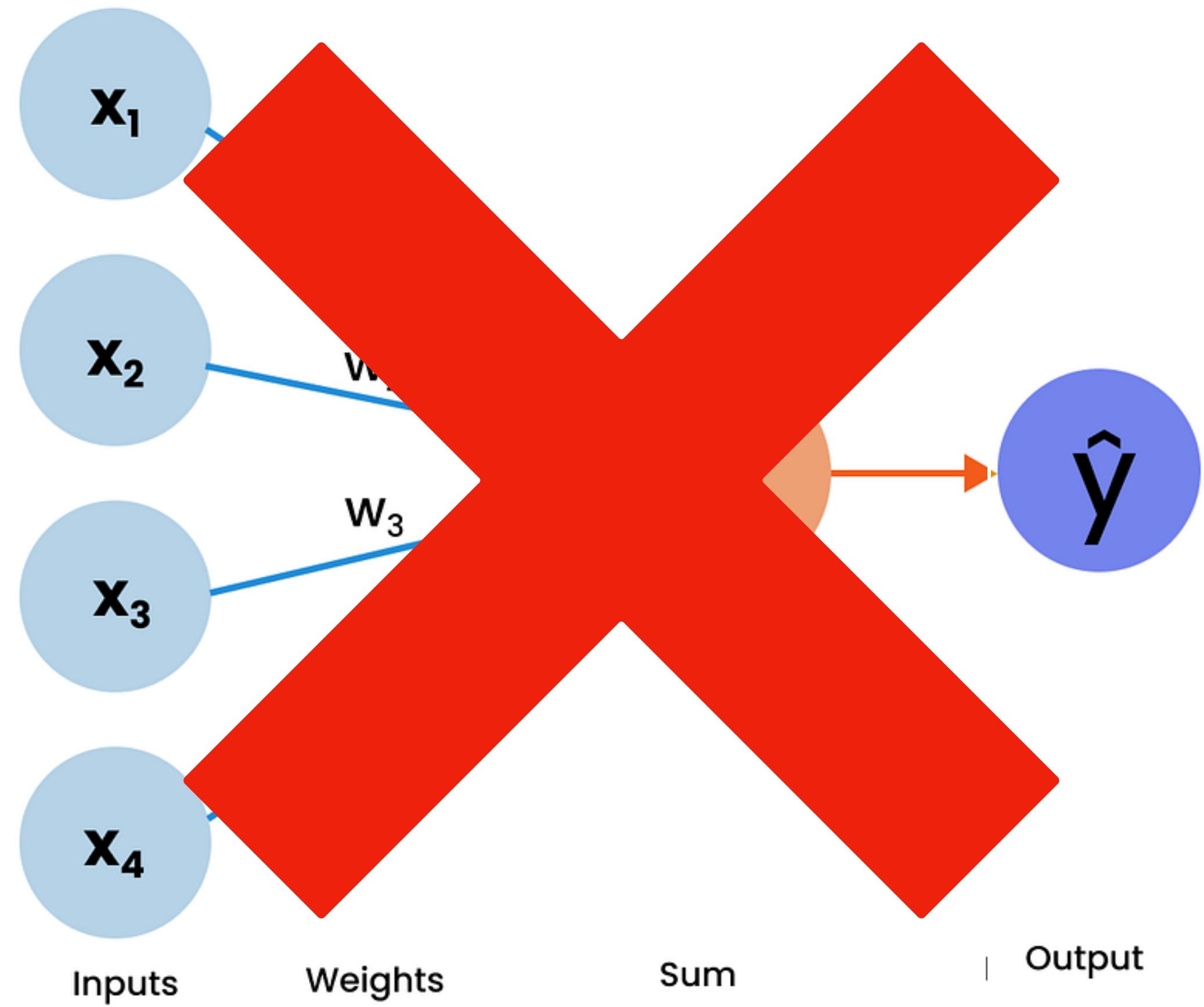
A Deep Network reaches 99.5% accuracy!

Your First Deep Network!

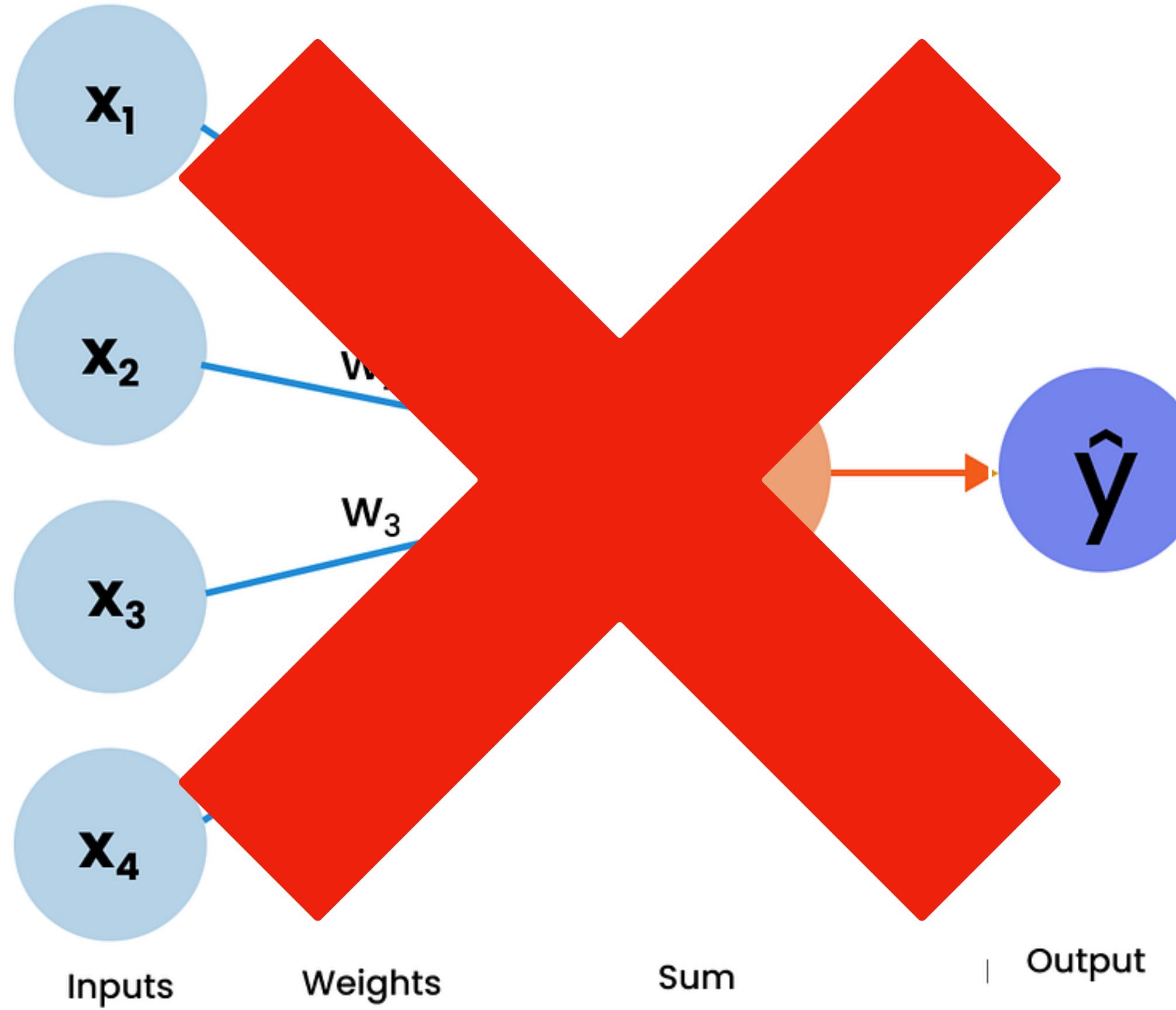
Your First Deep Network!



Your First Deep Network!

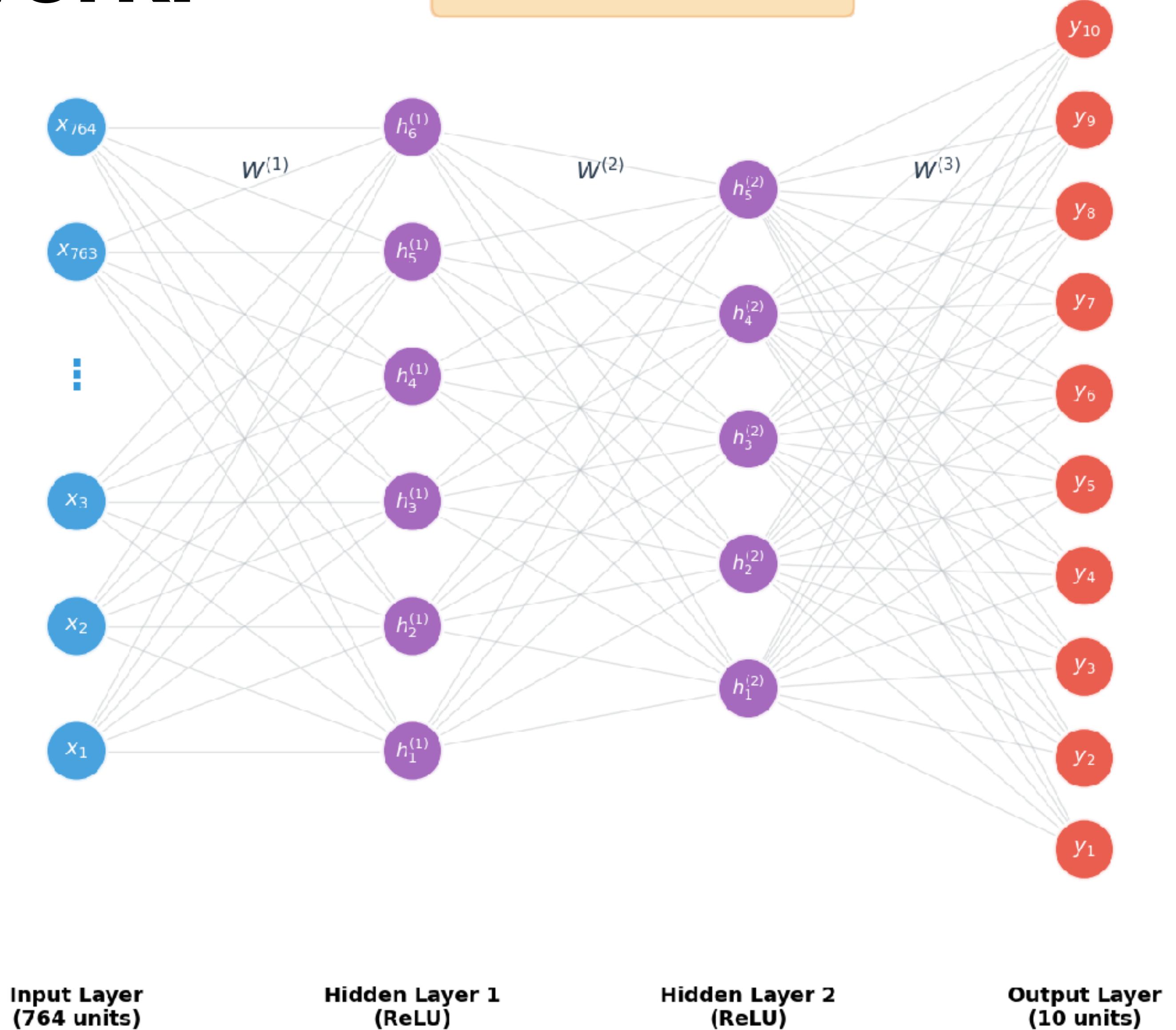


Your First Deep Network!

