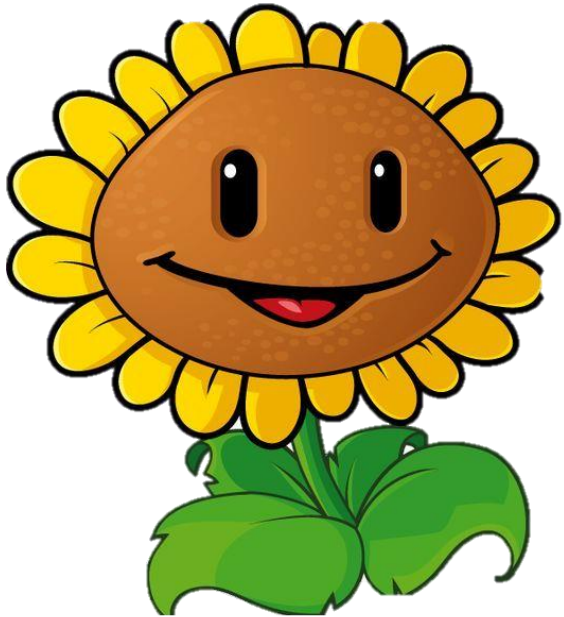
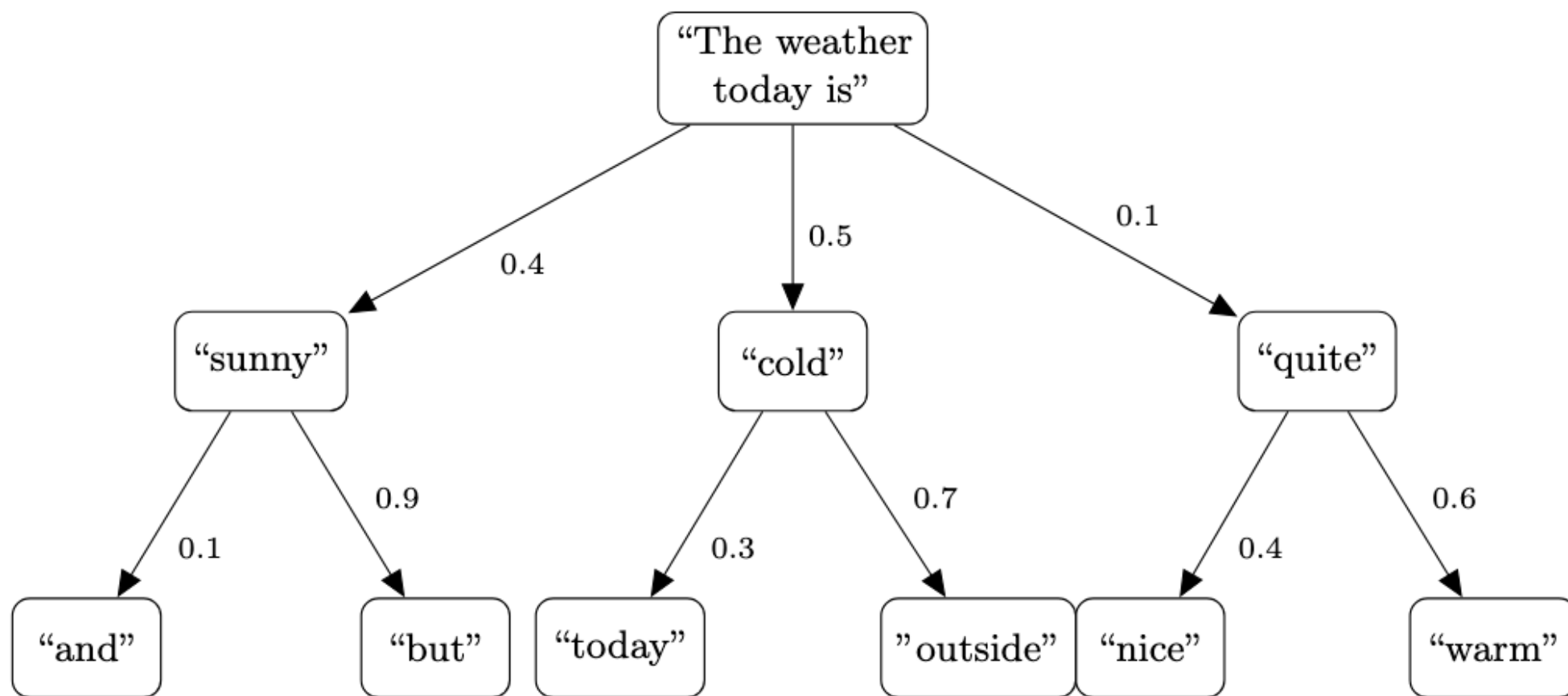


