

Exercise

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TUM Department of Informatics

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Dimensionality Reduction and Matrix Factorization

Problem 1:

Leslie: Votes 3 for Alien, 4 for Titanic.

Original space: $[0, 3, 0, 0, 4]$

To obtain the wanted concept space a projection from original space to concept space is needed.

(script page 67)

$$P = A * V$$

$$P = [0, 4, 0, 0, 4] * \begin{bmatrix} 0.58 & 0 \\ 0.58 & 0 \\ 0.58 & 0 \\ 0 & 0.71 \\ 0 & 0.71 \end{bmatrix}$$

$$P = [1.74, 2.84]$$

This means Leslie will most likely favor the Titanic and Casablanca movies (score: 2.84) over the sci-fi genre (score: 1.74). She already rated Titanic, which means she has already seen it, so Casablanca would be a good recommendation.

Problem 2:

Integrating out z (script page 31):

$$x_i \sim \mathcal{N}(\mu, WW^T + \sigma^2 I)$$

x has a gaussian distribution with mean μ and covariance $WW^T + \sigma^2 I = WW^T + \Phi$.

$y = Ax$ is a linear transformation $\implies y$ has still a gaussian distribution.

y now has a mean of $A\mu$ and a covariance of $AWW^T A^T + A\Phi A^T$.

(Because the covariance after a linear transformation with A is $cov(AZ) = Acov(Z)A^T$.)

If μ_{ML} , W_{ML} , Φ_{ML} represent the max. likelihood solution before the transformation, $A\mu_{ML}$, AW_{ML} , $A\Phi_{ML}A^T$ will represent the max. likelihood solution after a transformation with A .

A is orthogonal $\implies AA^T = I$, which means $A\Phi A^T = A\sigma^2 I A^T = \sigma^2 I A A^T = \sigma^2 I I = \sigma^2 I^2 = \sigma^2 I$

Which means the form of the model is preserved.

Appendix

We confirm that the submitted solution is original work and was written by us without further assistance.
Appropriate credit has been given where reference has been made to the work of others.

Munich, January 15, 2020, Signature Marcel Bruckner (03674122)

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