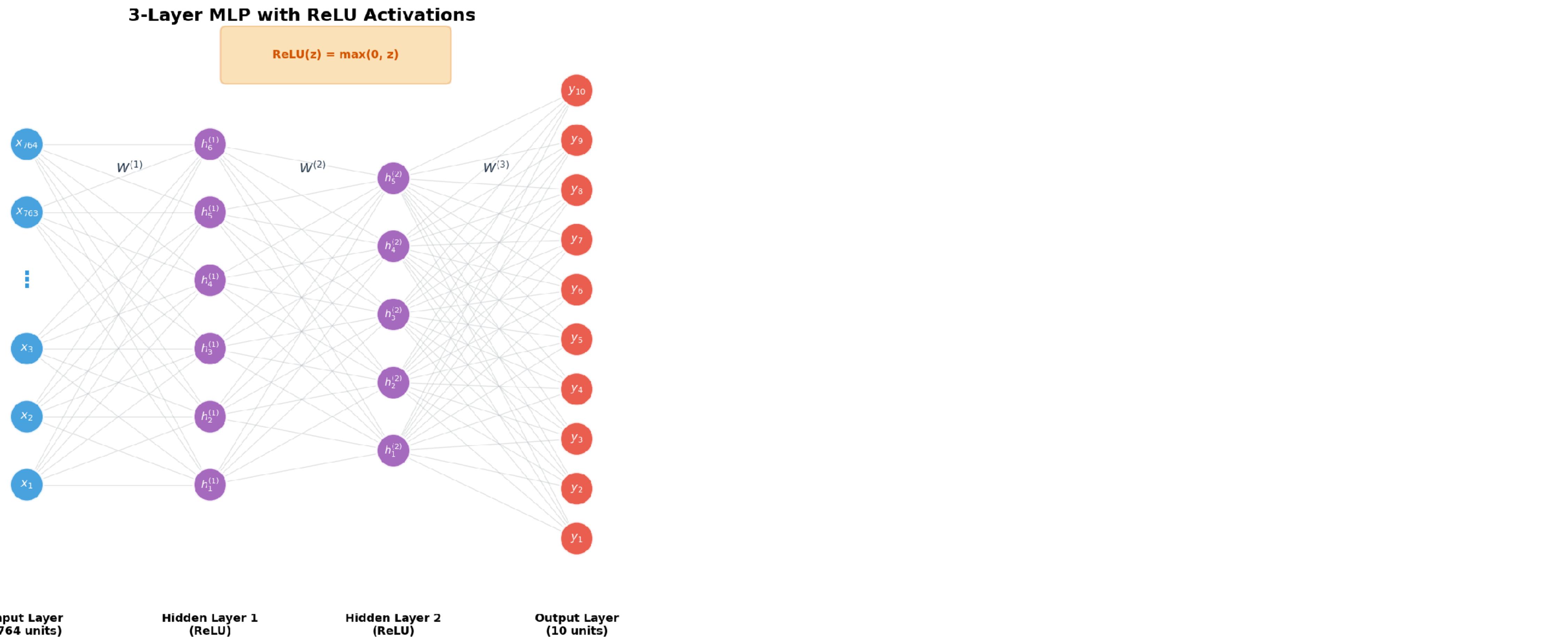


3-Layer MLP with ReLU Activations

$$\text{ReLU}(z) = \max(0, z)$$

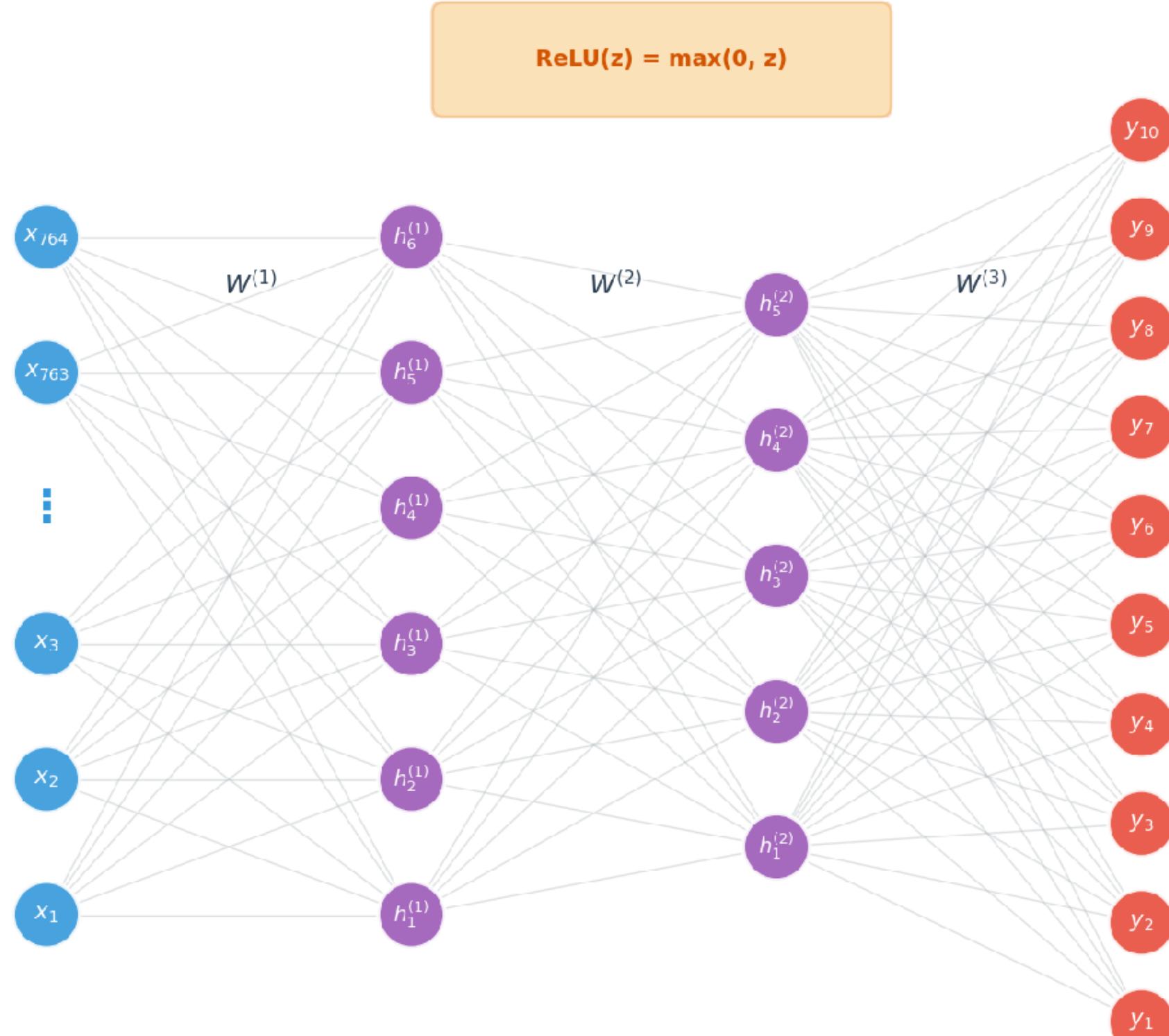


Your First Deep Network: Why?



Your First Deep Network: Why?

3-Layer MLP with ReLU Activations



Input Layer
(764 units)

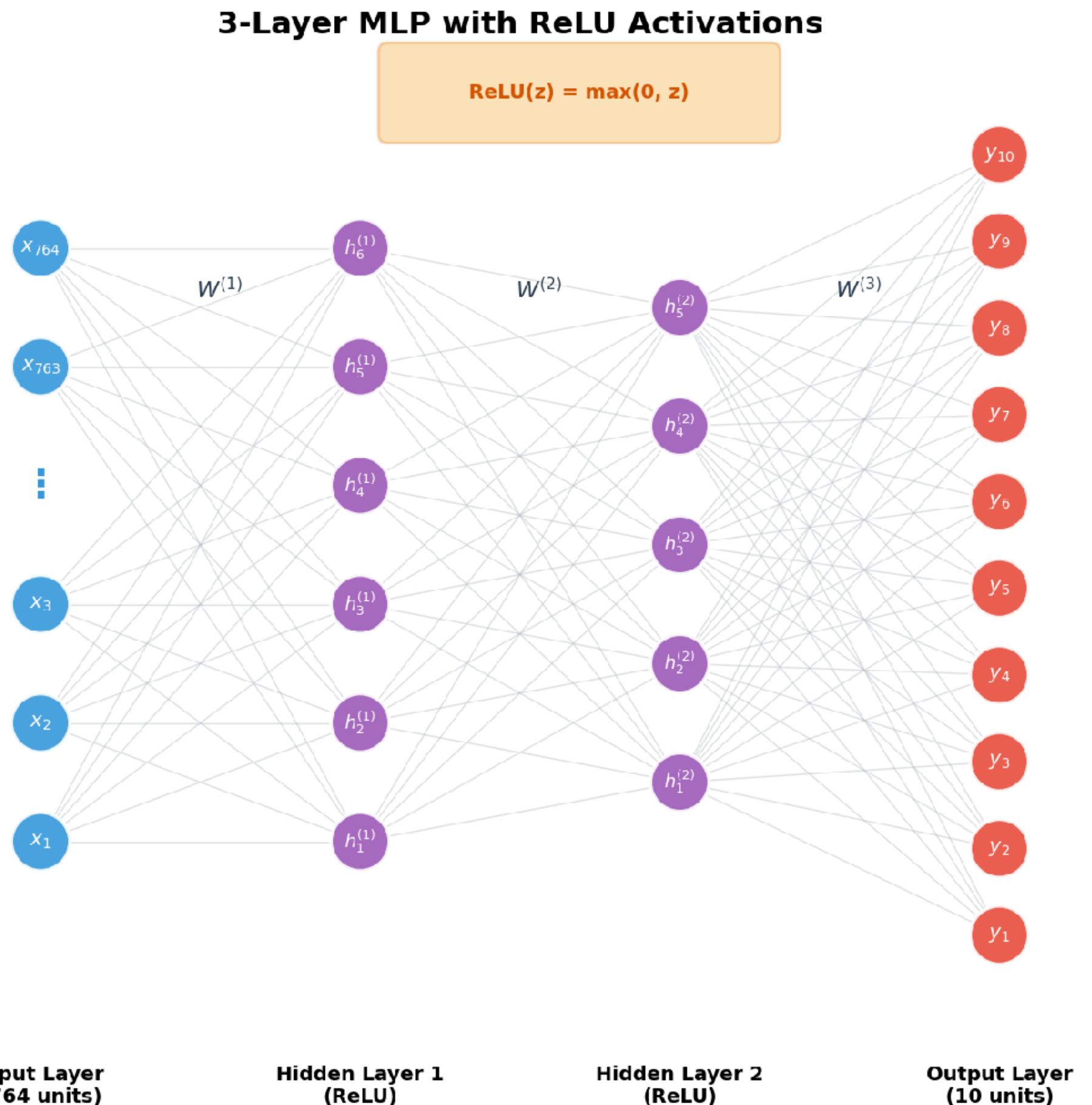
Hidden Layer 1
(ReLU)

Hidden Layer 2
(ReLU)

Output Layer
(10 units)