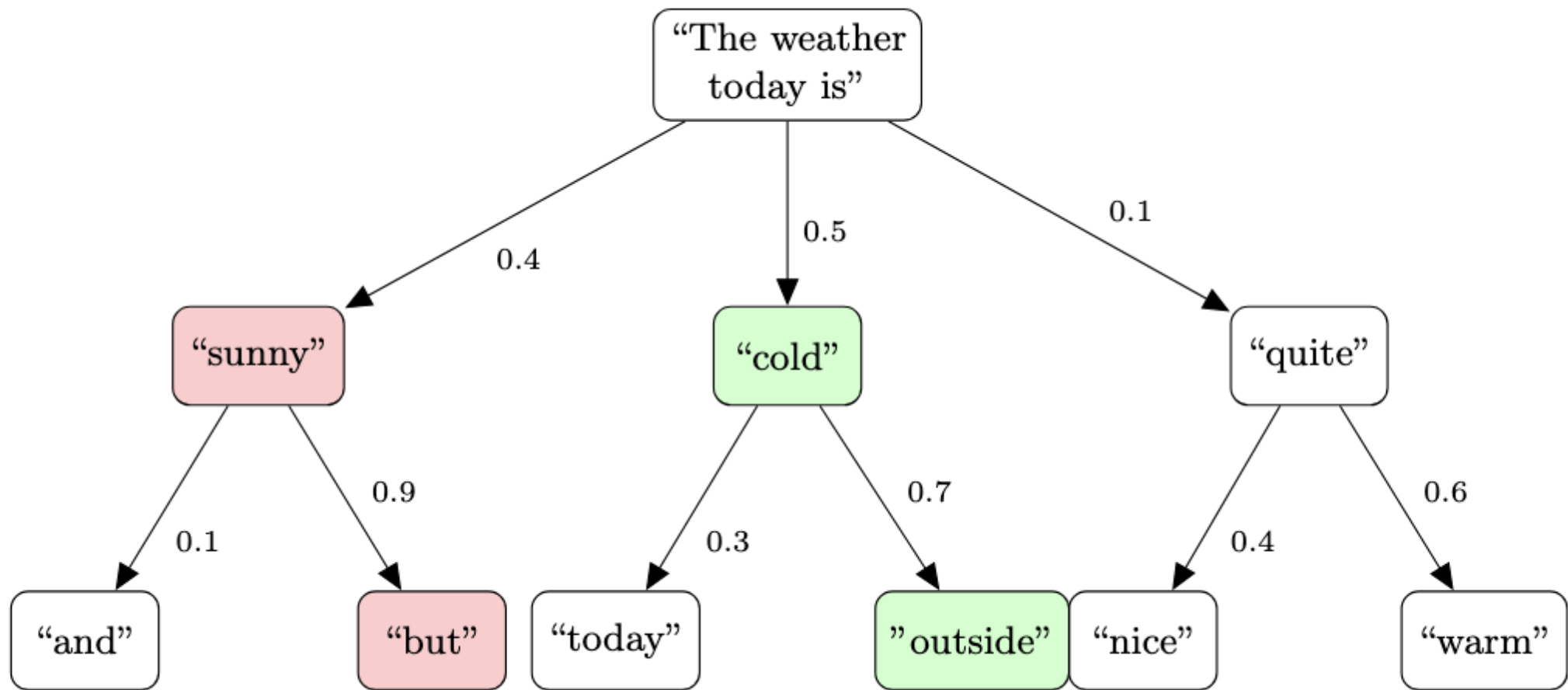
# Informed Search

Eric Ewing