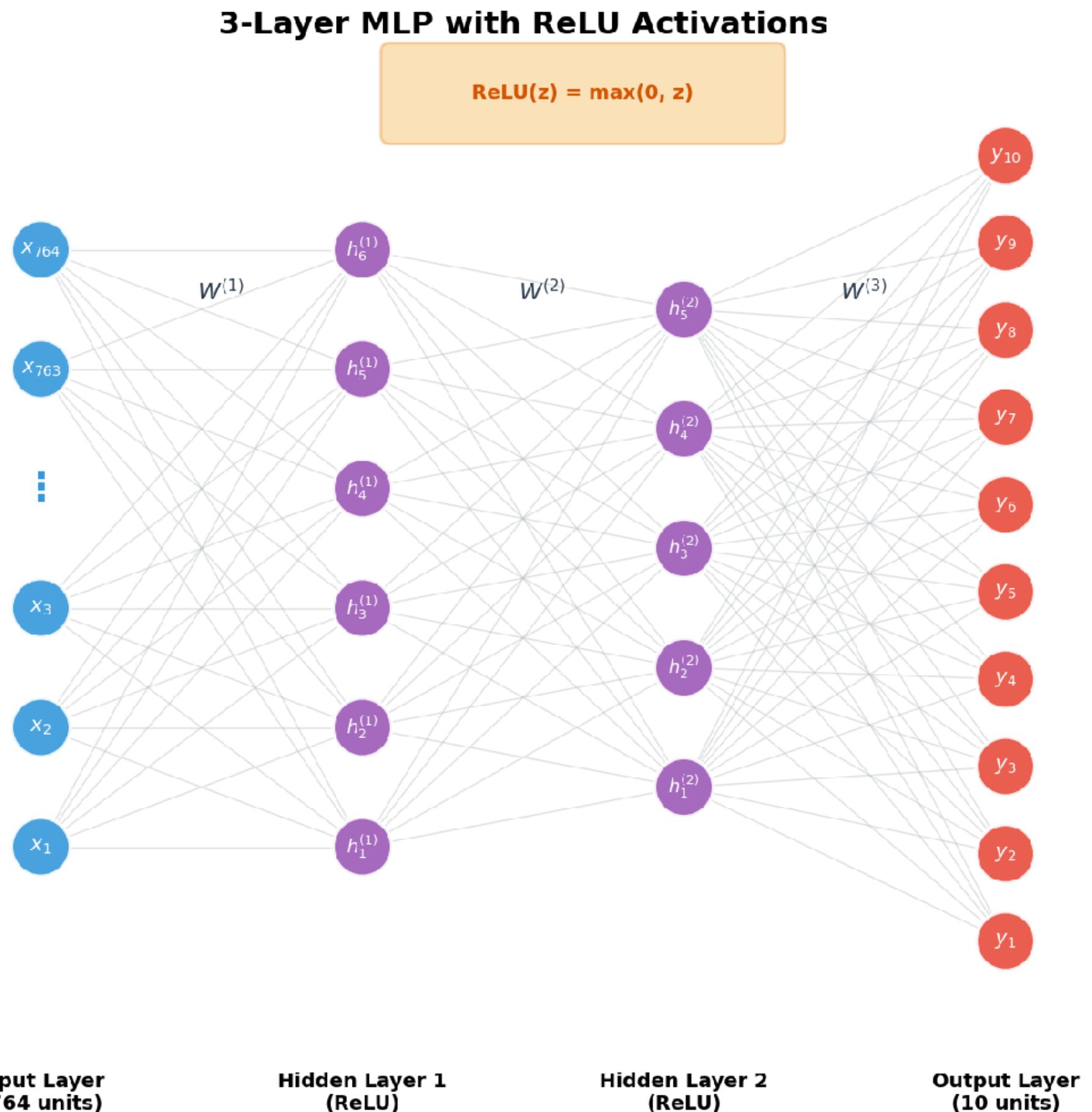
- Why 2 hidden layers?

Your First Deep Network: Why?



- Why 2 hidden layers?
- Why do we need a “ReLU”?

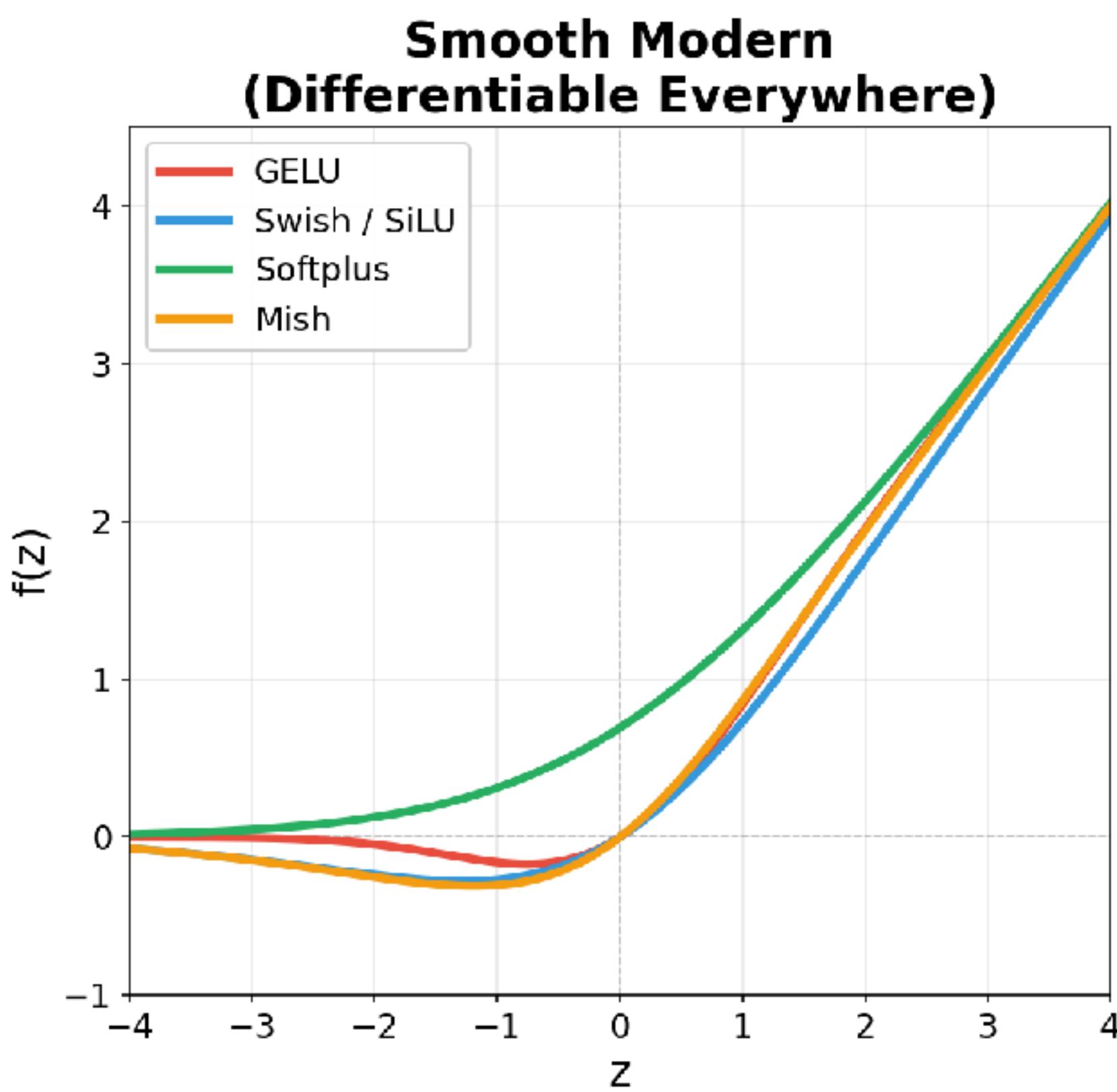
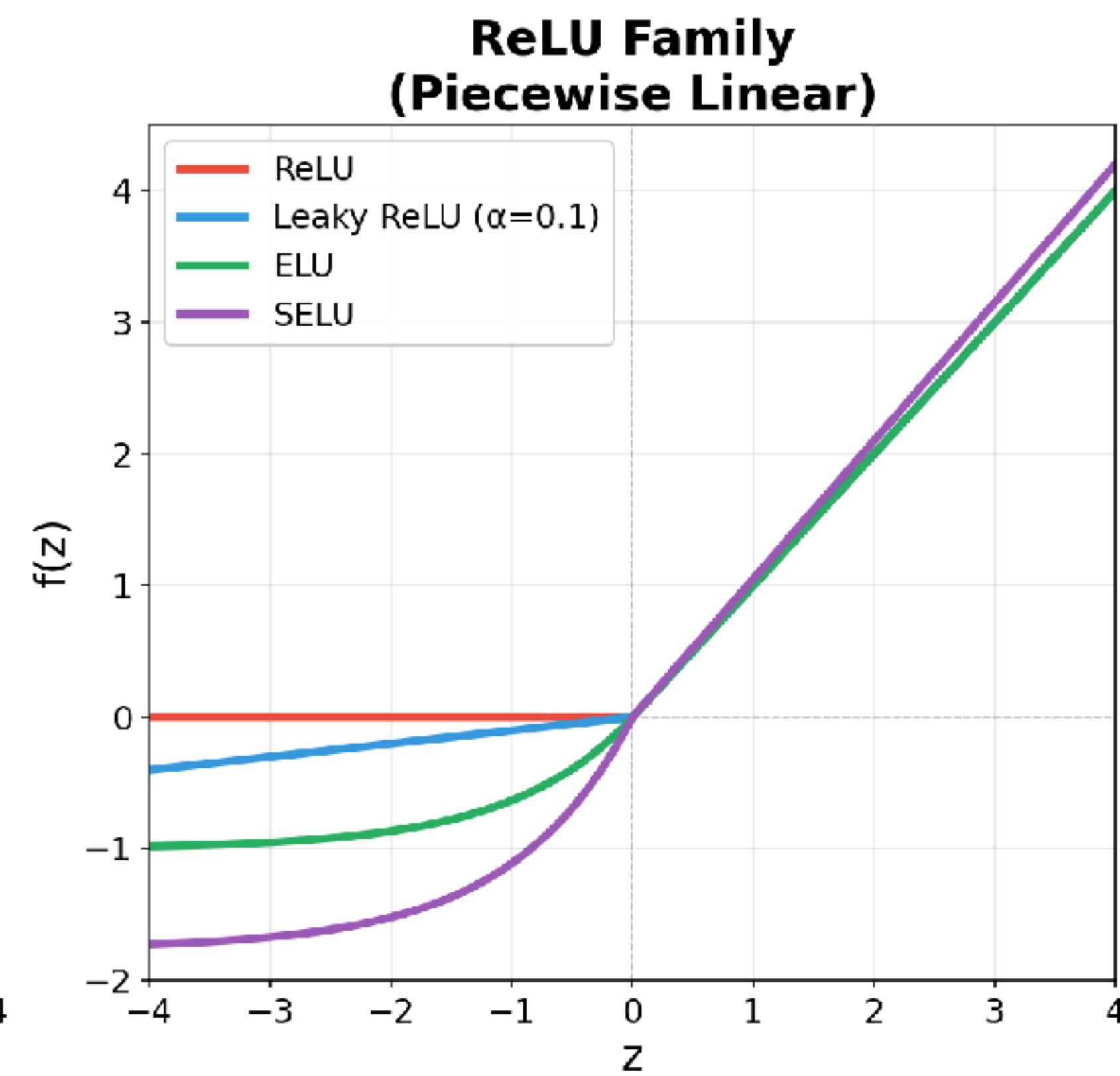
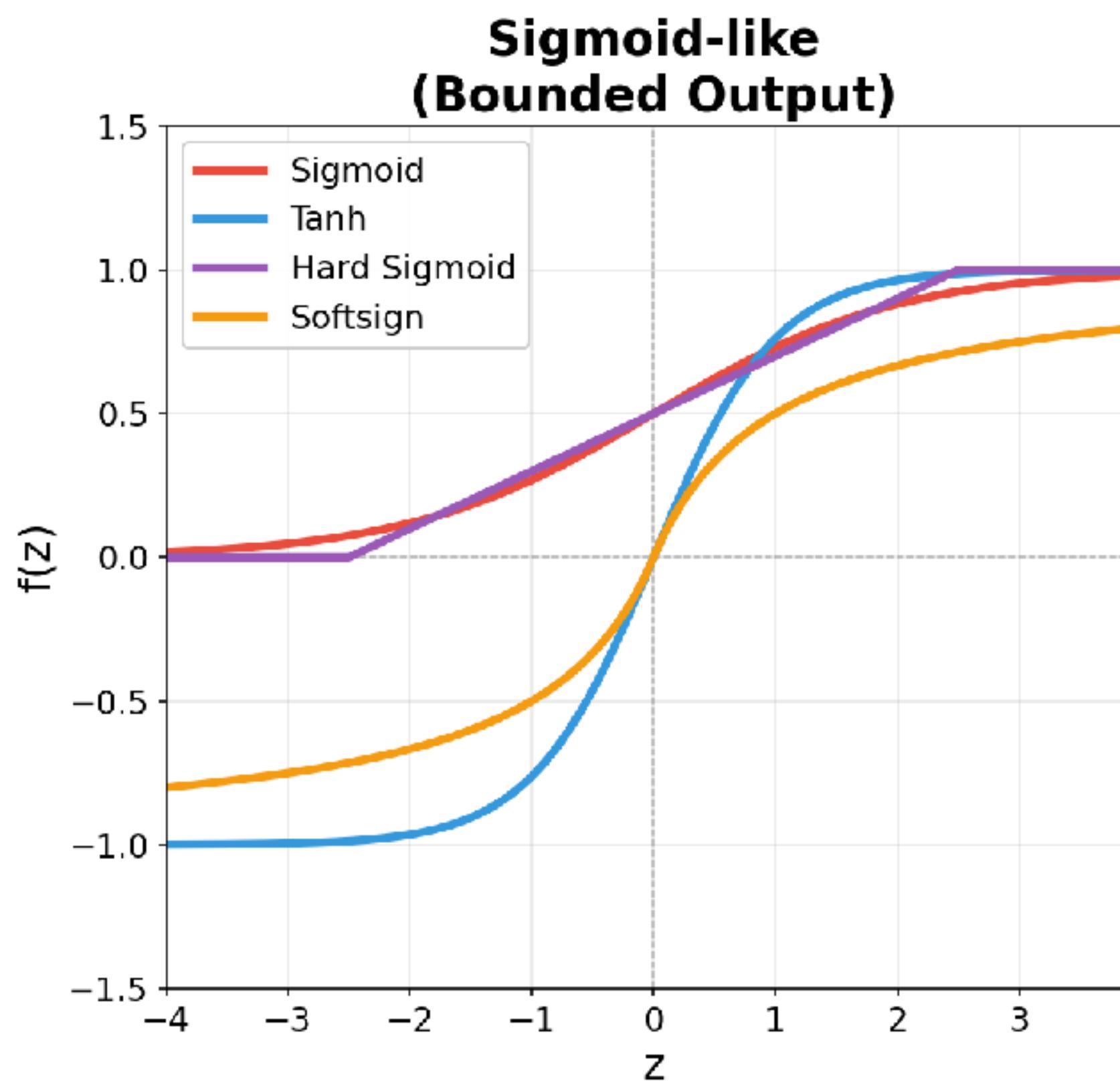
Your First Deep Network: Why?



- Why 2 hidden layers?
- Why do we need a “ReLU”?
- What else besides a “ReLU”?

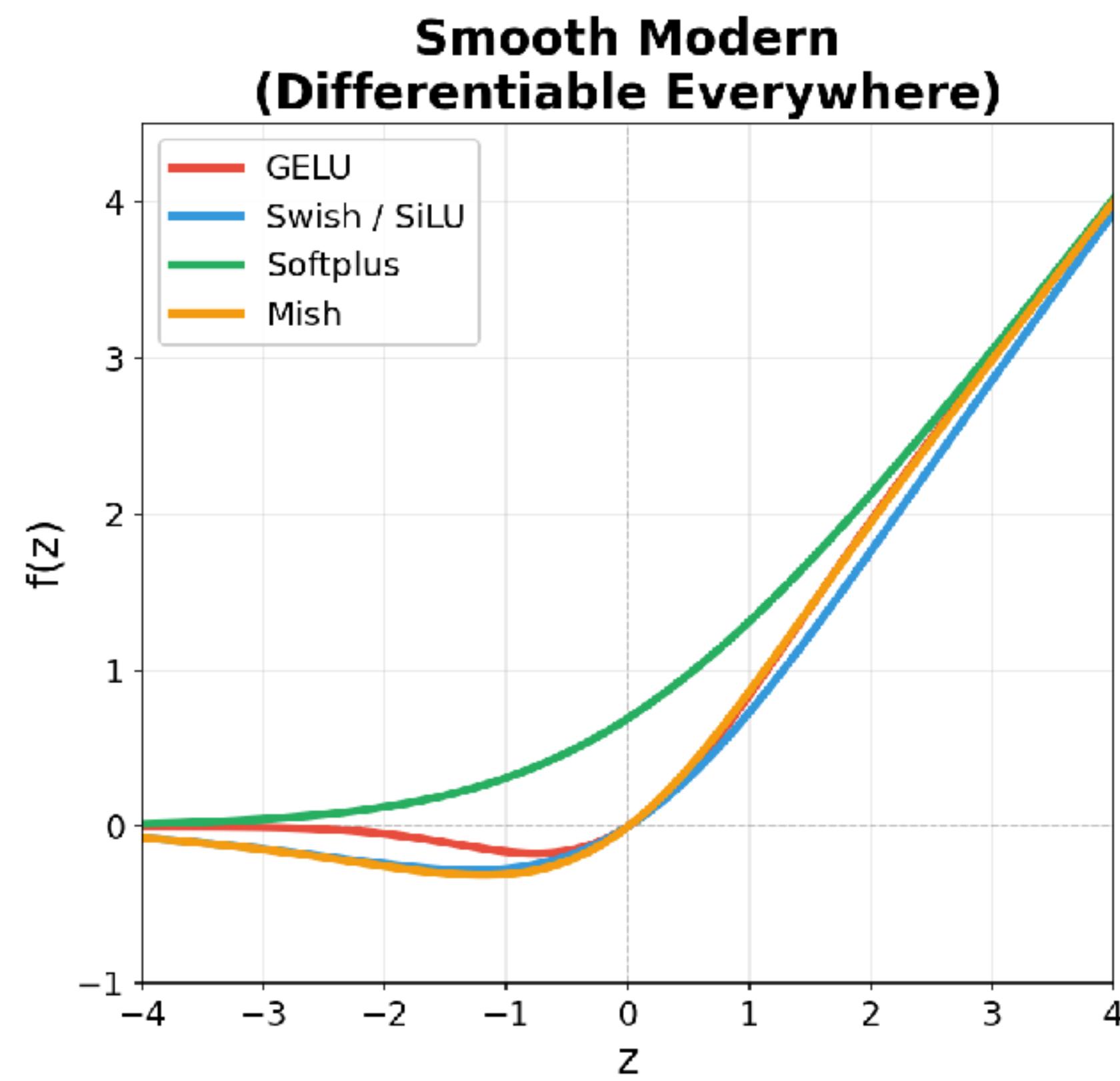
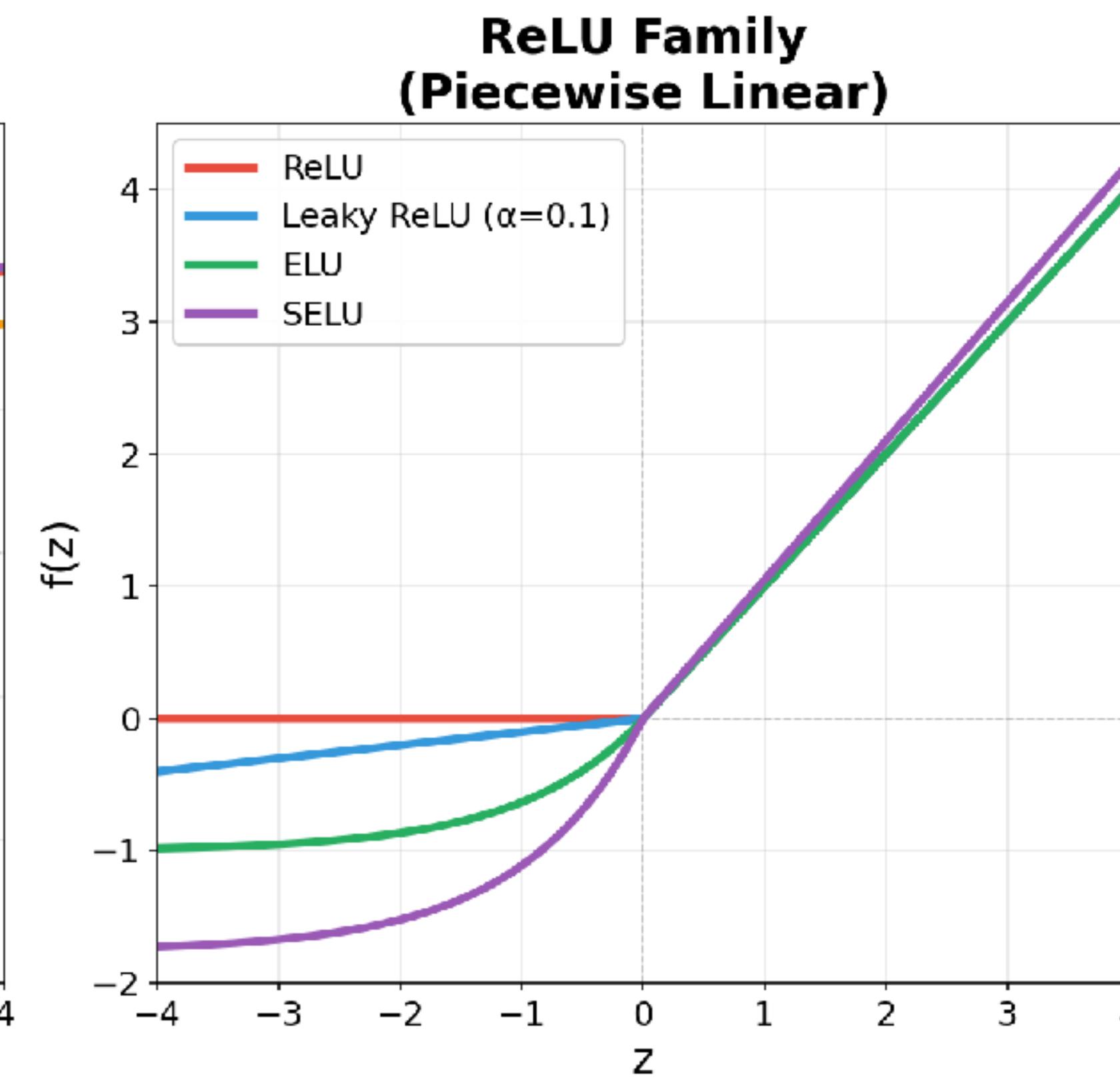
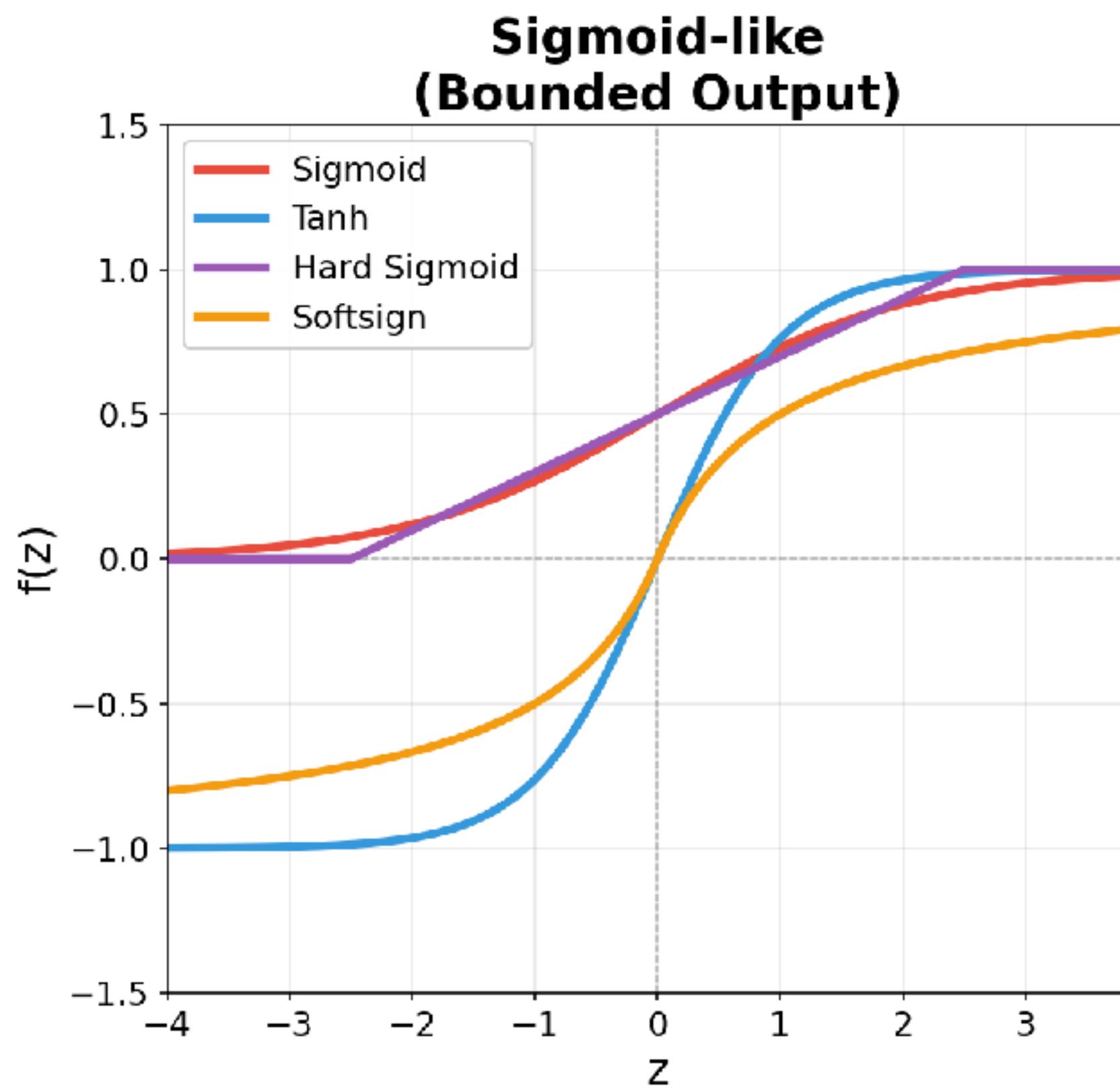
Your First Deep Network: Why?