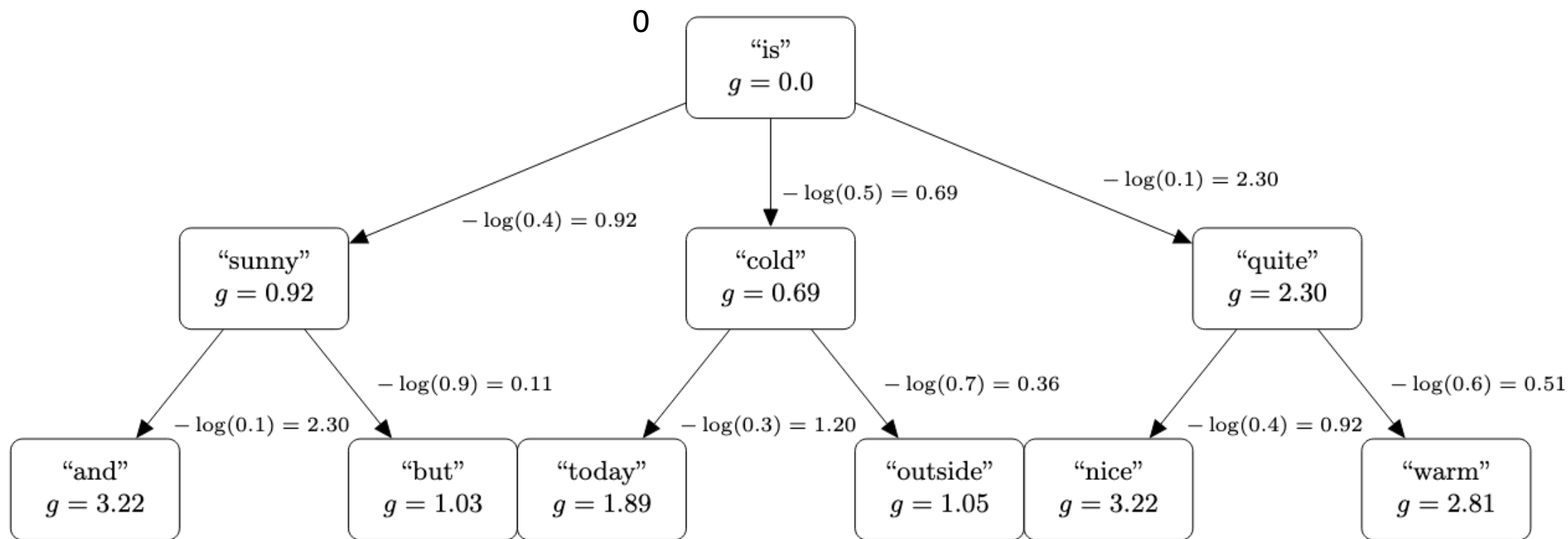


What is the best two word continuation?