Common Activation Functions in Neural Networks



Your First Deep Network: Why?

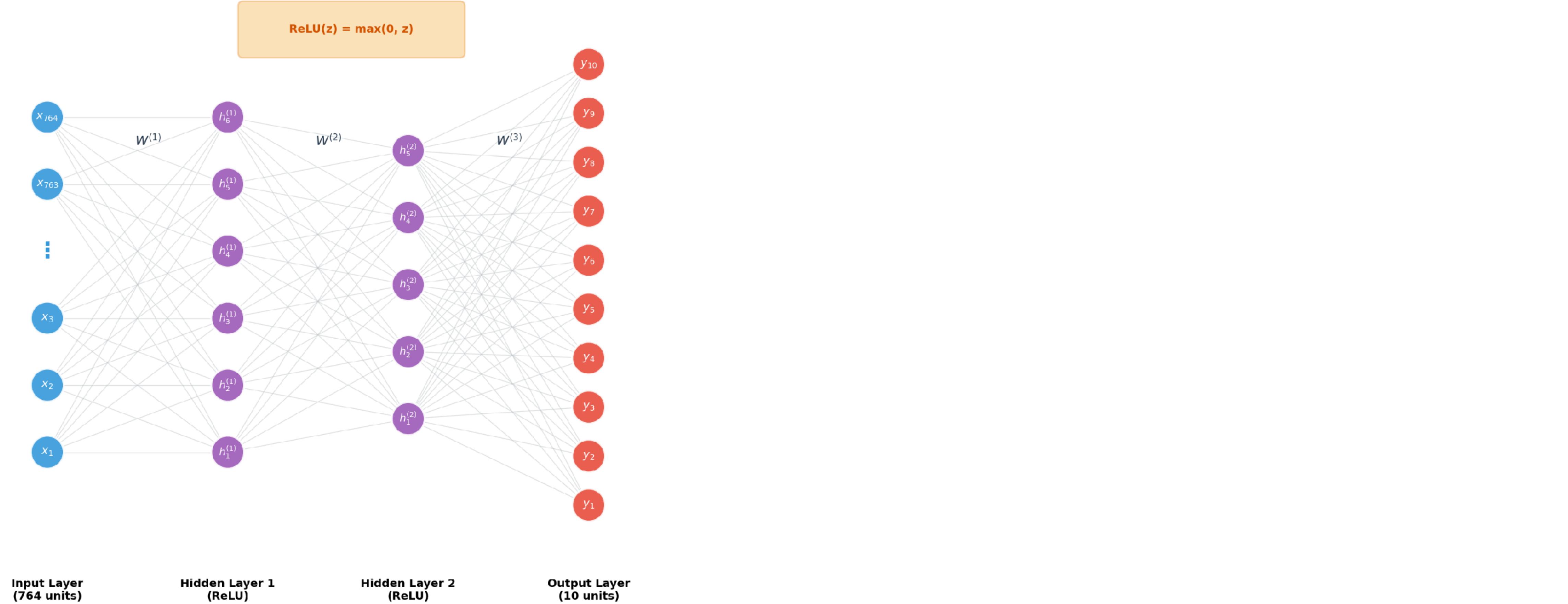
Common Activation Functions in Neural Networks



Can you think of “problems” for some of them?

Your First Deep Network!

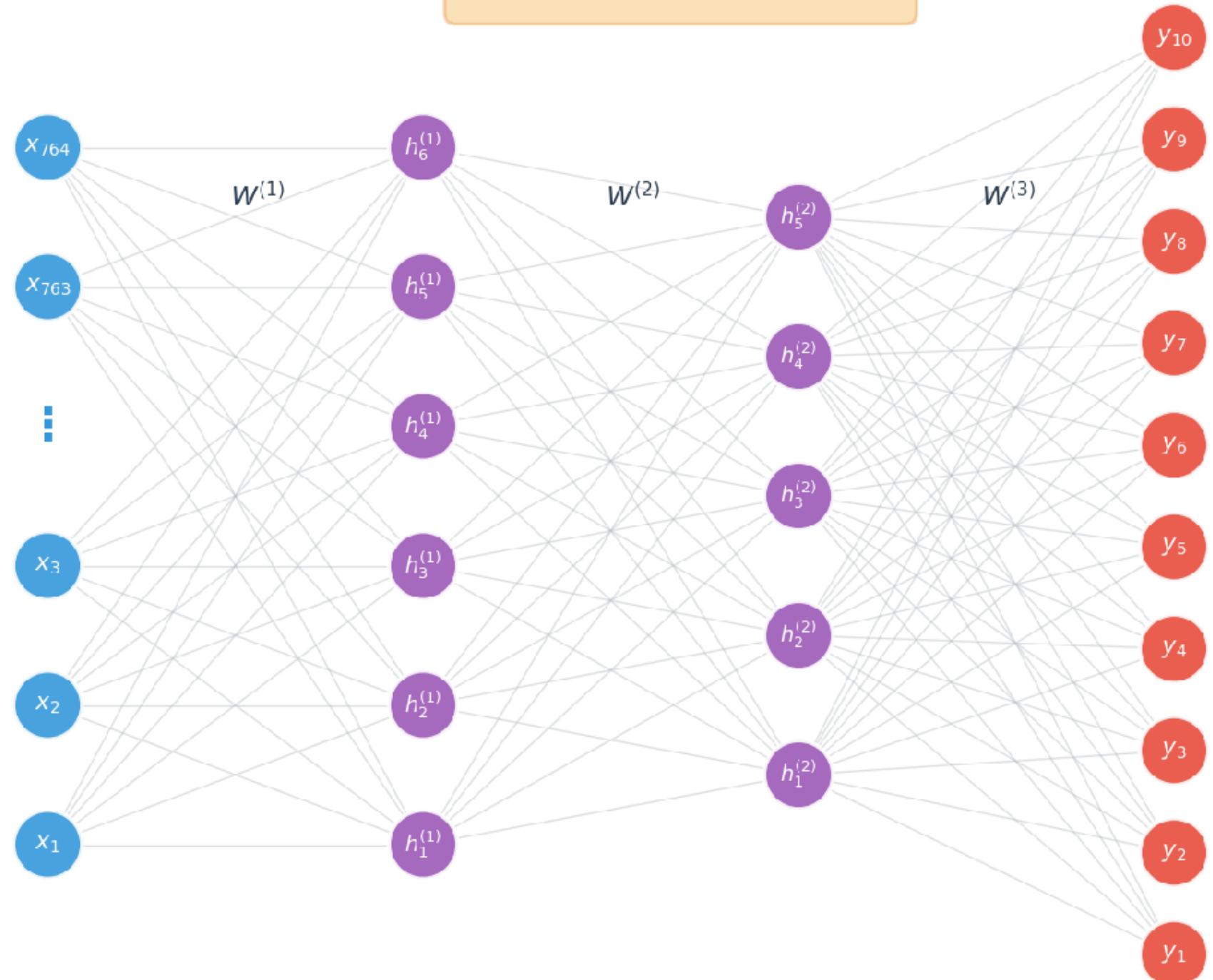
3-Layer MLP with ReLU Activations



Your First Deep Network!

3-Layer MLP with ReLU Activations

$$\text{ReLU}(z) = \max(0, z)$$



What training loss?

Input Layer
(764 units)

Hidden Layer 1
(ReLU)

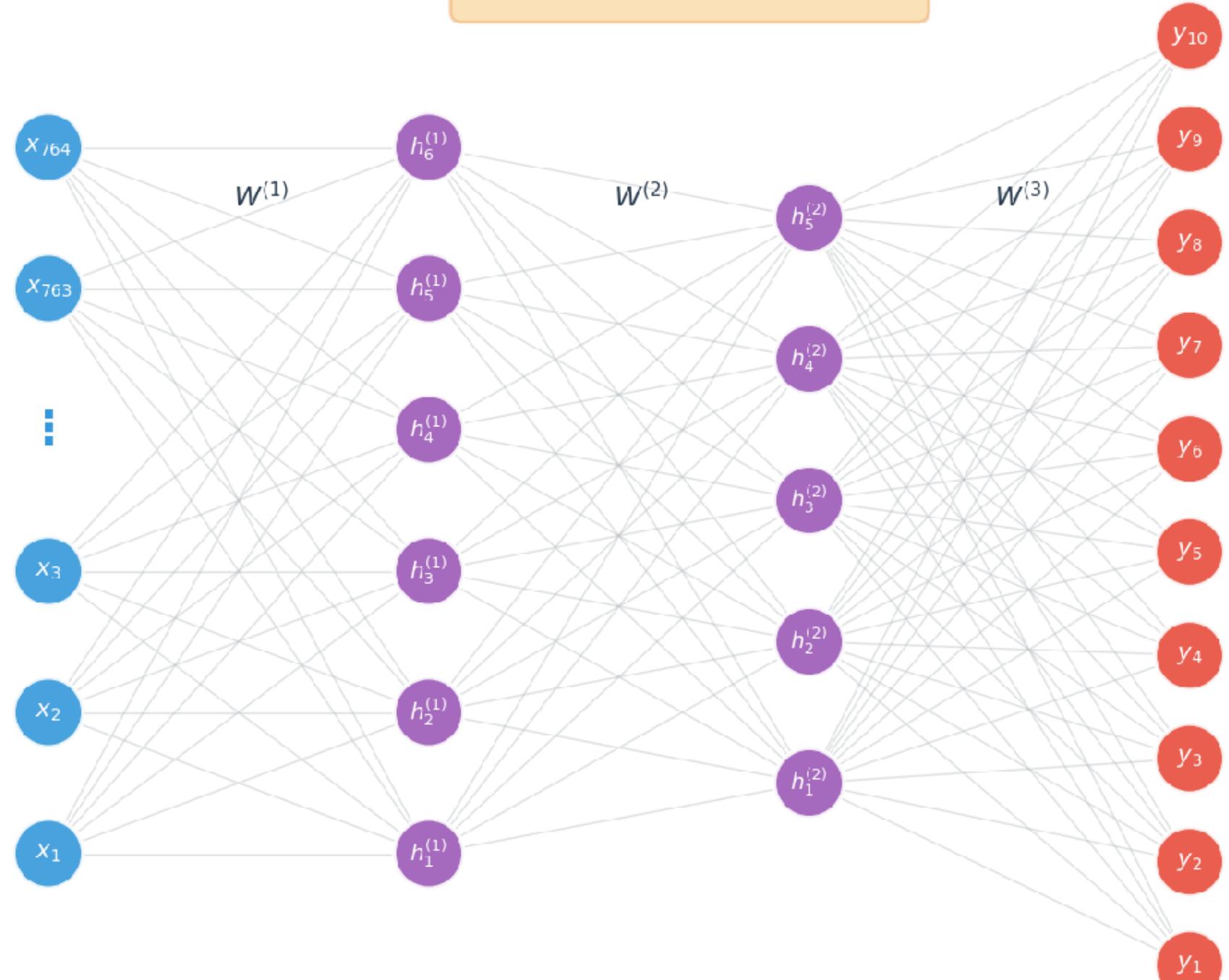
Hidden Layer 2
(ReLU)

Output Layer
(10 units)

Your First Deep Network!

3-Layer MLP with ReLU Activations

$$\text{ReLU}(z) = \max(0, z)$$



What training loss?

$$p(y = 9 | x_n)$$

Input Layer
(764 units)

Hidden Layer 1
(ReLU)

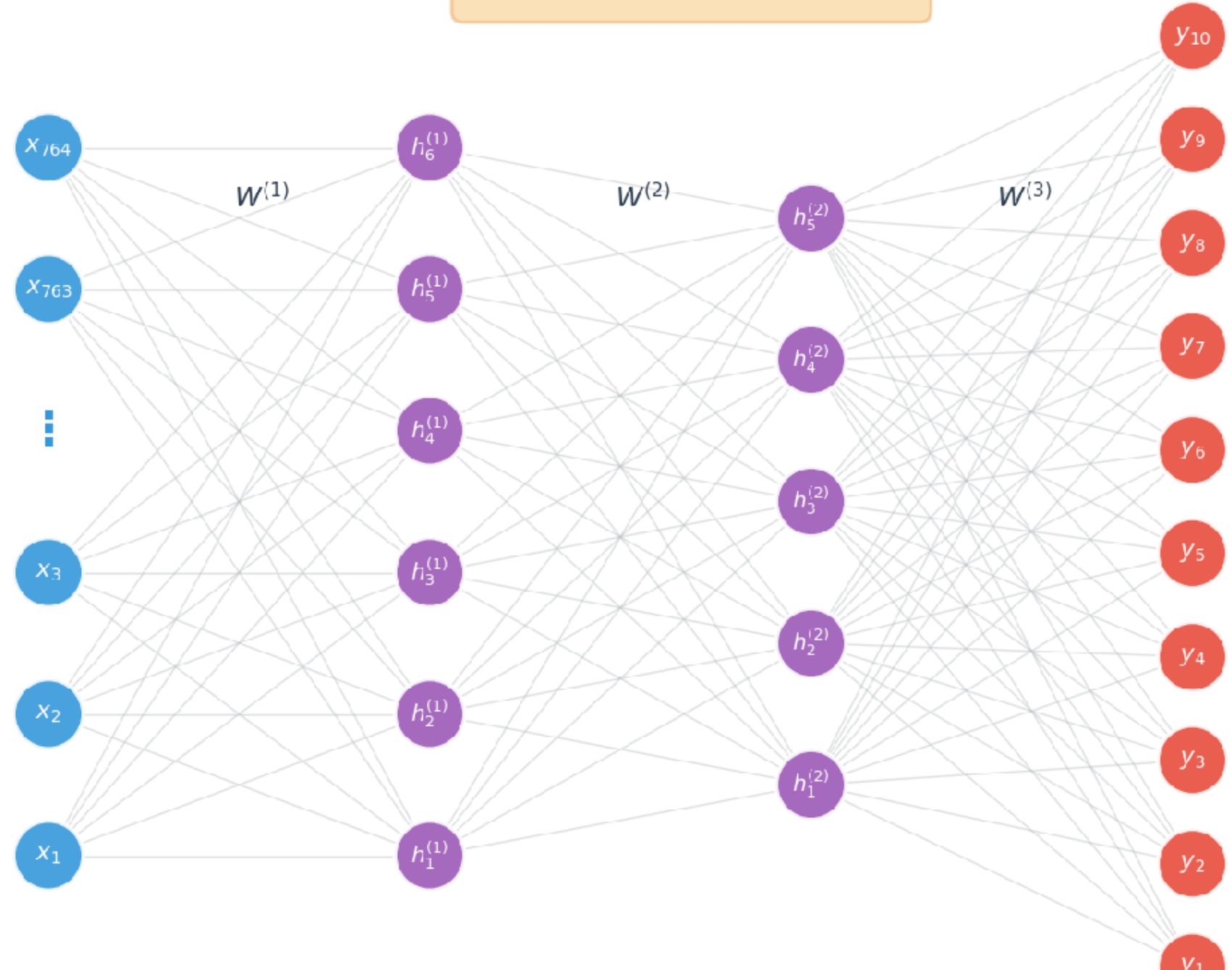
Hidden Layer 2
(ReLU)

Output Layer
(10 units)

Your First Deep Network!

3-Layer MLP with ReLU Activations

$$\text{ReLU}(z) = \max(0, z)$$



What training loss?

$$p(y = 9 | x_n)$$

$$\mathcal{L} = - \sum_{n=1}^N \sum_{c=1}^{10} 1_{\{y_n=c\}} \log(p(y = c | x_n))$$

Input Layer
(764 units)

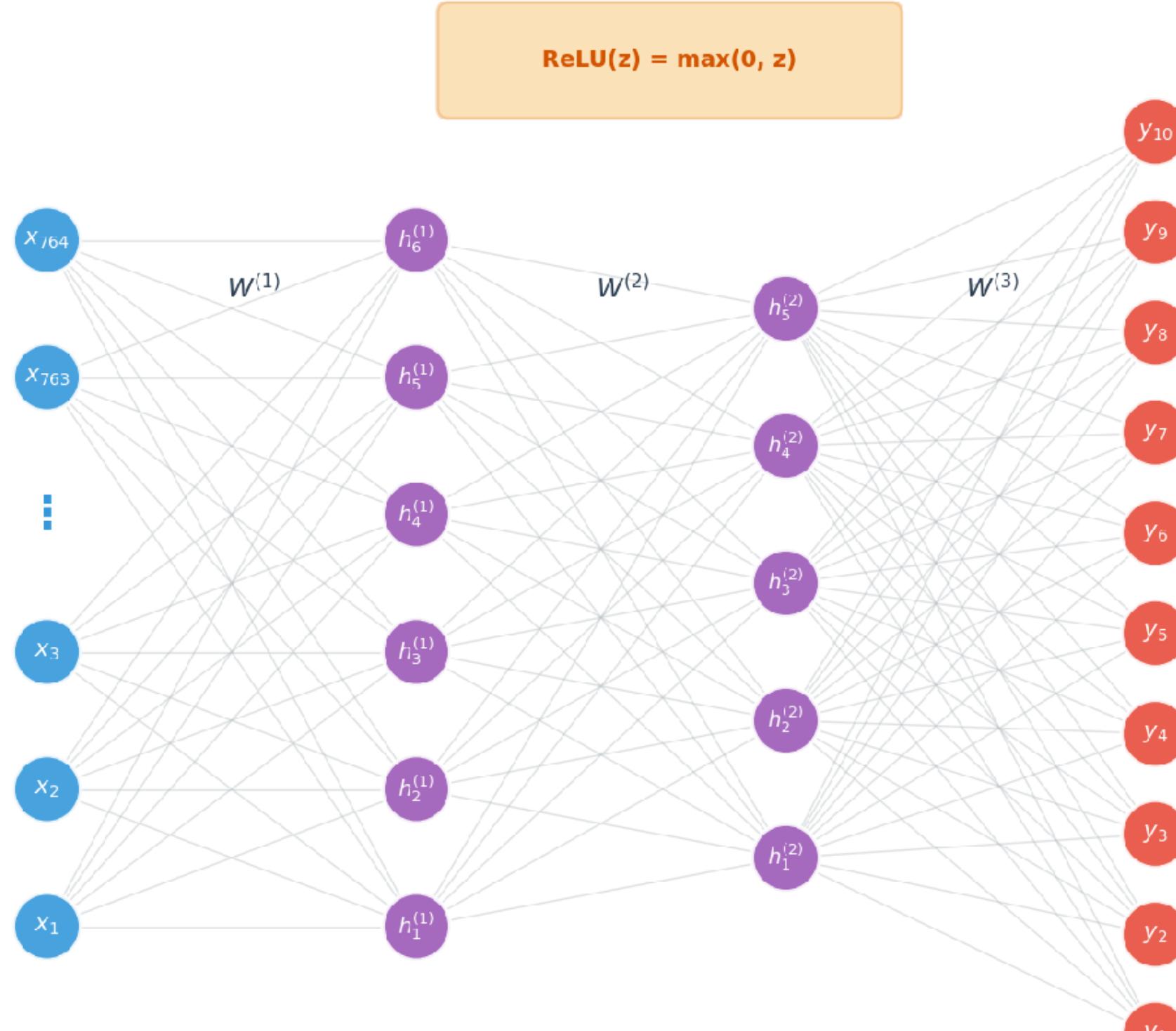
Hidden Layer 1
(ReLU)

Hidden Layer 2
(ReLU)

Output Layer
(10 units)

Your First Deep Network!

3-Layer MLP with ReLU Activations



What training loss?

$$p(y = 9 | x_n)$$

$$\mathcal{L} = - \sum_{n=1}^N \sum_{c=1}^{10} 1_{\{y_n=c\}} \log(p(y = c | x_n))$$