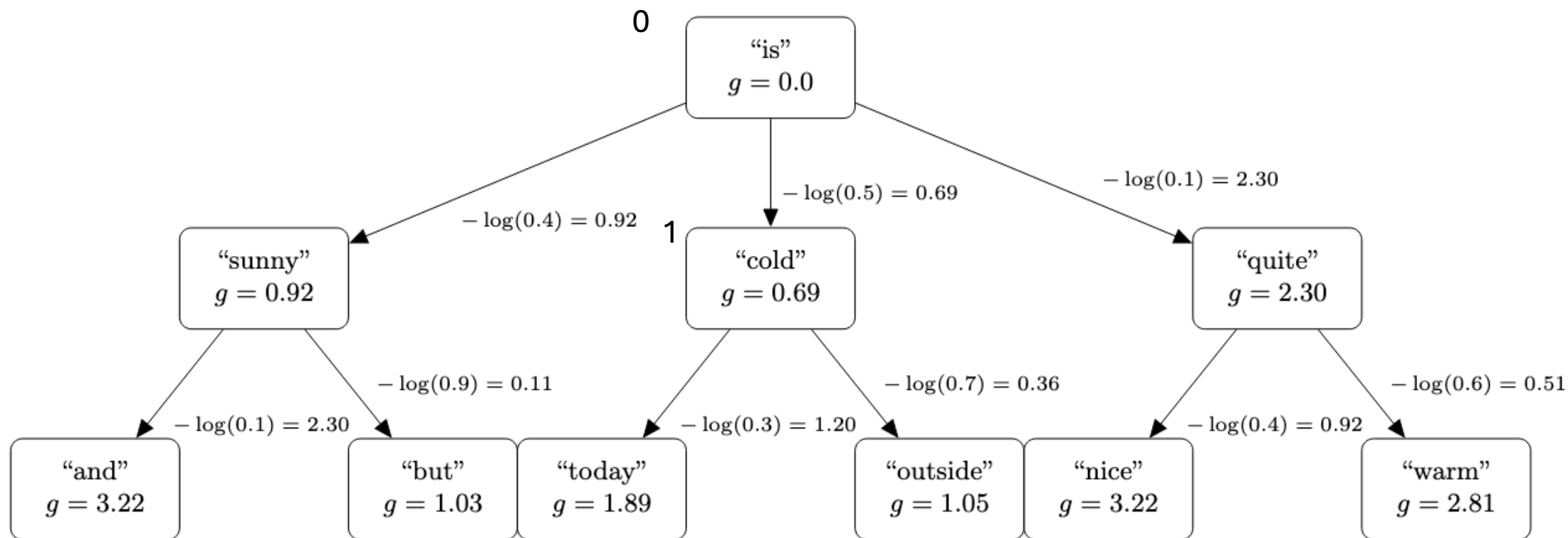


$$P(\text{The weather today is sunny but}) \\ = 0.4 \cdot 0.9 = 0.36$$

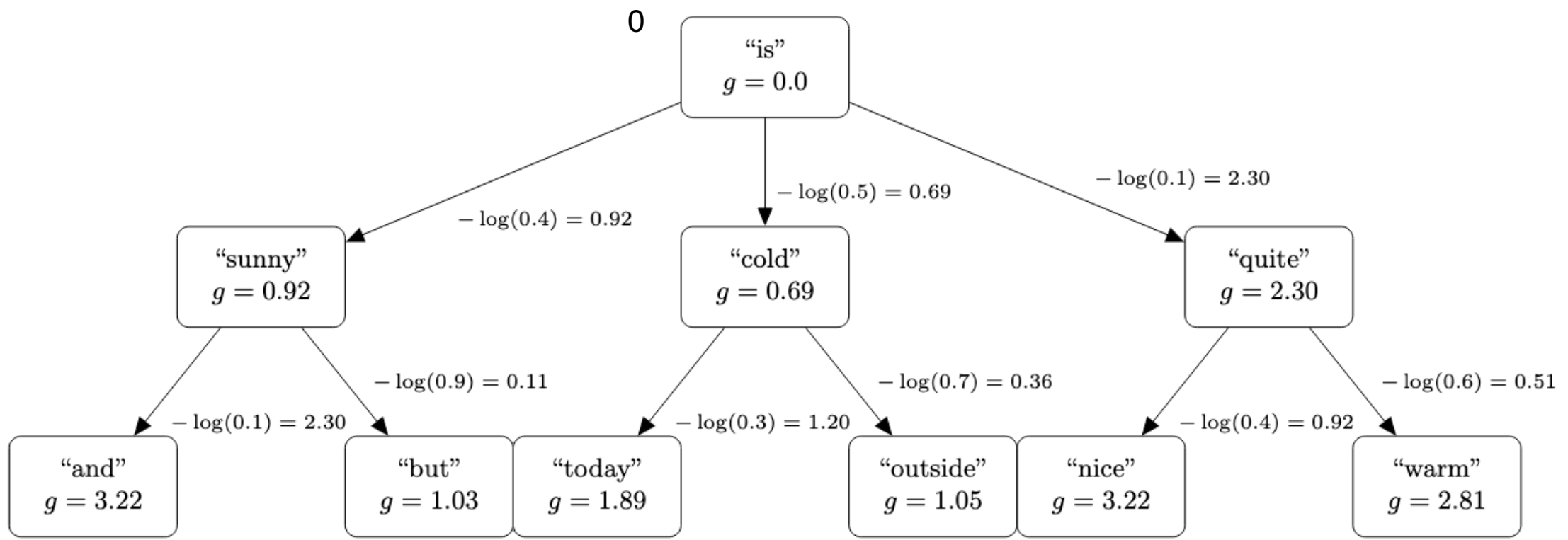
$$P(\text{"The weather today is cold outside"}) \\ = 0.5 \cdot 0.7 = 0.35$$