$$\hat{y}_n = \arg \max_{c=1, \dots, 10} p(y = c | x_n)$$

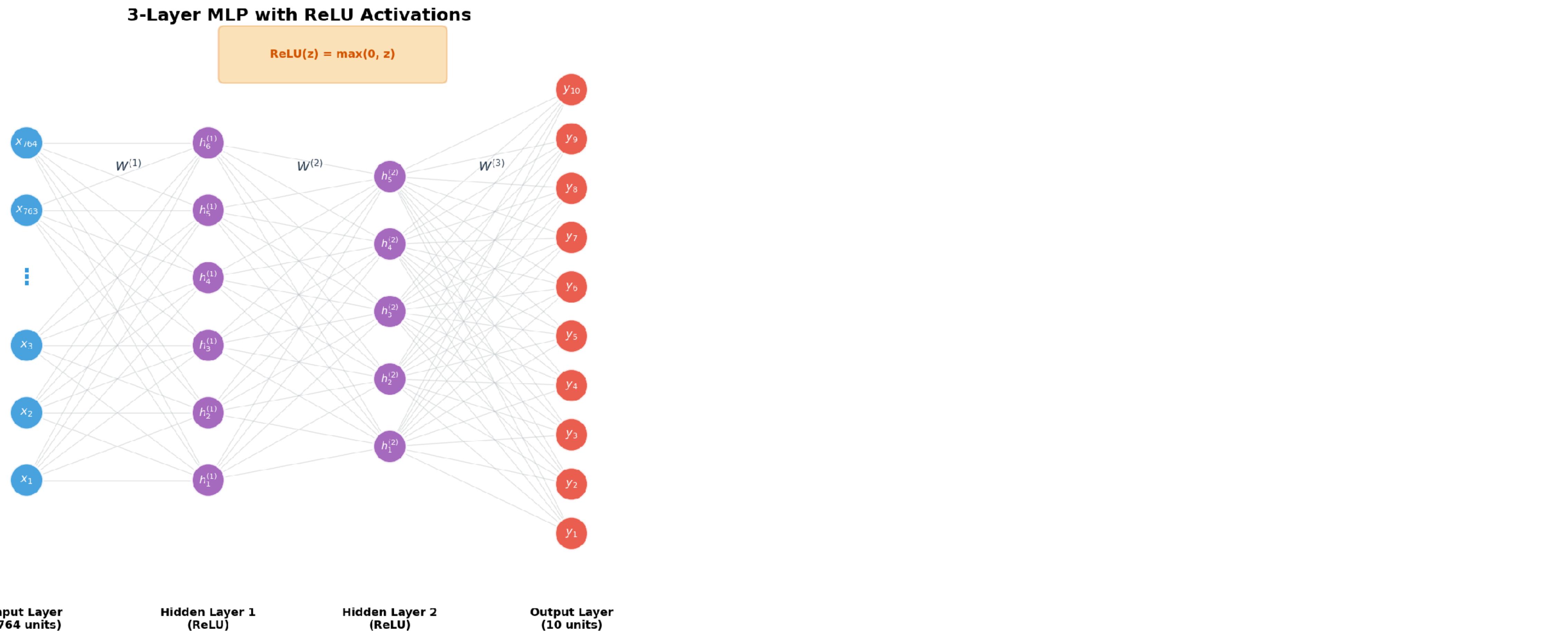
**Input Layer
(764 units)**

**Hidden Layer 1
(ReLU)**

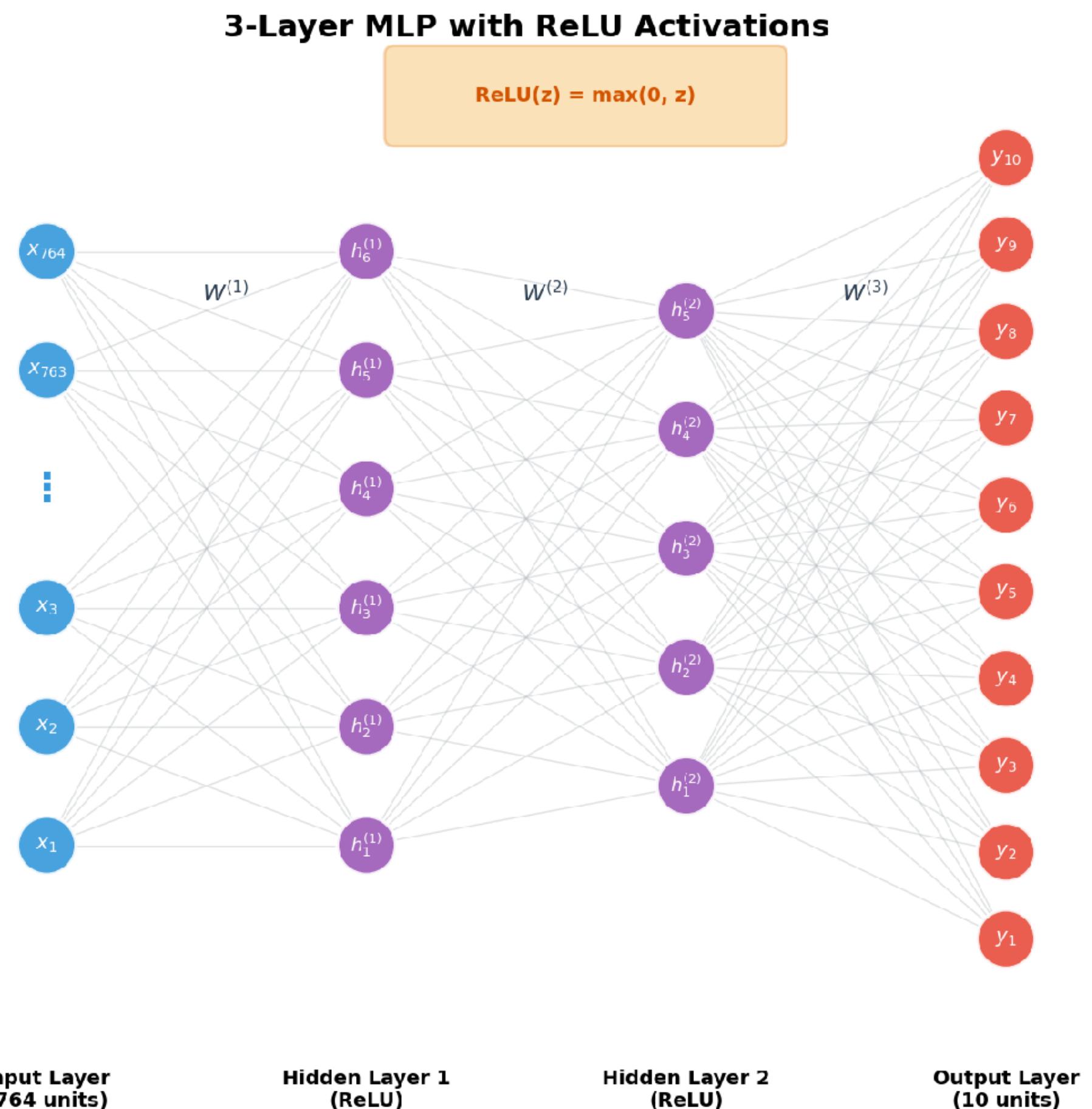
**Hidden Layer 2
(ReLU)**

**Output Layer
(10 units)**

Your First Deep Network: Training

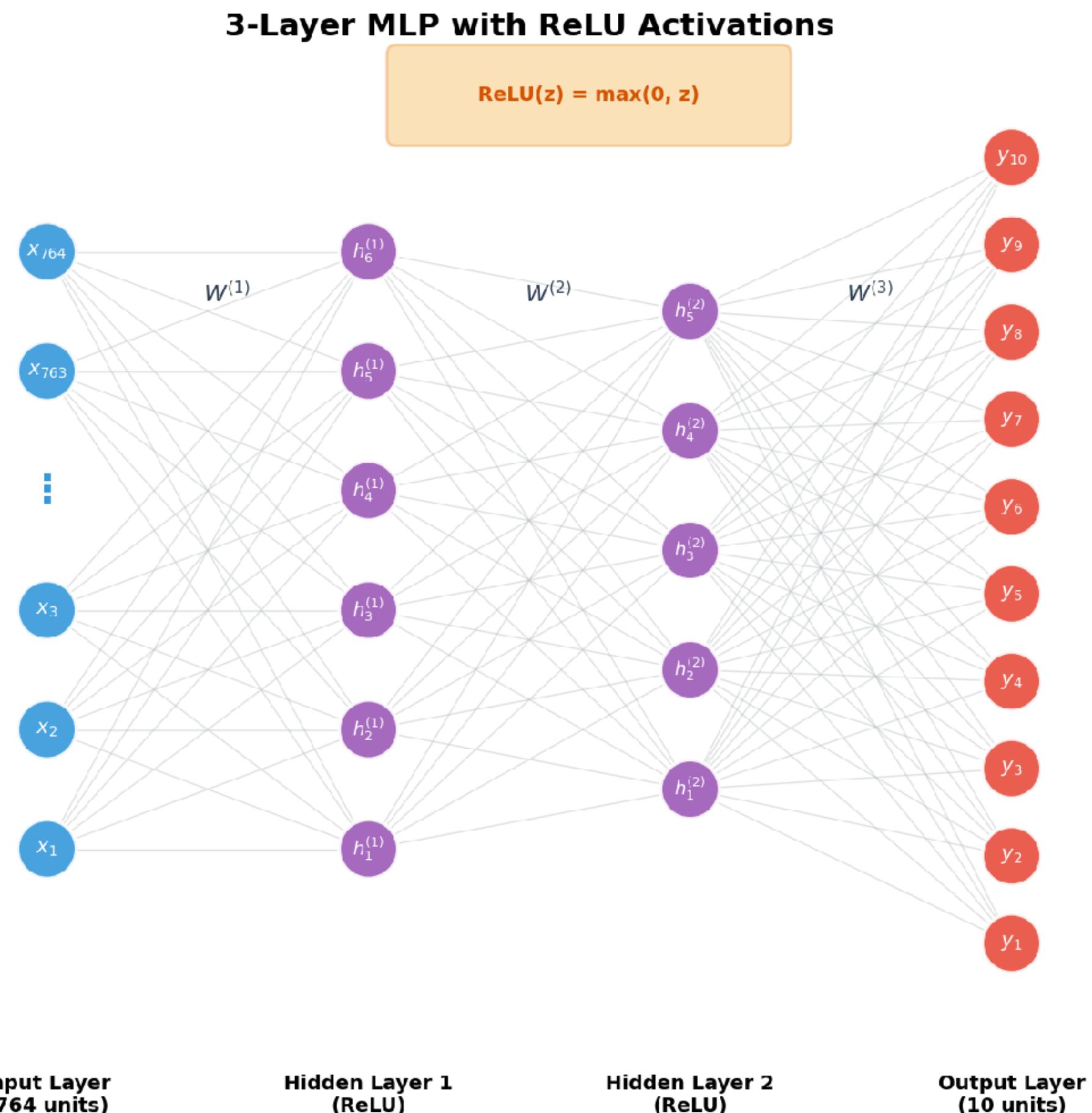


Your First Deep Network: Training



How to train the parameters $W^{(1)}, W^{(2)}, W^{(3)}$?

Your First Deep Network: Training



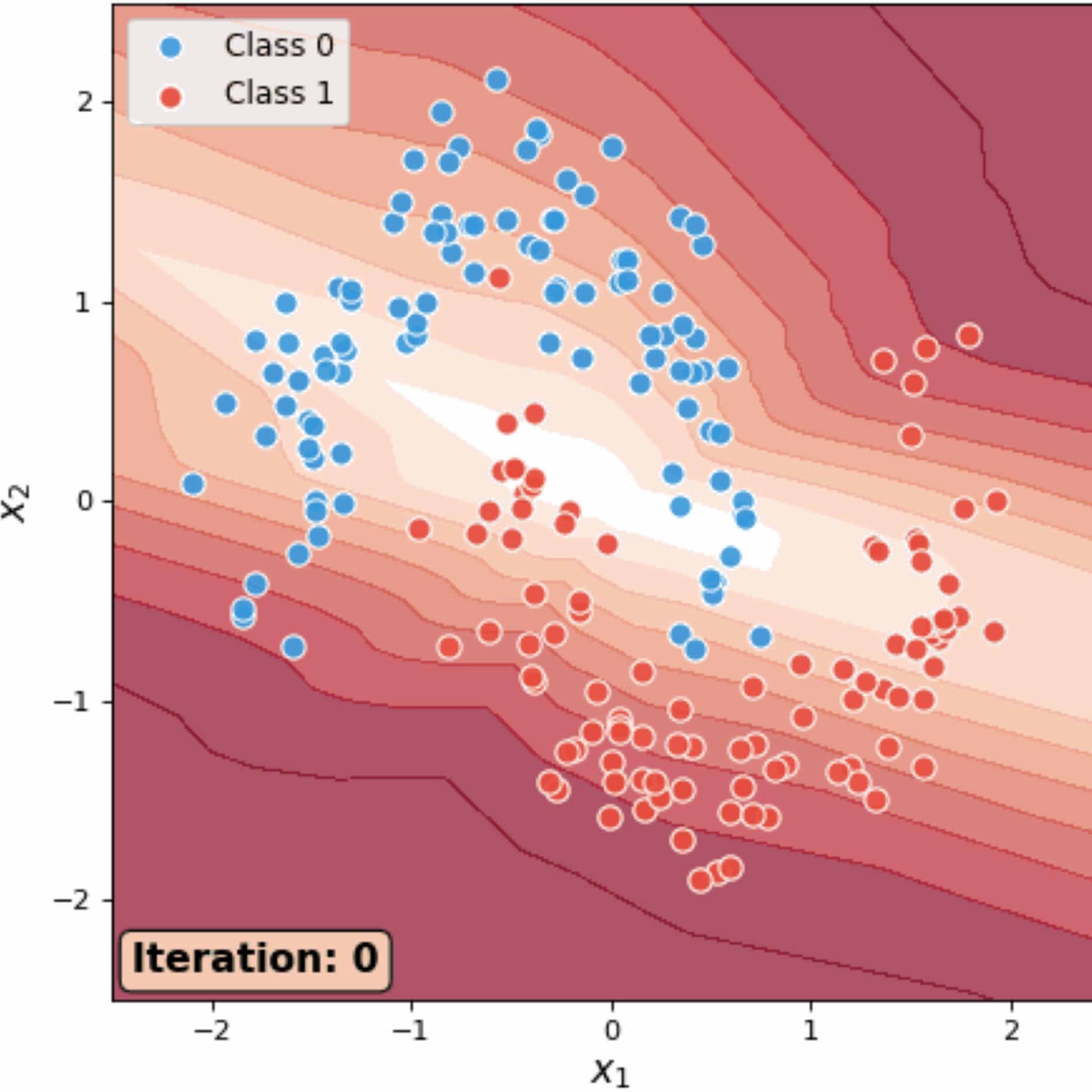
How to train the parameters $W^{(1)}, W^{(2)}, W^{(3)}$?