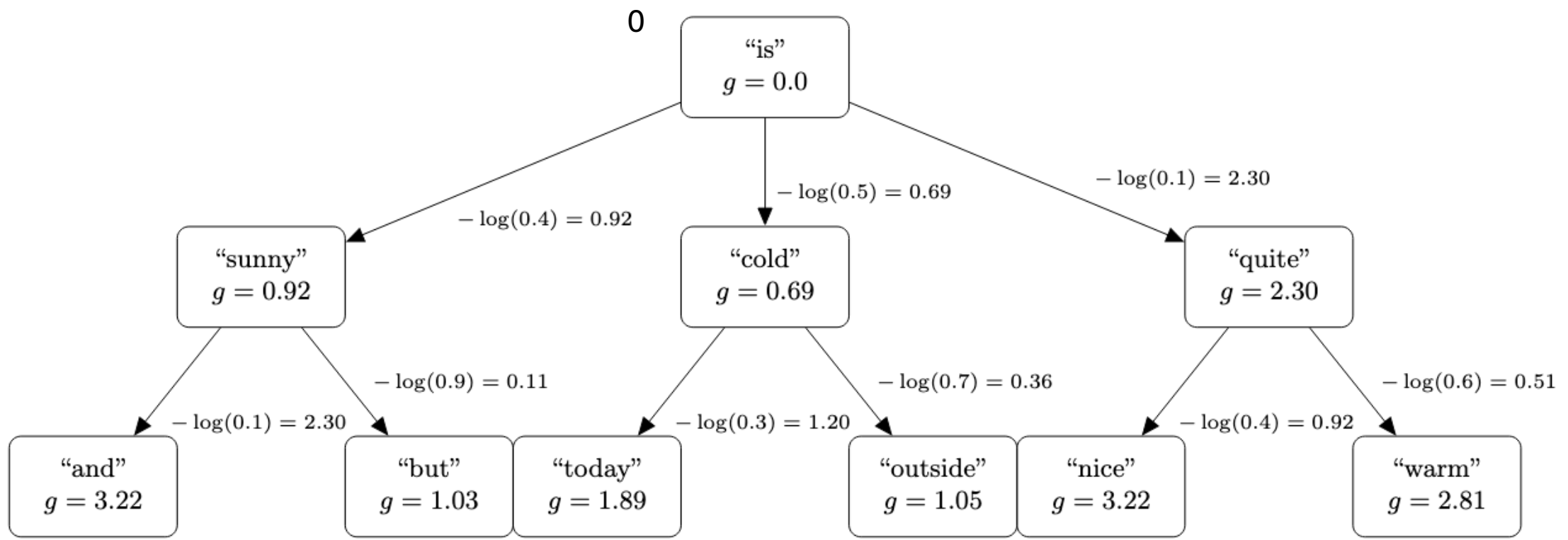
Open Set = [("is", 0)]



Open Set = [(“cold”, 0.69), (“sunny”, 0.92), (“quite”, 2.3)]



Open Set = [(“sunny”, 0.92), (“outside”, 1.05), (“today”, 1.89), (“quite”, 2.3)]



Open Set = [(“but”, 1.03), (“outside”, 1.05), (“today”, 1.89), (“quite”, 2.3), (“and”, 3.22)]

Solving Mazes with Informed Search

		Start			
Goal					



## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[(2, 0), 4]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((1, 3), 3), ((3, 0), 5)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((0, 0), 2), ((3, 0), 5)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((0, 1), 1), ((3, 0), 5)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((1, 1), 2), ((3, 0), 5)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((2, 1), 3), ((3, 0), 5)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((3, 1), 4), ((3, 0), 5)]$



## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((3, 0), 5), ((4, 1), 5)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

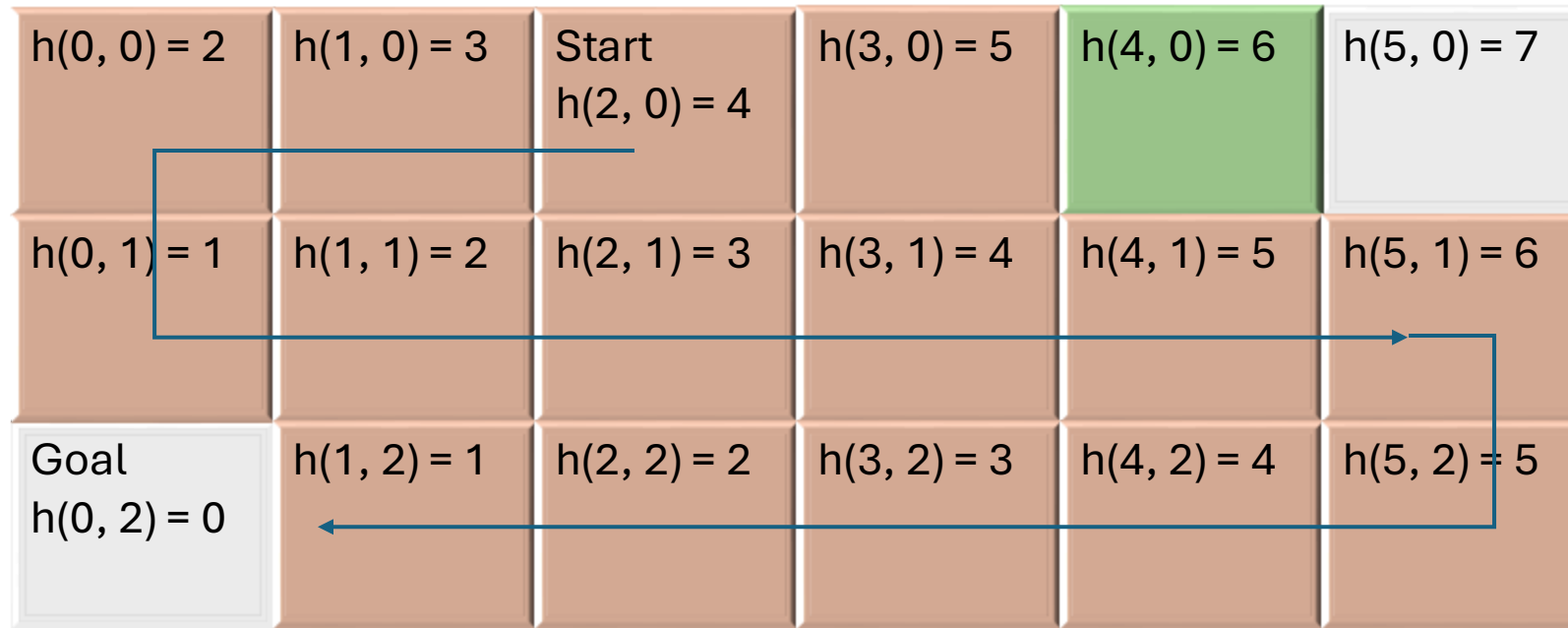
Open Set:  $[((4, 1), 5), ((4, 0), 6)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((5, 1), 6), ((4, 0), 6)]$

## Heuristic Function: Manhattan Distance



Best-h search greedily follows the heuristic. It does not provide optimal (lowest cost) paths.

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((2, 0), 4)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((1, 0), 4), ((3, 0), 6)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((0, 0), 4), ((3, 0), 6)]$



## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((0, 1), 4), ((3, 0), 6)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$	$h(5, 0) = 7$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((3, 0), 6), ((1, 1), 6)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((1, 1), 6), ((4, 0), 8)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$ $g(2, 1) = 5$ $f(2, 1) = 8$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((4, 0), 8), ((2, 1), 8)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$ $g(5, 0) = 3$ $f(5, 0) = 10$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$ $g(2, 1) = 5$ $f(2, 1) = 8$	$h(3, 1) = 4$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((2, 1), 8), ((5, 0), 10)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$ $g(5, 0) = 3$ $f(5, 0) = 10$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$ $g(2, 1) = 5$ $f(2, 1) = 8$	$h(3, 1) = 4$ $g(3, 1) = 6$ $f(3, 1) = 10$	$h(4, 1) = 5$	$h(5, 1) = 6$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((5, 0), 10), ((3, 1), 10)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$ $g(5, 0) = 3$ $f(5, 0) = 10$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$ $g(2, 1) = 5$ $f(2, 1) = 8$	$h(3, 1) = 4$ $g(3, 1) = 6$ $f(3, 1) = 10$	$h(4, 1) = 5$	$h(5, 1) = 6$ $g(5, 1) = 10$
Goal $h(0, 2) = 0$	$h(1, 2) = 1$	$h(2, 2) = 2$	$h(3, 2) = 3$	$h(4, 2) = 4$	$h(5, 2) = 5$

Open Set:  $[((5, 0), 10), ((3, 1), 10)]$

## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$ $g(5, 0) = 3$ $f(5, 0) = 10$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$ $g(2, 1) = 5$ $f(2, 1) = 8$	$h(3, 1) = 4$ $g(3, 1) = 6$ $f(3, 1) = 10$	$h(4, 1) = 5$	$h(5, 1) = 6$ $g(5, 1) = 4$ $f(5, 1) = 10$
Goal $h(0, 2) = 0$ $g(0, 2) = 10$ $f(0, 2) = 10$	$h(1, 2) = 1$ $g(1, 2) = 9$ $f(1, 2) = 10$	$h(2, 2) = 2$ $g(2, 2) = 8$ $f(2, 2) = 10$	$h(3, 2) = 3$ $g(3, 2) = 7$ $f(3, 2) = 10$	$h(4, 2) = 4$ $g(4, 2) = 6$ $f(4, 2) = 10$	$h(5, 2) = 5$ $g(5, 2) = 5$ $f(5, 2) = 10$

Open Set: [((5, 0), 10), ((3, 1), 10)]



## Heuristic Function: Manhattan Distance

$h(0, 0) = 2$ $g(0, 0) = 2$ $f(0, 0) = 4$	$h(1, 0) = 3$ $g(1, 0) = 1$ $f(1, 0) = 4$	Start $h(2, 0) = 4$ $g(2, 0) = 0$ $f(2, 0) = 4$	$h(3, 0) = 5$ $g(3, 0) = 1$ $f(3, 0) = 6$	$h(4, 0) = 6$ $g(4, 0) = 2$ $f(4, 0) = 8$	$h(5, 0) = 7$ $g(5, 0) = 3$ $f(5, 0) = 10$
$h(0, 1) = 1$ $g(0, 1) = 3$ $f(0, 1) = 4$	$h(1, 1) = 2$ $g(1, 1) = 4$ $f(1, 1) = 6$	$h(2, 1) = 3$ $g(2, 1) = 5$ $f(2, 1) = 8$	$h(3, 1) = 4$ $g(3, 1) = 6$ $f(3, 1) = 10$	$h(4, 1) = 5$	$h(5, 1) = 6$ $g(5, 1) = 4$ $f(5, 1) = 10$
Goal $h(0, 2) = 0$ $g(0, 2) = 10$ $f(0, 2) = 10$	$h(1, 2) = 1$ $g(1, 2) = 9$ $f(1, 2) = 10$	$h(2, 2) = 2$ $g(2, 2) = 8$ $f(2, 2) = 10$	$h(3, 2) = 3$ $g(3, 2) = 7$ $f(3, 2) = 10$	$h(4, 2) = 4$ $g(4, 2) = 6$ $f(4, 2) = 10$	$h(5, 2) = 5$ $g(5, 2) = 5$ $f(5, 2) = 10$

Open Set:  $[((5, 0), 10), ((3, 1), 10)]$