Same old gradient descent!

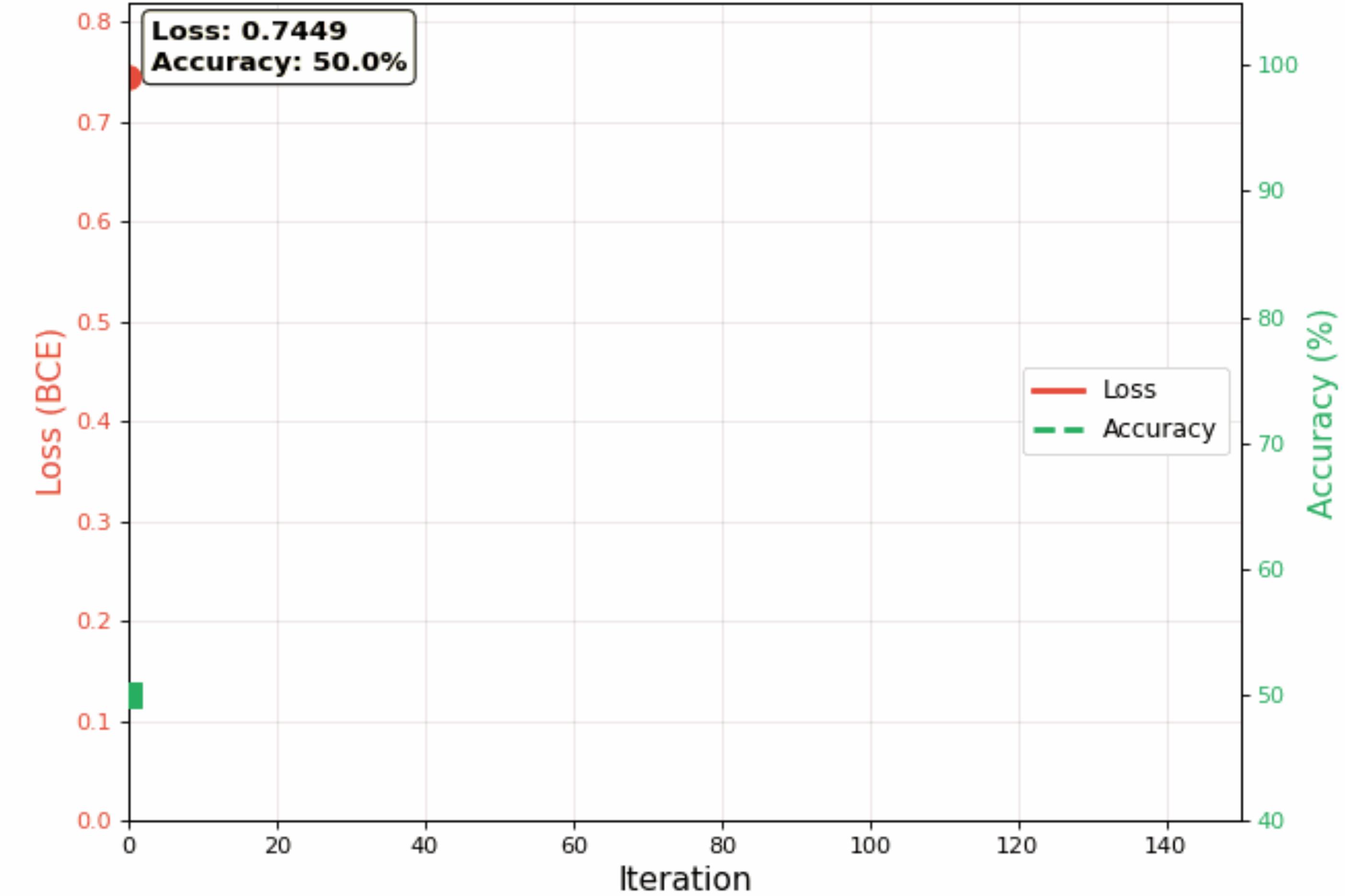
At home: try to derive the gradient for those 3 matrices

Your First Deep Network: Action!

MLP Decision Boundary (Nonlinear)

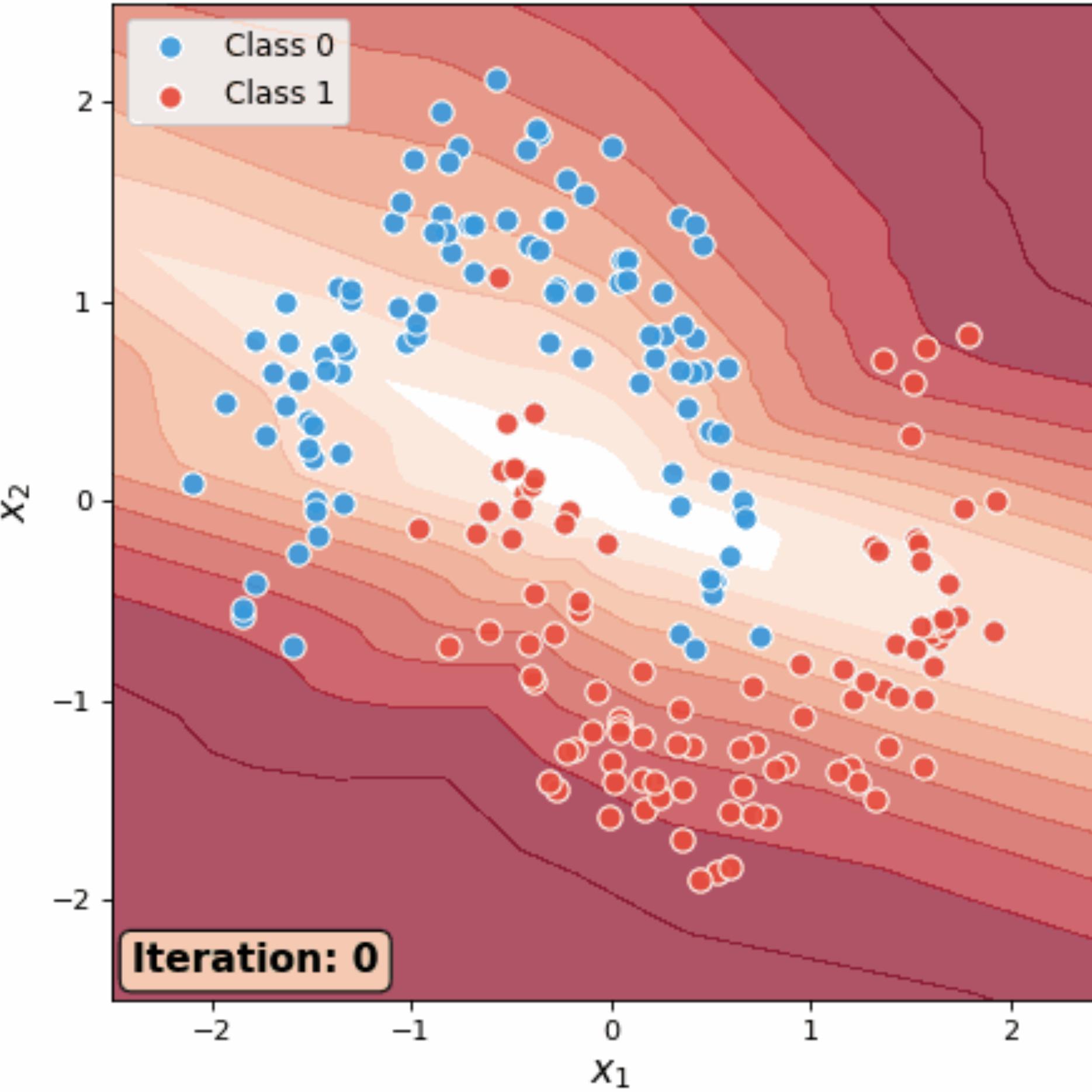


Training Progress

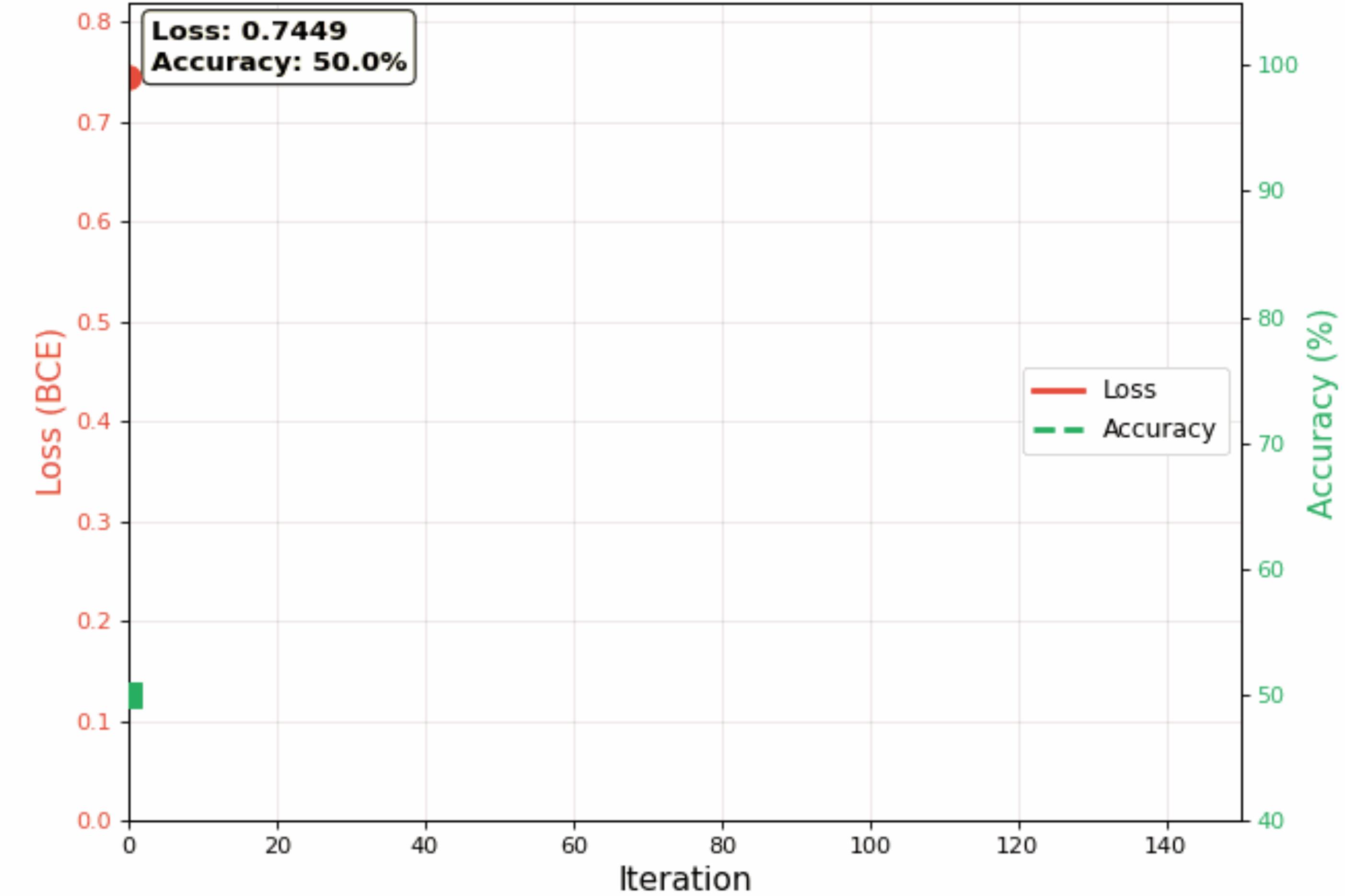


Your First Deep Network: Action!

MLP Decision Boundary (Nonlinear)



Training Progress



Open Discussion

Open Discussion

- Can a Deep Network solve anything?

Open Discussion

- Can a Deep Network solve anything?
- How to search for the right “architecture”?

Open Discussion

- Can a Deep Network solve anything?
- How to search for the right “architecture”?
- How many lines of codes to implement the MNIST model and reach 99.5%?

Questions?